Lecture 8 Finding Shapes

COMP3204 Computer Vision

How can we group points to find shapes?

Book
pp
225-239;
247-254

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Content

1. How do we define and detect shapes in images?
2. How can we improve the detection process?

Feature extraction by thresholding

(a) image | (b) low threshold | (c) high threshold

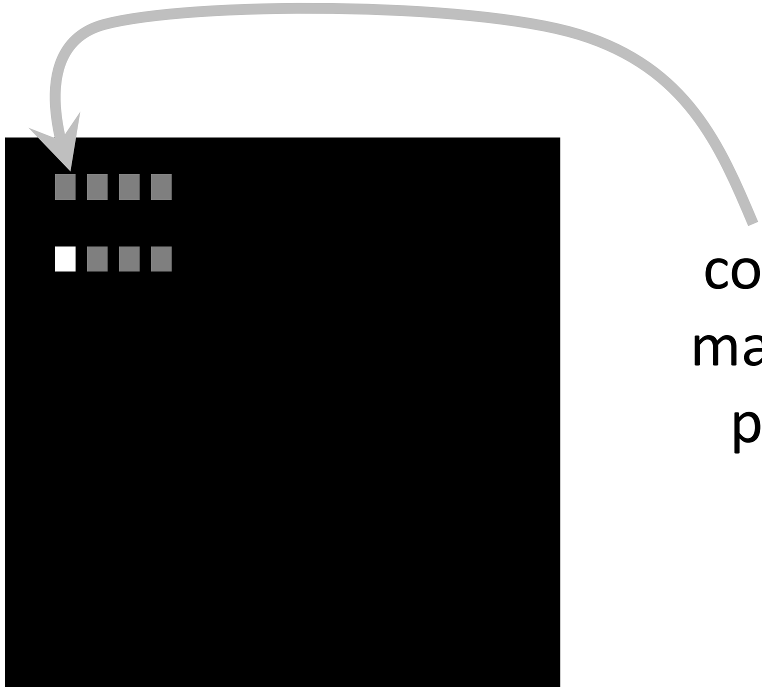
Conclusion: we need shape!

Template Matching -basis

Process of template matching

image

template



count of
matching
points

accumulator space

Suggestions for improving the process? Use edges!

