Lecture 9 Finding More Shapes

COMP3204 Computer Vision

How can we go from conic sections to general shapes?

Book pp
254-259; 275-279

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Content

1. What more versions of the Hough transform are possible?
2. What are its limits?
3. Can it be used to detect shapes that are not given by an equation?

Hough Transform for Circles

Again, it's duality: $(x - x_0)^2 + (y - y_0)^2 = r^2$

Points: x, y centre: x_0, y_0 radius: r

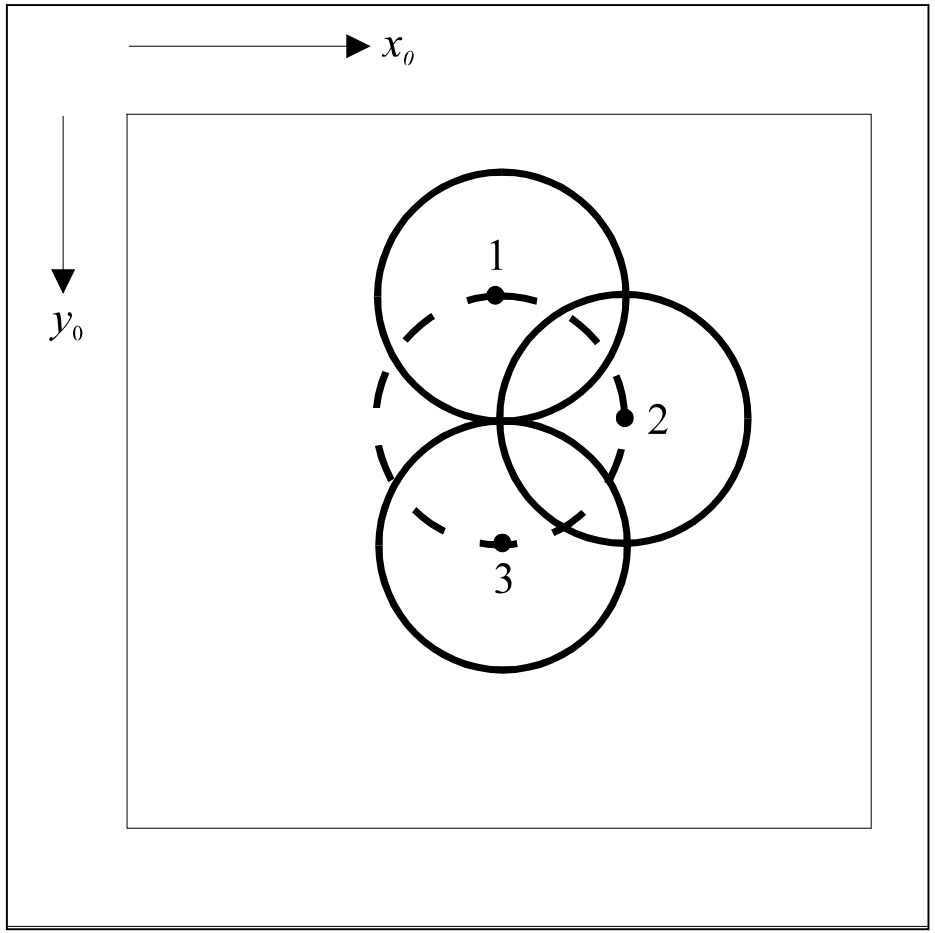
" x_0, y_0 " x, y " r

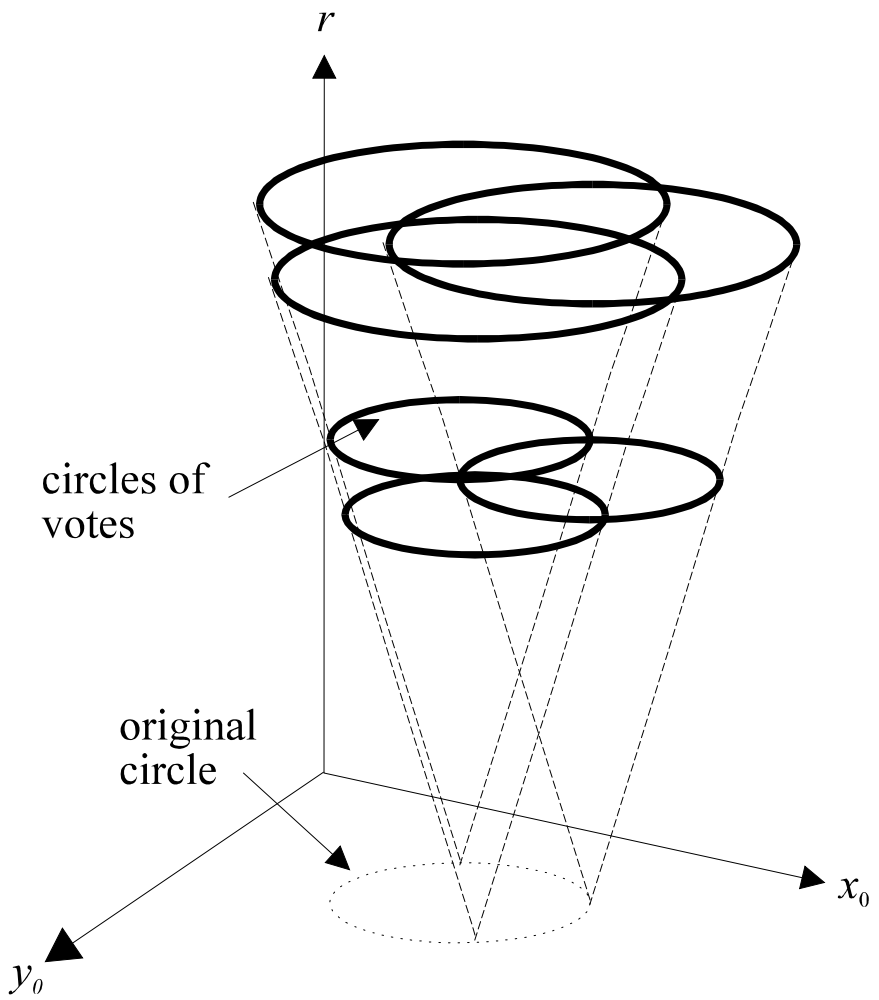
Let's translate if into code

Pseudocode

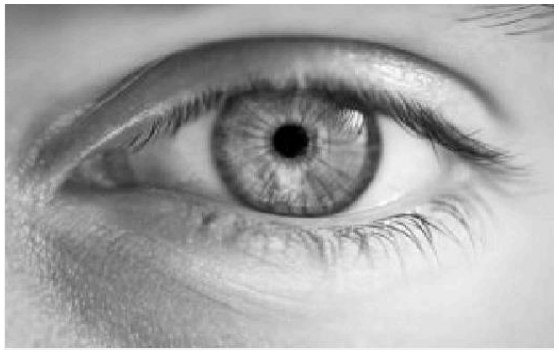
```
accum=0
for all x,y                                  !look at all points
    if edge(y,x)>threshold                   !check significance
        for r=min_r, max_r                   !do values of radius
            for theta = 1,2*pi               !go around a circle
                x0=x+r*cos(theta)            !generate x
                y0=y+r*sin(theta)            !generate y
                accum(y0, x0, r ) PLUS 1     !vote in accumulator
y0, x0, r= argmax(accum)                     !peak gives parameters
```

