

DC/DC Converters

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1. Buck Converter

A step-down DC/DC converter will be used in regulated power supply. The specifications are; the input voltage range is 12-24 V and the output voltage is fixed at 5 V. The output voltage control is maintained by means of feedback control. The switching frequency is selected as 500 kHz. The L and C filter components are given as 5 μ H and 10 μ F. Assume ideal components, ignore all parasitic effects and assume ideal switches.

a) Find the load current that guarantees CCM operation under all operation conditions. Don't just use the formula; derive your steps.

b) Assume that rated output power is 15 W. Calculate the maximum inductor current ripple and output voltage ripple for the given input voltage range.

c) Simulate the steady-state behaviour of the converter and show the important waveforms for boundary conduction mode with 24 V of input voltage. Plot following waveforms and comment on the results.

- Inductor voltage and current
- Output voltage
- Diode voltage and current
- Switch voltage and current

d) Repeat part-c with 12 V input and 1 W output power. Comment on the results.

e) What is inrush current, define it. Considering the case in part-d, what is your inrush current at input current for this case. Propose a method to avoid inrush current and implement your solution to your simulation model. Compare the results by plotting the cases in this part and part-d.

f) Now, consider that the output capacitor has 50 m Ω ESR. Simulate the converter for boundary conduction mode with 24 V of input voltage. Compare the results with ideal case of part-c. Comment on the effect of adding capacitor ESR to the converter parameters such as output voltage ripple. Also, offer a solution to decrease the equivalent ESR of the output capacitor and to reduce the output voltage ripple.

- a) Find the load current that guarantees CCM operation under all operation conditions.
Don't just use the formula; derive your steps.

The question is asking us to ensure the system is continuing in CCM for any condition.

That means, the current value should be always higher than $I_{LB(MAX)}$ (Boundary current that separates CCM and DCM)

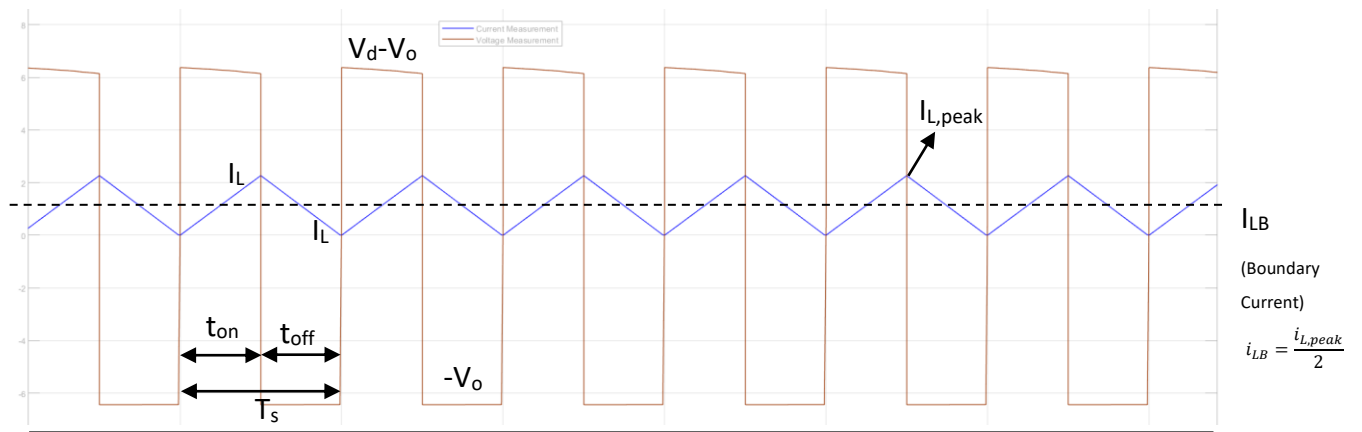


Figure 1. Buck Converter Inductor Current & Voltage Waveform

$$i_L = \frac{1}{L} \int V_L dt + i_o$$

$$i_{L,peak} = \frac{1}{L} \int (V_d - V_o) dt + i_o$$

$$i_{LB} = \frac{i_{L,peak}}{2} \rightarrow I_{LB} = \frac{t_{on} \cdot (V_d - V_o)}{2L}$$

$$I_{LB} = \frac{D \cdot T_s \cdot (V_d - V_o)}{2L}$$

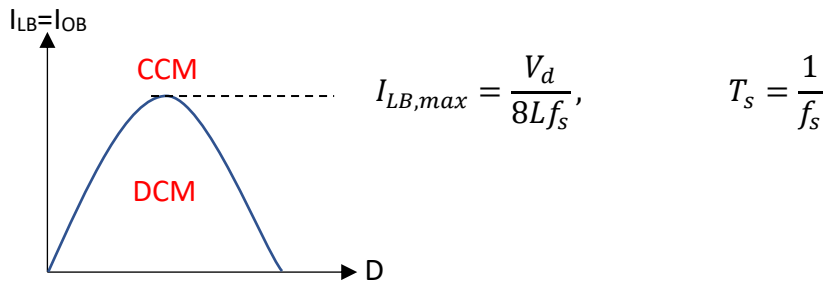
In buck converter, $V_o = D \cdot V_d$

$$I_{LB} = \frac{D \cdot T_s \cdot V_d (1 - D)}{2L}$$

Boundary current between
Continuous Conduction Mode & Discontinuous Conduction Mode

When $D = 0.5$

$$I_{LB,max} = \frac{T_s \cdot V_d}{8L}$$



If it is needed to stay in CCM longer, either L should be increased or higher switching frequency or V_d should be reduced.

For 12V V_d , $I_{LB,max} = \frac{12}{8 \times 5 \times 10^{-6} \times 500 \times 10^3} = 0.6A$

For 24V V_d , $I_{LB,max} = \frac{24}{8 \times 5 \times 10^{-6} \times 500 \times 10^3} = 1.2A$

To guarantee CCM operation under both conditions, $I_{LB,max}$ should be 1.2A. That means, the inductor current should always be higher than 1.2A

- b) Assume that rated output power is 15 W. Calculate the maximum inductor current ripple and output voltage ripple for the given input voltage range.

Assure $R = 1.66\Omega$. (To reach 15W rated output power)

First, we need to obtain transfer function of the plant system which is

$$G_p(s) = \frac{Y(s)}{u(s)} \frac{V_i}{LCs^2 + \frac{L}{R}s + 1}$$

Put our passive parameters value into the equation above

Calculate for $V_i = 12V$ (It's OK for $V_i = 24V$)

$$G_p(s) = \frac{Y(s)}{u(s)} \frac{12}{50 \times 10^{-12} s^2 + \frac{5 \times 10^{-4}}{166} s + 1}$$

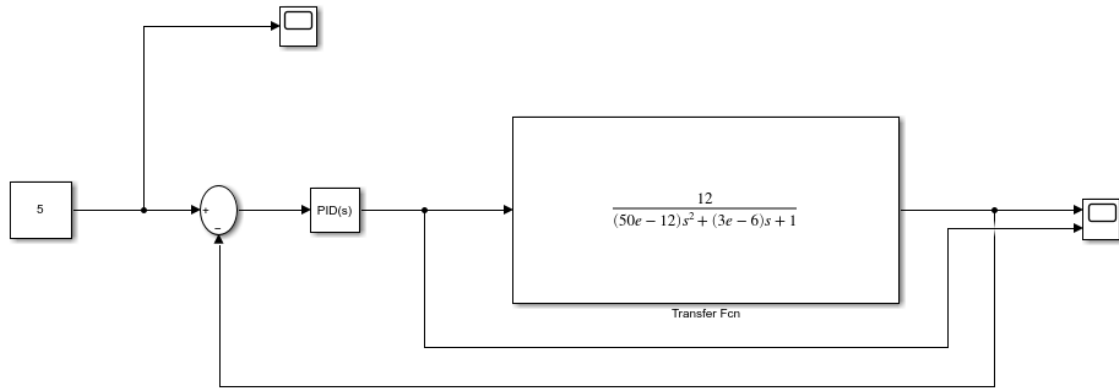
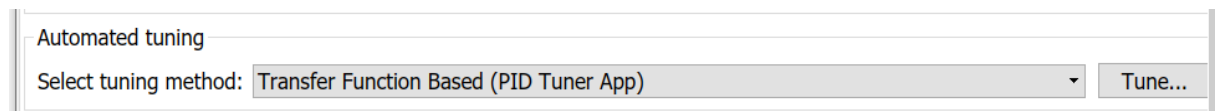


Figure 2. Design of PID Controller for Feedback Control

We design our transfer function in the MATLAB/Simulink. To adjust PID Controller, there is an option for autotune in property in the PID controller:



When it is pressed to Tune button, the screen will be opened:

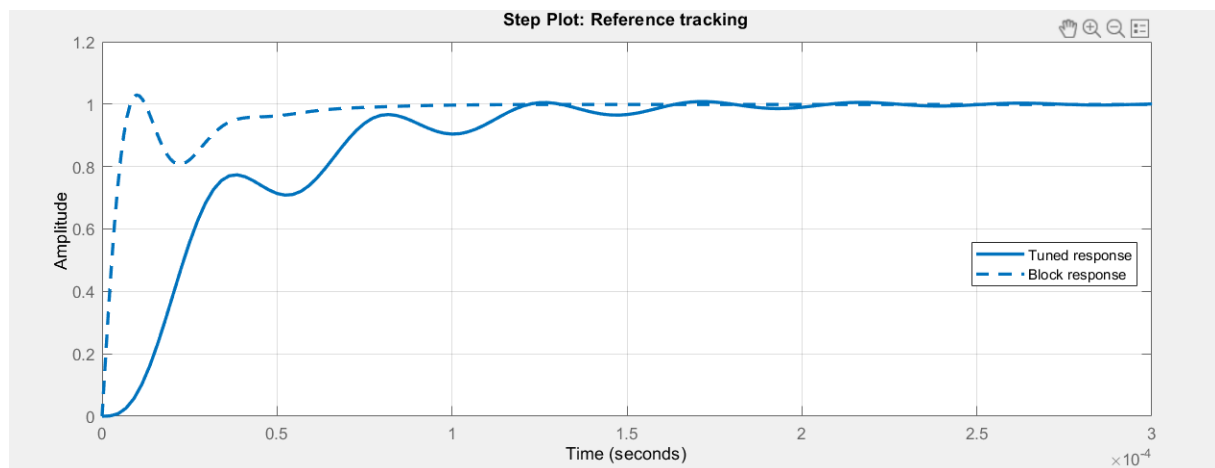


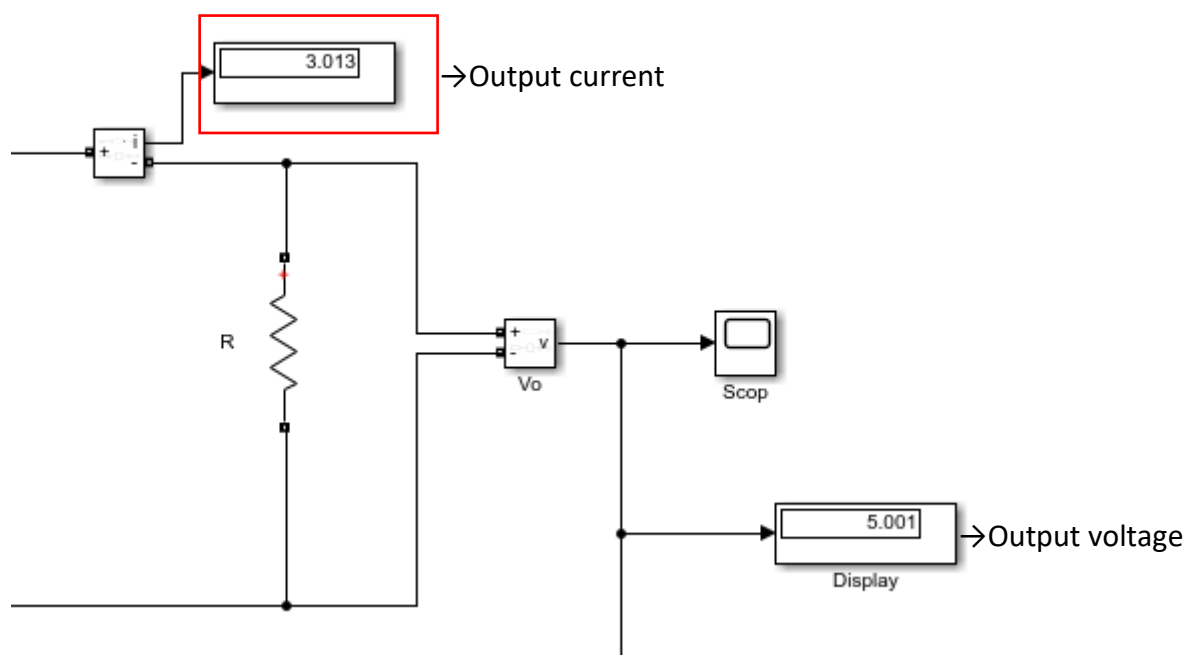
Figure 3. PID Tuner

In the PID Tuner, the dashed waveform is already belongs to the designed system, when it is designed and updated block, the PID tuner will give the parameters of P,I,D, and N. The key factor here is the adjusting overshoot and finding desired waveform. The values will be given by PID Tuner:

Main	Initialization	Output Saturation	Data Types	State Attributes
Controller parameters				
Source:	internal			
Proportional (P):	0.193023461102604			
Integral (I):	11345.4466552033			
Derivative (D):	8.10525057340423e-07			
<input checked="" type="checkbox"/> Use filtered derivative				
Filter coefficient (N):	33123779.7603993			

Figure 4. PID Parameters

When the parameters is applied to the feedback control, the output voltage and the output current values are measured:



- The second part of the question is calculate the maximum inductor current ripple and output voltage ripple for the given input voltage range.

