

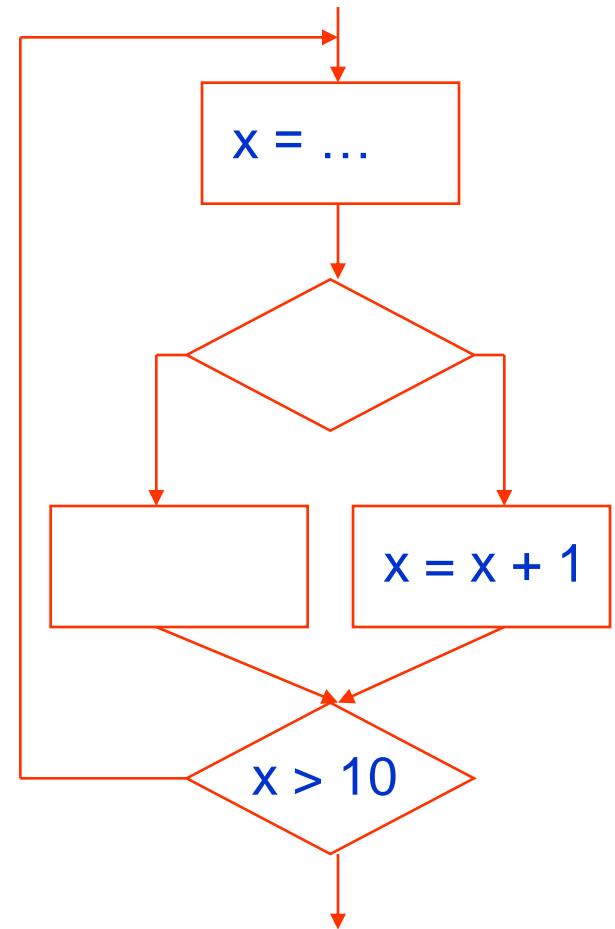
Data Flow Testing

Data Flow Testing

- **Data flow testing** uses the control flow graph to explore the unreasonable things that can happen to data (data flow anomalies).
- **Data flow anomalies** are detected based on the associations between values and variables.
 - ❑ Variables are used without being initialized.
 - ❑ Initialized variables are not used once.

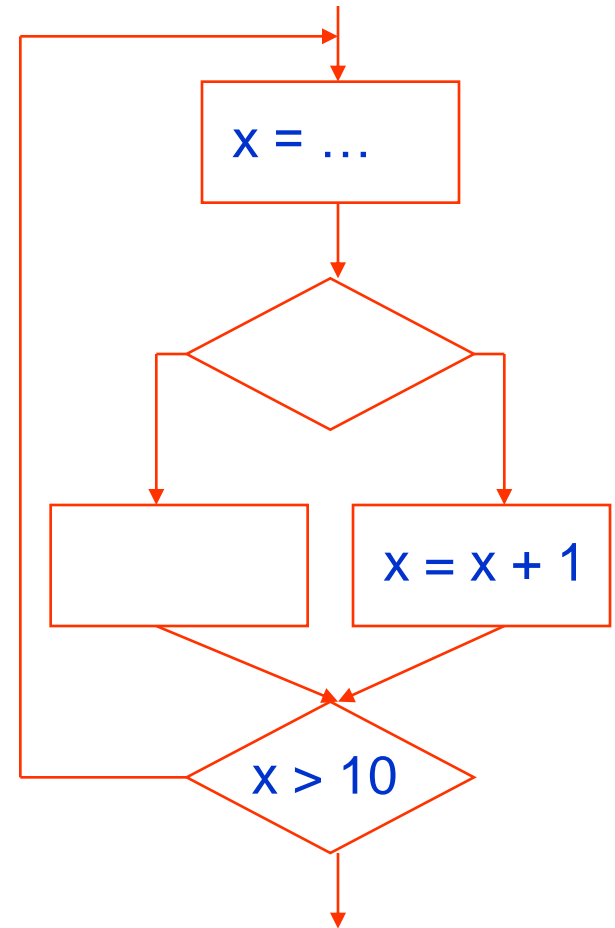
Definitions and Uses of Variables

- An occurrence of a variable in the program is a **definition** of the variable if a value is bound to the variable at that occurrence.
- An occurrence of a variable in the program is a **use** of the variable if the value of the variable is referred at that occurrence.



Predicate Uses and Computation Uses

- A use of a variable is a **predicate use (p-use)** if the variable is in a predicate and its value is used to decide an execution path.
- A use of a variable is a **computation use (c-use)** if the value of the variable is used to compute a value for defining another variable or as an output value.

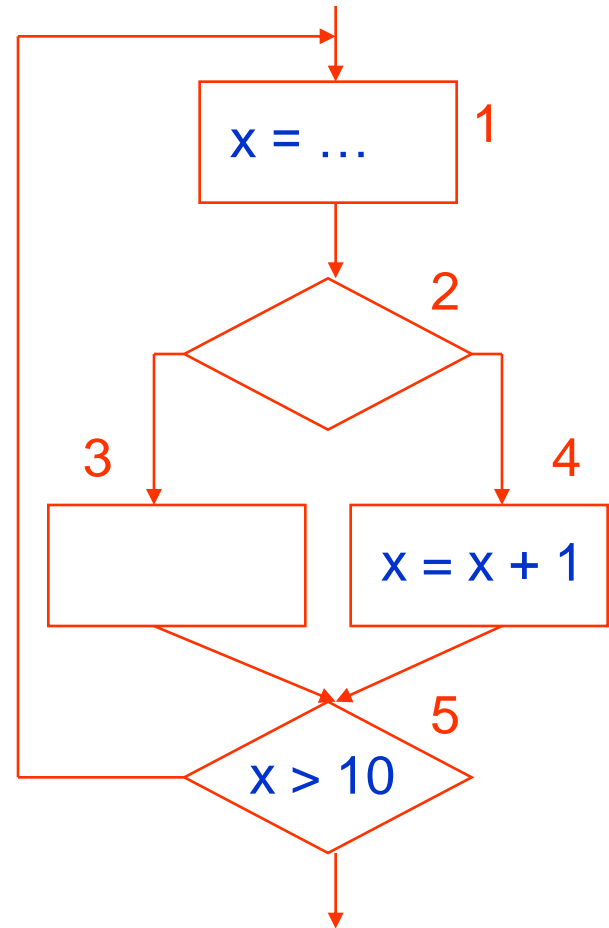


Definition Clear Paths

- A path $(i, n_1, n_2, \dots, n_m, j)$ is a **definition-clear path** for a variable x from i to j if n_1 through n_m do not contain a definition of x .

(1, 2, 4)

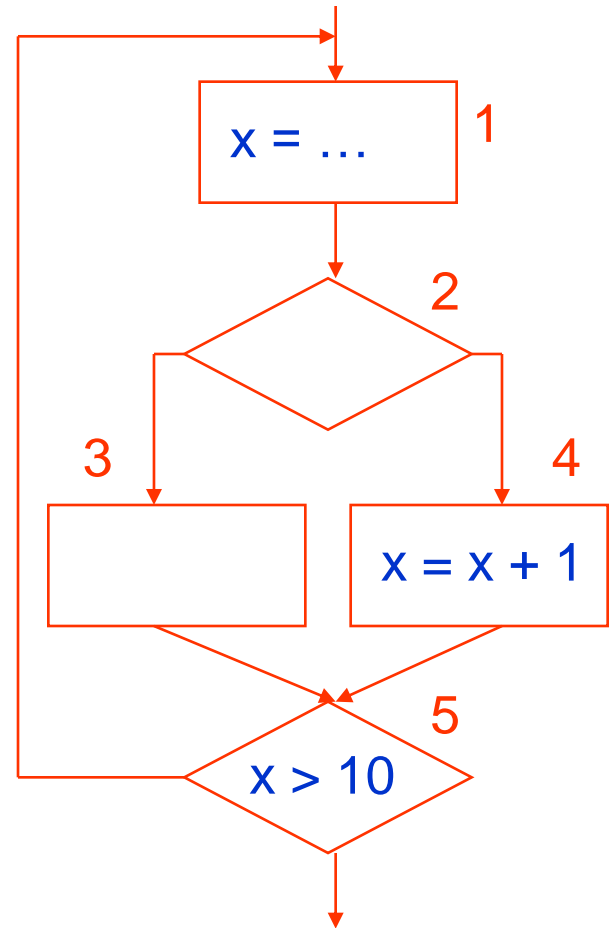
(1, 2, 3, 5)



Definition-C-Use Associations

- Given a definition of x in node n_d and a c-use of x in node n_{c-use} , the presence of a definition-clear path for x from n_d to n_{c-use} establishes the **definition-c-use association** (n_d, n_{c-use}, x) .