Circle Voting and Accumulator Space



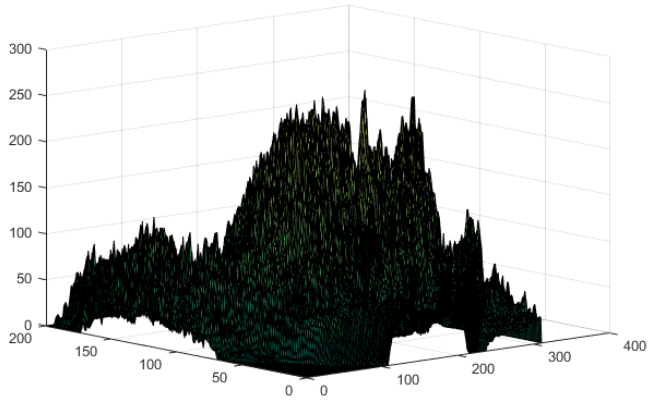


Applying the HT for circles

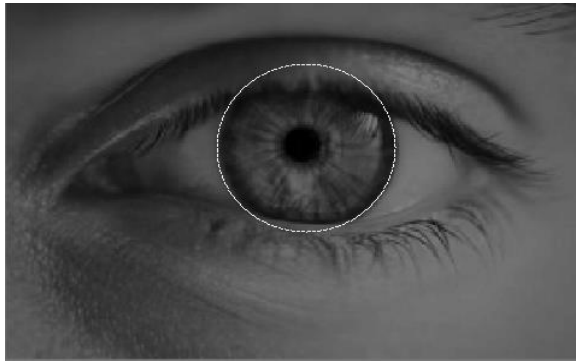


image

(Sobel) edges

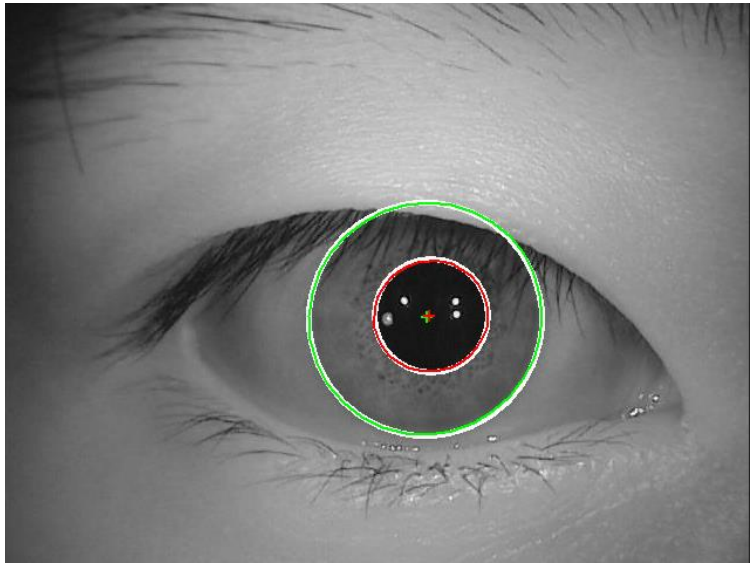


accumulator



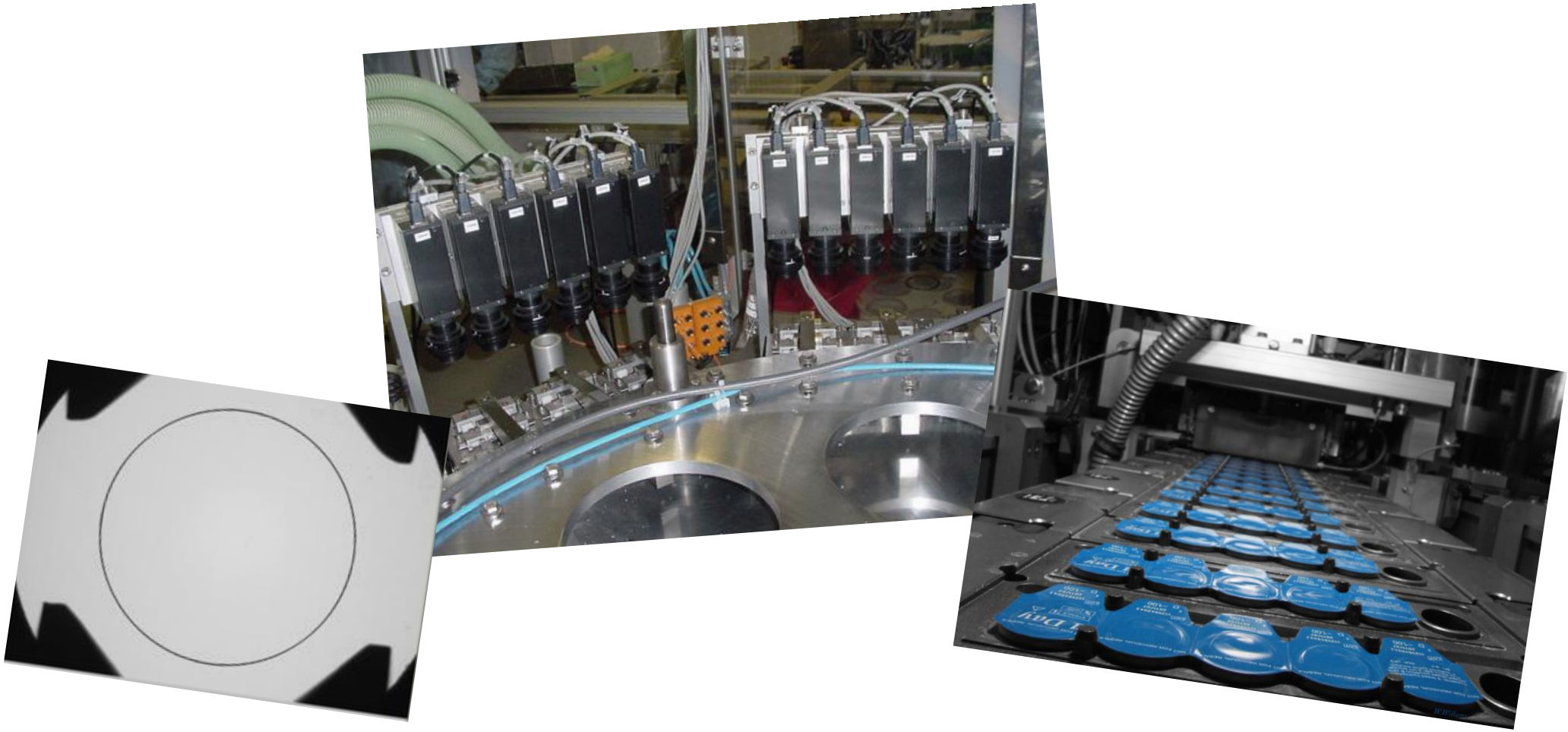
small and large circles

Integrodifferential operator?



https://stackoverflow.com/questions/27058057/comparing-irises-images-with-opencv

Contact lenses



Extensions to conic sections

Ellipse $$\frac{(x-x_0)^2}{a^2}+\frac{(y-y_0)^2}{b^2}=1$$

Described by 4 parameters. If each has 100 values,

