## ECE 531 | Software Defined Radio

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## Part 1.a

Below is a screenshot of the constructed signal flow graph:

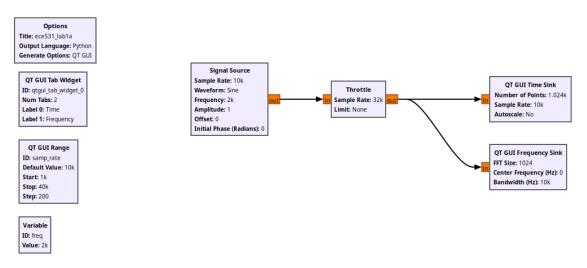


Figure 1: A screenshot of the constructed signal flow graph.

When executing the previously shown signal flow graph, we get the following GUI popup.

Examining the time domain signal of that is displayed, we can notice quite a bit of aliasing in the time sink gui module. This is initially an odd experience because up to this point, we have been taught that as long as our sample rate is double the frequency of interest, then we can perfectly reconstruct a signal back from it's samples. So not seeing the perfect sine wave (that is currently at 2kHz).

However, when looking at the output on the gui, we see that this isn't the case. The measured signal frequency when sampling at a rate of 10kHz is approximately 2kHz for the signal as expressed by holding the mouse over the peak of the signal in the frequency sink gui module.

When increasing the sample rate using the slider, the definition of the time-domain wave begins to increase, that is, the graph that is shown looks like a smoother sine wave then the wave shown with only 10k samples. This is likely solely because there are more samples that are being captured in the time domain, which allows the time sink to show the wave with more definition. One of the main aspects of the wave that is more accurate is the amplitude of the wave. When looking at resources present in the DSP industry, such as this article by Seimens, we can see that they recommend sampling at a sample rate at least 10x higher than the frequency of interest. Seimens state that finding the correct amplitude of the signal in the frequency domain only requires that the sample rate be 2x higher than the frequency of interest (according to the Shannon-Nyquist Theorem), however, this only applies in the frequency, or the fourier domain.

In practice, when using the time domain, sample rates that are only 2x greater than the frequency of interest render a wave with inaccurate amplitudes, this is shown to be the case in te time domain representation of the wave when the sample rate was 10kHz. However, as shown in the image below, the amplitude is closer to 1 (the actual amplitude of the signal source) when the sample rate is raised to 40kHz.

When changing the sample rate to 3.5 kHz, there is quite an interesting change in both the frequency representation and time domain representation.

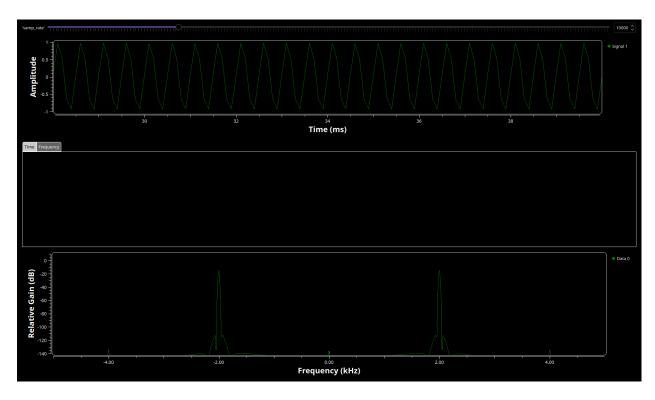


Figure 2: This is the gui that is displayed when running the signal flow gnuradio signal flow graph.

In the frequency domain, the measured peak of the signal is 1.5kHz. This is a change in about 500 Hz from the actual frequency of the signal. The reason for this is because of the normalization of frequency of the sampled signal.

Taking the actual frequency of the signal: 2kHz, we know that the sample rate is not high enough to represent the signal in the frequency domain. This causes aliasing/frequency mis-normalization appearing in the gnuradio.

