Defining the Semantics of Agent Based Modelling in InterDyne

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Abstract

This paper defines the semantics of agent based modelling within the Interdyne simulator. A converter has been created that links an agent based model step wise to a difference equation based language, this language is created in such a way that it is directly relatable to lambda calculus which can then be used as definition of the semantics of the agent based model.

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1 Introduction

2 Background

This section explains the rational behind the creation of InterDyne by Clack [1]; InterDyne is bespoke simulation software designed to model emegernt behaviour within the financial markets. This research was inspired by the "Flash Crash" of 2010, this crash can be seen as a change in phase between a stable and unstable market; it has been shown that emergent behaviour in physical systems can lead to phase transitions and postulated that this could also be true within the financial markets [2]. InterDyne hence exists to see if this flash crash and ones like it could be examples of this critical behaviour caused by emergence within the markets.

This section will explain emergence within the financial markets, the approach taken to model these markets, examples of emergence within these models, a method to simulate these models and a detailed description of InterDyne.

2.1 Emergent Behaviour from Interaction Dynamics

Emergent behaviour is a term used to describe macro-behaviour of a system that is not obvious from analysis of the micro-behaviour of the system, more formally this is behaviour that can not be predicted through analysis of any single component of a system [3].

A misunderstanding of emergence can lead to the fallacy of division, this is that a property of the system as a whole most also be a property of an individual component of the system; water for example has a number of properties including being able to be cooled down to become ice and heated to become steam, saying the same must also be true of a molecule of water however is incorrect. This concept continues into economics, being called the fallacy of composition, where what is true for the whole economy my not hold for an individual and vice versa [4].

A simple way to demonstrate emergence is in the Game of Life [5], which is an example of cellular automaton; this game takes place on an infinite two-dimensional grid in which cells can either be 'alive', coloured for example green, or 'dead', a different colour usually black. Wether a cell is 'alive' or 'dead' is based on a set of simple rules:

- 1. 'Alive' cells will transition to be 'dead' cells in the next time step if they have few than two 'alive' neighbours.
- 2. 'Alive' cells with two or three 'alive' neighbours remain 'alive' at the next time step.
- 3. 'Alive' cells will transition to be 'dead' cells in the next time step if they have more than three 'alive' neighbours.
- 4. 'Dead' cells with exactly three 'alive' neighbours will transition to 'alive' at the next time step.

With this simple set up very complex patterns evolving through time can be created, these patterns can be seen as emergence, with an individual cell not being able to encapsulate this behaviour.

Emergent behaviour can be seen occurring naturally, with physics offering many well explored examples, for instance the n-body problem [6]. This historically is explained as n planets in proximity to each other, who interact via gravity in accordance with Newtons laws, this interaction gives rise to motion which is unsolvable analytically and can be viewed as an emergent property of the system. There is a certain amount of intuition with this observation, this is a very complex system and hence it seems reasonable that the interactions may not be analytically solvable. Also as likely expected a case with only one two bodies does have a solution, however the three-body case does not have a solution and generates this emergent behaviour. This outcome is not as obvious and many may assuming that such a simple system would not express emergent behaviour, the three-body problem is hence a good example

of emergent behaviour in a simple system within nature.

Emergent behaviour can be generated in many-body systems, in which these bodies them selfs do not inherently create the emergent behaviour but interactions between them give rise to it. For example in the planet n-body problem interactions are via gravity which passes information about each body to the others, such as a planets mass and momentum, however if the gravity was some how removed, there would be no emergence and the planets would all move with a constant velocity [7].

It is intuitive to assume that the financial markets will demonstrate some interaction based emergent behaviour due to the similarities between the financial markets and a n-body problem. The markets each be seen as a body within this problem that interact via traders who operate in more then one market simultaneously; these trades for example could be hedging against risk or exploiting arbitrage opportunities between markets. The individual markets them selfs could in turn also be seen in a similar way, with different entities such as, dealers, brokers, traders and exchanges acting as bodies. These entities then interact via communications sent between them, such as a sell order sent from a trader to a exchange, in modern markets these processes are automated so the interactions are computers sending messages between each other.

Though one could expect emergent behaviour to occur to some extent in such a large and complex system as the financial markets, continuing with the analogy of n-body problem and remembering the three-body part of it, the question naturally arises, can complex emergent behaviour be observed in a very simplified model of the financial markets?

It has been shown that yes, simple models of the financial markets can produces complex emergence. For example bull and bear markets created from the interaction between two traders operating different simple trading strategies and a market maker [8].

