

... 1.40. (2)

c) From part (a), can you conclude that if the input to a linear system is zero between times  $t_1$  and  $t_2$  (continuous time) or  $n_1$  and  $n_2$  (discrete time), then its output is zero between those times?

No. Consider the ~~discrete~~ discrete-time system that transforms a signal  $x[n]$  into  $y[n] = x[n-1]$ .

Linearity check:

$$x'[n] = \alpha x_1[n] + \beta x_2[n] \Rightarrow y[n] = x'[n-1] = \alpha x_1[n-1] + \beta x_2[n-1]$$

$$\alpha y_1[n] + \beta y_2[n] = \alpha x_1[n-1] + \beta x_2[n-1] = y[n] \Rightarrow \text{linear}$$

Consider  $x[n] = \delta[n]$ :  $x[n] = 0 \quad \forall n \in (-\infty, -1] \cup [1, \infty)$

$$y[n] = \delta[n-1] \Rightarrow y[+1] = \delta[+1-1] = \delta[0] = 1 \neq 0$$

$$\cancel{x[n] = 0 \quad \forall n \in \{n \in \mathbb{Z} : n-1 \neq 0\}}$$

$x[n]$  is 0 between 1 and 2, but  $y[n]$  is not 0 at 1.