

5.1.2.

Repeat previous problem for slotted Aloha

For slotted aloha: success \Leftrightarrow no other transmissions in T_{tx} time frame:

$$P(\text{success}) = P(k=0) = e^{-G}$$

$$\text{Efficiency } S = G \cdot e^{-G}$$

$$\text{Maximize } S: \frac{dS}{dG} = e^{-G} - G e^{-G} = 0 \Leftrightarrow G = 1$$

$$\frac{d^2S}{dG^2} = -e^{-G} < 0 \Rightarrow \text{maximum}$$

$$G = \lambda T_{tx} \Rightarrow \lambda = \frac{G}{T_{tx}} = \frac{1}{1 \mu s} = 10^6 \frac{tx}{s}$$

$$\lambda_{\text{stat}} = \frac{\lambda}{n} = \frac{10^6 \frac{tx}{s}}{100 \text{ stat}} = \boxed{10000 \frac{tx/s}{\text{station}}}$$