Template Matching

Intuitively simple

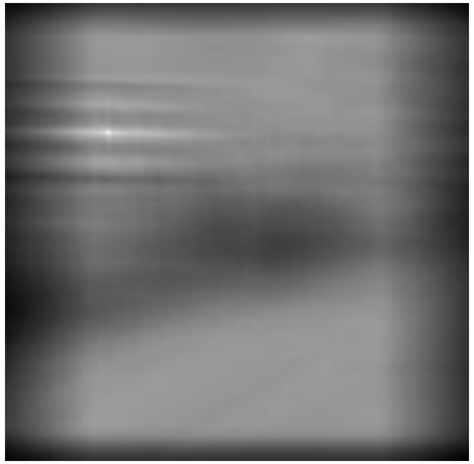
Correlation and convolution

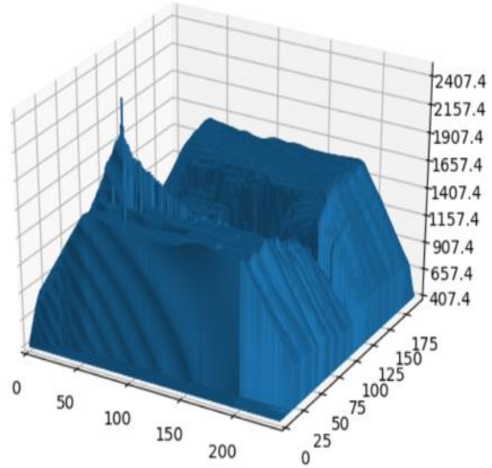
Implementation via Fourier

Relationship with matched filter, viz: optimality

image

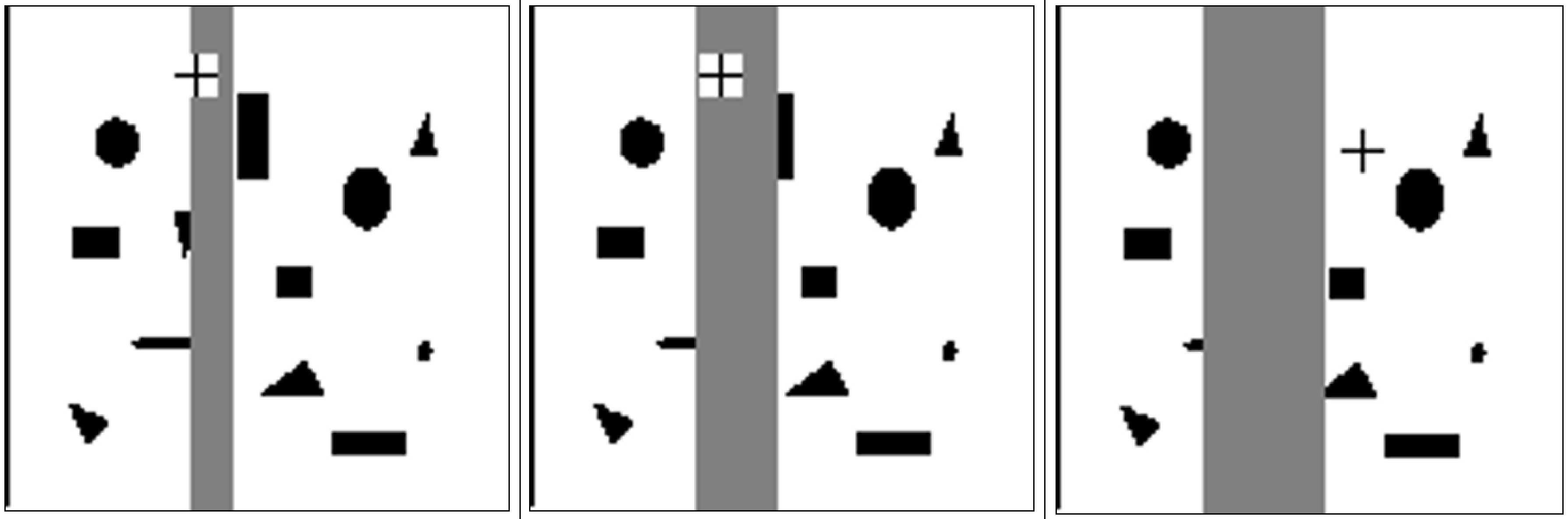
template





accumulator space

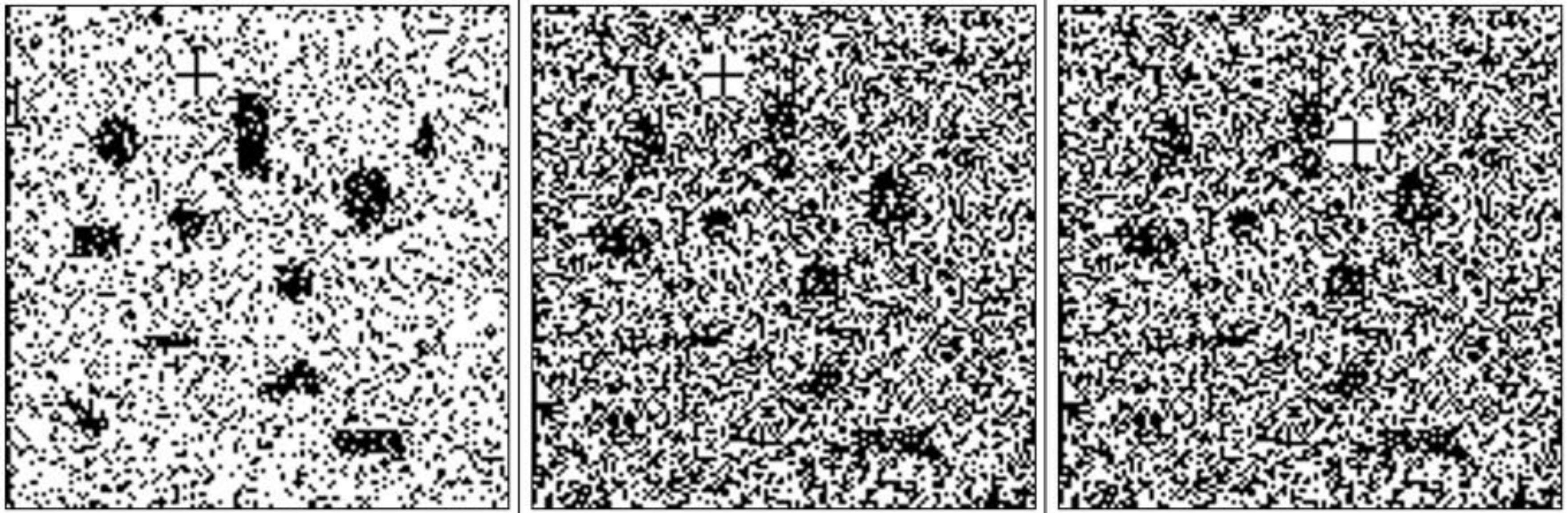
Template matching in occluded images



(a) extraction (of the black rectangle) in no occlusion | **(b)** extraction in some occlusion | **(c)** extraction in complete occlusion (failed)

Template matching is optimal in occlusion