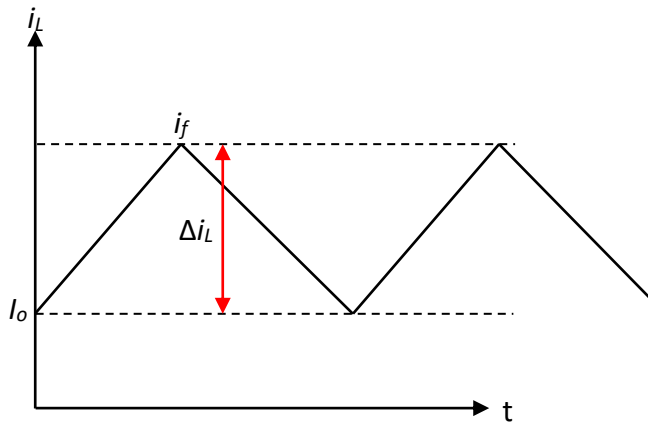
Inductor Current Ripple

Our $V_o = 5V$, $V_i = 12/24V$

$$V_o = D \cdot V_i$$

$$\text{For } V_i = 12V \rightarrow D = \frac{5}{12} = 0.42$$

$$\text{For } V_i = 24V \rightarrow D = \frac{5}{24} = 0.21$$



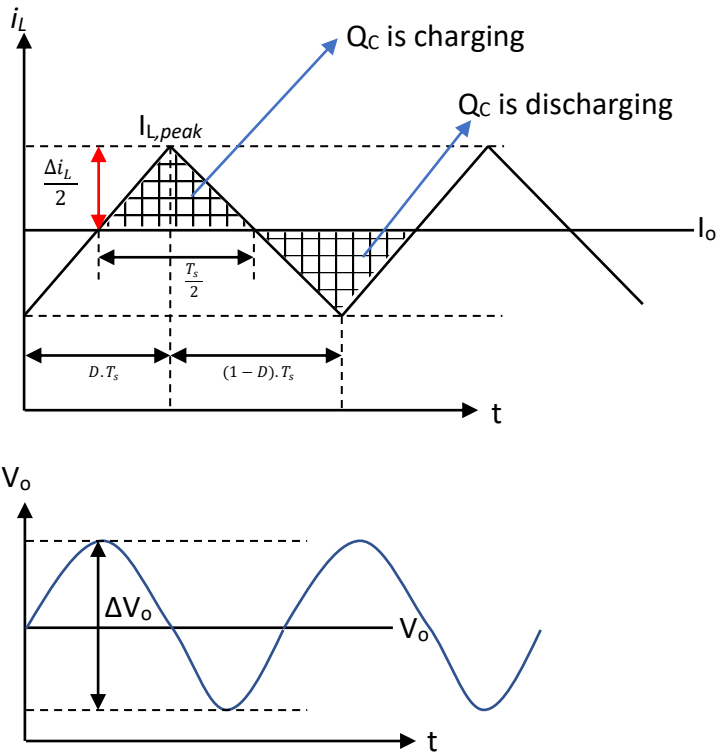
$$i_f = \frac{1}{L} \int V_L dt + I_o$$

$$I_f - I_o = \Delta i_L = \frac{1}{L} \int V_L dt = \frac{V_i - V_o}{L} D \cdot T_s \text{ or } \frac{V_o(1-D)}{L \cdot f_s}$$

$$\Delta i_L = \frac{5(1 - 0.42)}{5\mu * 500k} = 1.16A \text{ for } V_i = 12V$$

$$\Delta i_L = \frac{5(1 - 0.21)}{5\mu * 500k} = 1.58A \text{ for } V_i = 24V$$

Output Voltage Ripple



$$Q = \int i_C dt$$

$$\Delta Q = \frac{\frac{\Delta I_L}{2} \cdot \frac{T_s}{2}}{2} = \frac{T_s \cdot \Delta I_L}{8}$$

$$\Delta V_o = \frac{\Delta Q}{C} = \frac{T_s \cdot \Delta I_L}{8C}$$

$$\text{Using off time } (1-D) \rightarrow \Delta I_L = \frac{V_o \cdot (1-D) T_s}{L}$$

$$\Delta V_o = \frac{T_s \cdot V_o (1-D) T_s}{8LC}$$

$$\Delta V_o = \frac{T_s^2 \cdot V_o (1-D)}{8LC}$$

$$\Delta V_o = 0.029V \text{ for } V_i = 12V$$

$$\Delta V_o = 0.0395V \text{ for } V_i = 24V$$

- c) Simulate the steady-state behaviour of the converter and show the important waveforms for boundary conduction mode with 24 V of input voltage. Plot following waveforms and comment on the results.

- Inductor voltage and current

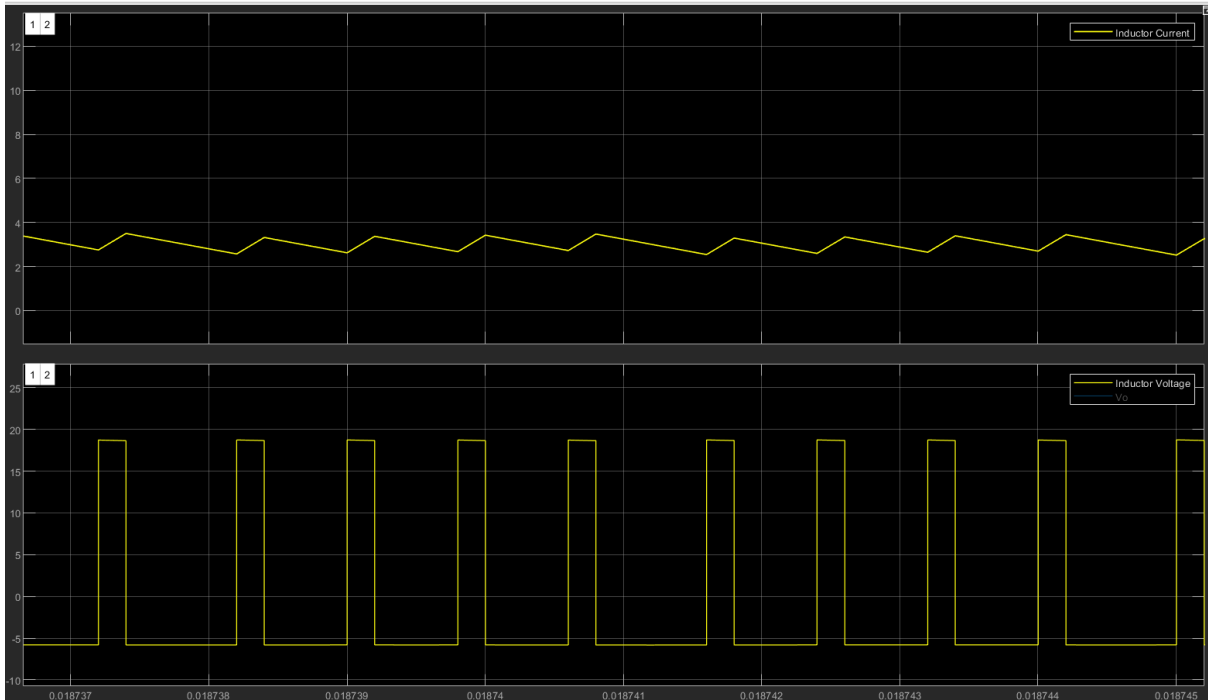


Figure 5. Inductor current & voltage

Comments: As it is showed in the graph above, Inductor current increases during ON operation, and $V_L = V_i - V_o$ that means $V_L = 24 - 5 = 18V$ during ON op.

1	0.019	1.867e+01
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From the measurement, we can see $V_L = 18.67V$. It is a bit different from ideal case because of parameters which we did not include in ideal case.

And during OFF op., $V_L = -V_o$. It is expected that V_L is -5V during OFF op.

2	0.019	-5.820e+00
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The measurement says the inductor voltage during OFF op., is -5.8V

- Output voltage

Output voltage is 5V always because feedback control provides fixed output voltage from the various input voltage (12/24V).

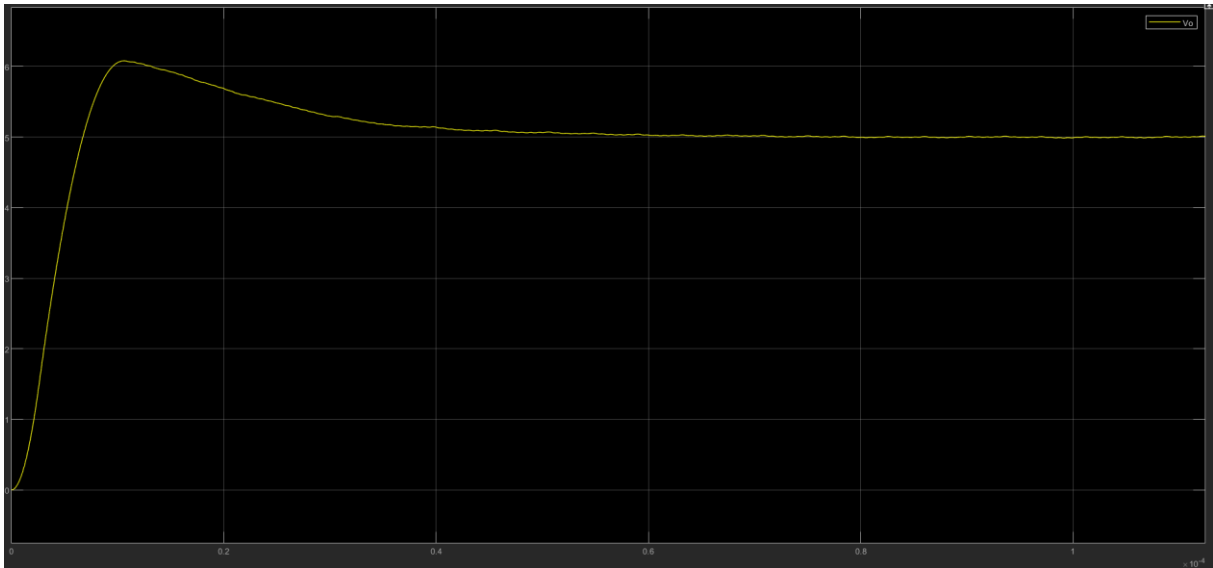


Figure 6. Output Voltage Waveform

As the system is designed like critically damped (desired one). The output voltage waveform is smooth and less ripple as compared to other types.

