

Linear Search

```
LinearSearch.java
1 package LinearSearch;
2
3 public class LinearSearch {
4
5     @
6     public int linearSearch(int[] a, int x){
7
8         int ans = -1;
9
10        for (int i = 0; i < a.length; i++){ // Time complexity : O(n)
11            if (a[i] == x){
12                ans = i;
13                return i;
14            }
15        }
16
17        return -1;
18    }
19}
```

*. Question: "static" in Java function?

ex.

```
public class App {
```

```
    public static void main(...)
```

```
    public static int linearSearch(...)
```

↳ ~~static~~ 非 static

不需創 App obj 即可

使用 static function

? { This is a class method
rather than a instance
method.

Primary Search Recursion

* 前提: Data must be sorted!

* Procedure: public int binarySearch(int x, int[] A)



1° $P=0, R=A.length-1$

2° while ($p \leq r$) do

a) set $q = \lfloor \frac{p+r}{2} \rfloor$ ↓ integer division
舍尾捨去小數

b) if $A[q] = x$, return q

c) if $A[q] > x$, $R = q-1$ ← minus!

else $A[q] < x$, $P = q+1$ ← plus!

3° return -1

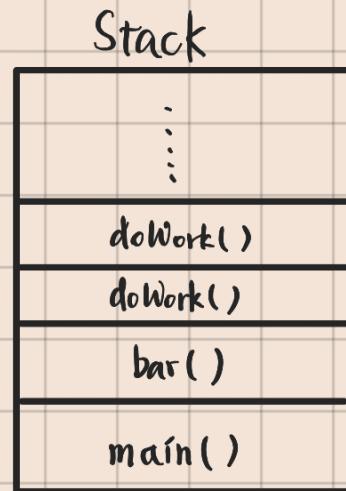
BinarySearch.java × SearchApp.java × Recursion.java ×

```
1 package SearchAlgorithm;
2
3 public class BinarySearch {
4
5     @ public static int binarySearch(int[] a, int x) {
6
7         int p = 0;
8         int r = a.length - 1;
9
10        while (p <= r){
11
12            int q = (p + r) / 2;
13
14            if(x < a[q]) r = q-1;
15            else if (x > a[q]) p = q+1;
16            else return q;
17
18        }
19    }
20
21
22 }
```

Recursion

bar() { doWork(); }

doWork() { doWork(); }



* Recursive.java

```
BinarySearch.java × SearchApp.java × Recursion.java × DoublyLinkedListApp.java ×
```

```
3  public class Recursion {  
4  
5      public static void reduceByOne(int n){  
6  
7          if (n >= 0){ // Base case : condition for recursion to stop  
8              reduceByOne(n: n - 1);  
9          }  
10  
11         System.out.println("Complete call: " + n); // executed after recursive function  
12         从 print 到 n  
13     }  
14  
15     public static int recursiveLinearSearch(int[] A, int i, int x) {  
16  
17         if (i > A.length - 1) return -1; // x was not found in array  
18         else if (A[i] == x) return i; // found x  
19         else return recursiveLinearSearch(A, i: i + 1, x); // index+1 & search again  
20         是 "return" recursive function  
21     }  
22  
23     public static int recursiveBinarySearch(int[] A, int p, int r, int x){  
24         System.out.println("[" + p + "..." + r + "]"); → print 亂序 p,r  
25  
26         if (p > r) return -1;  
27         else {  
28             int q = (p + r)/2;  
29  
30             if (A[q] == x) return q;  
31             else if (A[q] > x) return recursiveBinarySearch(A, p, r:q-1, x);  
32             else return recursiveBinarySearch(A, p:q+1, r, x);  
33         }  
34     }  
35 }
```

p A[q] r A[q] > x → . 返 "r"

p A[q] r A[q] > x → . 返 "p"

* Math

```
SearchApp.java × Recursion.java × BinarySearch.java × DoublyLinkedListApp.java ×
```

```
1 package SearchAlgorithm;
```

```
2
```

```

3 import ...
6
7 public class SearchApp {
8
9     public static void main(String[] args) {
10
11         System.out.println(binarySearch(new int[] {1, 2, 3, 4, 5}, 1));
12         // linearSearch(new int[] {1, 2, 3, 4, 5}, 1);
13         System.out.println(recursiveLinearSearch(new int[] {1, 2, 3, 4, 5}, 0, 5));
14         System.out.println(recursiveBinarySearch(new int[] {1, 2, 3, 4, 7, 9, 12, 18},
15                                         p: 0, r: 7, x: 18));
16         // first element index
17         // last element index
18     }
19

```

*. Big O Notation of Binary Search

Binary Search $\rightarrow O(\log n)$

原理: $\log_{10} 100 = 2 \leftarrow 100 \text{ 是 } 10 \text{ 的 } 2 \text{ 次方}$

$\log_2 4 = 2 \leftarrow 4 \text{ 是 } 2 \text{ 的 } 2 \text{ 次方}$

$\log_2(n) \leftarrow \text{表示 } n \text{ 除以 } 2 \text{ 的次数} = 1, n \text{ 代表 input size}$

Binary Search 基于二分法: input array size 可以执行每次 \log_2 次

$\therefore \text{Time complexity} = \log_2(n)$, 一般写 $\log(n)$