accumulator size = $10^2 \times 10^2 \times 10^2 \times 10^2 = 10^8$=0.1GB

Add rotation, that's 10GB …. Ouch!

Motivates approaches to save memory and improve speed (since result is optimal)

Speeding it up…..

Now it's a 3D accumulator, fast algorithms are available

E.g. by differentiation

Differentiating $(x-x_0)^2+(y-y_0)^2=r^2$ gives $\frac{dy}{dx}=-\frac{(x-x_0)}{(y-y_0)}$

Substitute back into Eqn. for circle

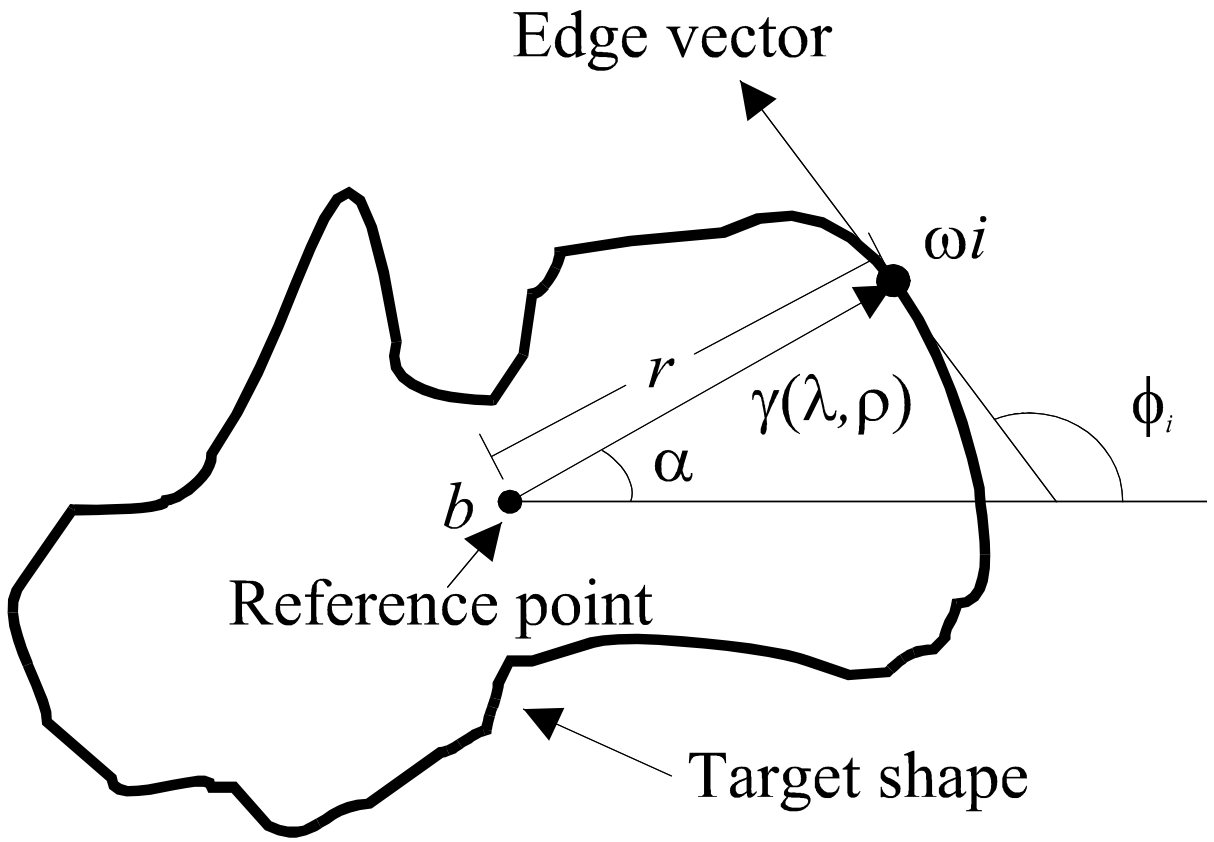
$$\left(\frac{dy}{dx}\right)^2(y-y_0)^2+(y-y_0)^2=r^2$$ 2D accumulator

$$y-y_0=\frac{r}{\sqrt{1+\left(\frac{dy}{dx}\right)^2}}$$ This is the edge direction