2.1.1 Feedback Loops

A prominent form of emergence in the financial markets is feedback loops, this is where the input information to an entity is directly caused by its output information. The way in which the output information is transformed into the input information can be very simple, directly feeding back into the entity, or very complex going via an number of other entities before returning to its originator. Figure 1 demonstrates these two types of feedback loops with entity 1 having a direct feedback loop and a more complex feedback loop going through two other entities.

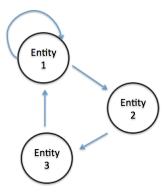


Figure 1: Feedback loops within a system of three interacting entities. Entity 1 has two feedback loops, one direct to its self, the other going through entity 2 and 3 before returning to entity 1.

feedback oscillation in electronics [H. Barkhausen, Lehrbuch der Elektronen-Rhren und ihrer technischen Anwendungen: Rckkopplung, Hirzel:Leipzig, 1935.]. An everyday example of undesirable

behaviour arising from interaction arises when the loudspeaker output of an audio amplification system interacts with the microphone input; the interaction causes a feedback loop, resulting in a high-pitched oscillation.

19.1.2 Feedback loops A good example of undesirable emergent behaviour in the financial markets is the creation of feedback loops, where a component system observes in its input some value that derives from its own output. The process by which an output value is transformed into a derived input value may be complex and transitive (i.e. it may involve processing by one or more other component systems). The description and classification of feedback loops is not straghtforward. Feedback loops may exist in a financial market ab initio, or may be created dynamically after the financial market has been operational for a period of time. It is also possible for feedback loops to increase or decrease in size or effect, to split or merge, or to disappear. Some feedback loops may have a benign effect (we call these stabilising loops) and some are malignant (destablilising loops). In addition to categorising loops as either stablilising or destabilising, we identify whether they are static or dynamic. For a given SoS, a static loop is one that always exists, with unchanging size and effect, and which could be detected by a straightforward static analysis of a formal description of the SoS. Such loops may be intended or unintended. By contrast a dynamic loop may be transient, may have changing size or effect, and might not be detectable via straightforward static analysis. Dynamic loops may be highly unpredictable and difficult to detect, analyse and understand.

A good example of complex interaction dynamics in the financial markets is the creation of feedback loops, where a component system observes in its input some value that derives from its own output. For example, falling market prices can cause traders to sell (to prevent further loss) and this selling causes prices to fall further (which provokes further selling). Some feedback loops may have a benign effect (we call these stabilising feedback loops) whereas others may be malignant (we call these destabilising feedback loops). Control systems routinely use stabilising feedback loops to ensure an output signal stays close to a desired reference signal (See for example [Skogestad, Sigurd, and Ian Postlethwaite. Multivariable feedback control: analysis and design. Vol. 2. New York: Wiley, 2007, Zames, George. "On the input-output stability of time-varying nonlinear feedback systems part one: Conditions derived using concepts of loop gain, conicity, and positivity." IEEE transactions on automatic control 11.2 (1966): 228-238, and Horowitz, Isaac. "Fundamental theory of automatic linear feedback control systems." IRE Transactions on Automatic Control 4.3 (1959): 5-19.]). The process by which an output value is transformed into an observed input value may be complex and transitive (i.e. it may involve intermediate processing by one or more other component systems); this is illustrated in Figure 19.1 below, where interactions between four components are depicted by directional arrows? one direct feedback loop is depicted by an arrow from component 1 to itself, and one indirect feedback loop can be evinced by following the arrows from component 2 to component 3, to component 4, and back to component 2. A practical example of a direct feedback loop would be a trading algorithm that issues orders to a stock exchange where the size and price of those orders is based on the previously issued order (or perhaps on a history of previously issued orders). Alternatively, the size and price of an issued order may depend on the current size of the trader?s inventory? when each order is executed at the exchange this will cause the trader?s inventory to be changed, and this will affect the next order issued. Notice how in these two examples the feedback loop does not exist in a single timestep but rather across timesteps? the trader?s inventory is affected by orders filled in a previous time step, which are due to orders issued in a time step before that, and whose sizes were affected by the size of the trader?s inventory in a further previous time step. The fact that a feedback loop extends across time steps does not make it less real (nor, potentially, less powerful) but it can make it more difficult to identify and to analyse. LC- is using the term time step justified? Can you just say previously in time? As we havent introduced quantisied time yet, nor anything to do with time or how we will model it

