

Defining the Semantics of Agent Based Modelling in InterDyne

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Abstract

This paper defines the semantics of agent based modelling within the Interdyne simulator. A converter has been created that links an agent based model step wise to a difference equation based language, this language is created in such a way that it is directly relatable to lambda calculus which can then be used as definition of the semantics of the agent based model.

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1 Introduction

This research was inspired by the "Flash Crash" of 2010, this crash can be seen as a change in phase between a stable and unstable market; it has been shown that emergent behaviour in physical systems can lead to phase transitions and postulated that this could also be true within the financial markets [1]. InterDyne hence exists to see if this flash crash and ones like it could be examples of this critical behaviour caused by emergence within the markets

2 InterDyne

InterDyne is bespoke simulator created by Clack and associates [2], it is a general-purpose simulator for exploring emergent behaviour and interaction dynamics within complex systems.

InterDyne design is that of an agent-based model interacting via a harness. This creates a structure of individual autonomous agents who interact through messages sent to one another.

Similar to other agent-based models InterDyne operates in discrete-time rather than continuous time. These quantised time chunks which move the simulation forward can be left with out proper definition, simply having things defined in a number of time steps, or they can be equated to a real time usually with the smallest time gap needed be a single time step and then all other timings being integer multiples of this. This discrete time is most important to message passing, meaning messages between agents are only sent on a integer time step.

Messages in InterDyne are just small packets of data, such as a series of numbers. Agents can only communicate via these messages, meaning that any emergent behaviour observed, that is not directly due to one agent, must be caused by linking of agents mediated by these messages. An agent can send private messages that are only received by a single other agents, one-to-one messages, or can send broadcast messages received by a number of agents, one-to-many messages. To facilitate this a communication topology can be made for InterDyne, this is done in the form of a directed graph determining which agents can communicate with each other. Due to the directional nature of these messages this topology could allow an agent to send messages to another but not be able to receive messages from that same agent. Messages have a defined order to them, an agent will, unless otherwise instructed, always process messages in the order in which they arrive. To change the order in which messages arrive delays can be added to communication paths between agents, this can be a static delay which always applies to messages sent from one agent to another, meaning this will arrive a set number of time steps later. Or a more complex dynamic delay, which is achieved by using another agent to mediate the passing of these messages delaying by an amount decided on in some internal logic. All messages in InterDyne are passed through a harness, this does not alter the messages or delay them¹, but does store the messages and their order which can be used in post analyse.

Each of the agents within an InterDyne simulation can be completely unique and modelled to different levels of complexity, allowing system components to be created to the level needed for the required experiment. As a whole InterDyne simulations are deterministic, repeated experiments will return identical results. However non-determinism can be added via the agents, making some part of an agent stochastic will lead to repeated experiments on the whole returning different results. A pseudo-random element can also be added by instructing InterDyne to randomly sort the message order for any agent receiving multiple messages in one time step. This is only pseudo-random as, as long as the same seed is used each run of the simulation will order the rearranged messages in the same way.

2.1 Emergent Behaviour from Interaction Dynamics

As mentioned previously InterDyne is designed to allow the simulation and investigation of emergent behaviour caused by interaction dynamics.

¹Unless instructed to using the static delay.

Emergent behaviour is a term used to describe macro-behaviour of a system that is not obvious from analysis of the micro-behaviour of the system, more formally this is behaviour that can not be predicted through analysis of any single component of a system [3].

A misunderstanding of emergence can lead to the fallacy of division, this is that a property of the system as a whole must also be a property of an individual component of the system; water for example has a number of properties including being able to be cooled down to become ice and heated to become steam, saying the same must also be true of a molecule of water however is incorrect. This concept continues into economics, being called the fallacy of composition, where what is true for the whole economy may not hold for an individual and vice versa [4].

A simple way to demonstrate emergence is in the Game of Life [5], which is an example of cellular automaton; this game takes place on an infinite two-dimensional grid in which cells can either be 'alive', coloured for example green, or 'dead', a different colour usually black. Whether a cell is 'alive' or 'dead' is based on a set of simple rules:

1. 'Alive' cells will transition to be 'dead' cells in the next time step if they have few than two 'alive' neighbours.
2. 'Alive' cells with two or three 'alive' neighbours remain 'alive' at the next time step.
3. 'Alive' cells will transition to be 'dead' cells in the next time step if they have more than three 'alive' neighbours.
4. 'Dead' cells with exactly three 'alive' neighbours will transition to 'alive' at the next time step.

With this simple set up very complex patterns evolving through time can be created, these patterns can be seen as emergence, with an individual cell not being able to encapsulate this behaviour.