Arbitrary Shapes

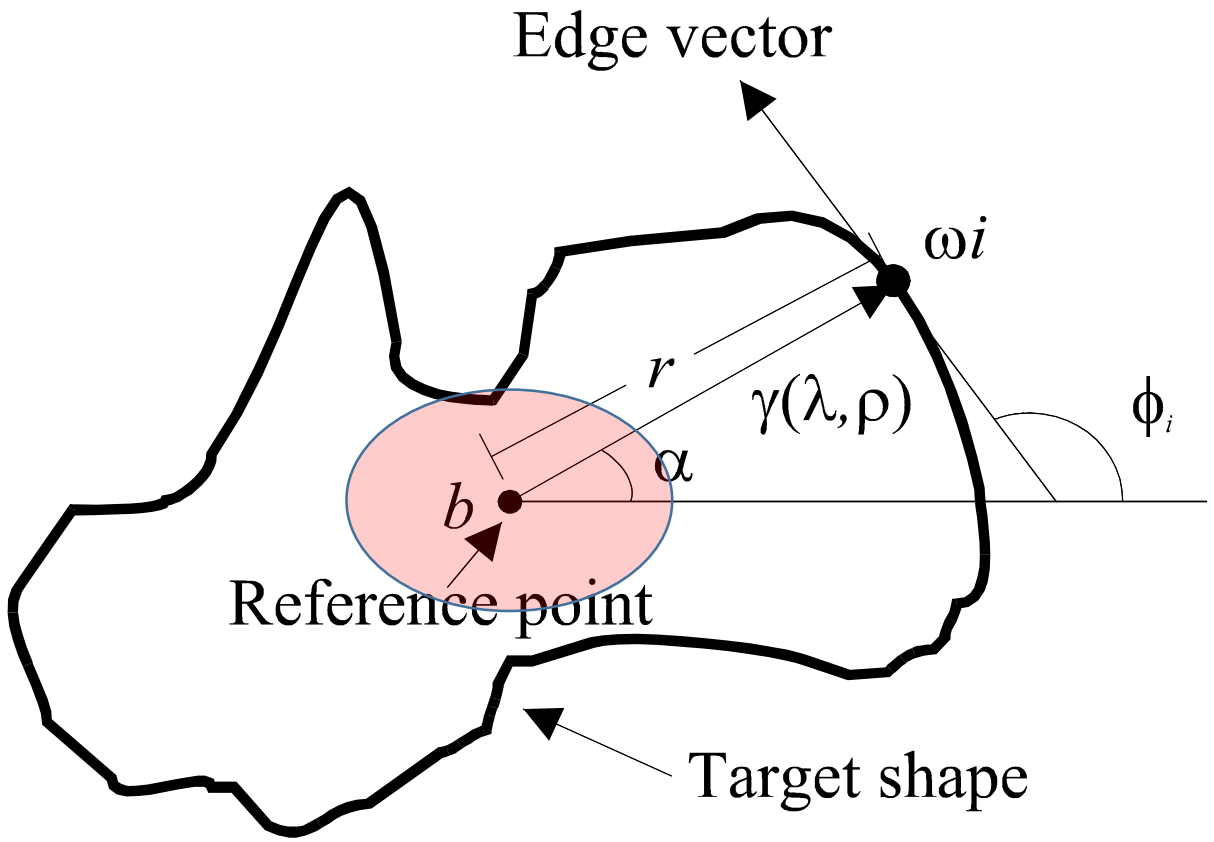
- Use Generalised HT
- Form (discrete) look-up-table (R-table)
- Vote via look-up-table

R-table Construction



$\hat{\varphi}_i'$	$\gamma = (r, \alpha)$
0	$(r_0, \alpha_0), (r_1, \alpha_1), (r_2, \alpha_2)$
$\Delta\phi$	⋮
$2\Delta\phi$	⋮
…	…