Template matching in noisy images



(a) extraction (of the black rectangle) in some noise

(b) extraction in a lot of noise

(c) extraction in too much noise (failed)

Template matching is optimal in noise

…but….

Convolution and correlation

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and involves flipping the template $\mathbf{I} * \mathbf{T} = \sum_{(x,y)\in W} \mathbf{I}_{x,y} \mathbf{T}_{x-i,y-j}$

Convolution and correlation

Beware centring with transforms

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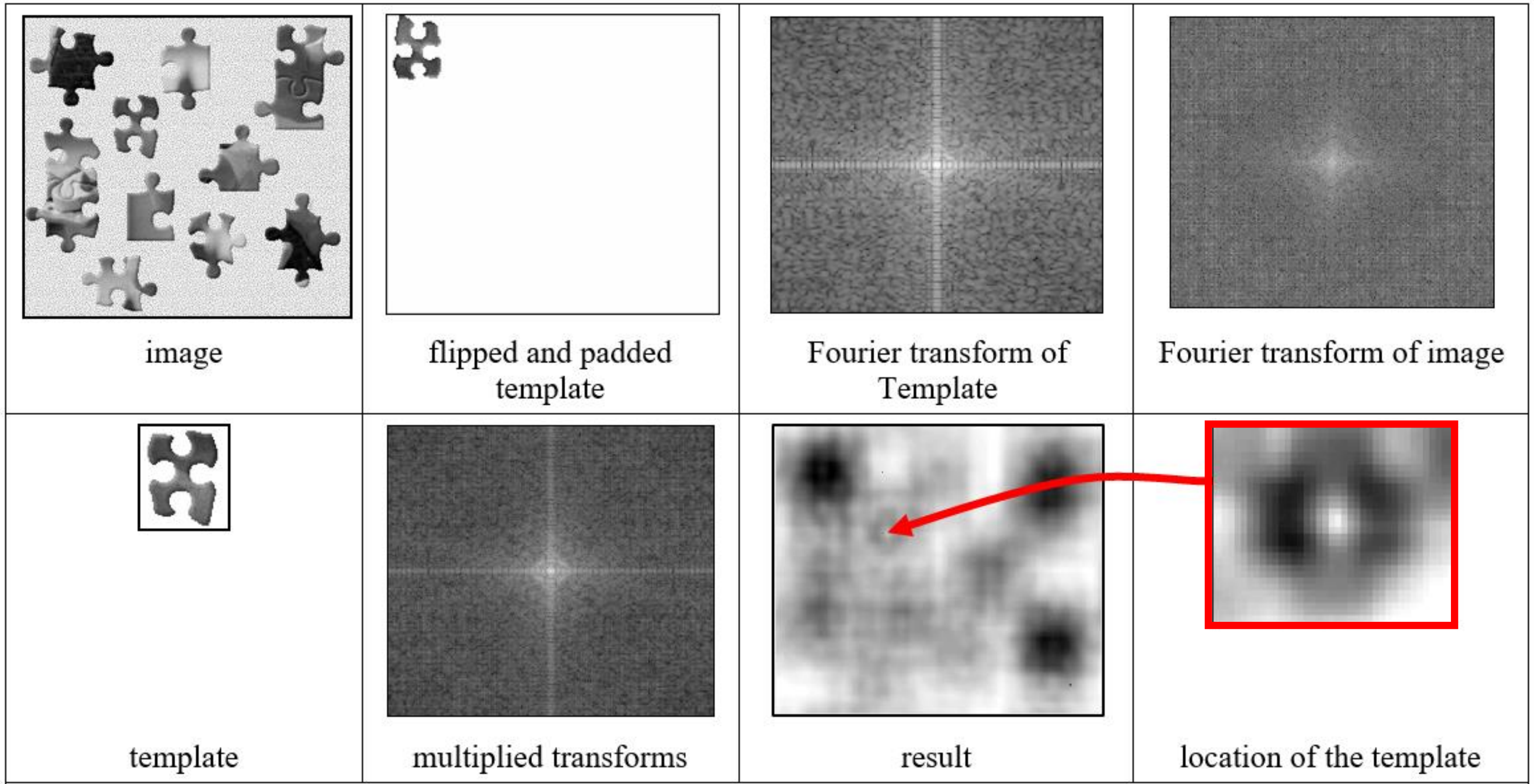
Jon needs this!!