$(1, 4, x)$

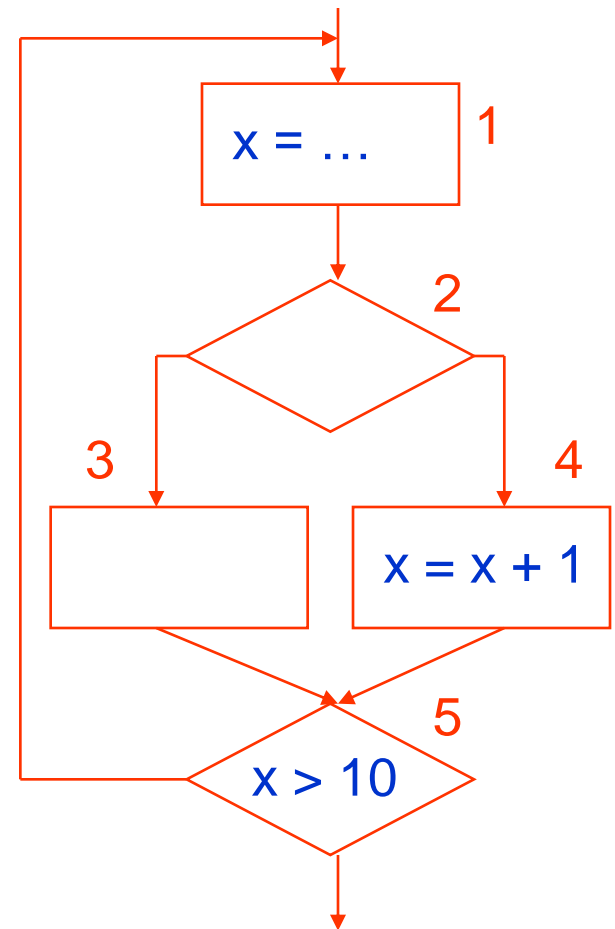


Definition-P-Use Associations

- Given a definition of x in node n_d and a p-use of x in node n_{p-use} , the presence of a definition-clear path for x from n_d to n_{p-use} establishes a pair of **definition-p-use associations** $(n_d, (n_{p-use}, t), x)$ and $(n_d, (n_{p-use}, f), x)$.

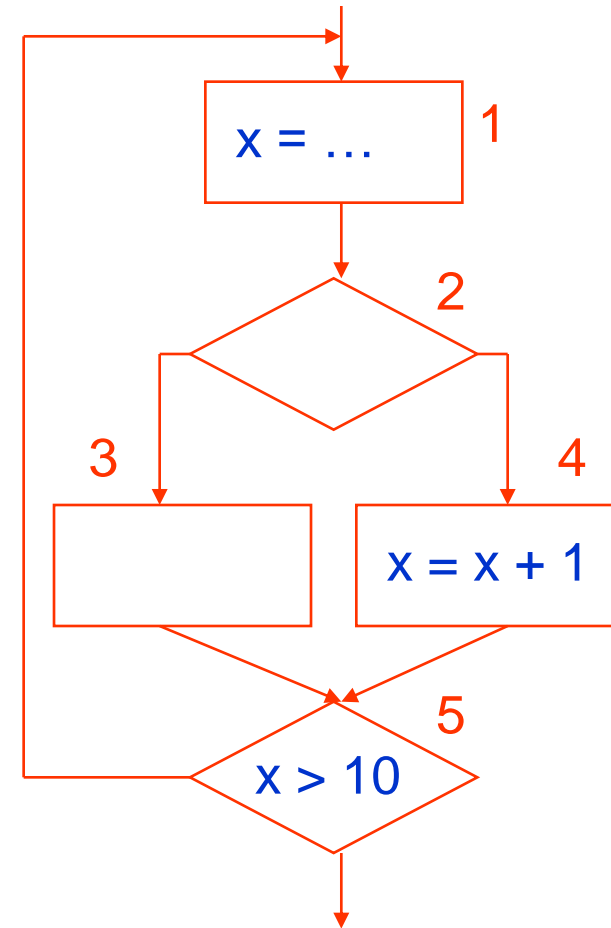
$(1, (5, t), x)$

$(1, (5, f), x)$



DU-Paths

- A path (n_1, \dots, n_m) is a **du-path** for variable x if n_1 contains a definition of x and either n_m has a c-use of x and (n_1, \dots, n_m) is a **definition-clear simple path** for x (all nodes, except possibly n_1 and n_m , are distinct) or is a p-use of x and is a **definition-clear loop-free path** for x (all nodes are distinct) .



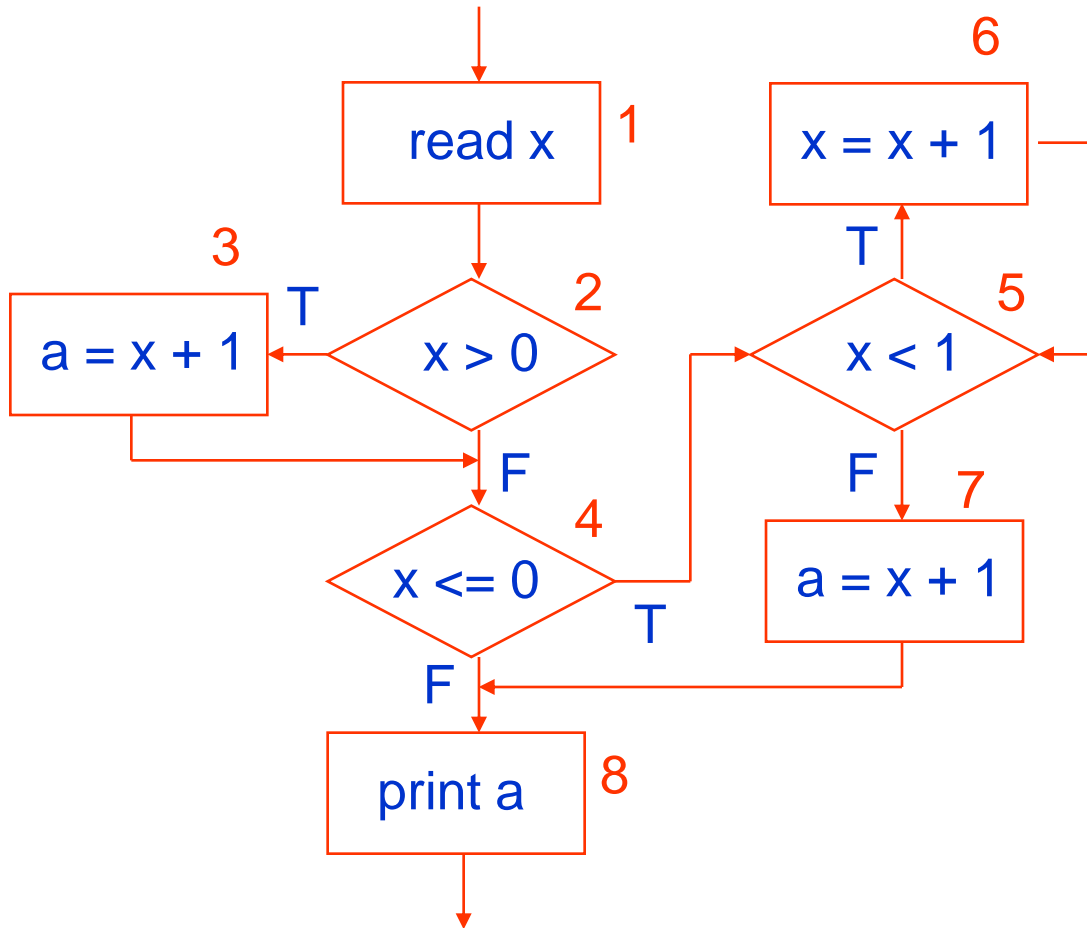
$(1, 2, 4)$

$(1, 2, 3, 5)$

Test Coverage Criteria

- All-defs coverage
 - All-c-uses coverage
 - All-c-uses/some-p-uses coverage
 - All-p-uses coverage
 - All-p-uses/some-c-uses coverage
 - All-uses coverage
 - All-du-paths coverage
-