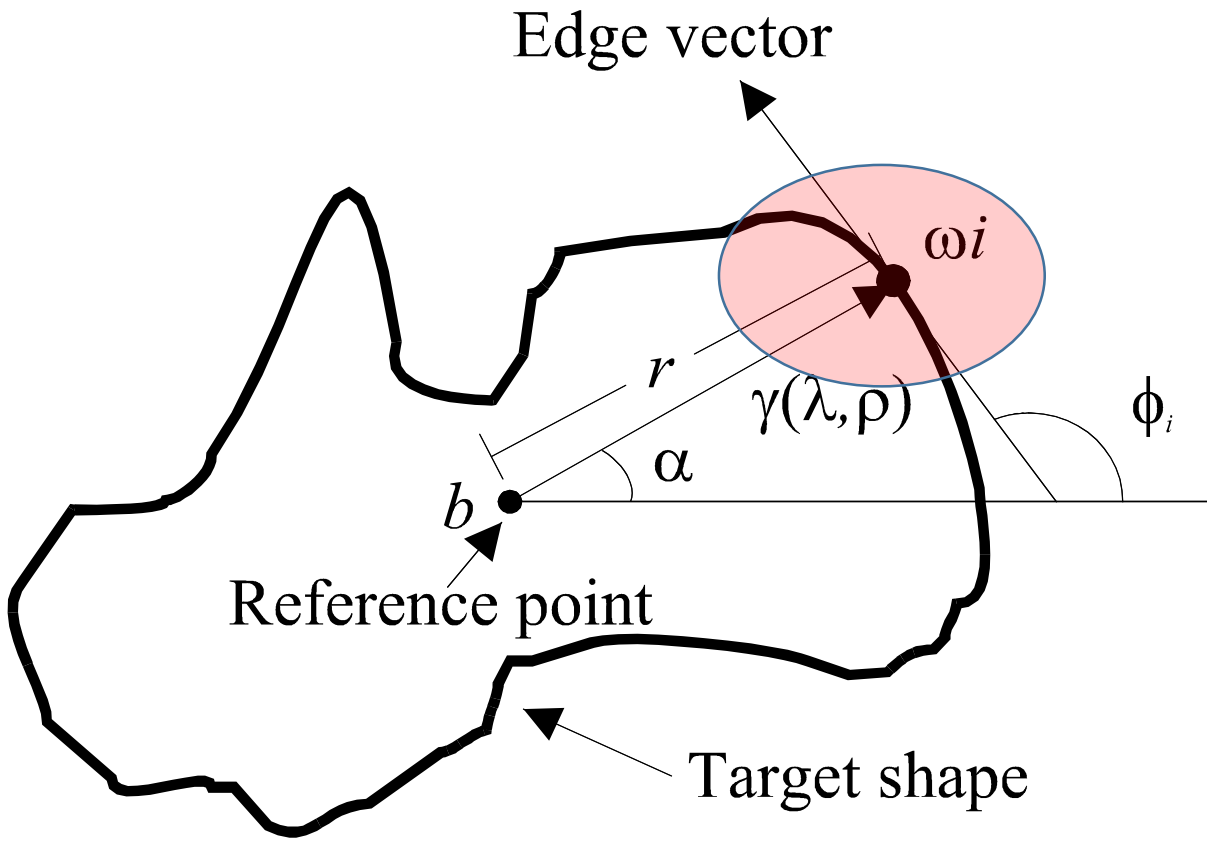
R-table Construction



$\hat{\varphi}_i'$	$\gamma = (r, \alpha)$
0	$(r_0, \alpha_0), (r_1, \alpha_1), (r_2, \alpha_2)$
$\Delta\phi$	⋮
$2\Delta\phi$	⋮
…	…

Need to start somewhere

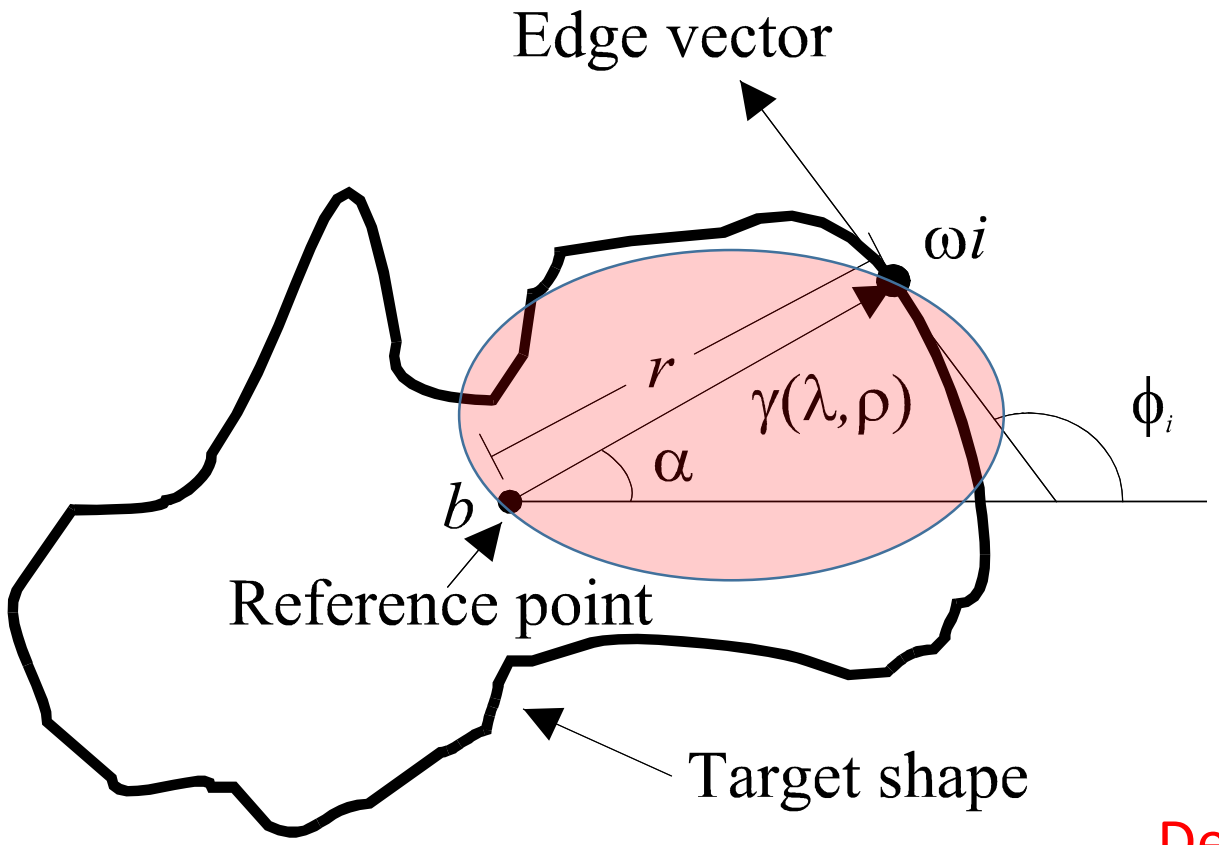
R-table Construction



$\hat{\varphi}_i'$	$\gamma = (r, \alpha)$
0	$(r_0, \alpha_0), (r_1, \alpha_1), (r_2, \alpha_2)$
$\Delta\phi$	⋮
$2\Delta\phi$	⋮
…	…