Emergent behaviour can be seen occurring naturally, with physics offering many well explored examples, for instance the n-body problem [6]. This historically is explained as n planets in proximity to each other, who interact via gravity in accordance with Newtons laws, this interaction gives rise to motion which is unsolvable analytically and can be viewed as an emergent property of the system. There is a certain amount of intuition with this observation, this is a very complex system and hence it seems reasonable that the interactions may not be analytically solvable. Also as likely expected a case with only one two bodies does have a solution, however the three-body case does not have a solution and generates this emergent behaviour. This outcome is not as obvious and many may assuming that such a simple system would not express emergent behaviour, the three-body problem is hence a good example of emergent behaviour in a simple system within nature.

Emergent behaviour can be generated in many-body systems, in which these bodies them selfs do not inherently create the emergent behaviour but interactions between them give rise to it. For example in the planet n-body problem interactions are via gravity which passes information about each body to the others, such as a planets mass and momentum, however if the gravity was some how removed, there would be no emergence and the planets would all move with a constant velocity [7].

2.1.1 Feedback Loops

Emergent behaviour from interaction dynamics can take a number of forms, with a prominent type being feedback loops.

Feedback loops are where the input information to an entity is dependent on the output information of that same entity, from a previous moment in time. For this to be worth investigating all entities involved must be set up so that they make decisions about their output, such as what messages they send or who they send them to, based on some input information.

A very simple example could be two algorithms who send each other messages, see Fig 1, where the message algorithm 1, A1, sends to algorithm 2, A2, is twice what it received and A2 sends A1 three times what it received. It is trivial to find that if the initial input for A1 was 1 then the subsequent four

inputs would be: 6, 36, 216, 1296. However if A2 always returned the same value, say 4, this would not be considered a feedback loop as its result would be constant and trivial.

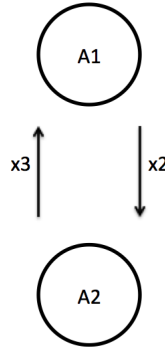


Figure 1: *Feedback loop between two algorithms A1 and A2, with each algorithm altering its output dependent on its input. A1s output is twice its input and A2s output is three times its input.*

This example was very simple and feedback loops can be much more complex, encompassing any number of entities, each of whom can have very complex algorithms for transforming their inputs. Feedback loops can operate across time, meaning that an event in the past can feedback to a present decision. A simple example being a single entity sending itself a message to process in the future effecting its actions at that time. For a feedback loop containing a large number of entities the time scale on which the feedback occurs can be come significantly large.

Not all feedback loops have a negative impact, some can be stabilising feedback loops due to a benign effect.

Feedback loops can be present in a system in two ways, either they can be a constant fixture, a static feedback loop, or they can form and change, dynamic feedback loops. A static feedback loop is present in the system from the start whether this is intentional and known, or unintentional and unknown to the members of the system. Dynamic feedback loops may not be present at the start and can form and change over time, with new entities joining or leaving them, allowing them to increase or decrease in size or effect, to split or merge, or to disappear.

Due to the potential complexity of feedback loops both in construction and in time, they can be difficult to detect therefore methods are usually used to expose them. For static loops, forms of static analysis can be used such as, analysing initial setup, this is possible since the loops do not change through out time. Dynamic loops can be much harder to observe and analyse, an important aspect to detecting these loops is the interactions, messages sent between different entities within the system. Since the loops can evolve over time being able to track and analyse these messages over a time series is vitally important for the analysis of these loops, this time dependent analyse is called dynamic analyse.

2.2 Applicability to Finance

Though InterDyne is a general purpose simulator, its main use thus far has been the exploration of financial markets. In particular InterDyne has been used to explore “Flash Crash” of 2010, during which market prices and rational valuations became disconnected, with some stocks trading as low as a penny per share, this lead to frenzied trading and irrational prices which spread between markets causing a massive price crash [8]. This event lasted around 36 minutes and has been described as “one of the most turbulent periods in their history” for the US financial markets [9].

The hypotheses for this crash which InterDyne exists to investigate, is that this crash is an emergent

phenomenon caused by the interaction between High Frequency Traders (HFTs) within the market. HFTs are a subset of algorithmic traders who normally participate in the market as arbitrageurs or market makers, they invest in ultra-high speed technology allowing them to detect, analyses and react to market condition in nanoseconds [10]. This means HFTs can trade huge quantities of assets in very short time frames, with some estimates stating that 10-40% of all trades were initiated by them during 2016 [11].