- Diode voltage and current

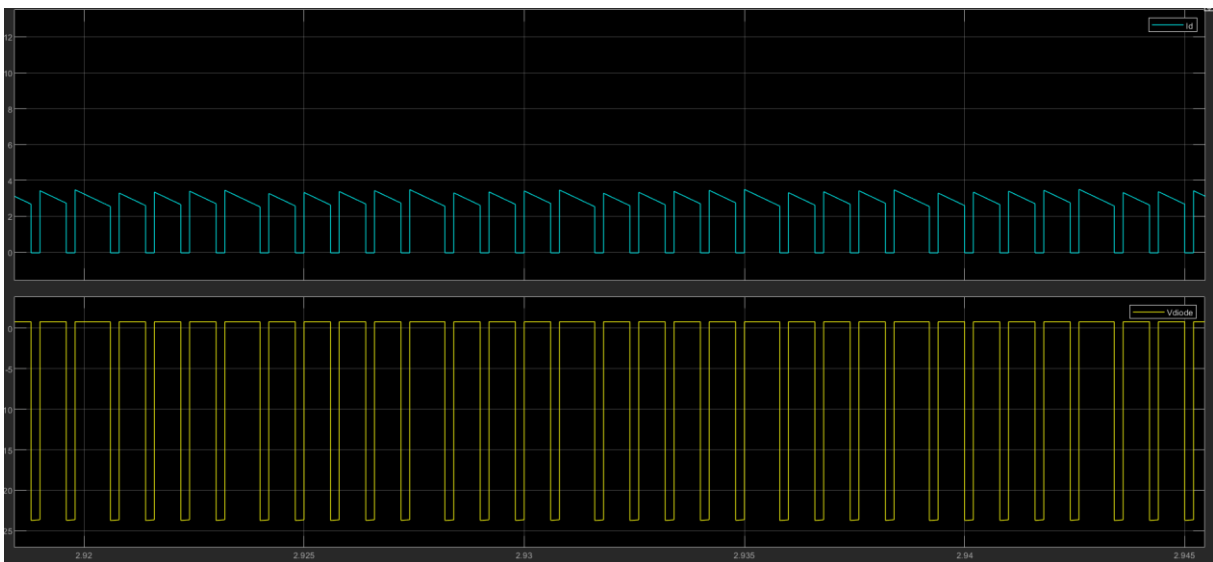


Figure 7. Diode Current & Voltage Waveforms

It can be stated that during ON time, there is no current flow through the diode $I_{diode} = 0A$ because it is reverse biased. In OFF condition, voltage across the diode is $V_{diode} = -V_i = -24V$. The diode current is like discharging because of the inductor.

- Switch voltage and current,

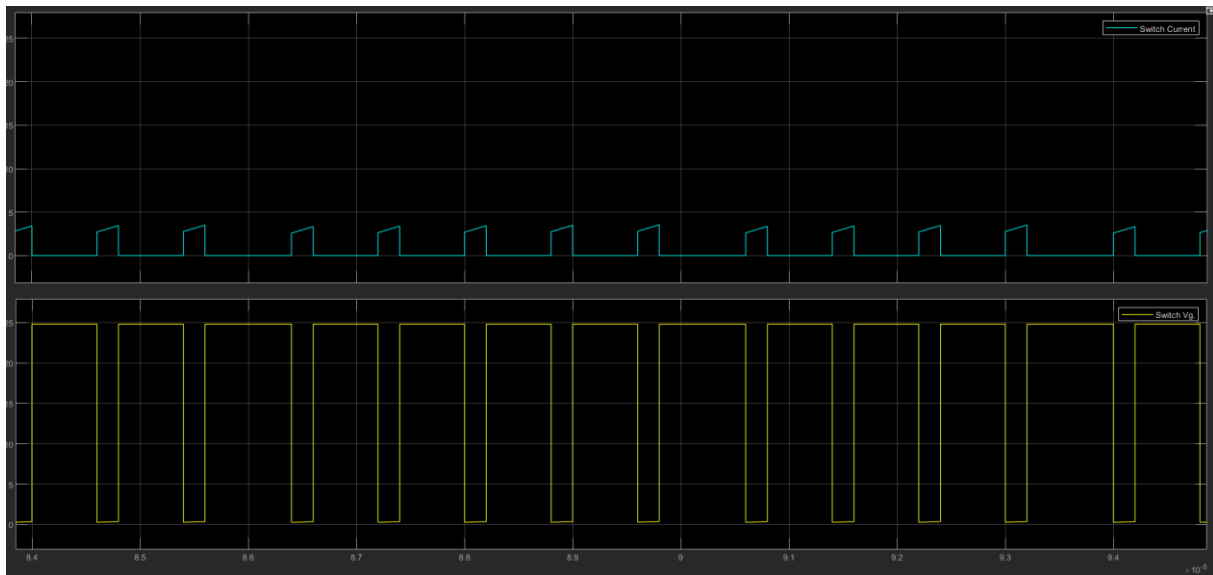


Figure 8. Switch Voltage & Current Waveforms

The switch current is varying between 2.577A and 3.325A. The variation happens due to inductor. During ON time, the switch voltage is 0.3V (ideal case is 0V). During OFF time, the switch voltage is 24.8V (ideal case is $24V = V_i$)

- Repeat part-c with 12 V input and 1 W output power. Comment on the results.

- Inductor voltage & current

The load resistance is adjusted to 25Ω to get 1W output power. The waveforms of the inductor voltage and current:

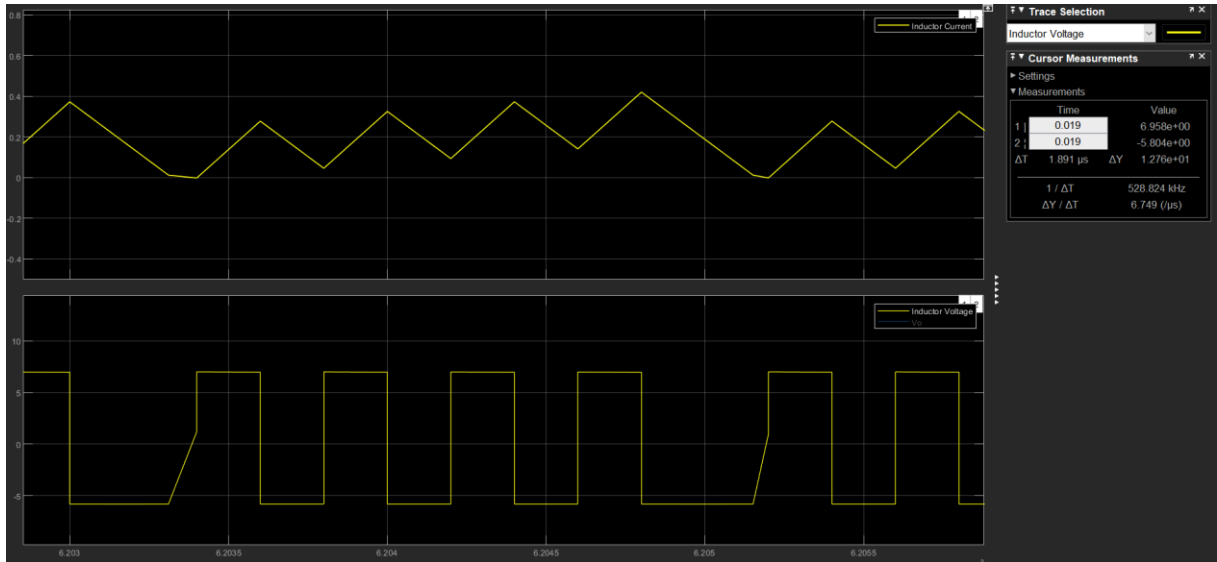


Figure 9. Inductor voltage and current

It is very obvious that because the output resistance is increased, so the current value is decreased sharply. That means it is in DCM (Discontinuous Conduction Mode) now.

As it is found previous section

$$I_{LB,max} = \frac{V_d}{8Lf_s}$$

Above formula is being adapted in the current situation will be

$$I_{LB,max} = \frac{12}{8 \times 5 \times 10^{-6} \times 500 \times 10^3} = 0.6A$$

If the current value gets lower than $I_{LB,max} = 0.6A$ means the system goes into DCM.

- Output voltage

Because feedback control is still used, the output voltage value is to be not expected change.



Figure 10. Output voltage waveform

- Diode voltage & current

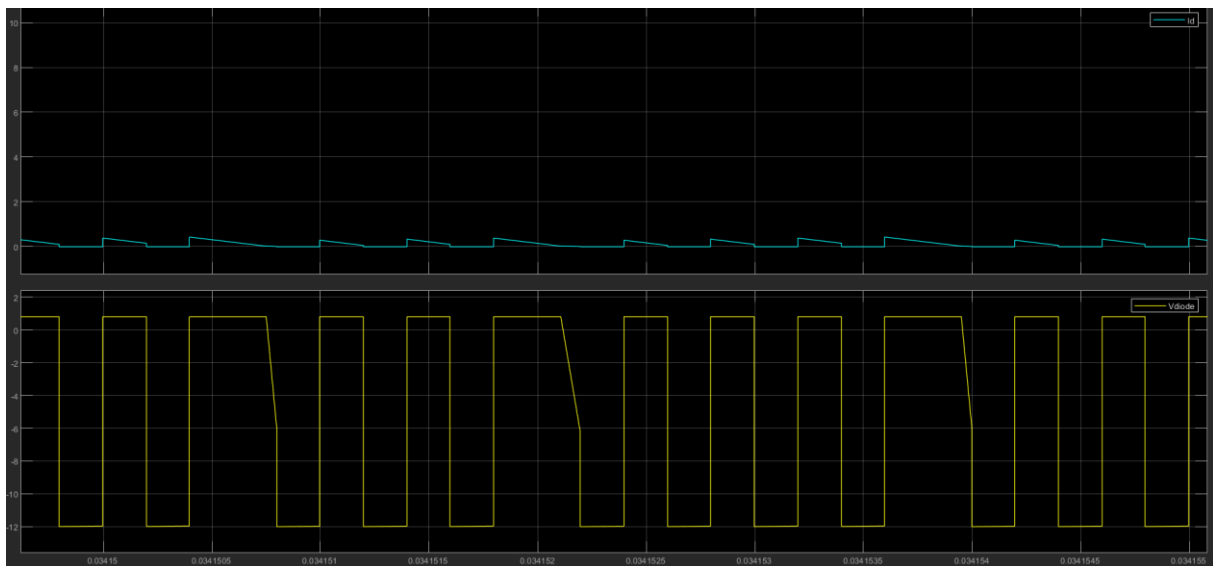


Figure 11. Diode voltage & current

- Switch voltage & current

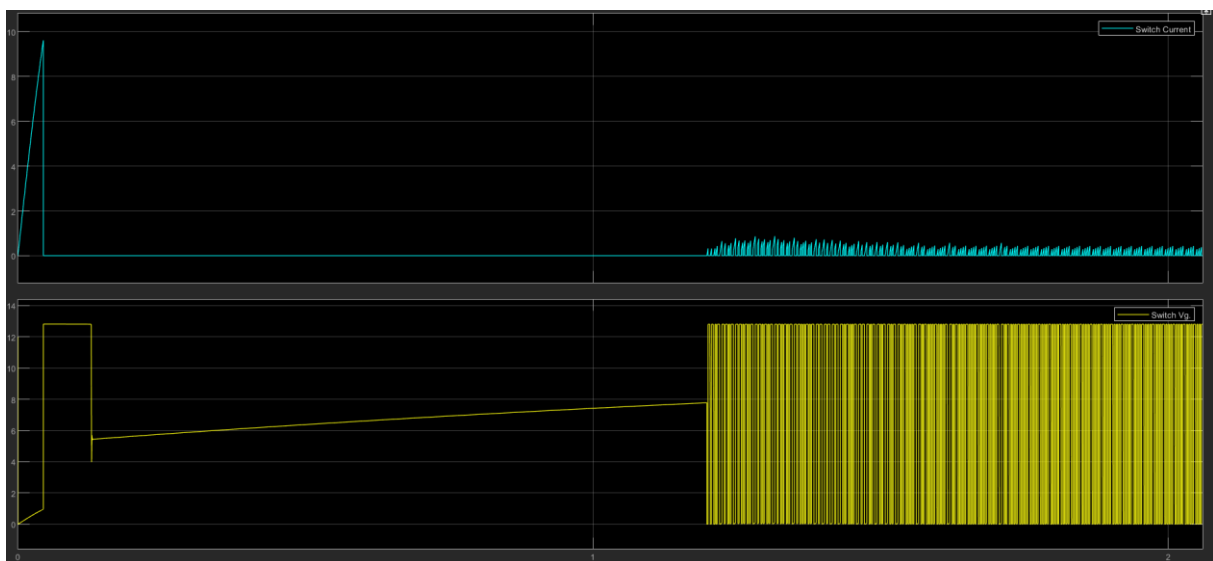


Figure 12. Switch voltage & current

As it can be observed from the graph, there is huge current draw at the start of the system. The huge current draw is called “*inrush current*”. It is peak value and dependent on characteristics of the input source and input impedance.