Figure 19.1 - Four components, with one direct feedback loop and one indirect feedback loop. When constructing a model of a financial market, the behaviour of the market components will be specified and initial conditions will be set. In such a model, feedback loops may exist ab initio, and may

potentially be discoverable by analysis of the specification and initial conditions. We call this a static analysis of the specification, because it does not require the behaviour of the components to be traced (simulated) in time. Different kinds of static analysis may be required to identify different kinds of feedback loop? for example, identification of a circular loan relationship between banks might require a different analysis to identification of a feedback effect on the calculation of order sizes for trading. Alternatively, feedback loops might be created dynamically as a result of the changing behaviour of the components specified in the model (for example, a new loan relationship may create a feedback loop where there was none previously). The role of the content of messages should not be underestimated, since coupling between components may for example depend upon the sizes of transactions and whether one component is buying or selling. Similarly, dynamic coupling effects may involve several components, and feedback effects may depend upon repeated patterns of messages occurring between several components. To identify and understand such dynamically-created feedback loops requires analysis of the dynamic behaviour of the different components in the model? for example, it requires the values of different functions and state variables to be traced from one time step to the next, and it may require inspection of the history of messages (including their data content) sent from one component to another. We call this a dynamic analysis of the model. As part of dynamic analysis, we may also wish to investigate whether feedback loops increase or decrease in size or effect (that is, their effect on various? typically high-level - properties of the model) and whether such feedback loops split, merge or disappear. For a given model of a System of Systems, including its specification and initial conditions, we define a static feedback loop as one that always exists, with unchanging size and effect. We expect that a static feedback loop is potentially discoverable by a static analysis of the model. By contrast we define a dynamic feedback loop to be any feedback loop that is not static: i.e. it may be transient, may have changing size or effect, and might not be detectable via static analysis. We expect that the identification of a dynamic feedback loop would require a dynamic analysis of the model, and we anticipate that dynamic feedback loops might be highly unpredictable and difficult to identify, analyse and understand.

2.2 Approach to Modelling the Financial Markets

from the book Our focus is to explore emergent behaviour in the financial markets that arises from the dynamics of interaction between component systems, although the modelling and simulation technique that we use is applicable to other Systems of Systems. We aim to assist economists, regulators, and financial services practitioners in understanding the complexity of such emergent behaviour; to model both simple and highly complex systems, to analyse and categorise emergent behaviour, to detect artefacts such as feedback loops, and to utilise modelling and simulation to predict the possible consequences of innovative practices (such as high-frequency trading) and regulatory interventions (such as transaction taxes). Our initial interest in the financial markets derived from reading the reports of the staffs of the CFTC and the SEC into the ?Flash Crash? of May 6th 2010 [REF], coupled with observations from academics [REFS] and from industry practitioners [REFS]. We noticed that much of the approach and reasoning that was employed did not take into account the SoS nature of the financial markets; the issue of emergent behaviour was not discussed, and although the evidence presented in the formal CFTC/SEC report described several key feedback loops we felt that there was insufficient attention paid to the high-level market impact of low-level dynamic interaction, including these feedback loops. Our research therefore seeks to improve the conceptual understading of financial markets as a SoS with emergent behaviour arising from interaction dynamics.

2.2.1 Fine-Grained Microstructure Approach to Financial Markets

from book As we investigated the interaction dynamics involved in the Flash Crash, we realised that it would be necessary to model message-passing at a very fine-grained level. For example, it would be necessary to model the timing of the arrival of limit orders at an exchange, because the sequence in

which limit orders were processed by the exchange might support or defeat a feedback loop. It would be necessary not only to model message-passing but also to run experiments to collect and observe the precise orderings of messages and their content. Furthermore, several reports [REFS] had mentioned the existence of communication delays and it was important to model the effects of increasing delays. Thus, our task has been to model market microstructure [REF] in great detail

2.2.2 Discrete Time

Market Microsture

Therefore, market microstructure describes financial markets both in terms of individual optimization problems and statistic ensembles of ?zero-intelligent? agents. Complicated global phenomena emerge as a result of the local interactions between many heterogeneous agents when the system throughput becomes sufficiently large.