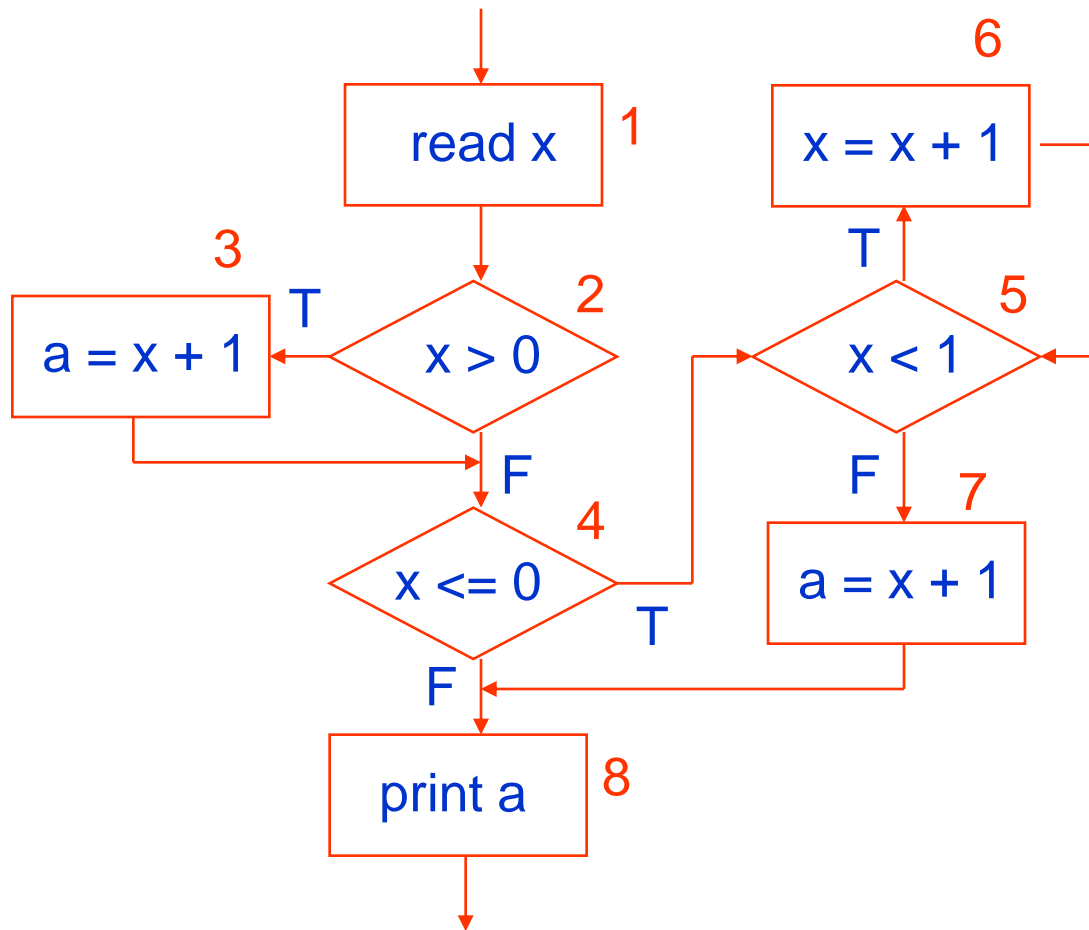
A Running Example



$x = 1$
 $P_1: (1, 2, 3, 4, 8)$
 $a = 2$

$x = -1$
 $P_2: (1, 2, 4, 5, 6,$
 $5, 6, 5, 7, 8)$
 $a = 2$

A Running Example



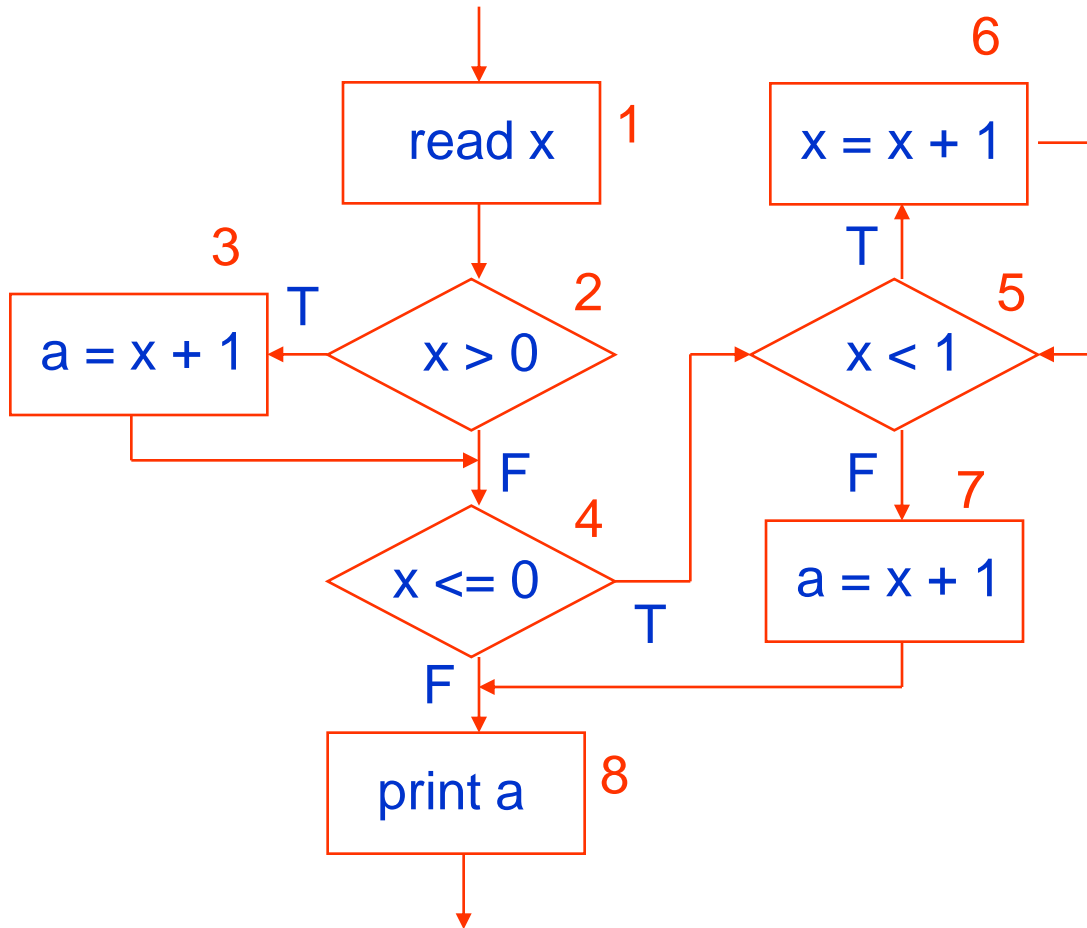
Associations:

(1, (2, t), x)
(1, (2, f), x)
(1, 3, x)
(1, (4, t), x)
(1, (4, f), x)
(1, (5, t), x)
(1, (5, f), x)
(1, 6, x)
(1, 7, x)
(3, 8, a)
(6, 6, x)
(6, 7, x)
(6, (5, t), x)
(6, (5, f), x)
(7, 8, a)

All-Defs Coverage

- Test cases include a definition-clear path from every definition to some corresponding use (c-use or p-use).