Measure edge direction

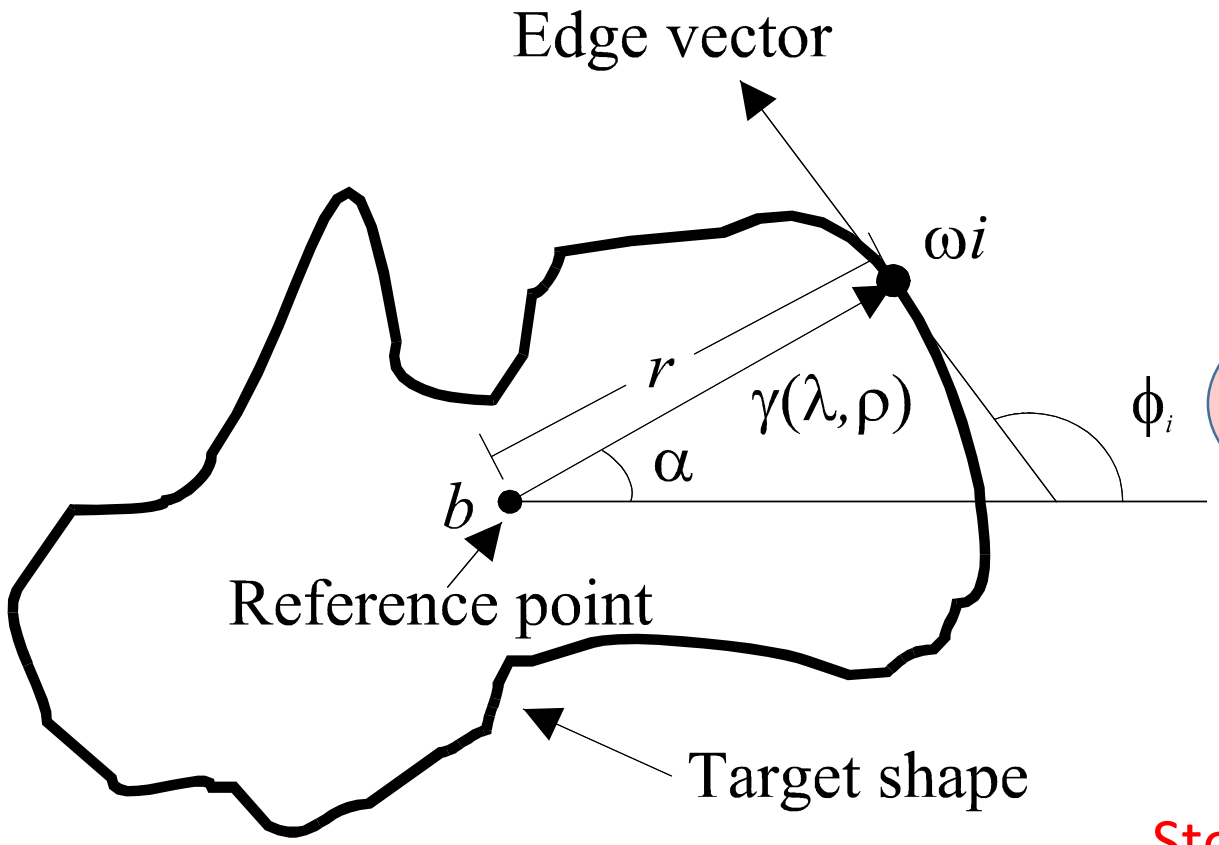
R-table Construction



$\hat{\varphi}_i'$	$\gamma = (r, \alpha)$
0	$(r_0, \alpha_0), (r_1, \alpha_1), (r_2, \alpha_2)$
$\Delta\phi$	⋮
$2\Delta\phi$	⋮
…	…