- e) What is inrush current, define it. Considering the case in part-d, what is your inrush current at input current for this case. Propose a method to avoid inrush current and implement your solution to your simulation model. Compare the results by plotting the cases in this part and part-d.

Inrush current in a DC-DC converter is the initial, high level of current that flows into the converter when it is first turned on. This high level of current is caused by the charging of the input capacitance and the output inductance of the converter. It is typically much higher than the steady-state operating current of the converter and can cause damage to the converter if not properly managed. Inrush current limiting is a common technique used to prevent this high level of current from causing damage.

Inrush current limiting is a technique used to prevent high levels of inrush current from damaging a DC-DC converter. There are several methods that can be used to limit inrush current, including using NTC thermistors, using series resistors, and using active circuits. Using a series resistor is a simple method to limit inrush current. A resistor is placed in series with the input of the converter to limit the current that can flow into it. The value of the resistor is chosen so that the inrush current is within safe limits. However, this method causes a voltage drop across the resistor and results in a loss of efficiency.

When a series resistor is added to the input of the converter, ($R = 10\Omega$). The switch voltage and current waveform will be

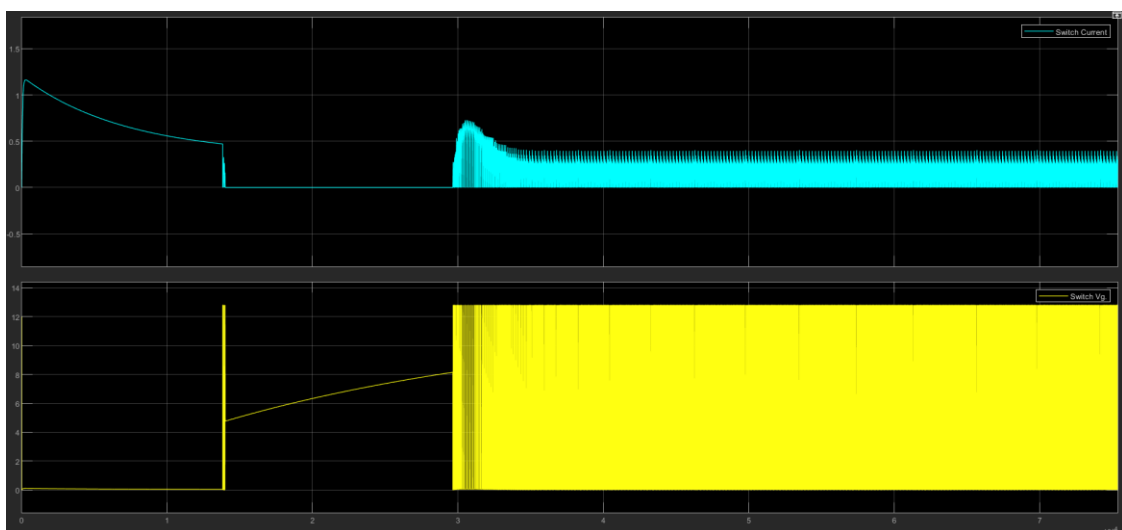


Figure 13. Switch voltage and current with a series resistor ($R = 10\Omega$)

- f) Now, consider that the output capacitor has 50 mΩ ESR. Simulate the converter for boundary conduction mode with 24 V of input voltage. Compare the results with ideal case of part-c. Comment on the effect of adding capacitor ESR to the converter parameters such as output voltage ripple. Also, offer a solution to decrease the equivalent ESR of the output capacitor and to reduce the output voltage ripple.

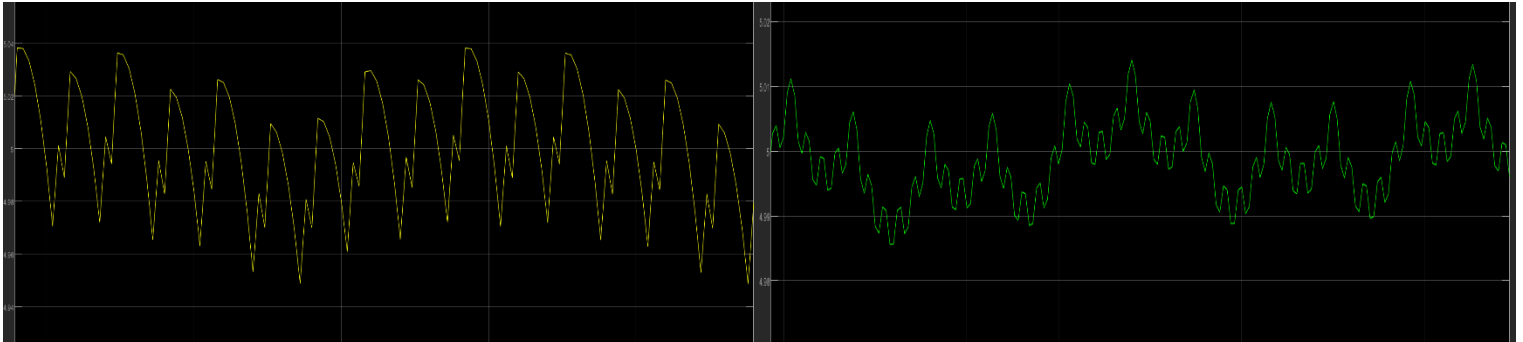
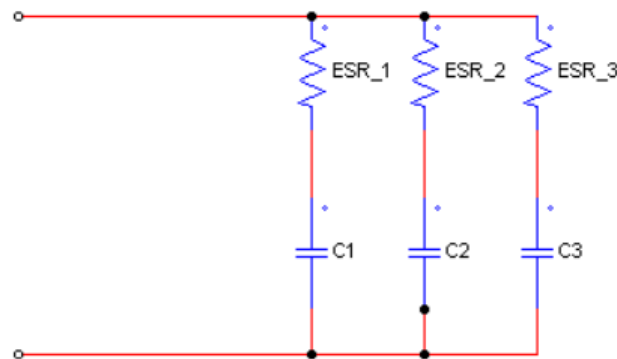


Figure 15. Output voltage waveform with capacitor with ESR

Figure 14. Output voltage waveform without capacitor with ESR

It is seen on the graph that capacitor with ESR increases the ripple at the output voltage. To reduce ESR, there is a method that is commonly used widely. That is connecting capacitor(s) in series with the capacitor.



$$C_{eq} = C_1 + C_2 + C_3$$

$$\frac{1}{ESR_{eq}} = \frac{1}{ESR_1} + \frac{1}{ESR_2} + \frac{1}{ESR_3}$$

The effect of ESR is reducing by connecting capacitors in parallel. For example, we have 10 μ F capacitor. It can be connected as two 5 μ F capacitors in parallel.

2. Boost Converter

In step-up DC/DC converter, let input voltage range be 5-12 V and output voltage be 16 V with switching frequency of 300 kHz. Assume that rated output power is 16 W.

a) Consider all components as ideal. Calculate minimum inductance that will keep the converter operating in the CCM operation for rated output power.

b) Calculate the output capacitance for peak-to-peak voltage ripple less than 2% under rated output power.

c) Simulate the steady-state behaviour of the converter and show the important waveforms for boundary conduction mode of part-a. Plot following waveforms and comment on the results.

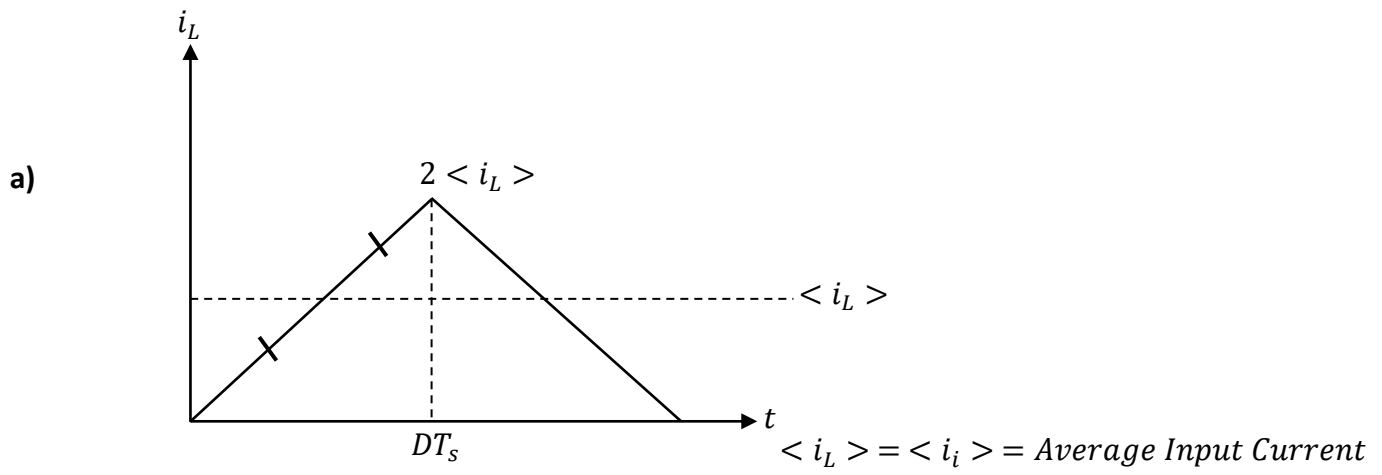
- Inductor voltage and current
- Output voltage
- Diode voltage and current
- Switch voltage and current

d) Assuming the switches and capacitors are ideal, but the inductor has 30 m Ω ESR, and considering the load resistance is equal to the rated load resistance, derive the voltage gain as a function of the duty cycle. Show your steps clearly. On the MATLAB, plot the voltage gain with and without ESR on the same graph as a function of duty cycle. Comment on the results.

e) Repeat the same steps in part-d for the converter efficiency.

f) Choose commercial semiconductor products using Digikey that is appropriate for your design. Calculate the losses on these devices for rated power operation with 12 V input voltage. How would losses on the diode and switch change if the duty cycle is increased? Explain in detail.

g) Using the calculated loss values, construct a thermal lumped element model and estimate the junction temperature without a heatsink. If necessary, choose a thermal interface material and heatsink and find out the junction temperature with these materials. Clearly state any assumption that you made.



$$V_L = L \frac{di_L}{dt} = L \frac{\Delta i_L}{\Delta t}$$

$$LV_L = V_L \frac{\Delta t}{\Delta i_L} = V_i \frac{\Delta T_s}{\Delta i_{L,peak}}$$

$$L_{critical} = \frac{V_i \cdot D \cdot T_s}{2 \langle i_i \rangle}$$

$$P_i = P_o$$

} Input characteristics are generally not given, so we need to manipulate the formula a bit

$$V_i \langle i_i \rangle = V_o \langle i_o \rangle \rightarrow V_i \langle i_i \rangle = \frac{V_o^2}{R_o}$$

$$L_{critical} = \frac{V_i \cdot D \cdot T_s \cdot R_o}{2 V_o^2}$$

$$L_{critical} = \frac{V_i \cdot D \cdot R_o}{2 \cdot V_o^2 \cdot f_s}$$

Boundary Conduction Mode

If $L > L_{critical}$ means system in CCM

If $L < L_{critical}$ means system in DCM

$$\text{For } V_i = 5V \rightarrow V_o = 16V \rightarrow V_o = \frac{V_i}{1-D} \rightarrow D = 0.6875$$

$$\text{For } V_i = 12V \rightarrow V_o = 16V \rightarrow V_o = \frac{V_i}{1-D} \rightarrow D = 0.25$$

In the question, it is asked to calculate minimum inductance that will keep the converter operating in the CCM operation for rated output power.

$$P_o = \frac{V_o^2}{R_o} \rightarrow 1W = \frac{16^2}{R_o} \rightarrow R_o = \frac{16^2}{1} \rightarrow R_o = 256\Omega$$

$$T_s = \frac{1}{f_s} \rightarrow f_s = 300kHz$$

$$L_{critical,5V} = \frac{5V \times 0.6875 \times 256\Omega}{2 \times 16^2 \times 300 \times 10^3} = 5.73 \times 10^{-6}H$$