All-Defs Coverage

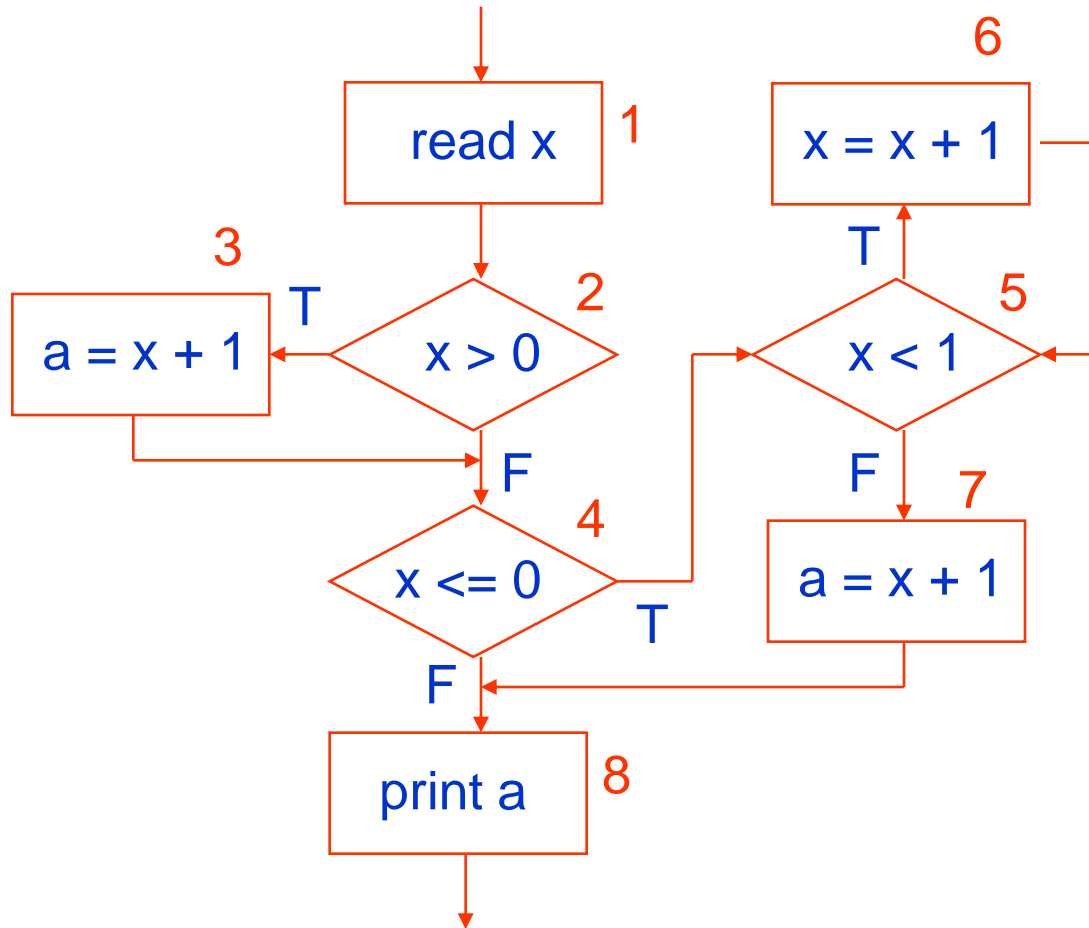


Associations	all-defs
(1, (2, t), x)	✓
(1, (2, f), x)	
(1, 3, x)	
(1, (4, t), x)	
(1, (4, f), x)	
(1, (5, t), x)	
(1, (5, f), x)	
(1, 6, x)	
(1, 7, x)	
(3, 8, a)	✓
(6, 6, x)	✓
(6, 7, x)	
(6, (5, t), x)	
(6, (5, f), x)	
(7, 8, a)	✓
Paths	{P ₁ , P ₂ }

All-C-Uses Coverage

- Test cases include a definition-clear path from every definition to all of its corresponding c-uses.

All-C-Uses Coverage



Associations all-c-uses

(1, (2, t), x)

(1, (2, f), x)

(1, 3, x)

✓

(1, (4, t), x)

(1, (4, f), x)

(1, (5, t), x)

(1, (5, f), x)

(1, 6, x)

✓

(1, 7, x)

✓

(3, 8, a)

✓

(6, 6, x)

✓

(6, 7, x)

✓

(6, (5, t), x)

(6, (5, f), x)

(7, 8, a)

✓

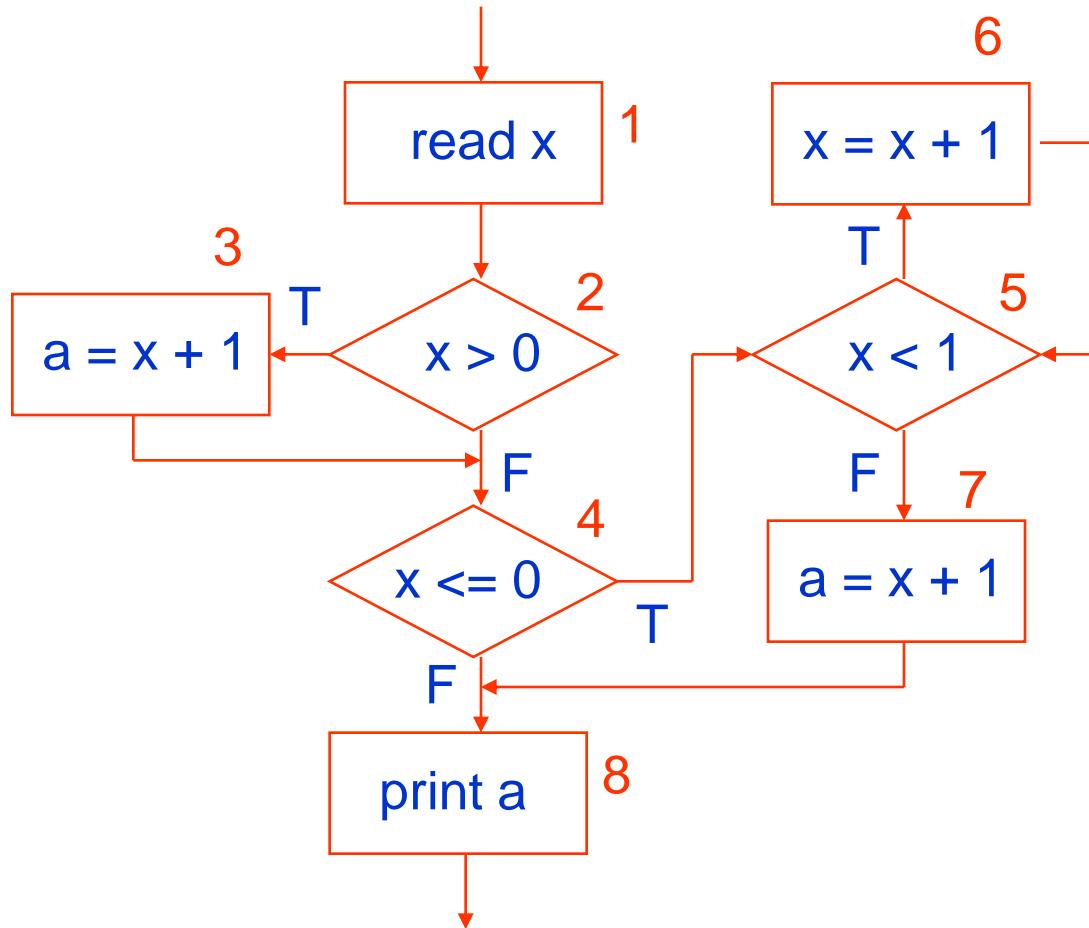
Paths

{P₁, P₂}

All-P-Uses Coverage

- Test cases include a definition-clear path from every definition to all of its corresponding p-uses.