Encore, Baron Fourier!

Template matching is slow, so use FFT



Template Matching via Fourier Transform

$$\mathbf{I} \otimes \mathbf{T} = \sum_{(x,y)\in W} \mathbf{I}_{x,y}\mathbf{T}_{x+i,y+j}$$

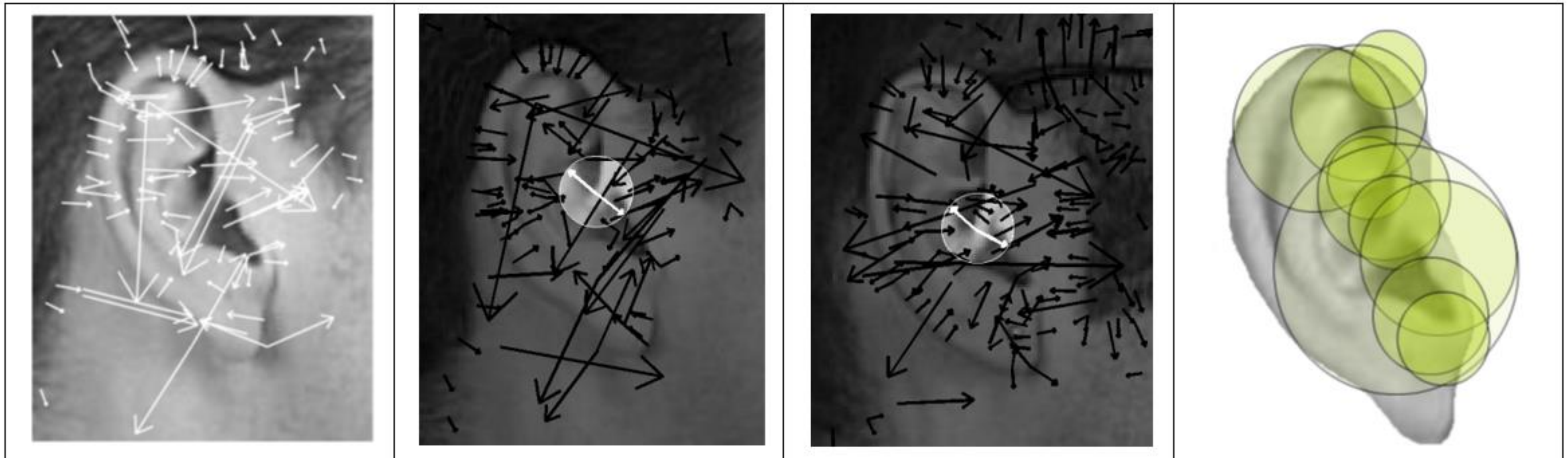
$$= F^{-1}(F(\mathbf{I}) .\times F(-\mathbf{T}))$$

No sliding of templates here;

Cost is 2×FFT plus multiplication

Applying template matching

Applying SIFT in ear biometrics



(a) detected SIFT points

(b) one feature

(c) same feature as (b) in a different ear

(d) regions of influence

Over to Jon Hare!