Determine length and direction to reference point

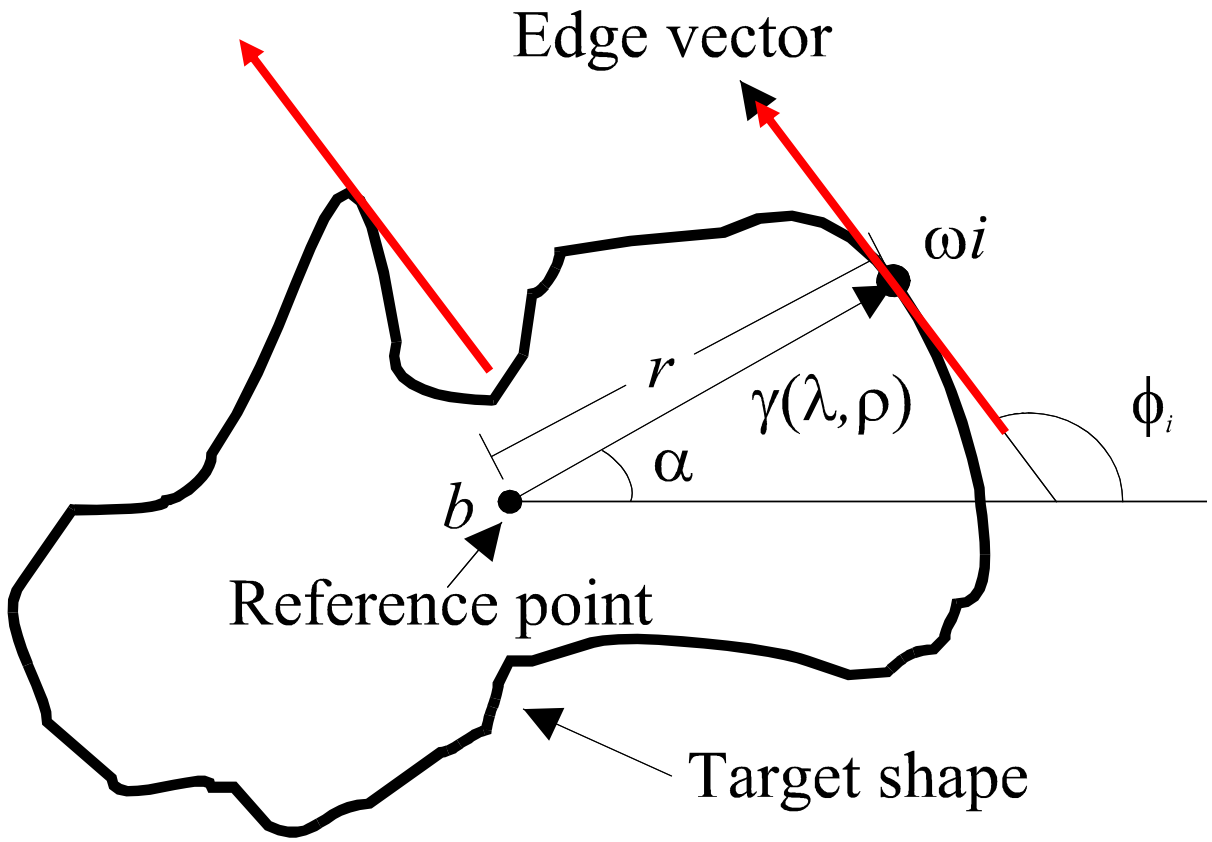
R-table Construction



$\hat{\varphi}_i'$	$\gamma = (r, \alpha)$
0	$(r_0, \alpha_0), (r_1, \alpha_1), (r_2, \alpha_2)$
$\Delta\phi$	⋮
$2\Delta\phi$	⋮
…	…

Store length and direction indexed by edge direction

R-table Construction



$\hat{\varphi}_i'$	$\gamma = (r, \alpha)$
0	$(r_0, \alpha_0), (r_1, \alpha_1), (r_2, \alpha_2)$
$\Delta\phi$	⋮
$2\Delta\phi$	⋮
…	…

Edge direction is not a unique description
Gives noise in accumulator

Procedure for GHT

1. Determine centre of template shape
2. Form R-table from template shape
3. Use R-table to vote for points in the real image

```
For edge points > threshold
Get edge direction(x,y)
For all R-table entries with direction(x,y)
   Vote in accumulator (@distance, @direction)
```

4. `Argmax(accumulator)` gives centre co-ordinates of shape

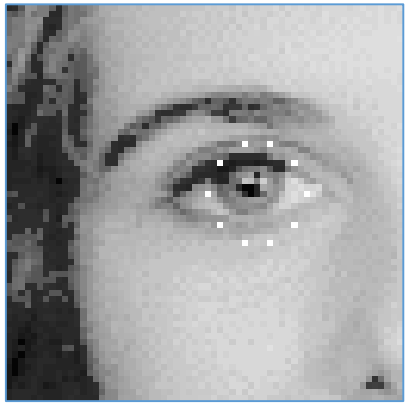
Arbitrary Shapes

- Use Generalised HT
- Form (discrete) look-up-table (R-table)
- Vote via look-up-table
- Scale? scale R-table voting
- Orientation? Rotate R-table voting
- Inherent problems with discretisation

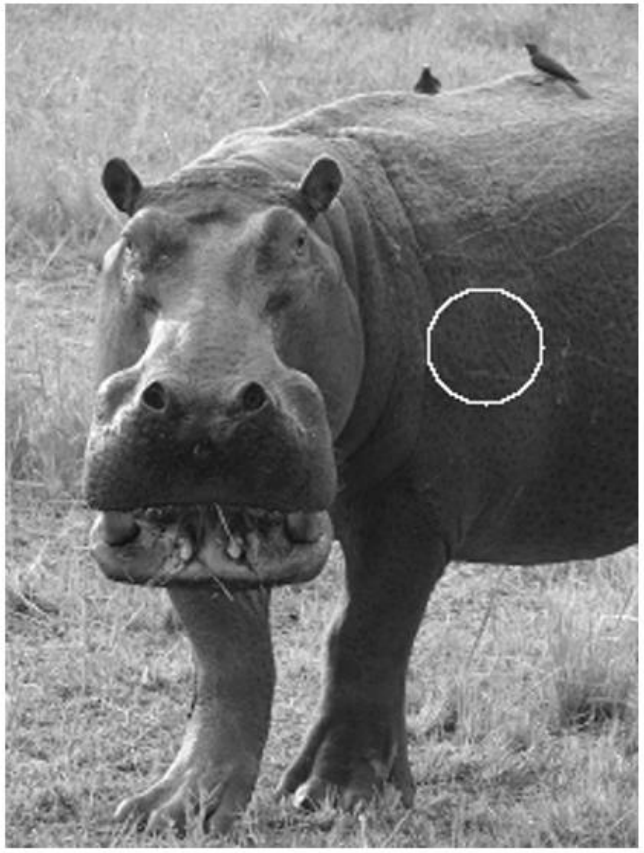
Visual inspection

Active Contours

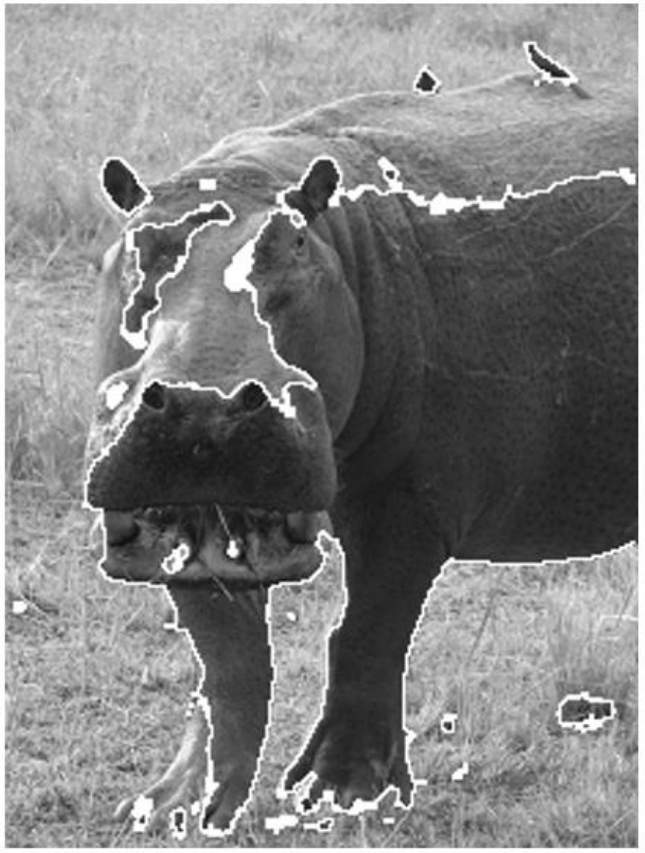
- For unknown arbitrary shapes: extract by evolution
- Elastic band analogy
- Balloon analogy
- Discrete vs. continuous
- Volcanoes?




