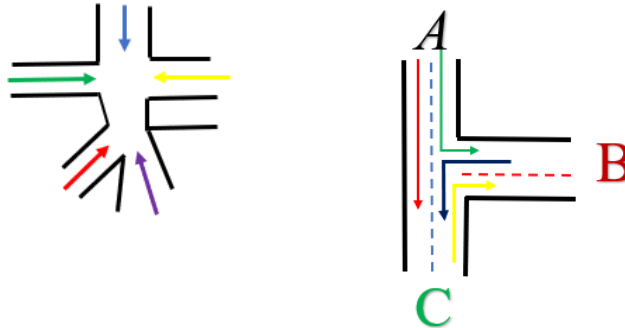


**Rule of representation****Example**

3 Segments

A- One way

B&amp;C Two ways

**Goal**

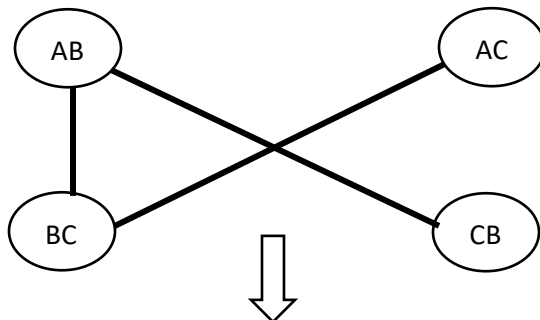
Design traffic light control pattern to make this intersection as safe as possible

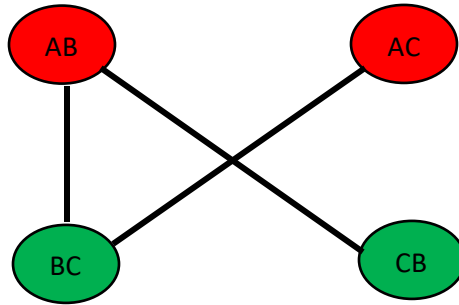
1. Identify safe and unsafe trans (simultaneals)

	AB	AC	BC	CB
AB	■	O	×	×
AC	O	■	×	O
BC	×	×	■	O
CB	×	O	O	■

× Unsafe

O Safe

**Using graph concept** $G = \langle V, E \rangle$  it can be directed and undirect graphVertices  $\rightarrow$  transEdges  $\rightarrow$  let the edge connect trans that are not compatible (unsafe)



### Graph Coloring

How to come up with these colors

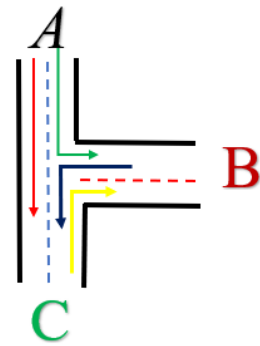
1. Problem description
2. Representation
3. Solution (method, algorithms .....)

How do we color the graph?

### Graph coloring

A greedy approach

1. Pick a node and color it with a color "X".
2. Select any node with unconnected to the one you just colored and mark it with color "X".
3. Repeat (2) until there are no have node you can color after "X".
4. Pick another color and repeat 2 and 3.



### Representation

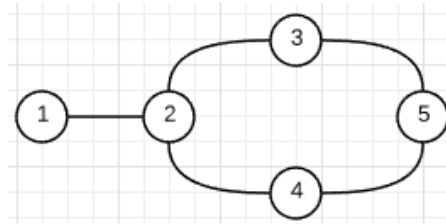
- Traffic
- Graph
- Graph Coloring

### Greedy approach (pitfall)

Heuristic

- solving problem more efficiently at expense of optimality

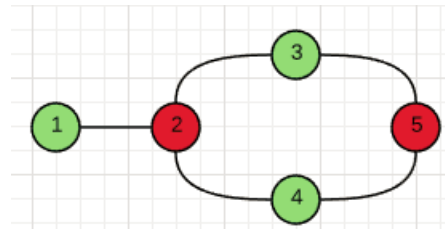
### Example (pitfall)