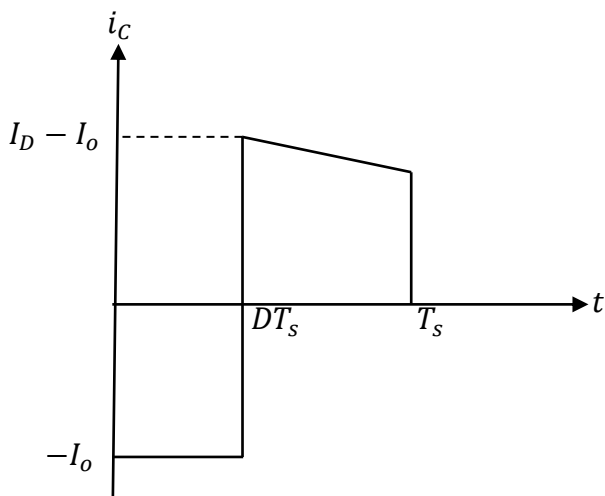
$$L_{critical,12V} = \frac{12V \times 0.25 \times 256\Omega}{2 \times 16^2 \times 300 \times 10^3} = 5 \times 10^{-6}H$$

To ensure CCM operation in both cases, it is necessary to choose higher value which is

$$L_{critical,5V} = L_{critical,sys} = 5.73 \times 10^{-6}H$$

b) Calculate the output capacitance for peak-to-peak voltage ripple less than 2% under rated output power.

$$\Delta V_o = 2\% = 0.02$$



$$i_c = C \frac{dV_c}{dt} = C \frac{\Delta V_c}{\Delta t}$$

$$C = i_c \frac{\Delta t}{\Delta V_c} = C \frac{\Delta V_c}{\Delta t} = I_o \frac{D \cdot T_s}{\Delta V_c} = I_o \frac{D \cdot T_s}{\Delta V_o}, \quad I_o = \frac{V_o}{R_o}$$

$$C = \frac{V_o}{R_o} \cdot \frac{D \cdot T_s}{\Delta V_o} \quad \text{or} \quad C = \frac{V_o}{R_o} \cdot \frac{D}{\Delta V_o \cdot f_s}$$

Put the values into the equation for both cases. Again our rated output power is 1W.

$$C_{5V} = \frac{16}{256} \times \frac{0.6875}{0.02 \times 300 \times 10^3} = 7.2 \mu F$$

$$C_{12V} = \frac{16}{256} \times \frac{0.25}{0.02 \times 300 \times 10^3} = 2.6 \mu F$$

To ensure output voltage ripple is 2% for both cases, it is needed to use the bigger value.

So, 10 μ F is chosen.

L is found 5.73 μ H for ideal case; however it does not provide CCM in the design, so 50 μ H is was tried and it ensured CCM.

c) Simulate the steady-state behaviour of the converter and show the important waveforms for boundary conduction mode of part-a. Plot following waveforms and comment on the results.

- **Inductor voltage and current**
- **Output voltage and current**
- **Diode voltage and current**
- **Switch voltage and current**

Inductor voltage and current waveforms:

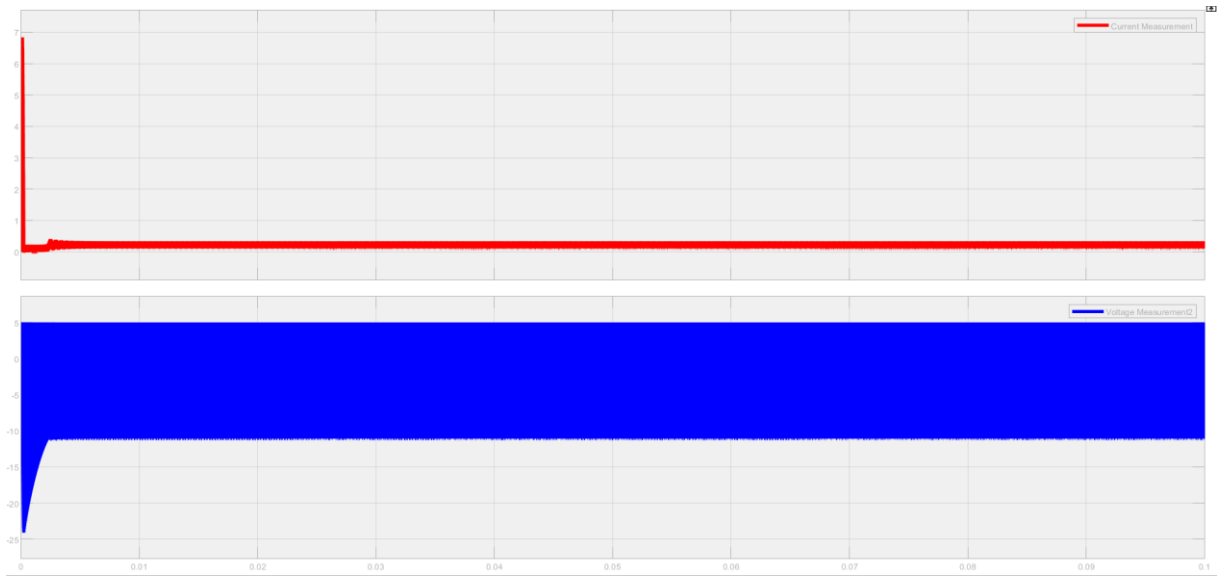


Figure 16. Inductor voltage and current waveform

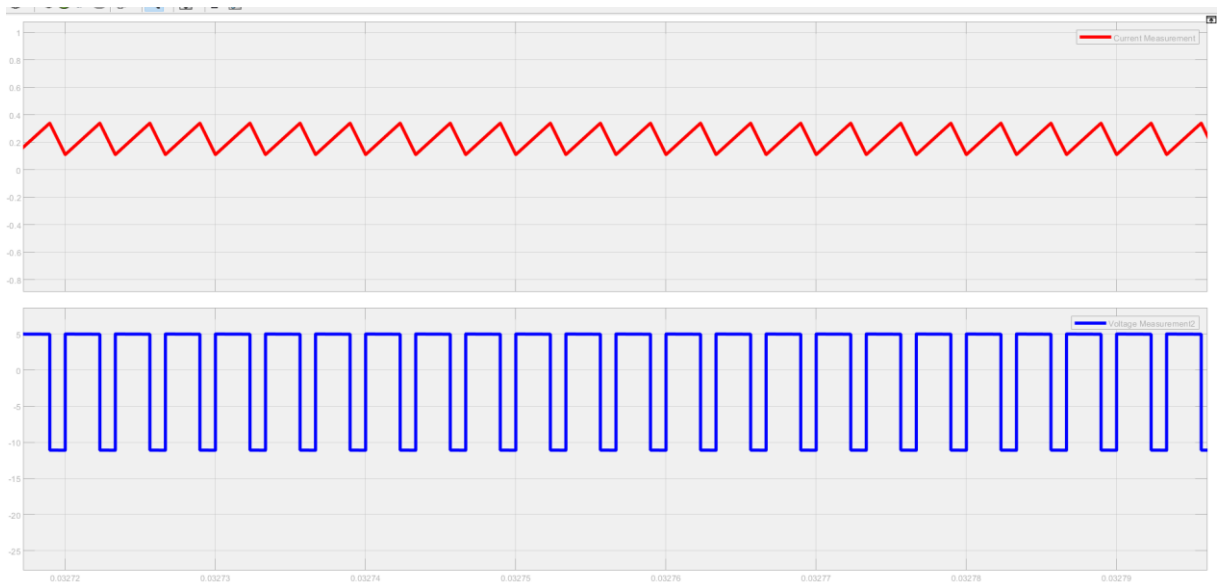


Figure 17. Close-up view to waveforms

It can be observed from Fig.17, our system is in CCM, inductor voltage $V_L = 5V$ for switch ON, $V_L = -11V$ for switch OFF. It confirms the desired specifications.

Output voltage and current:

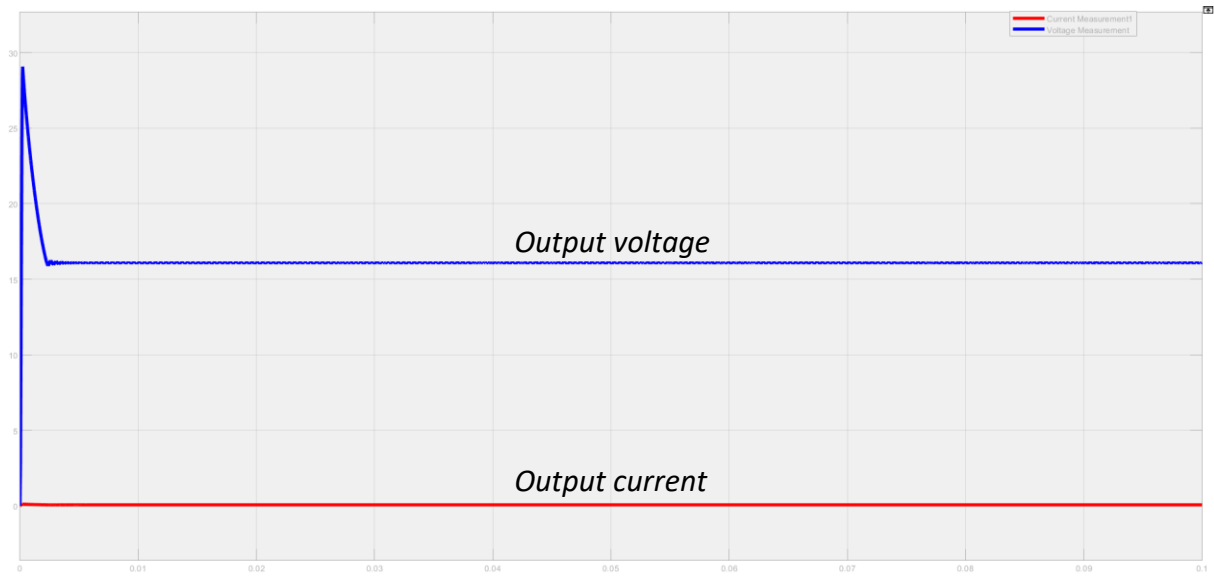


Figure 18. Voltage and current waveforms

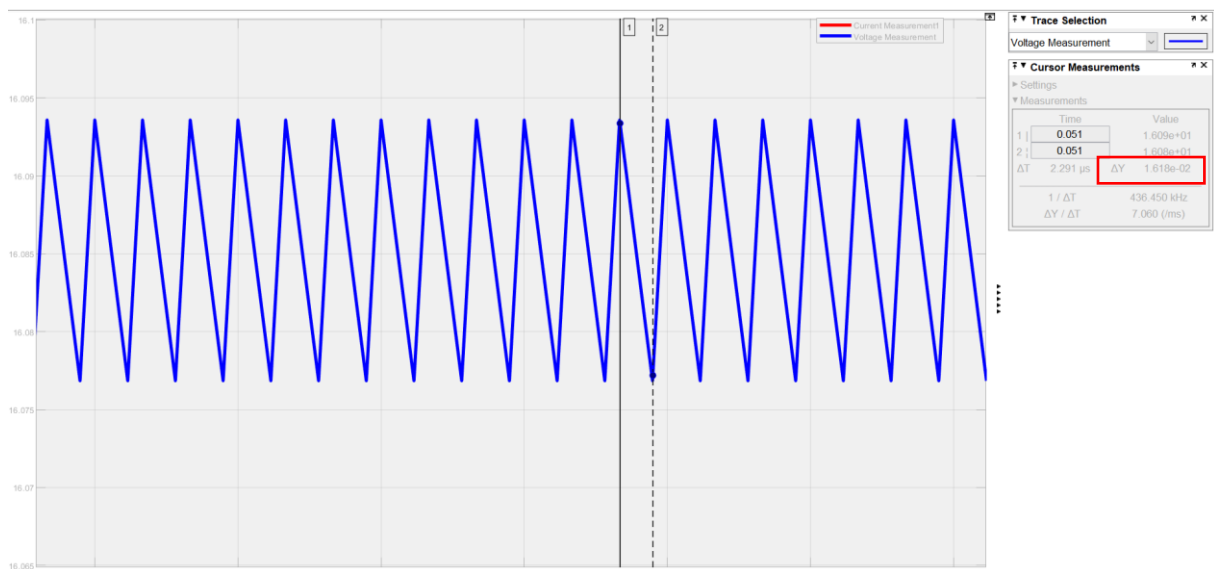


Figure 19. Voltage ripple at the output

As it can be seen on the Fig.19, voltage ripple at the output is less than 2%. ($\Delta Y = 1.618e-02$)

In steady-state, average output voltage is 15.94V, average output current is 6.226e-02A.

$$P_{\text{output}} = 15.94 \times 6.226e-02 = 0.9924W \cong 1W$$

Desired values are met.