Geometric active contours



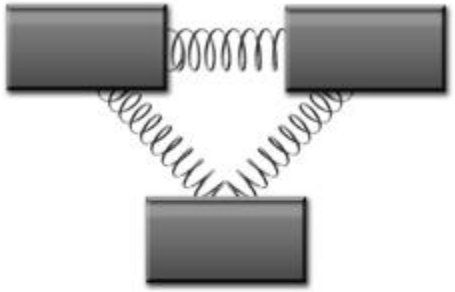
(a) initialisation



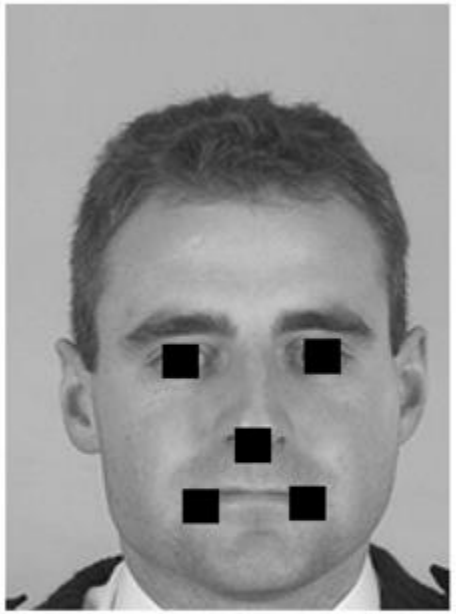
(b) result

Extraction by a Level-Set Based Approach

Parts-based shape modelling



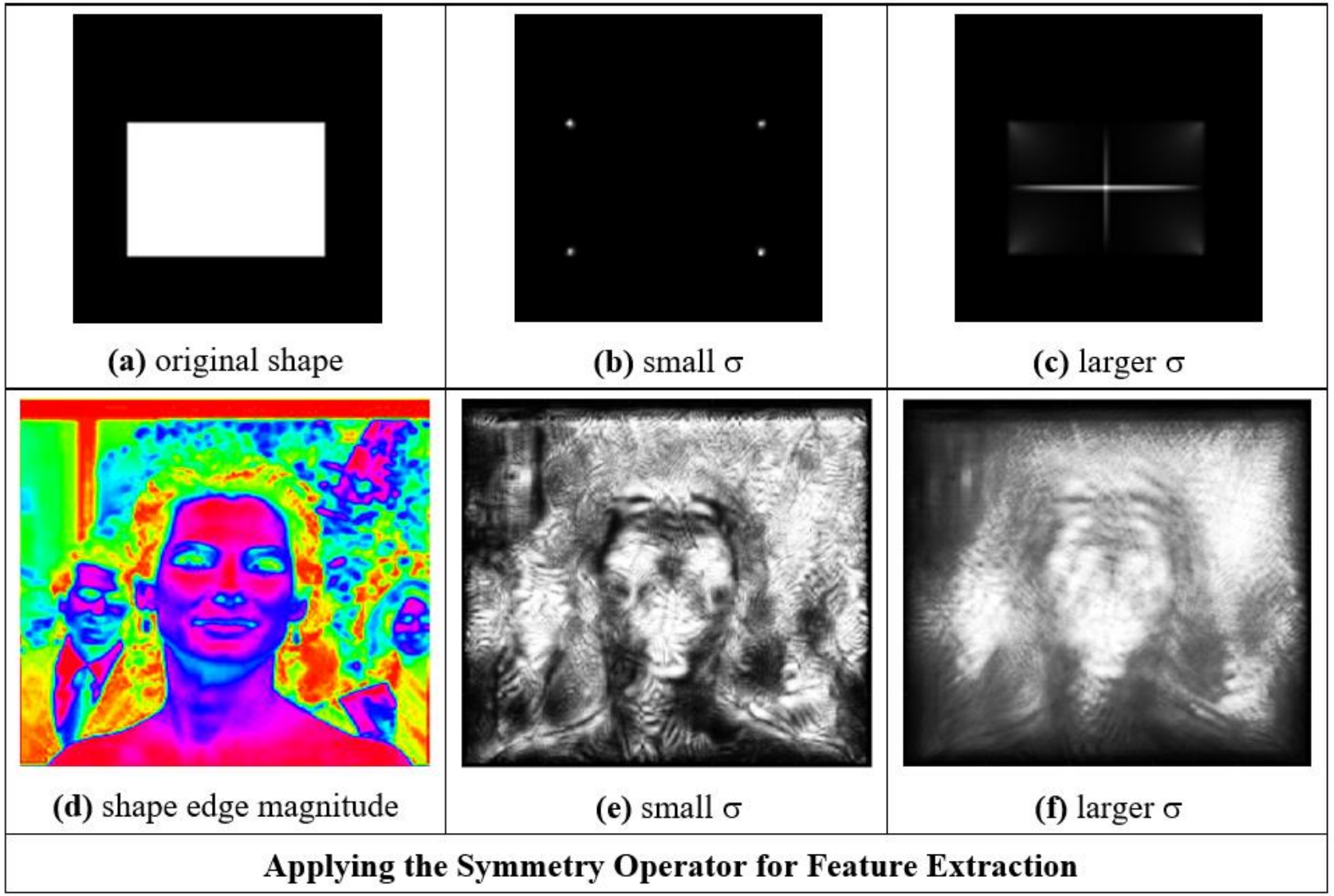
(a) mechanical equivalent



(b) finding face features

Parts-based Shape Model

Symmetry



Applying the Symmetry Operator for Feature Extraction

Takeaway time

1 – conic sections become more complex and take more time

2 – can use Generalised Hough Transform for complex shapes

3 – shape detection IS computer vision. Many more approaches

Let’s see how computer vision can work