- Label nodes with  $\{1,2,3,4,5\}$
- In the particular order

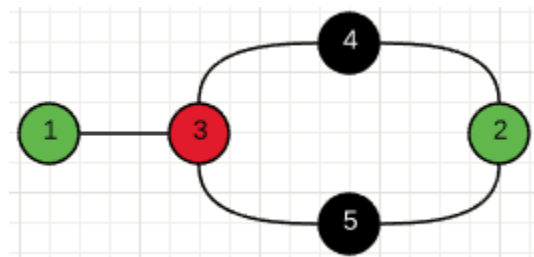
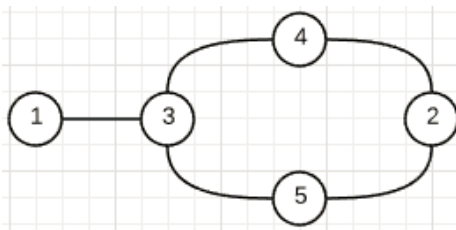
### Order A

$\{1,2,3,4,5\}$



### Order B

The same strategy that is pick up the node with lowest number



## State Space

- Capture the condition / situation of system at point in the time


## Example

8 Puzzle

*initial state*


3X3 board with 9 tiles

{1,2,3,...,8 and blank tile}



2	8	3
1	6	4
7		5

*Goal state (final state)*



1	2	3
8		4
7	6	5

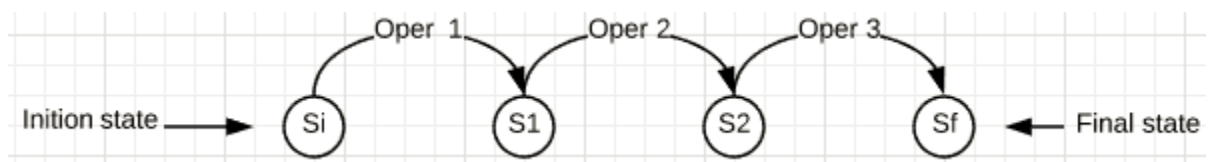
- To solve it; need to make a series of moves

## Moves

- Up
- Down
- Left
- Right

In state space based approach, we define

1. State space
2. Initial state
3. Goal state
4. Operators moves / action that transfer / travers state space



5. Control strategy

## 8 Puzzle

### 1. State space

$B = \{(T_{ij}) \mid i=1,2,3 ; j=1,2,3 ; T_{ij} = \{1,2,\dots,8, \text{blank}\}\}$

And  $\neg (\exists T_{ij} \ \& \ \exists T_{km} \text{ such that } T_{ij} = T_{km} \text{ for } i \neq j \text{ or } k \neq m = \{1,2,3\})$

1	2	3
8		4
7	6	5

### 2. Initial state

2	8	3
1	6	4
7		5

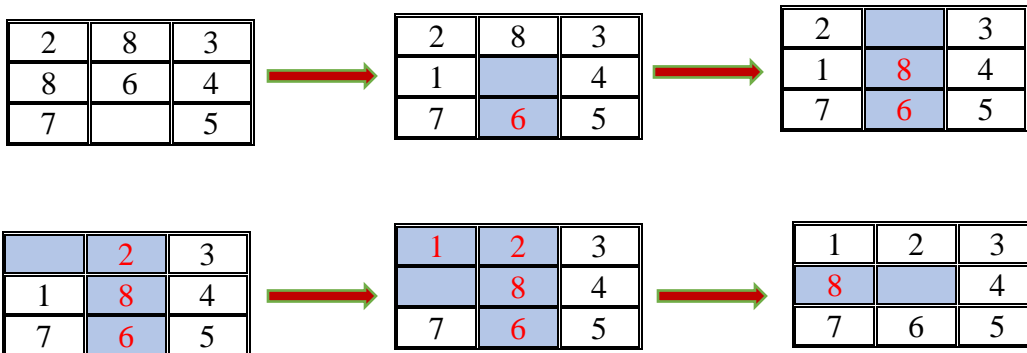
### 3. Goal state

1	2	3
8		4
7	6	5

### 4. Operators

- Up   Down   Left   Right

### 5. Control Strategy (CS)



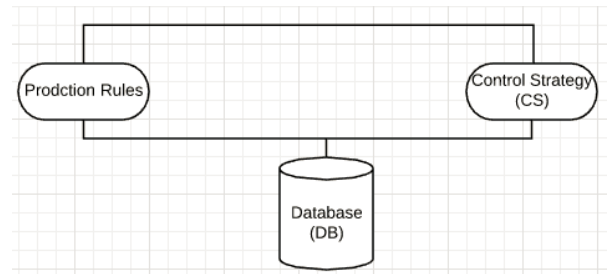
Solution is

- Up -----> Up -----> Left ----->Down ----->Right

### Continue with state space approach

- The concept of AI production system

- DB → way of present State Space
- Rules (operator) if < condition >  
Then < action >