from the book When viewed in ?human time?, the financial markets appear to operate in continuous time. However, at a very fine-grained level of detail all computer operations are effected in discrete time dictated by the change in voltage of a system clock (a chip that emits an extremely precise square-wave oscillating voltage). The passing of messages between two component systems of a financial market is a communication between two discrete-time systems linked by a transmission system; the transmission system itself would comprise a sequence of cables and intermediary devices, where the intermediary devices are typically operating in discrete time yet the cables (and the transmission delays introduced by the lengths of those cables) do not operate in discrete time. Yet despite the continuoustime nature of some parts of the transmission system, a message will only be received by a computer at a discrete time determine by the receiving computer?s system clock (a message arriving earlier will not be processed until the next triggering edge of the clock voltage). A challenge in modelling the interaction behaviour of financial markets is the linking of the extremely fast behaviour of discrete-time computers (and the automated trading and matching algorithms that they run) with the comparatively slow human observation of market behaviour. Another view of the markets that can be taken is an exceptionally large grain approach, where instead of looking at the markets in incredibly small time steps you instead look at larg ones, such as days, weeks, months or even years. Though this is not the approach taken in our research it will also lead to discrete time, where each time tick could be a new day. This approach could be used when investigating stock protifolies which are only rebalanced rarely.

2.3 Example

Day and Huang [Day, R. And Huang, W., ?Bulls, Bears and Market Sheep?, Journal of Economic Behaviour and Organisation, 1990] for example have demonstrated how interactions between two simple but different trading strategies and a market-maker can cause complex emergent features of stock market prices such as alternating periods of rising (?bull market?) and falling (?bear market?) with sudden switching between the two at irregular intervals. Further, Lyons [Lyons, R.K. ?A Simultaneous Trade Model of the Foreign Exchange Hot Potato?, Journal of International Economics 42 (1997) 275?298] has shown how a feedback loop can emerge between foreign exchange dealers, causing them to repeatedly transfer inventory between themselves. Yet these are simple models of interaction. Our aim is to develop a framework for modelling and analysing more complex emergent behaviour that arises from the dynamics of interaction, and in the context of our case study to analyse behaviour that may increase risk to the stability of the financial markets.

2.3.1 Hot Potato

To understand the hot potato effect one must first know that High Frequency Traders have strict inventory limits and that when these limits are passed they are said to be in a "panic state". During a panic state the traders will issue large sell market orders to reduce their inventories back into their ideal

trading regions. A High Frequency Trader can go into a panic state when it unintentionally buys more inventory then intended, which can happen due to information delays in the confirmation of purchases. It is thought that in the flash crash High Frequency Trades panicked when buying from a mutual fund who issued an unusually large sell order. Once one High Frequency Trader has panicked its now sold inventory can be bought by another trader who, again because of information delay, surpass their inventory limits and in turn panics. This processes can continue indefinitely depending on the system and is known as the hot potato effect as the inventory is constantly passed around and not retained by an one trader [9]. This feedback effect has been shown, in the InterDyne simulator, to create instabilities in market prices and even lead to crashes [10].

2.3.2 Flash Crash

A flash crash is defined as a quick drop and then recovery in securities prices, with the most infamous crash occurring on the 6th of May 2010 and lasting for around 20 minutes in which time almost one trillion dollars of market value was lost [11].

There is no consensus on the exact cause of the flash crash, however a number of theories exist. The theory that InterDyne models is that the flash crash was caused by an interaction effect between High Frequency Trader Market Makers, known as the hot potato effect [9].

2.4 Agent Based Modelling

2.4.1 Benefits

2.4.1.1 Tracking Messages

2.4.1.2 Conceptually Easy to Understand

2.5 InterDyne

InterDyne is a simulator designed to look at interaction dynamics, these dynamics have been with in the financial sector but can in theory be any interacting system. This is an agent based simulator, this means that each component of an interacting system can be expressed as an agent, in the case of a financial system agents could be individual traders. Interactions between the agents can then be defined, these could be messages sent between a trader and an exchange for placing an order. Once the simulator is set up in this way it can run through steps, at each step the interactions between the agents are passed and each agents response to the interaction is processed, these steps can represent discrete time. InterDyne adds no direct mechanism that would force the system as a whole to exhibit any specific behaviour, any emergent behaviour experienced by the system is a result of the interaction dynamics only.