All-P-Uses Coverage



Associations all-p-uses

(1, (2, t), x) ✓

(1, (2, f), x) ✓

(1, 3, x)

(1, (4, t), x) ✓

(1, (4, f), x) ✓

(1, (5, t), x) ✓

(1, (5, f), x) ✓

(1, 6, x)

(1, 7, x)

(3, 8, a)

(6, 6, x)

(6, 7, x)

(6, (5, t), x) ✓

(6, (5, f), x) ✓

(7, 8, a)

Paths

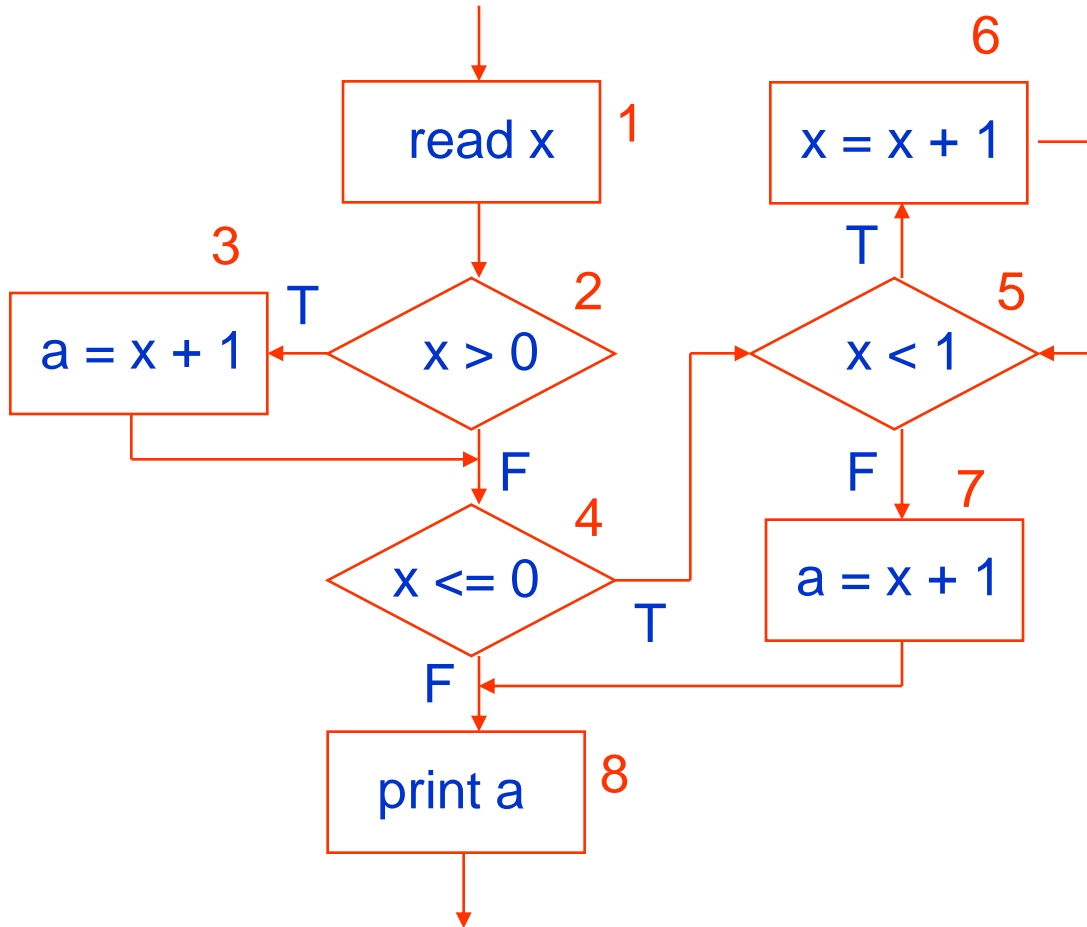
{P₁, P₂}

All-C-Uses/Some-P-Uses Coverage

- Test cases include a definition-clear path from every definition to all of its corresponding c-uses. In addition, if a definition has no c-use, then test cases include a definition-clear path to some p-use.

All-C-Uses/Some-P-Uses Coverage

Associations all-c-uses/
some-p-uses



(1, (2, t), x)

(1, (2, f), x)

(1, 3, x)

✓

(1, (4, t), x)

(1, (4, f), x)

(1, (5, t), x)

(1, (5, f), x)

(1, 6, x)

✓

(1, 7, x)

✓

(3, 8, a)

✓

(6, 6, x)

✓

(6, 7, x)

✓

(6, (5, t), x)

(6, (5, f), x)

(7, 8, a)

✓

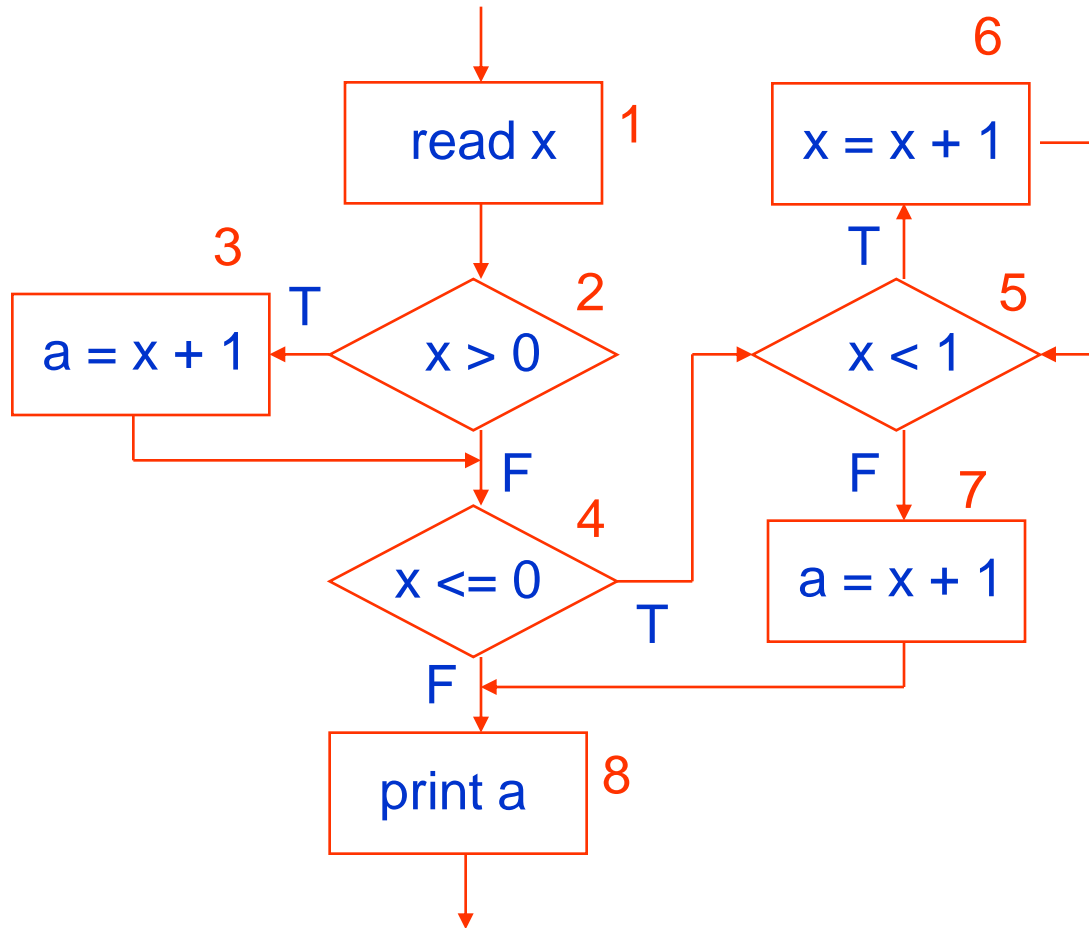
Paths

{P₁, P₂}

All-P-Uses/Some-C-Uses Coverage

- Test cases include a definition-clear path from every definition to all of its corresponding p-uses. In addition, if a definition has no p-use, then test cases include a definition-clear path to some c-use.

