Hypothesis

Question

Is there a difference between the average studentto-faculty ratio between public and private four-year colleges?

Data

Random sample of 85 private and 57 public fouryear colleges

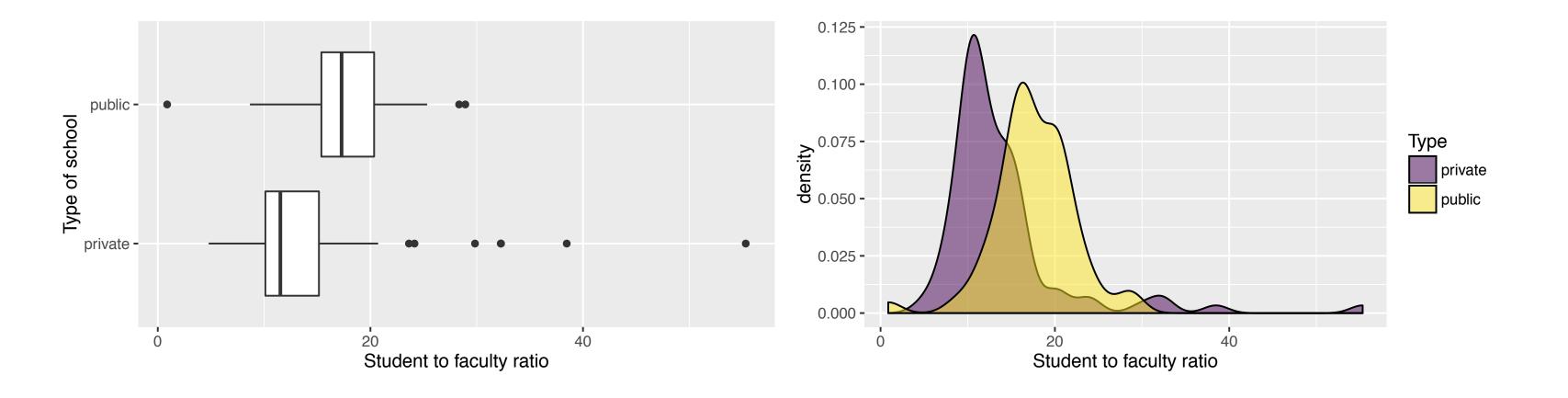
Basic summary statistics from R:

```
# A tibble: 2 × 9

type min Q1 median Q3 max mean SD n

<fctr> <dbl> <31 13.84 7.28 85

public 0.88 15.39 17.29 20.35 28.93 17.60 4.57 57
```



- 1. Formulate two competing <u>hypotheses</u> about the population
- 2. Calculate a <u>test statistic</u> summarizing the relevant information to the claims
- 3. Look at the <u>behavior of the test statistic</u> assuming that the initial claim is true
- 4. Compare the observed test statistic to the distribution created in step 3 to see if it is "extreme"

Formulate two competing <u>hypotheses</u> about the population

Notation Parameters vs. statistics

The null hypothesis

A claim that the parameter is equal to some value e.g. prior belief, "no effect", "no difference"

The alternative hypothesis

Opposition to the null: The claim for which we seek evidence

H₀:

Ha:

Calculate a <u>test statistic</u> summarizing the relevant information to the claims

```
# A tibble: 2 × 9
    type min Q1 median Q3 max mean SD n
    <fctr> <dbl> <3.31 13.84 7.28 85
    public 0.88 15.39 0.88 20.35 28.93 17.60 4.57 57</pre>
```

Look at the behavior of the test statistic assuming that the initial claim is true

Randomization distribution

A collection of statistics from samples simulated by assuming that the null hypothesis is true

