

3.2. CRC

[1 2 3 4 5 6 7 8 9 10]

3.2.1.

Calc remainder of $x^7 + x^5 + 1$ divided by $x^3 + 1$

$$\begin{array}{r}
 1001 \overline{) 101000.01} \\
 \underline{1001} \\
 001100 \\
 \underline{1001} \\
 01010 \\
 \underline{1001} \\
 001111
 \end{array}$$

$$R = x^2 + x + 1$$

3.2.2.

Bit stream 10011101 is transmitted with CRC, polynomial $x^3 + 1$

a) Show the bit string transmitted

b) Suppose the third bit from the left is inverted in transmission. Show that the receiver detects it.

c) Give an example of ~~error~~ bit errors not detected.

$$\begin{array}{r}
 1001 \overline{) 10011101000} \\
 \underline{1001} \\
 011001 \\
 \underline{01000} \\
 000100
 \end{array}$$

The string transmitted is
10011101100

$$R_x = 10111101100$$

$$\begin{array}{r}
 1001 \overline{) 10111101100} \\
 \underline{1001} \\
 001011 \\
 \underline{001001} \\
 00001001
 \end{array}$$

The remainder at receiver is $100 \neq 000$

c) Undetected: multiples of (x) . $R(x)(x^5 + x) = (x^3 + 1)(x^5 + x) = x^8 + x^5 + x^4 + x$

$$\begin{array}{l}
 E_x = 00100110010 \\
 T_x = 10011101100 \\
 R_x = 1011101110
 \end{array}$$

$$\begin{array}{r}
 1001 \overline{) 1011101110} \\
 \underline{1001} \\
 01011 \\
 \underline{0101} \\
 01111 \\
 \underline{01101} \\
 00001 \leftarrow \text{Undetected}
 \end{array}$$