Hough Transform

- Performance same as template matching, but faster

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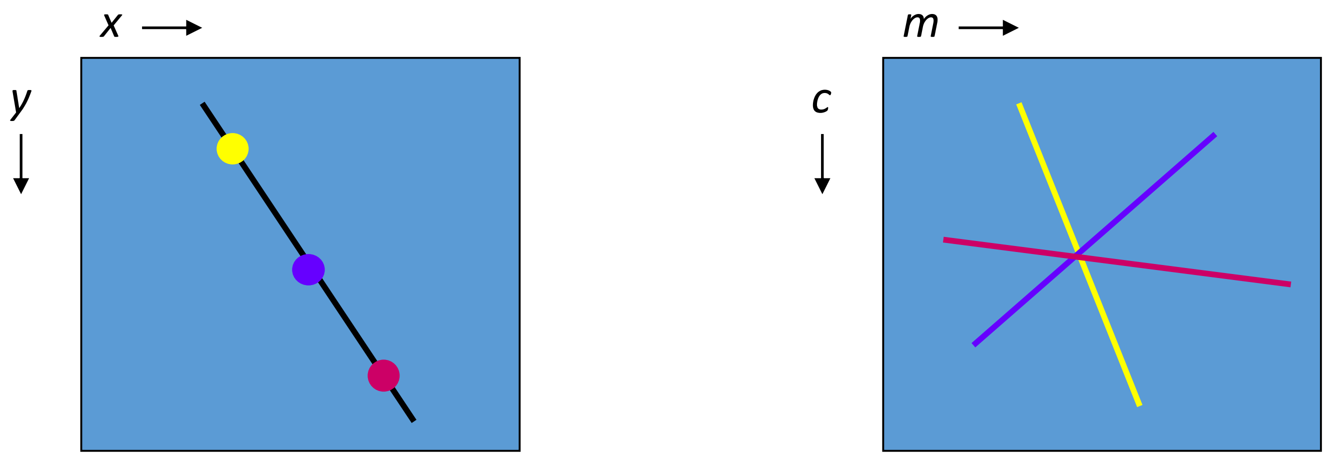

image　　　　accumulator space

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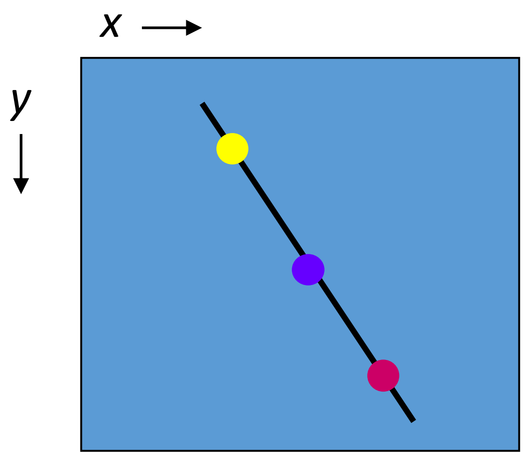
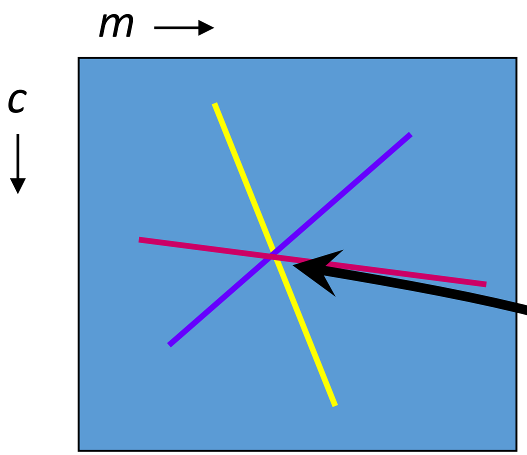