All-P-Uses/Some-C-Uses Coverage



Associations all-p-uses/
some-c-uses

(1, (2, t), x)	✓
(1, (2, f), x)	✓
(1, 3, x)	
(1, (4, t), x)	✓
(1, (4, f), x)	✓
(1, (5, t), x)	✓
(1, (5, f), x)	✓
(1, 6, x)	
(1, 7, x)	
(3, 8, a)	✓
(6, 6, x)	
(6, 7, x)	
(6, (5, t), x)	✓
(6, (5, f), x)	✓
(7, 8, a)	✓

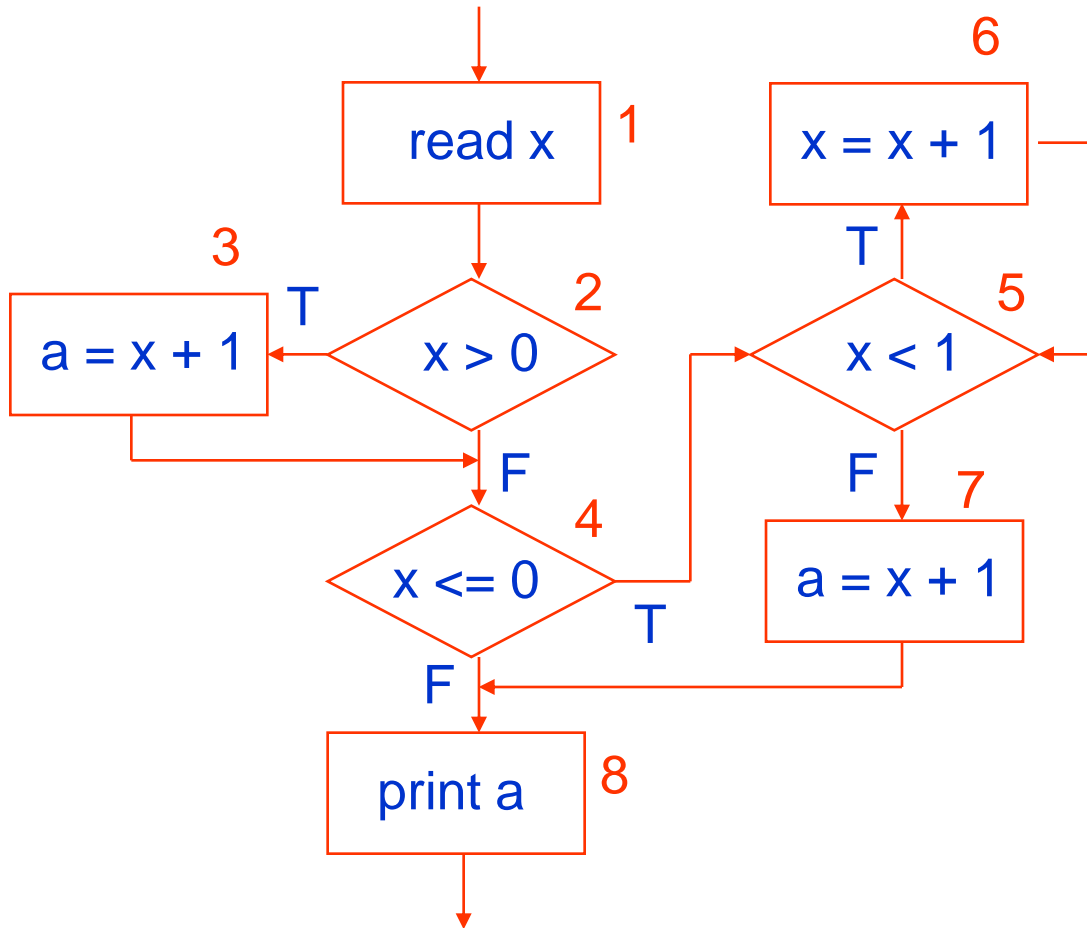
Paths

{P₁, P₂}

All-Uses Coverage

- Test cases include a definition-clear path from every definition to each of its uses including both c-uses and p-uses.

All-Uses Coverage

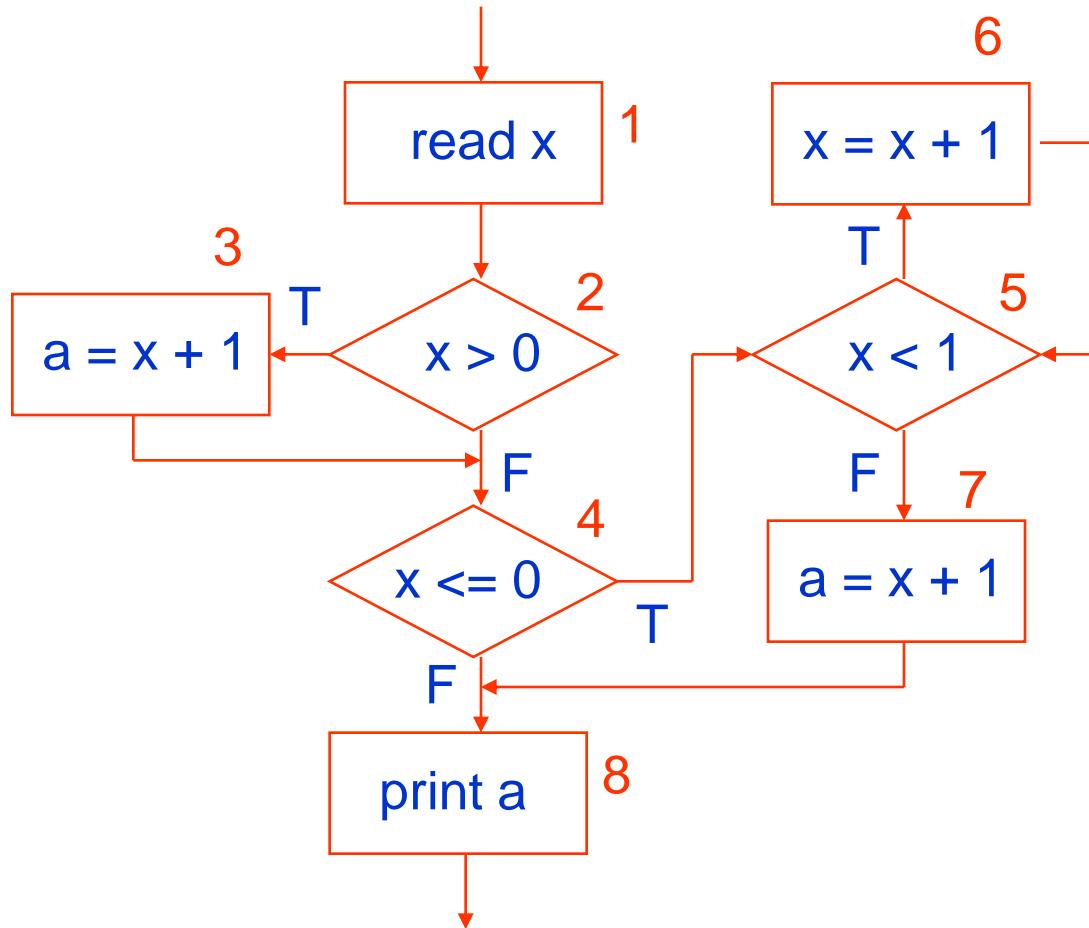


Associations	all-uses
(1, (2, t), x)	✓
(1, (2, f), x)	✓
(1, 3, x)	✓
(1, (4, t), x)	✓
(1, (4, f), x)	✓
(1, (5, t), x)	✓
(1, (5, f), x)	✓
(1, 6, x)	✓
(1, 7, x)	✓
(3, 8, a)	✓
(6, 6, x)	✓
(6, 7, x)	✓
(6, (5, t), x)	✓
(6, (5, f), x)	✓
(7, 8, a)	✓
Paths	{P ₁ , P ₂ }