Diode voltage and current:

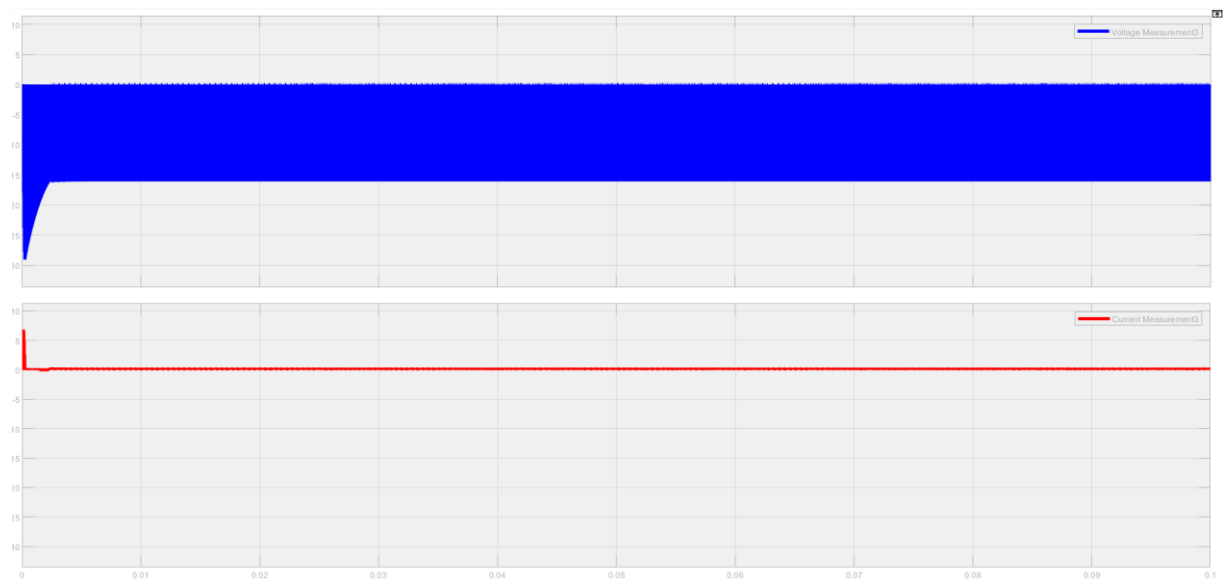


Figure 20. Diode voltage and current

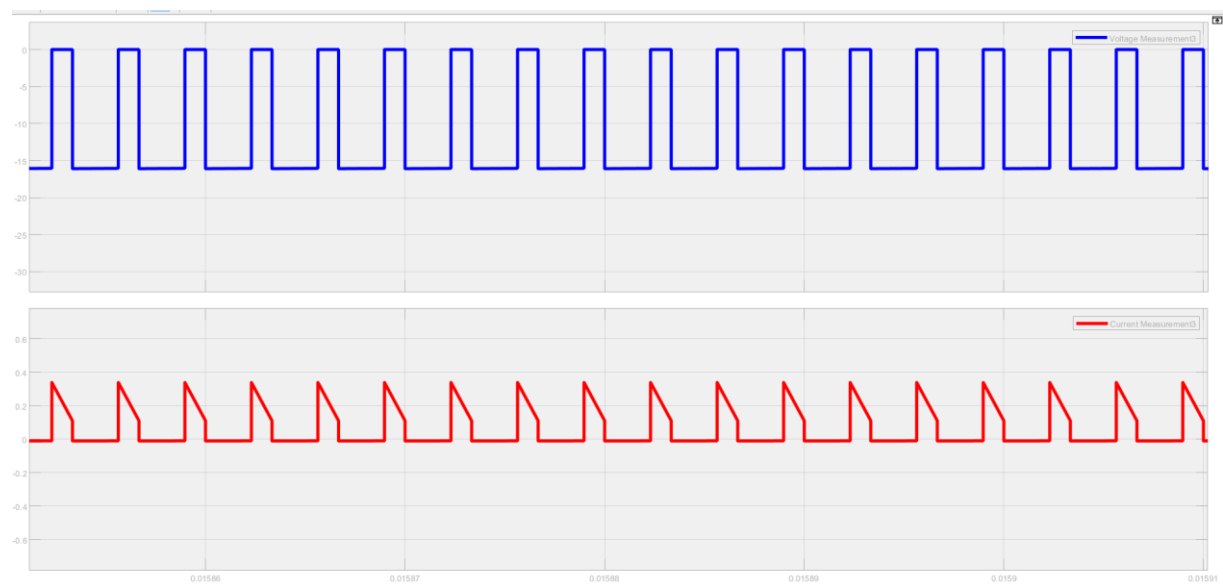


Figure 21. Close-up view to diode waveforms

Switch voltage and current:

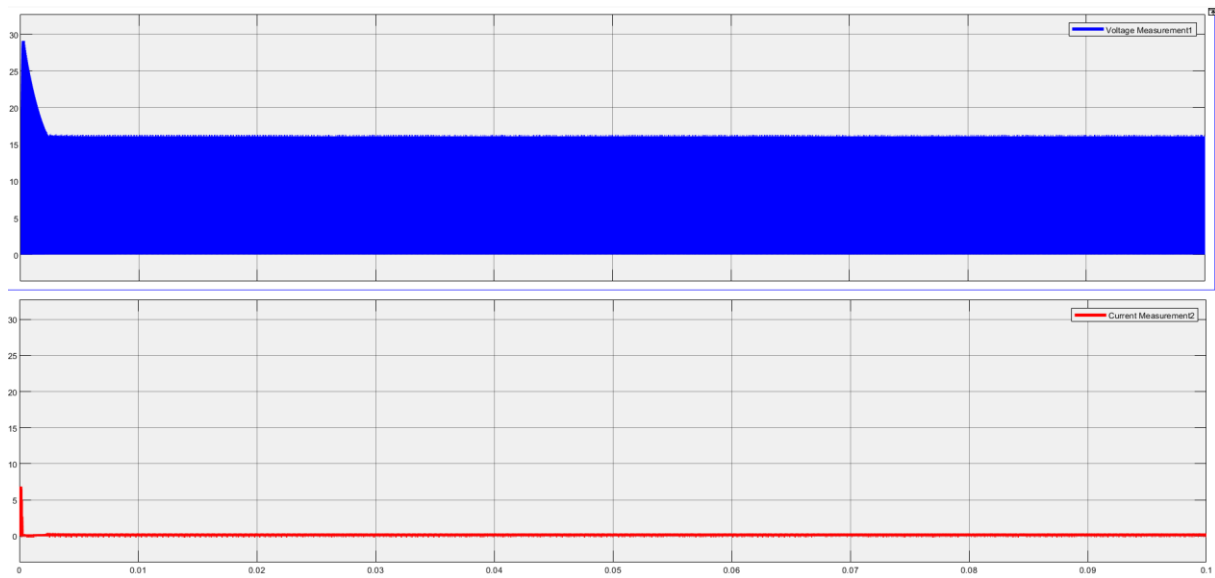


Figure 22. Switch voltage and current waveforms

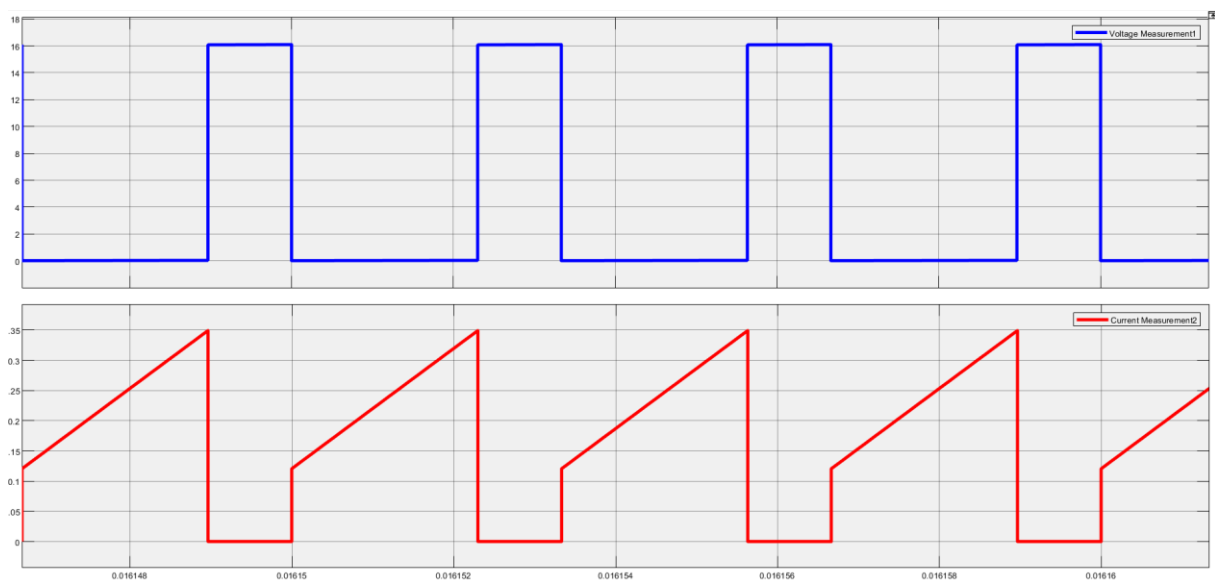


Figure 23. Close-up view to switch waveforms

When switch is ON, the switch voltage is 0V and switch current is increased, when switch is OFF, the switch voltage is $V_s = V_o = 16V$ and no current through switch.

d) Assuming the switches and capacitors are ideal, but the inductor has 30 mΩ ESR, and considering the load resistance is equal to the rated load resistance, derive the voltage gain as a function of the duty cycle. Show your steps clearly. On the MATLAB, plot the voltage gain with and without ESR on the same graph as a function of duty cycle. Comment on the results.

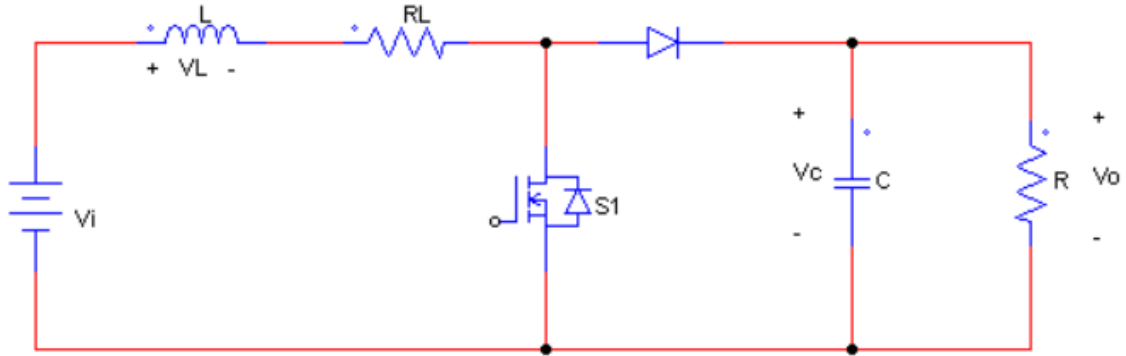


Fig. Boost Converter

From volt-second balance, the inductor voltage is as follows:

At on-state:

$$V_L = V_i$$

At off-state:

$$V_L = V_i - V_o$$

Therefore;

$$V_i(D)T_s + V_i - V_o(1 - D)T_s = 0$$

$$V_i(D) + V_i - V_iD - V_o + V_oD = 0$$

$$V_i = V_o(1 - D)$$

$$V_o = \frac{V_i}{(1 - D)}$$

$$\frac{V_o}{V_i} = \frac{1}{\left[(1 - D) \left(1 + \frac{R_L}{(1 - D)^2 R_o} \right) \right]}$$