When changing the code blocks to process 'Complex' instead of 'Float' we notice a few changes. First and foremost, the color of the inputs and outputs becomes blue instead of orange. When executing the flow graph we see two major changes. The first change happens in the frequency domain. There is notably, only one peak on the positive side of the frequency spectrum instead of the two that were previously present. Shifting our attention to the time domain, we get the gui telling the user that there are two sample signals. At first I thought that this was an error, however, after some debugging I realized that it was not. I found it to be quite interesting. I don't know what the implications of this are.

## Things to note:

- There is now only one peak in the frequency domain
- There are now two signals present in the time domain the phase relationship between them is about 90 degrees.
- Changing the sampling rate from 10kHz to 40kHz does not have as drastic of an effect on the amplitude of the time domain signal as the signal that was sampled using 'Floats'
- The measured frequency of the signal at a sample rate of 40kHz is 2kHz for the signal. (this is also true for a sample rate of 10kHz).
- When reducing the sample rate from 4kHz to 3.5 kHz we can examine that the peak on the frequency spectrum slowly moves to the right until the peak moves to the left side of the base-band. This indicates that a change in phase is being detected in our signal.

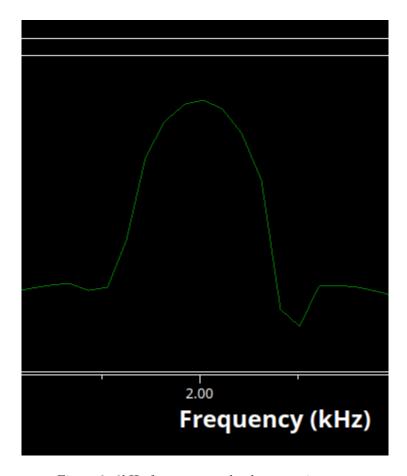


Figure 3: 2kHz frequency peak when mousing over

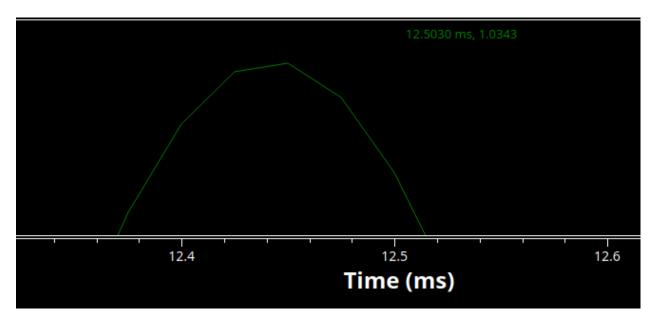


Figure 4: Screenshot of the time domain sine wave at a sample rate of  $40\mathrm{k}$ 

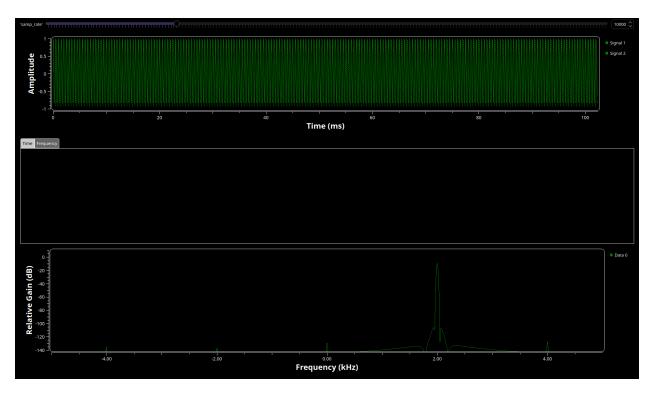


Figure 5: Default Appearance when data type of the modules is converted to 'Complex Float'

• Continuing to reduce the sample rate causes te frequency domain display to move the peak closer to zero. This happens at sample rates of 2kHz and 1kHz. which are both integer multiples/divisors of 2kHz.

After adding the frequency slider to the sfg on gnuradio, we can shift the frequency of the source signal over a range of frequency. One thing to note regarding the display of the frequency peak displayed in the frequency sink module is the fact that the frequency keeps cycling through the possible frequency ranges up to the sample rate. after that, the frequency jumps to the negative side and keeps increasing. This is because as the frequency of the signal approaches the