All-DU-Paths Coverage

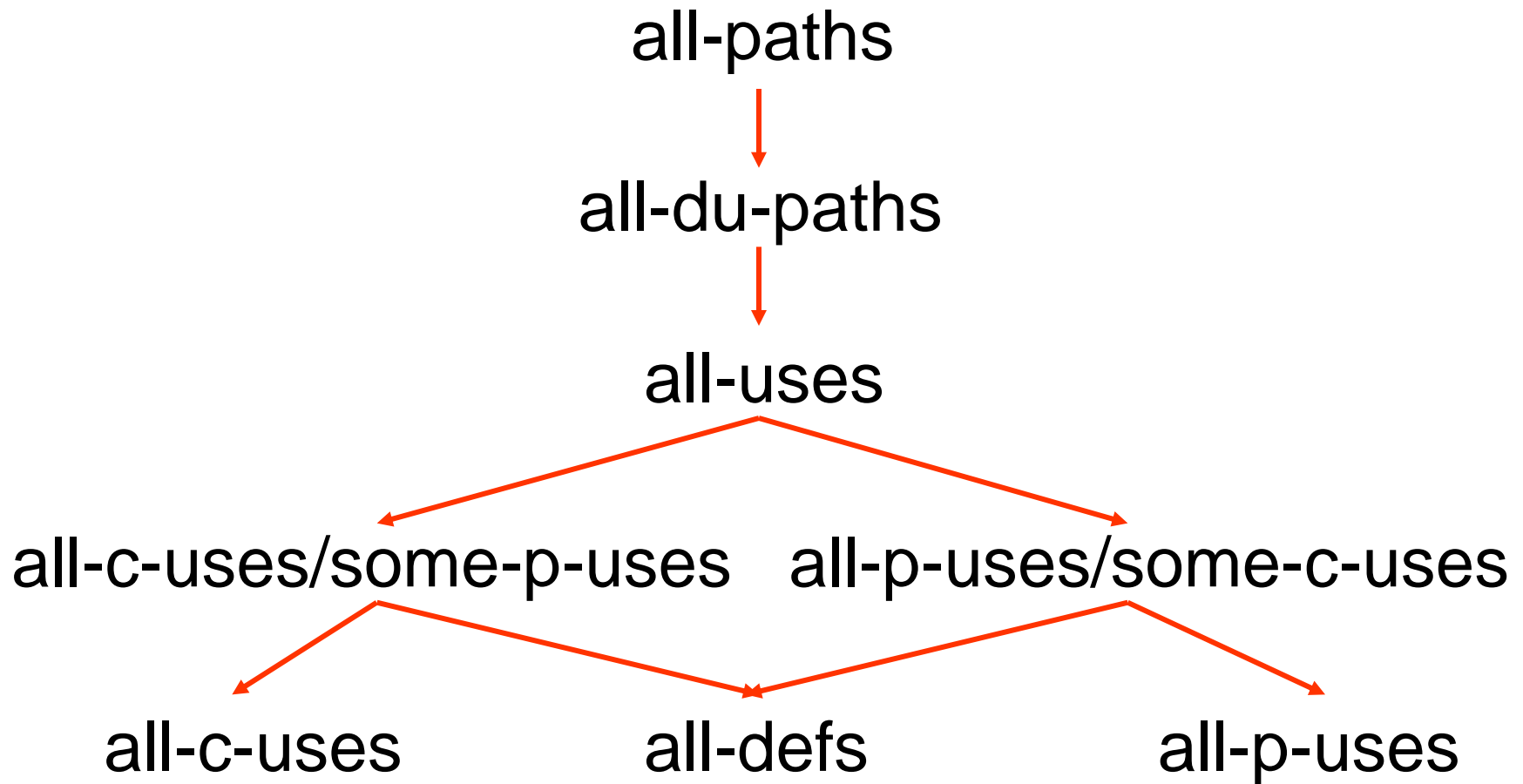
- Test cases include all du-paths for each definition. Therefore, if there are **multiple paths** between a given definition and a use, they must all be included.

All-DU-Paths Coverage



Associations	all-du-paths
(1, (2, t), x)	✓
(1, (2, f), x)	✓
(1, 3, x)	✓
(1, (4, t), x)	✓
(1, (4, f), x)	✓
(1, (5, t), x)	✓
(1, (5, f), x)	✓
(1, 6, x)	✓
(1, 7, x)	✓
(3, 8, a)	✓
(6, 6, x)	✓
(6, 7, x)	✓
(6, (5, t), x)	✓
(6, (5, f), x)	✓
(7, 8, a)	✓
Paths	{P ₁ , P ₂ }

Test Coverage Criteria Hierarchy



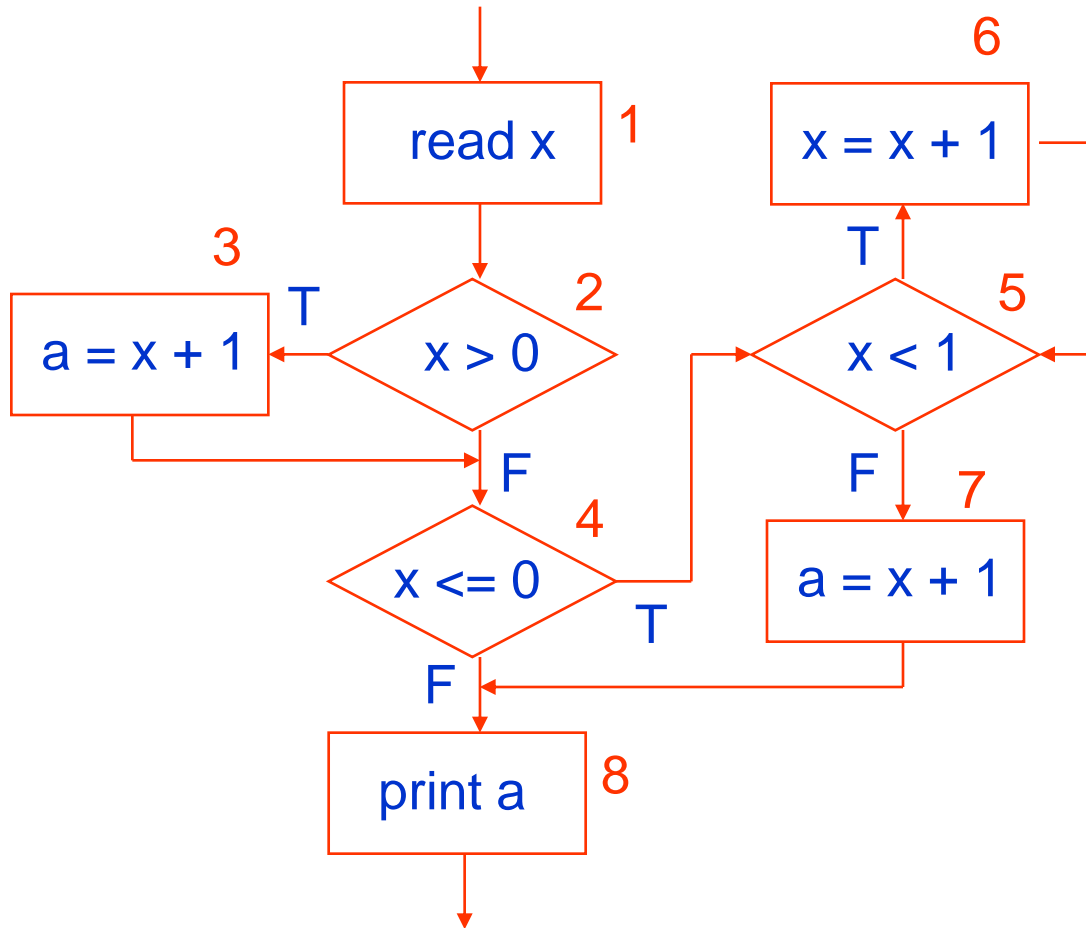
Slices

- A **slice** is a subset of a program.
- When testing a program, most of the code in the program is **irrelevant** to what you are interested in. Slicing provides a convenient way of filtering out **irrelevant** code.
- Slices can be computed automatically by statically analyzing the **control flow** and **data flow** of the program.

Slices

- A **slice** with respect to a **variable** v at a certain **point** p in the program is the **set of statements** that contributes to the value of the variable v at p .
- We use $S(v, n)$ to denote the set of nodes in the control flow graph that contributes to the value of the variable v at node n .