A more complete way of labelling InterDyne would be as; a simulator used to investigate interaction dynamics and feedback effects in non-smooth complex systems [1].

from book Interdyne is a simulator that is designed to allow for exploration of interaction dynamics and feedback effects in non-smooth complex systems, though this is a general purpose simulator that can be used in a variety of fields its setup makes it especially sorted to modelling the financial system that has been described above. Below the aspects of Interdyne will be explained showing how it satisfies the criteria needed to model the finical markets. Like other agent-based models InterDyne operates in discrete-time, this discrete-time can be left without a proper definition in terms of real time, this is normally done in experiments that are interested purely in general behaviour of a system. Though real time mapping is easily achievable by simply taking the smallest time step that will need to be used with in a simulation and then mapping all time steps as a integer multiple of it. Being an agent-based model InterDyne allows communication between agents as the only form of interaction. This communication can be done in a one-to-one or one-to-many format, allowing for agents to send out broadcast messages which can be read by all other agents or send private correspondents that can only

be seen by one other agent. Both of these messaging types are needed in modelling the markets, for example an exchange would send out a broadcast message to all members updating them on the order book, where as a trader would send a private message to a exchange when they want to place a order. To allow a full understanding and the precise use of these messages, a communication topology can be defined within InterDyne. This topology will defined the interaction paths between agents and as such which communication routes are possible and which are not. This topology takes the form of a directed graph (allowing on agent to trader with another but not vice versa) with the agents acting as the nodes and the communication paths acting as the edges. As with most real systems messages are not passed instantaneously and as such InterDyne supports the use of information delays, these delays are unique to each interaction path between agents, as defined in the communication topology. These delays apply to any messages using these interaction paths, whether the message is defined as a one-to-one or a one-to-many.

To allow InterDyne to model a system of systems and not just a flat system each agent can be modelled with differing levels of detail. This can take the form of having a simple agent generating outputs dependent on a statistical distribution, interacting with a trading algorithm, which contains a great amount of detail and complexity. An agent can also contain another InterDyne simulation as its internal structure, giving a true system of systems depth to the model. The InterDyne simulator as a whole is built to be deterministic, meaning that any run of an experiment that contains the same inputs will always give the same output. This behaviour is very beneficial for analysis of low-level interactions that cause complex behaviour as it allows for a more detailed examination of the causal pathways that cause this behaviour. Though InterDyne is designed to be deterministic, non-determinism can be added to a simulation in two different ways. Either non-deterministic elements can be added directly to the agents (such as use of stochastic calculus to calculate some aspect of placing orders), or for an agent that receives multiple messages in one time step (such as an exchange receiving orders from a large number of traders) these messages can be sorted randomly (alternatively they can be sorted according to the senders identity). This random sorting is in actuality pseudo-randomly, as for every run of the simulation the same random order will be reached, this can be changed to being truly random (or as much as a computer can allow) using a different seed for each run of the simulation.

2.5.1 Harness

3 Description and analysis of the problem

- 3.1 Why Agent Based Modelling is not enough
- 3.1.1 One-to-Many Problem
- 3.1.2 Semantics of the System
- 3.1.3 Inverse Function Problem?
- 3.2 Difference equations
- 3.2.1 Benefits and Problems
- 3.2.2 Lack of Visualisation
- 3.2.3 Optimisation Problems

3.3 Two Views Approach

from book As can be seen in the previous sections there is no one perfect method for modelling the interaction dynamics and emergent behaviour with in the financial system. Due to the nature of this system it has been concluded that the two most useful models are difference equations and agent based

models, however these two methods give very different views of the system making it impossible to be able to claim that one single method is more useful then the other in all cases. From this problem a natural question arises: is it possible to combine these two methods and hence reap the benefits that they both have, off setting the negatives of each other? The answer to this question we call the two-views approach, this is a way of combining both methods to tackle the same problem. The way in which we combine these two methods is to first define the problem using difference equations, allowing the benefits of this method to be used such as defining the semantics of the problem. Once the problem has been defined it is converted into an agent-based model using series of correctness preserving transformations. This allows the now agent-based version of this problem to still contain the same information that was present in its difference equation form, while now also now being able to be modelled with the benefits of the agent-based model. This method is specialised and a custom language for difference equations has been defined, that is an expansion of lambda calculus. This language has been defined in such a way that it can be used to express a problem so that the function of the agent-based model can still be fully utilised. The agent-based language that is used is designed to contain all the aspects need for expressing the financial markets: message passing, communication delays and interaction topology definition. We call this bespoke agent-based model Interdyne.

4 Converter

- 4.1 New Language
- 4.1.1 Syntax/Grammer
- 4.1.2 Parser
- 4.1.3 Examples
- 4.1.3.1 Simple Example
- 4.1.3.2 Complex Example
- 5 Conclusion
- 5.1 Further Work
- 6 Appendix
- 6.1 Appendix 1

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