Where R_L = resistance of the inductor, R_o = load resistance

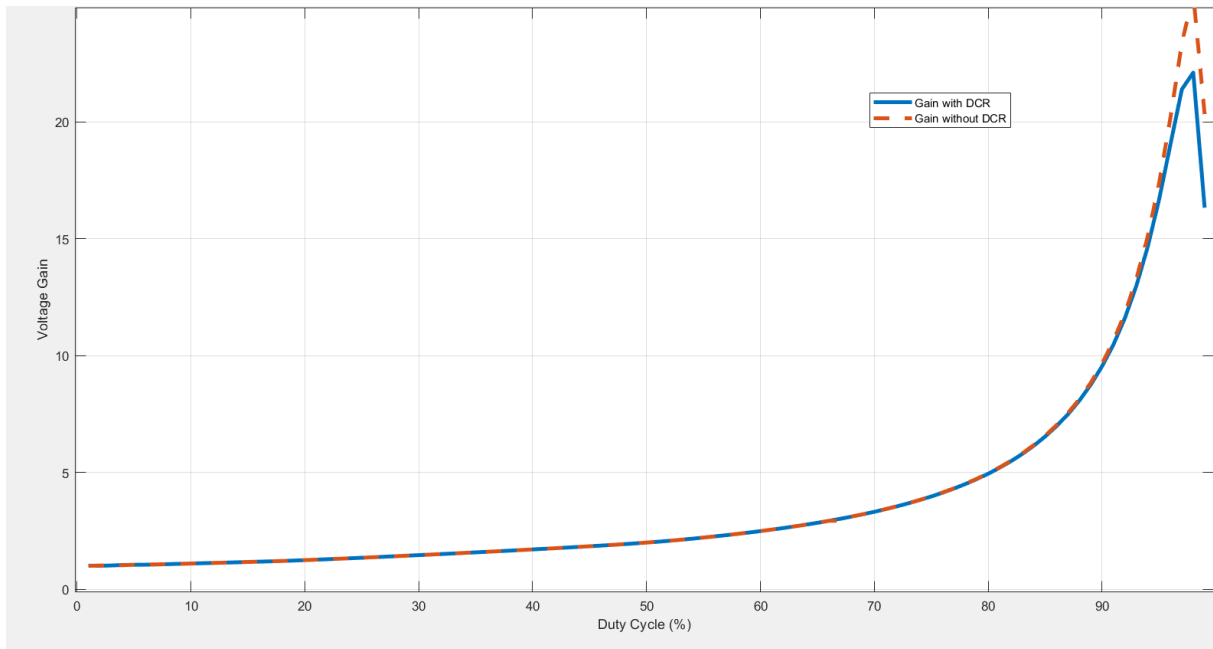


Figure 24. Gain with respect to duty cycle w/(out) DCR

It can be observed that DCR (ESR) will reduce the gain at the higher duty cycle ratio.

e) Repeat the same steps in part-d for the converter efficiency.

The converter efficiency is measured by the efficiency ratio (η) which is

$$\eta = \frac{P_{out}}{P_{in}} = \frac{P_{out}}{P_{out} + P_{losses}}$$

$$P_{losses} = P_{cu} + P_{switching} + P_{diode}$$

In the system, the diode and the switch are supposed to be ideal, so

$$P_{diode} = 0 \quad \& \quad P_{switching} = 0.$$

$$\eta = \frac{P_{out}}{P_{in}} = \frac{P_{out}}{P_{out} + P_{cu}}$$

$$P_{cu} = I_t^2 \times R_{inductor}$$

In MATLAB, following codes are implemented to graph efficiency with respect to (w.r.t.) duty cycle:

```
D = (0:0.01:0.99); %Variable Duty Cycle
V_i = 5; %Input Voltage
V_o = 16; %Output Voltage
P_o = 1; %Output Power
I_o = (P_o / V_o) * ones(1,100); %Output Current
I_i = I_o ./ (1-D); %input current w.r.t duty cycle
R_inductor = 0.03; % 30mΩ inductor resistor
P_cu = (I_i.^2) * R_inductor; %Copper loss w.r.t input Current
eff = P_o ./ (P_o + P_cu); %efficiency calculation
plot(D, eff) %plotting the efficiency w.r.t duty cycle
hold on %holds the graph
grid on %enables grid
R_inductor = 0; %to calculate without inductor resistance
P_cu = (I_i.^2) * R_inductor %P_cu = 0 (R_inductor = 0)
eff = P_o ./ (P_o + P_cu); %P_o / P_o = 1
plot (D, eff)
```

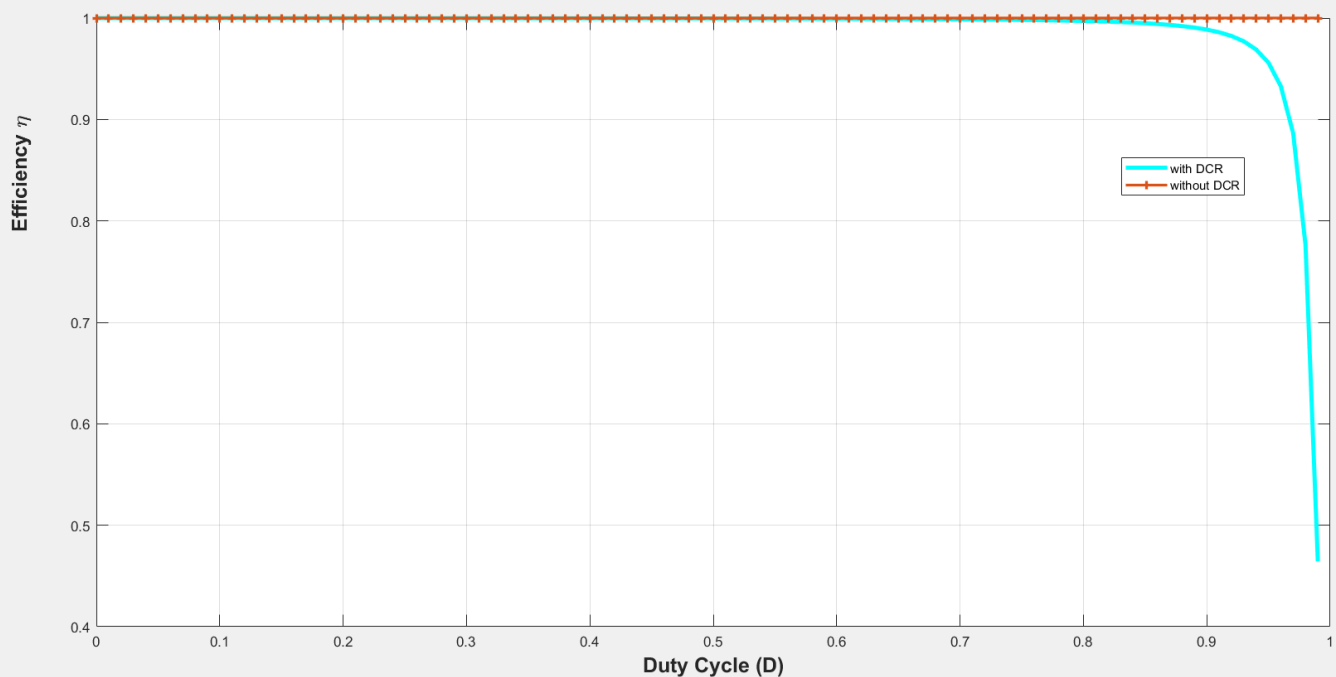


Figure 25. Efficiency w.r.t. duty cycle

f) Choose commercial semiconductor products using Digikey that is appropriate for your design. Calculate the losses on these devices for rated power operation with 12 V input voltage. How would losses on the diode and switch change if the duty cycle is increased? Explain in detail.

MOSFET

First, the parameters of the MOSFET should be defined:

As it can be seen on the fig. below, the maximum switch voltage is close to 31V

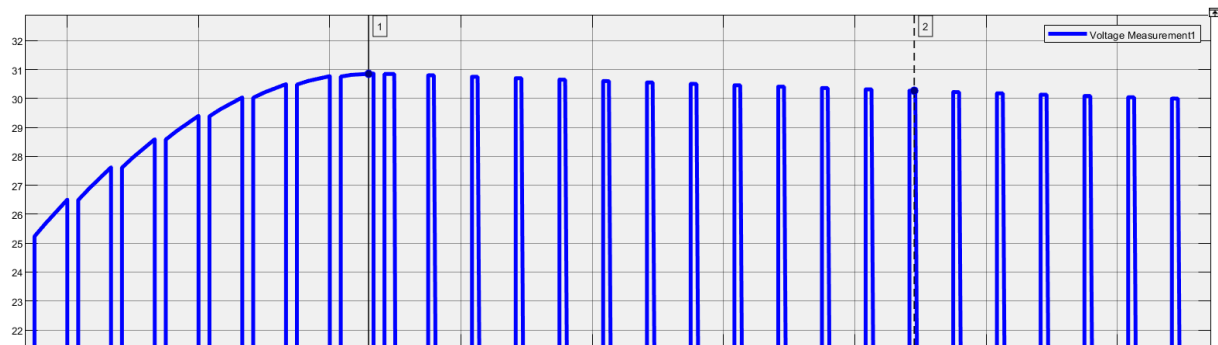


Figure 26. Switch voltage

Maximum spike current is shown below: 7.131A and steady-state max. current value is 0.2228A.

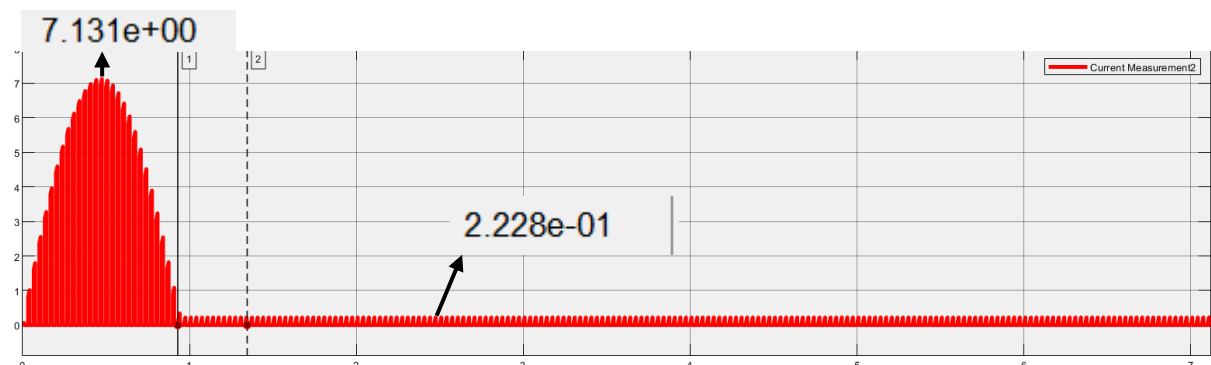


Figure 27. Switch Current

From [digikey.com](https://www.digikey.com), IRLML0040TRPbF n-channel MOSFET is available for the system.

Let's check the parameters of the MOSFET:

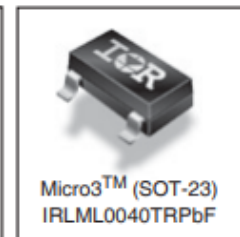
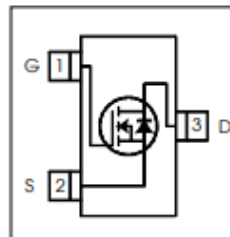
International
IR Rectifier

PD - 96309A

IRLML0040TRPbF

HEXFET® Power MOSFET

V_{DS}	40	V
$V_{GS\ Max}$	± 16	V
$R_{DS(on)\ max}$ (@ $V_{GS} = 10V$)	56	m Ω
$R_{DS(on)\ max}$ (@ $V_{GS} = 4.5V$)	78	m Ω



Application(s)

- Load/ System Switch
- DC Motor Drive

Features and Benefits

Features

Low $R_{DS(on)}$ ($\leq 56m\Omega$)
Industry-standard pinout
Compatible with existing Surface Mount Techniques
RoHS compliant containing no lead, no bromide and no halogen
MSL1, Consumer qualification

results in
 \Rightarrow

Benefits

Lower switching losses
Multi-vendor compatibility
Easier manufacturing
Environmentally friendly
Increased reliability

Absolute Maximum Ratings

Symbol	Parameter	Max.	Units
V_{DS}	Drain-Source Voltage	40	V
I_D @ $T_A = 25^\circ C$	Continuous Drain Current, V_{GS} @ 10V	3.6	A
I_D @ $T_A = 70^\circ C$	Continuous Drain Current, V_{GS} @ 10V	2.9	
I_{DM}	Pulsed Drain Current	15	W
P_D @ $T_A = 25^\circ C$	Maximum Power Dissipation	1.3	
P_D @ $T_A = 70^\circ C$	Maximum Power Dissipation	0.8	W/°C
	Linear Derating Factor	0.01	
V_{GS}	Gate-to-Source Voltage	± 16	V
T_J, T_{STG}	Junction and Storage Temperature Range	-55 to +150	°C

Thermal Resistance

Symbol	Parameter	Typ.	Max.	Units
$R_{\theta JA}$	Junction-to-Ambient ①	—	100	°C/W
$R_{\theta JA}$	Junction-to-Ambient ($t < 10s$) ②	—	99	

ORDERING INFORMATION:

See detailed ordering and shipping information on the last page of this data sheet.