An Example



$S(x, 1) = \{1\}$

$S(x, 2) = \{1\}$

$S(x, 3) = \{1, 2\}$

$S(x, 4) = \{1, 2\}$

$S(x, 5) = \{1, 2, 4\}$

$S(x, 6) = \{1, 2, 4, 5, 6\}$

$S(x, 7) = \{1, 2, 4, 5, 6\}$

$S(a, 3) = \{1, 2, 3\}$

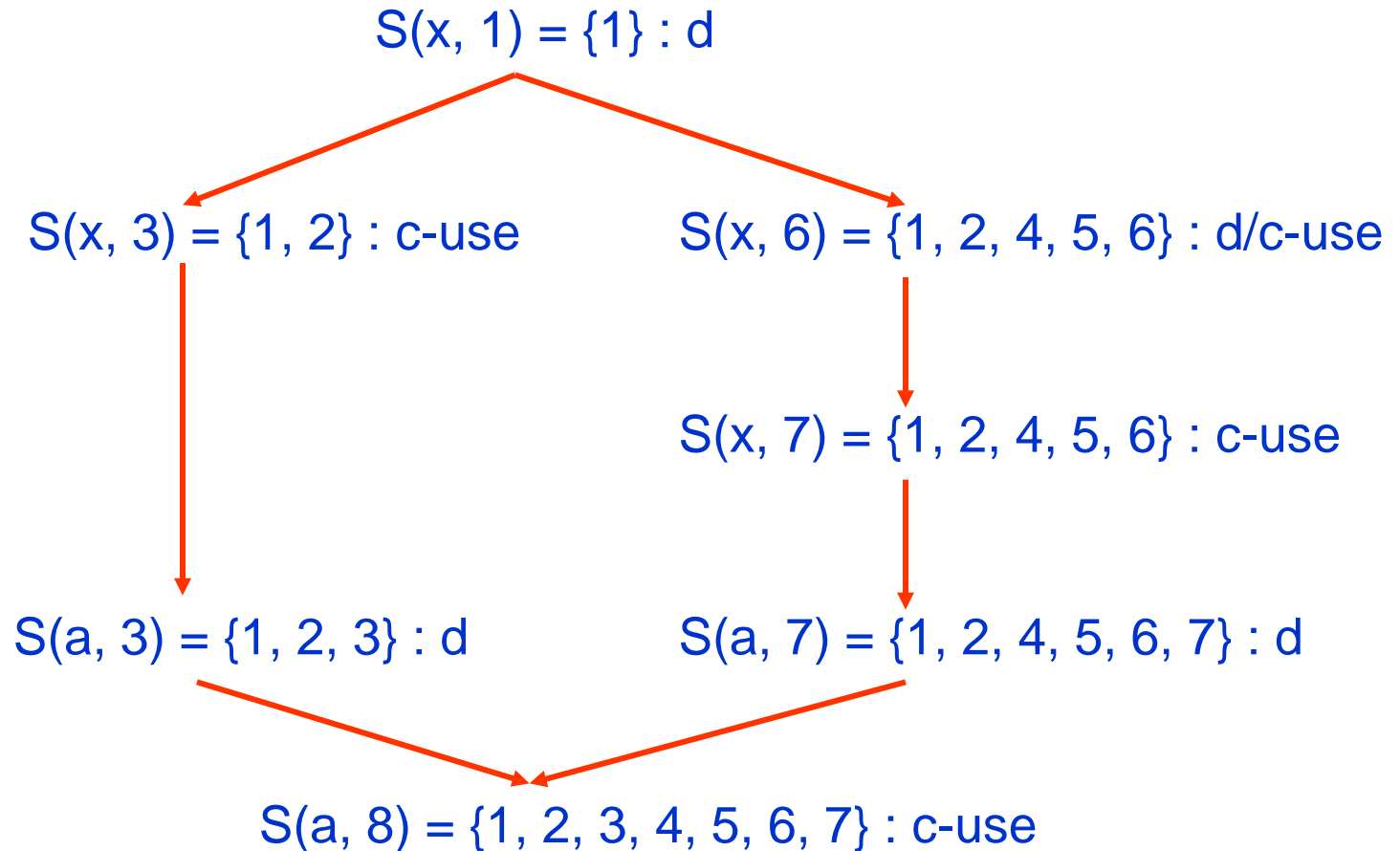
$S(a, 7) = \{1, 2, 4, 5, 6, 7\}$

$S(a, 8) = \{1, 2, 3, 4, 5, 6, 7\}$

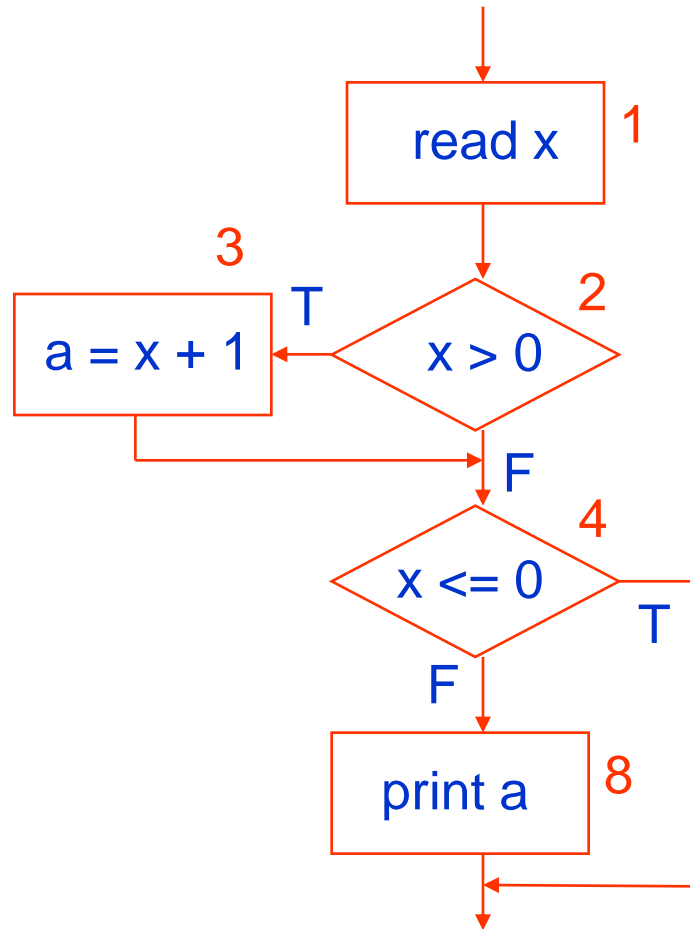
Lattices of Slices

- A definition of a variable v_n at node n usually uses the values of several variables v_1, \dots, v_m .
- The slice $S(v_n, n)$ will contain the slices $S(v_1, n), \dots, S(v_m, n)$.
- These subset relationships induce a **lattice** on slices of different variables.

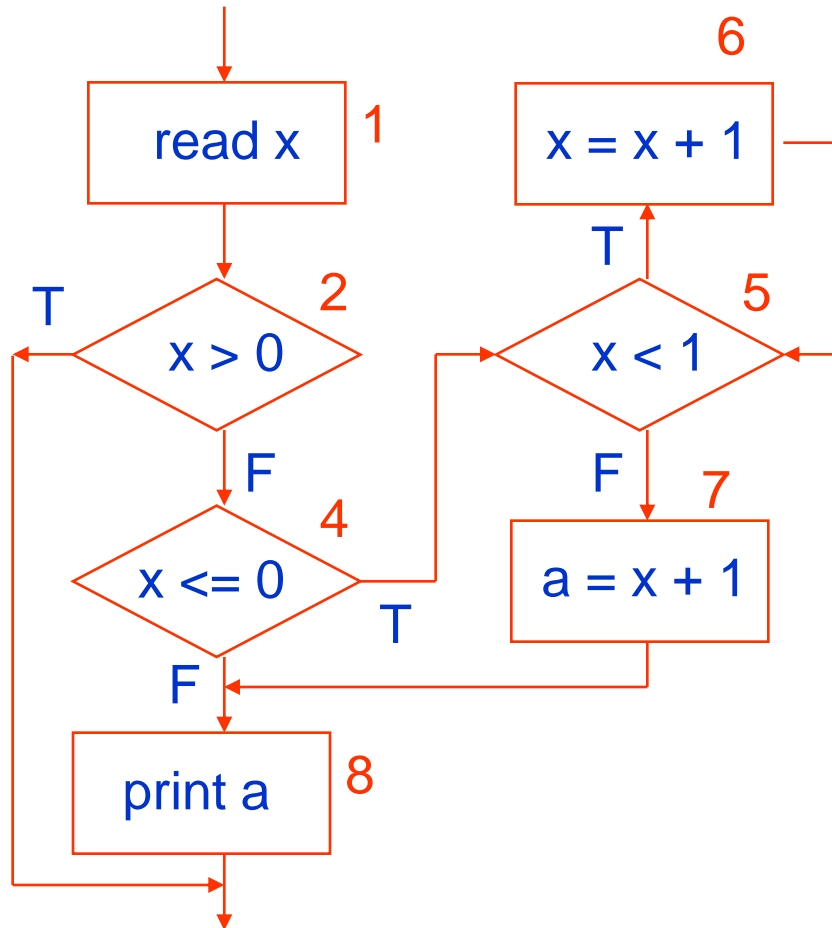
An Example



Test Case I



Test Case II



Exercise: What is S(sum,8)?

```
1 int i;  
2 int sum = 0;  
3 int product = 1;  
4 for(i = 0; i < N; ++i) {  
5   sum = sum + i;  
6   product = product * i;  
7 }  
8 write(sum);  
9 write(product);
```