Example of rule in the 8-puzzle problem

- Up
- Down
- Left
- Right

2	8	3
1	6	4
7		5

Changing state →

2	8	3
1		4
7	6	5

- Control Strategy (CS) a method /a way to select an operator rule in such a way that allows us to solve problem

### Procedure: - production

- $D \rightarrow$  Database (initial state)
- $\mathbb{R} \subseteq$  Operator (a set of applicable rules)

While  $\mathbb{R} \neq 0$  and  $D$  does not represent a goal state or does not meet termination condition.

Begin

- $R \leftarrow \text{Select } (\mathbb{R})$
- $D \leftarrow R(D)$
- **Update** ( $\mathbb{R}$ )

end

End

if blank in cell (1,3) then move blank (**Right**)

if blank in cell (1,8) then move blank (**Up**)

2	8	3
1	6	4
7		5

### Example

#### *8-Puzzle re-examine*

- **DB** (database) 3X3 board {1,2,3,...,8 and blank tile}
- Operators  
Translate move **UP Down Left Right** (U D L R) into production
  - If there exists no blank in top row  
and  
blank is in middle row
  - Then it can be moved UP
- Control Strategy (CS) → ? do later.

Initial State / Goal state

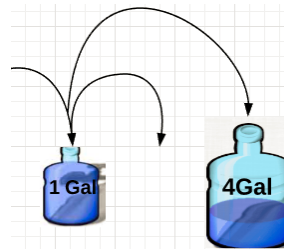
### Example (3)

#### **Water Jug**

Given two jugs with no marking on them with capacities of (4,3) gal respectively.

How can you fill in the (4) gal jug with exactly (2) gal.

Give the set of operators handed out in class.



### AI production system

- DB { (x,y) |  $0 \leq x \leq 4, 0 \leq y \leq 3$  }  
For our instance the initial state  $S_i (0,0)$   
Goal state  $S_g = (2,y)$  such that  $0 \leq y \leq 3$
- operators

### Example (3)

#### Water Jugs Problem

Given two jugs with no marking on them with capacities of (4, 3) gal respectively.

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#### AI production system

- DB { (x,y) |  $0 \leq x \leq 4, 0 \leq y \leq 3$  }

For our instance the initial state  $S_i (0, 0)$

Goal state  $S_g = (2, y)$  such that  $0 \leq y \leq 3$

- Operators

Initial state (0, 0)



Goal State (2, x)

- Control strategy (CS) to be discussed

#### Solution

$(0,0) \rightarrow (4,0) \rightarrow (1,3) \rightarrow (1,0) \rightarrow (0,1) \rightarrow (4,1) \rightarrow (2,3)$

#### Rules (3) & (4) Redundant

1	$(X,Y : X < 4) \rightarrow (4,Y)$	Fill the 4-gallon jug
2	$(X,Y : Y < 3) \rightarrow (X,3)$	Fill the 3-gallon jug
3	$(X,Y : X > 0) \rightarrow (X-D,Y)$	Pour some water out of the 4-gallon jug
4	$(X,Y : Y > 0) \rightarrow (X,Y-D)$	Pour some water out of the 3-gallon jug
5	$(X,Y : X > 0) \rightarrow (0,Y)$	Empty the 4-gallon jug on the ground
6	$(X,Y : Y > 0) \rightarrow (X,0)$	Empty the 3-gallon jug on the ground
7	$(X,Y : X+Y >= 4 \wedge Y > 0) \rightarrow (4,Y-(4-X))$	Pour water from the 3-gallon jug into the 4-gallon jug until the 4-gallon jug is full
8	$(X,Y : X+Y >= 3 \wedge X > 0) \rightarrow (X-(3-Y),3)$	Pour water from the 4-gallon jug into the 3-gallon jug until the 3-gallon jug is full
9	$(X,Y : X+Y <= 4 \wedge Y > 0) \rightarrow (X+Y,0)$	Pour all the water from the 3-gallon jug into the 4-gallon jug
10	$(X,Y : X+Y <= 3 \wedge X > 0) \rightarrow (0,X+Y)$	Pour all the water from the 4-gallon jug into the 3-gallon jug