image



accumulator space

The coordinates of the peak are the parameters of the line

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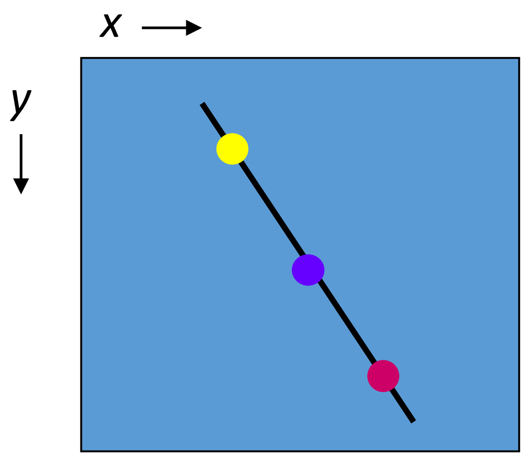
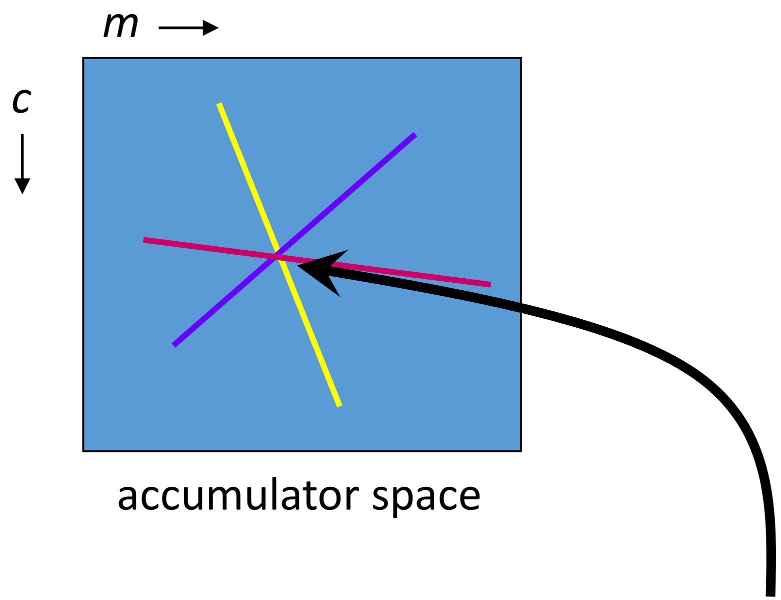


image



accumulator space

The coordinates of the peak are the parameters of the line

- In maths it's the principle of duality

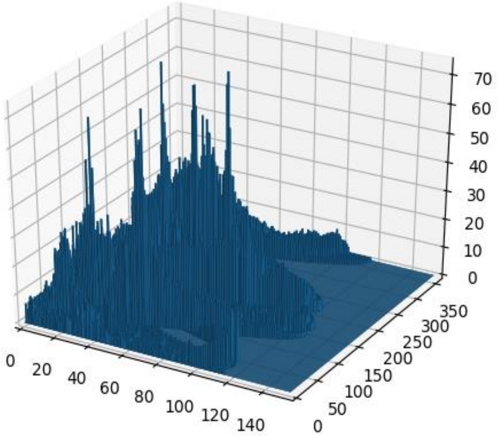
Pseudocode for HT

```
accum=0
for all x,y                                 !look at all points
    if edge(y,x)>threshold                  !check significance
        for m=-10 to +10                    !if so, go thru m
            c=-x*m+y                        !calculate c
            accum(m,c) PLUS 1               !vote in accumulator
m,c = argmax(accum)                         !peak gives parameters
```

Applying the Hough transform for lines

image

detected lines



accumulator space

OK, it works. Can anyone see a problem?

Hough Transform for Lines … problems

- *m,c* tend to infinity
- Change the parameterisation
- Use foot of normal $\rho = x\cos\theta + y\sin\theta$
- Gives polar HT for lines

