

2.9. Let $h(t) = e^{2t} u(t+4) + e^{-2t} u(t-5)$.

Determine A and B such that

$$h(t-\tau) = \begin{cases} e^{-2(t-\tau)} & , \tau \leq A \\ 0 & , A < \tau < B \\ e^{2(t-\tau)} & , B < \tau \end{cases}$$

$$\begin{aligned} h(t-\tau) &= e^{2(t-\tau)} u(-(t-\tau)+4) + e^{-2(t-\tau)} u(t-\tau-5) \\ &= \begin{cases} e^{2(t+\tau)} & , \underbrace{-t+\tau+4 \geq 0}_{\tau \geq t-4} \\ 0 & , \text{elsewhere} \end{cases} + \begin{cases} e^{-2(t-\tau)} & , \underbrace{t-\tau-5 \geq 0}_{\tau \leq t-5} \\ 0 & , \text{elsewhere} \end{cases} \\ &= \begin{cases} e^{-2(t-\tau)} & , \tau \leq t-5 \\ 0 & , t-5 \leq \tau \leq t-4 \\ e^{2(t-\tau)} & , t-4 \leq \tau \end{cases} \end{aligned}$$

$$\boxed{A=t-5, \quad B=t-4}$$