### Example (4)

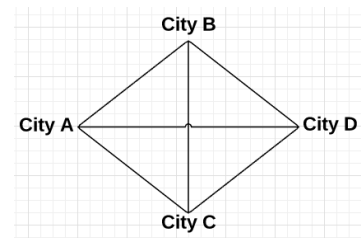
#### A traveling Salesman problem

A starting city (A) have to visit each city exactly once and return to start city.

#### Criterion

The path traveled should be minimum

- Distance  $\rightarrow d_{ij}$
- Cost  $\rightarrow C_{ij}$





## AI production system (PS) for traveling salesman problem (TSP)

- What is the database?

➤ **DB** → list of cities visited so far (**with a constraint**)  
That no city other than starting city occurs twice

➤ Operators

1) If possible (that is a city has not been visited)  
Then go to city A next

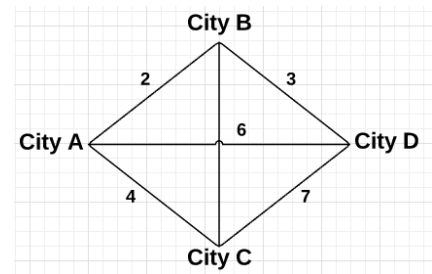
2) If possible then go to city B next

•

•

•

h.) If possible go to N next



➤ Control Strategy (CS)

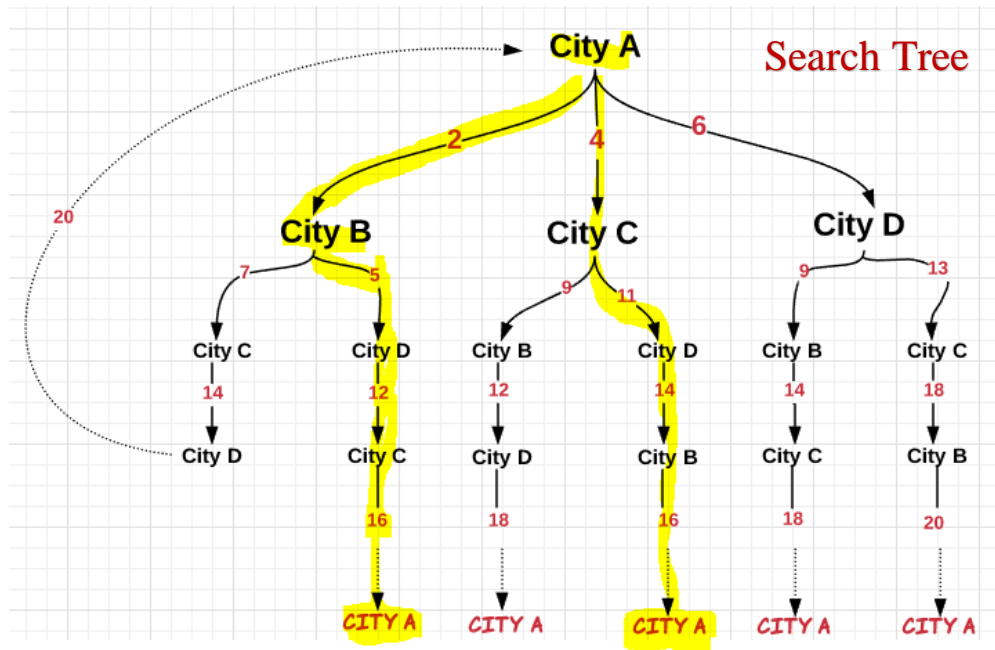
└── Greedy approach

DB= 0   A → B → C → D

DB= {A, B, D, C} = 16

➤ Control Strategy (CS)

└── Exhaustive search



### **Control Strategy (CS)**

- Desired Characteristics
  - 1) Systematic
  - 2) Cause motion
  - 3) Efficient