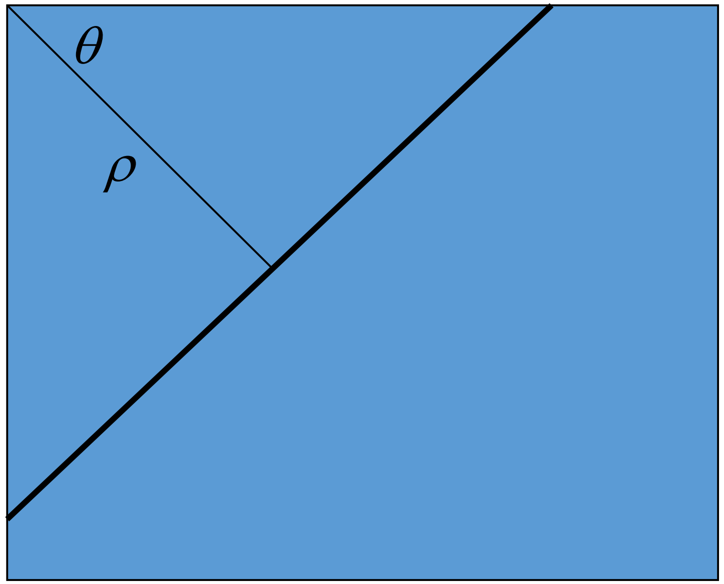
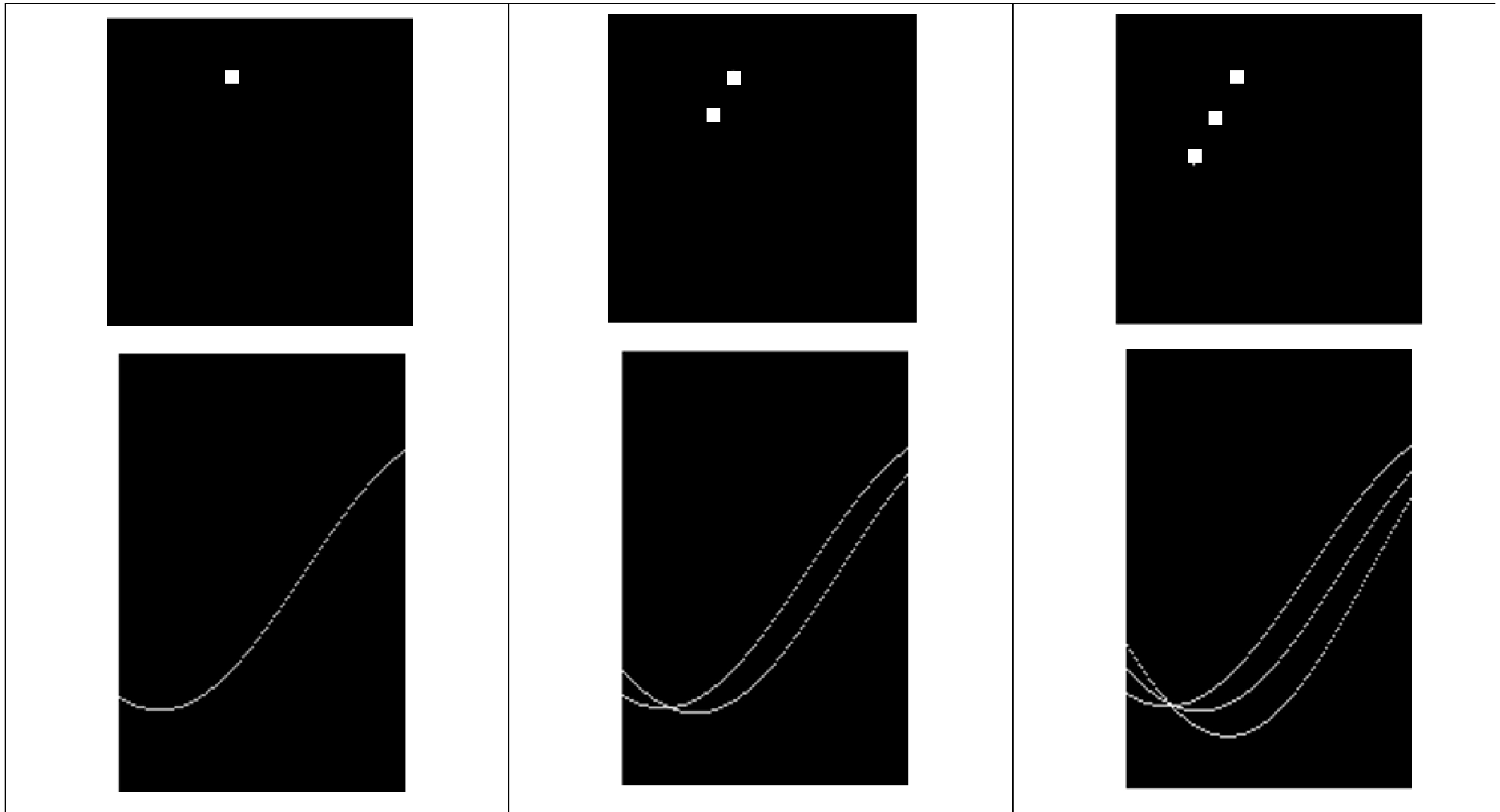


Image containing line

Images and the accumulator space of the polar Hough transform



(a) for one point	(b) for two points	(c) for three points

Applying the Hough transform

Takeaway time

1 – target shape defined by template

2 – and detected by template convolution

3 – optimal in occlusion and noise

4 – Hough transform gives same result, but faster

But shapes can be more complex than lines and not defined by an equations. That's next