Notes ① through ④ are on page 10
www.irf.com

1

02/29/12

Symbol	Parameter	Min.	Typ.	Max.	Units	Conditions
$V_{(BR)DSS}$	Drain-to-Source Breakdown Voltage	40	—	—	V	$V_{GS} = 0V, I_D = 250\mu A$
$\Delta V_{(BR)DSS}/\Delta T_J$	Breakdown Voltage Temp. Coefficient	—	0.04	—	V/°C	Reference to 25°C, $I_D = 1mA$
$R_{DS(on)}$	Static Drain-to-Source On-Resistance	—	44	56	mΩ	$V_{GS} = 10V, I_D = 3.6A$ ②
		—	62	78		$V_{GS} = 4.5V, I_D = 2.9A$ ②
$V_{GS(th)}$	Gate Threshold Voltage	1.0	1.8	2.5	V	$V_{DS} = V_{GS}, I_D = 25\mu A$
I_{DSS}	Drain-to-Source Leakage Current	—	—	20	μA	$V_{DS} = 40V, V_{GS} = 0V$
		—	—	250		$V_{DS} = 40V, V_{GS} = 0V, T_J = 125^\circ C$
I_{GSS}	Gate-to-Source Forward Leakage	—	—	100	nA	$V_{GS} = 16V$
	Gate-to-Source Reverse Leakage	—	—	-100		$V_{GS} = -16V$
R_G	Internal Gate Resistance	—	1.1	—	Ω	
g_{fs}	Forward Transconductance	6.2	—	—	S	$V_{DS} = 10V, I_D = 3.6A$
Q_g	Total Gate Charge	—	2.6	3.9	nC	$I_D = 3.6A$
Q_{gs}	Gate-to-Source Charge	—	0.7	—		$V_{DS} = 20V$
Q_{gd}	Gate-to-Drain ("Miller") Charge	—	1.4	—		$V_{GS} = 4.5V$ ②
$t_{d(on)}$	Turn-On Delay Time	—	5.1	—	ns	$V_{DD} = 20V$
t_r	Rise Time	—	5.4	—		$I_D = 1.0A$
$t_{d(off)}$	Turn-Off Delay Time	—	6.4	—		$R_G = 6.8\Omega$
t_f	Fall Time	—	4.3	—		$V_{GS} = 4.5V$
C_{iss}	Input Capacitance	—	266	—	pF	$V_{GS} = 0V$
C_{oss}	Output Capacitance	—	49	—		$V_{DS} = 25V$
C_{rss}	Reverse Transfer Capacitance	—	29	—		$f = 1.0MHz$

Source - Drain Ratings and Characteristics

Symbol	Parameter	Min.	Typ.	Max.	Units	Conditions
I_S	Continuous Source Current (Body Diode)	—	—	1.3	A	MOSFET symbol showing the integral reverse p-n junction diode. 
I_{SM}	Pulsed Source Current (Body Diode) ①	—	—	15		
V_{SD}	Diode Forward Voltage	—	—	1.2	V	$T_J = 25^\circ C, I_S = 1.3A, V_{GS} = 0V$ ②
t_{rr}	Reverse Recovery Time	—	10	—	ns	$T_J = 25^\circ C, V_R = 32V, I_F = 1.3A$
Q_{rr}	Reverse Recovery Charge	—	9.3	—	nC	$di/dt = 100A/\mu s$ ②

Important parameters are marked with red rectangle.

From the datasheet, all the parameters are in large margin that means the MOSFET can be used safely for this boost converter design.

DIODE

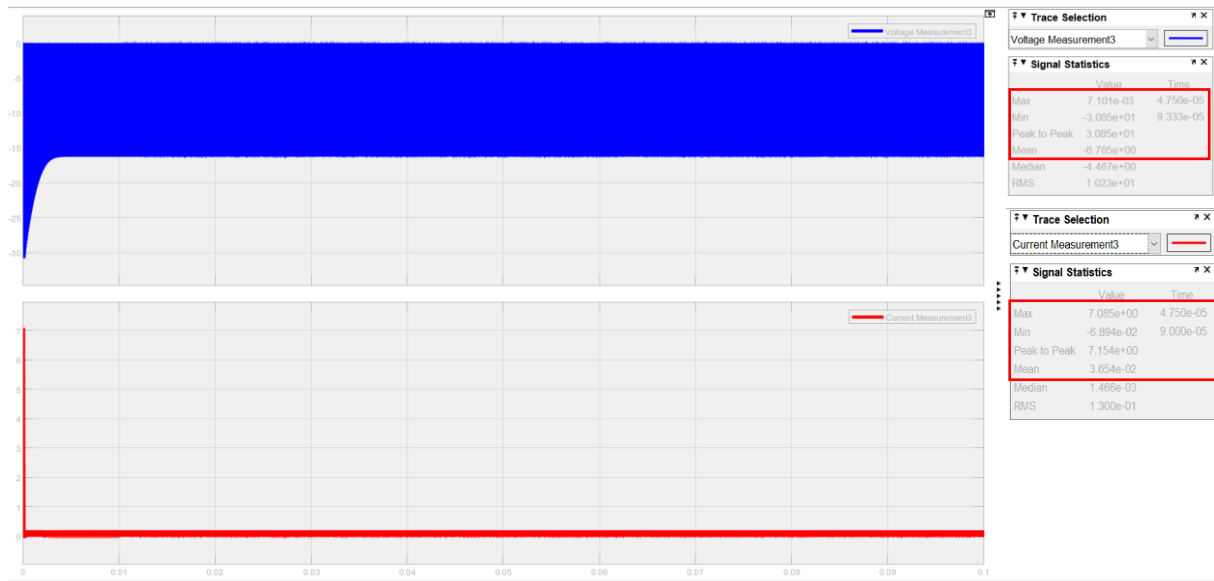


Figure 28. Diode voltage and current waveforms

The diode is used for blocking reverse voltage when $V_o > V_i$.

Therefore, reverse blocking voltage is important parameter here. Zener type is not useful because it should not allow reverse current.

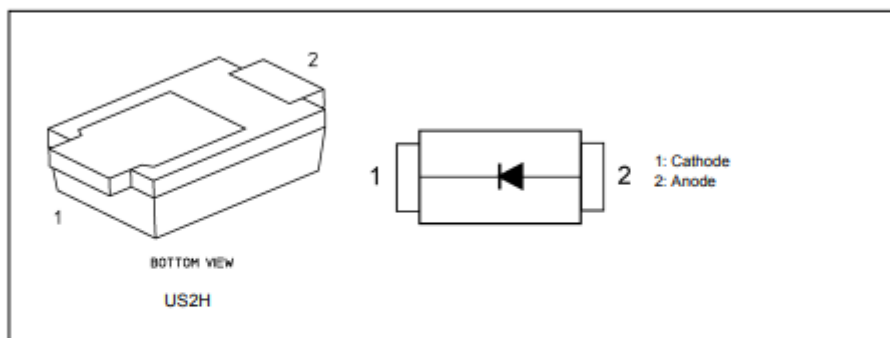
From [toshiba.semicon-storage.com](https://www.toshiba.semicon-storage.com), CUHS20F40 is available for our system design.

CUHS20F40

1. Applications

- High-Speed Switching

2. Packaging and Internal Circuit



3. Absolute Maximum Ratings (Note) (Unless otherwise specified, $T_a = 25^\circ\text{C}$)

Characteristics	Symbol	Note	Rating	Unit
Reverse voltage	V_R		40	V
Average rectified current	I_G	(Note 1)	2.0	A
Non-repetitive peak forward surge current	I_{FSM}	(Note 2)	10	A
Junction temperature	T_J		150	$^\circ\text{C}$
Storage temperature	T_{stg}		-55 to 150	$^\circ\text{C}$

Note: Using continuously under heavy loads (e.g. the application of high temperature/current/voltage and the significant change in temperature, etc.) may cause this product to decrease in the reliability significantly even if the operating conditions (i.e. operating temperature/current/voltage, etc.) are within the absolute maximum ratings.

Please design the appropriate reliability upon reviewing the Toshiba Semiconductor Reliability Handbook ("Handling Precautions"/"Derating Concept and Methods") and individual reliability data (i.e. reliability test report and estimated failure rate, etc.).

Note 1: Mounted on an FR4 board.

(25.4 mm × 25.4 mm × 1.6 mm, Cu Pad: 645 mm²)

Note 2: Pulse width 10 ms

CUHS20F40

4. Electrical Characteristics (Unless otherwise specified, $T_a = 25^\circ\text{C}$)

Characteristics	Symbol	Note	Test Condition	Min	Typ.	Max	Unit
Forward voltage	V_F (1)	(Note 1)	$I_F = 500\text{ mA}$	—	0.34	0.40	V
	V_F (2)		$I_F = 1\text{ A}$	—	0.39	0.45	
	V_F (3)		$I_F = 2\text{ A}$	—	0.47	0.54	
Reverse current	I_R (1)	(Note 1)	$V_R = 10\text{ V}$	—	7	—	μA
	I_R (2)		$V_R = 40\text{ V}$	—	13	60	
Total capacitance	C_t		$V_R = 0\text{ V}, f = 1\text{ MHz}$	—	300	—	pF

Note 1: Pulse measurement.

→ Calculate the losses on these devices for rated power operation with 12 V input voltage.
How would losses on the diode and switch change if the duty cycle is increased? Explain in detail.

MOSFET:

$$P_{cond} = R_{ds} \times I_L^2 \rightarrow 56m\Omega \times 0.08142A = 4.6mW$$

$$P_{switching} = V_o \times I_L \times f_s \times (t_{rise} + t_{fall}) \rightarrow 16V \times 0.08142 \times 300kHz \times 9.7ns \\ = 3.8mW$$

DIODE:

$$P_{cond} = V_f \times I_L \rightarrow 0.4V \times 0.08142A = 32mW$$

If the duty cycle is increased, I_L will increase. Because of all losses parameters depend on I_L , the losses will increase.

g) Using the calculated loss values, construct a thermal lumped element model and estimate the junction temperature without a heatsink. If necessary, choose a thermal interface material and heatsink and find out the junction temperature with these materials. Clearly state any assumption that you made.

Steps of thermal design in power electronics:

- Determining the components
- Calculating the losses
- Getting thermal resistances from datasheet
- Determining maximum heatsink thermal resistance
- Finding a proper heatsink, deciding on cooling type (natural, forced, etc...)
- Iterating until getting a reasonable operating temperature

MOSFET: IRLML0040TRPBF n-channel thermal resistance parameters:

$R_{thJA} = 100\text{ }^{\circ}\text{C/W}$ (Junction to ambient thermal resistance is used in cases which does not have heatsink connected to the case of the MOSFET)

Losses of the MOSFET:

$$P_{cond} = R_{ds} \times I_L^2 \rightarrow 56\text{m}\Omega \times 0.08142\text{A} = 4.6\text{mW}$$

$$P_{switching} = V_o \times I_L \times f_s \times (t_{rise} + t_{fall}) \rightarrow 16\text{V} \times 0.08142 \times 300\text{kHz} \times 9.7\text{ns} \\ = 3.8\text{mW}$$

$$P_{total,MOSFET} = P_{cond} + P_{switching} = 4.6\text{mW} + 3.8\text{mW} = 8.4\text{mW}$$

$$R_{thJA} = 100\text{ }^{\circ}\text{C/W}$$

$$T_{junction} = T_{ambient} + P_{losses} \times R_{thJA} \text{ where } T_{ambient} = 25^{\circ}\text{C}$$

$$T_{junction} = 25^{\circ}\text{C} + 8.4\text{mW} \times 100\text{ }^{\circ}\text{C/W}$$

$$T_{junction} = 25.84^{\circ}\text{C}$$

Conclusion: No need for heatsink on the MOSFET. It is in the safe range.

END