Centered around the parameter value specified in H₀

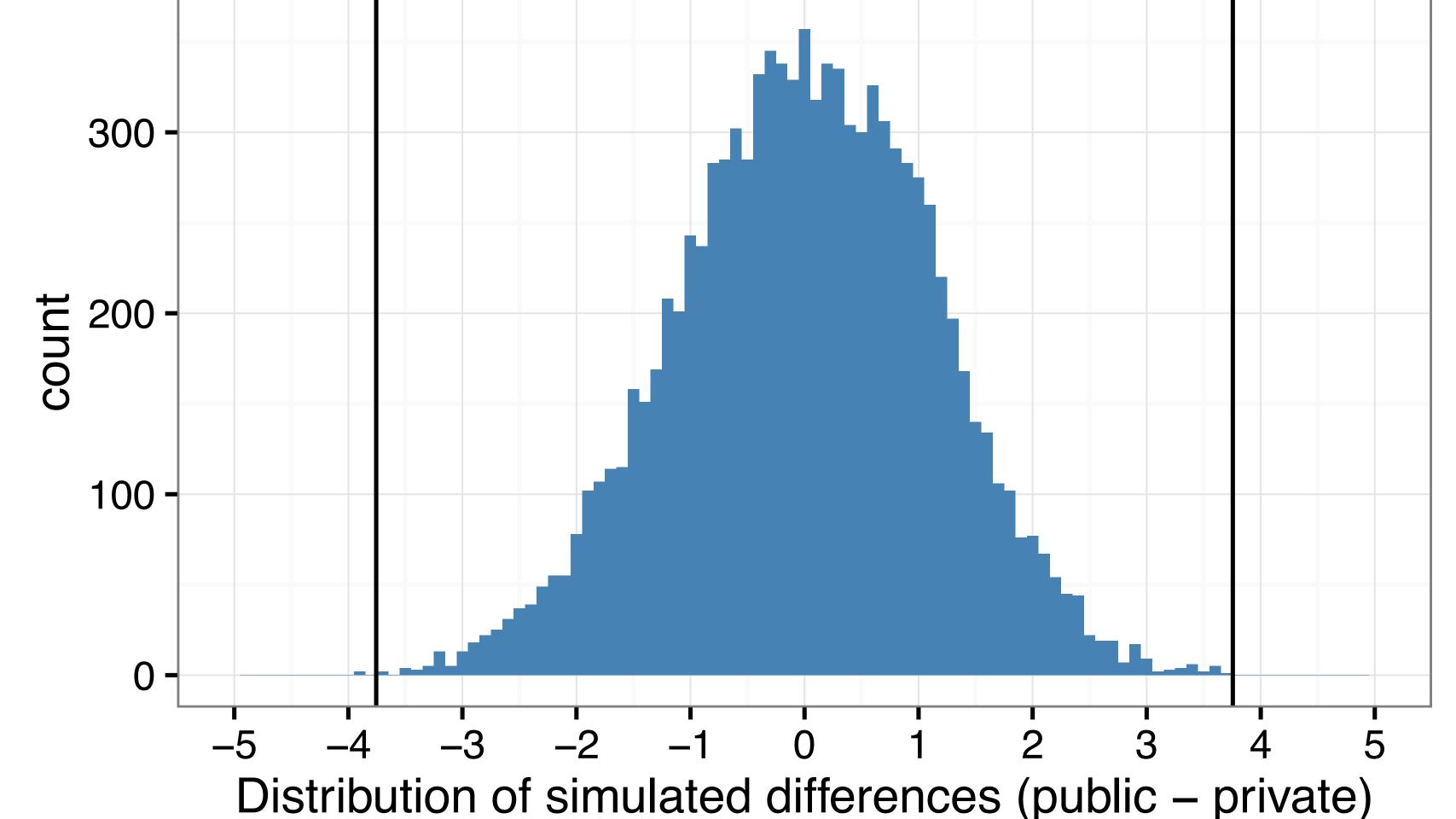
permTest(sf_ratio ~ type, data = colleges)

** Permutation test **

```
Permutation test with alternative: two.sided Observed mean private: 13.84482 public: 17.60018 Observed difference: -3.75535
```

Mean of permutation distribution: -0.00192 Standard error of permutation distribution: 1.13257 P-value: 6e-04

```
*----*
```



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Compare the observed test statistic to the distribution created in step 3 to see if it is "extreme"

Quantifying evidence

An observed test statistic is rare if it is "too far out in the tails" of the randomization distribution

<u>p-value</u>:

Proportion of statistics in a randomization distribution that are at least as extreme as the observed test statistic

Interpreting the p-value

The p-value is the chance of obtaining a test statistic at least as extreme as the observed test statistic, if the null hypothesis is true

Strength of evidence

Making decisions

A p-value of 0.05 or below is conventionally called "statistically significant"

A p-value of 0.01 or below is conventionally called "highly statistically significant"

CAUTION: These thresholds are arbitrary

What should we conclude about the difference between the average student-to-faculty ratio between public and private four-year colleges?