The type of interaction between these traders suggested to have caused the crash is “Hot Potato” trading, this is when inventory imbalance is repeatedly passed between HFTs market makers. A market maker is a trader who is required to have both a bid and a ask on the order book at all times, this means in theory that they are constantly buying and selling, a high frequency market maker as expected should be buying and selling very very often. Market makers make a profit from the spread and not long positions, hence they want to keep inventories low to avoid the market moving against them. To achieve this market makers have strict inventory limits that if they pass will cause them to go into what is known as a “panic state”, during this state the trader will sell off an amount of its inventory to return back into its normal trading region. This inventory now sold by the market maker can be bought by another market maker causing them to in turn go into “panic” and sell, this process is “Hot Potato” trading and can in theory continue indefinitely [12].

“Hot Potato” trading was observed in the market during the “Flash Crash” [8], this is thought to have been caused by a combination of an initial large sell order by a mutual fund and delays in communication between HFTs market makers and the exchange on which they were operating on, causing them to buy more inventory than they wanted and go into a “panic state” and hence a “Hot Potato” feedback loop. This section explains in more detail this hypotheses and how InterDyne is set up to investigate it.

2.2.1 Deterministic

The deterministic nature of InterDyne allows for experiments to be run multiple times with the same result always returned, this allows for changes to the experiment setup to be investigated. For example changing the number of traders in the market and comparing this to a previous run allows for an investigation into how many traders are required for emergent behaviour to be observed.

This becomes particularly interesting when comparing the interactions between market makers to that of the n-body problem, like with this problem one could expect emergent behaviour might occur to some extent in a large group of market makers, however the question of whether the emergence persists in a comparable market to the three-body problem and how this compares to a larger market can be investigated.

2.2.2 Message Delays

Allowing the delaying of messages is intrinsically important to the investigation of the hypotheses since the existence of delays is proposed as one of the main aspects in the “Hot Potato” trading that occurred. Delays exist between all aspects of the market which can account for the processing time of the different elements and the transmission time of messages between them. Some of these delays will be static but it has been proposed that the delays related to the exchange actually increased during the crashing, further worsening the situation [8].

Static delays built in InterDyne can be used to investigate the crash to see if it can occur without the need for dynamically varying delays. Dynamic delays created with agents can then be used to further investigate the events that occurred during the crash, allowing a situation to be set up where as more messages are sent to and from the exchange its delays increase. Asymmetric delays can be specified between two agents allowing further investigation into the environment in which a crash is mostly likely to occur and how delays could be altered to reduce this outcome.

2.2.3 Message Passing

2.2.4 Storing Passed Messages/Tracking

The financial markets are complex systems, so the entities involved in feedback loops will likely be interacting with a vast number of other entities, this can make detecting feedback loops very difficult. In the financial markets there can be a number of different objects involved in feedback loops such as, interbank loans or traded assets, this paper and the work that it is building on focus on the latter. A simple example of a feedback loop with traded assets is, a trader selling some of the assets due to falling market prices, causing the prices to be pushed down further and hence this trader to sell more of the asset to minimise their losses. This feedback loop can be considered malignant or a destabilising feedback loop, as it destabilise the market price. However not all feedback loops have a negative impact, some can be stabilising feedback loops due to a benign effect.

Using the example of the seller selling their inventory to mitigate loss again, it can be seen that this loop operates over a time series, the seller sells some of their stock causing the price to go down then, however the process for this to happen and the seller to become aware of it is not, so at a later time the seller will see the drop in price and hence sell more stock.

Since the loops can evolve over time being able to track and analyse these messages over a time series is vitally important for the analysis of these loops, this time dependent analyse is called dynamic analyse.

With InterDyne it is possible to trace full information about (i) all messages sent by an agent; (ii) all messages received by an agent; and (iii) all messages held in a delay queue awaiting delivery to an agent. The latter is possible because of the way that InterDyne implements delays ? the simulator harness receives all messages output by agents, determines their destinations, and constructs queues of messages awaiting delivery to each agent.

2.2.5 Discrete Time

the time gaps between events are just as important as the events themselves, since for example excessive time gaps may represent information delays that have been suggested by some observers to be contributory to emergent behaviour such as the Flash Crash (CFTC and SEC 2010, Nanex 2010b). Thus, we require a discrete-time model rather than a discrete-event model; furthermore, our interest is focused on the interaction between entities rather than on the entities themselves, and we require the ability to observe these interactions in detail.

To model the market microstructure, message order and delays, time progression within the market must also be modelled. Though naively it is easy to assume that this time is continuous, this is not always the case and discrete time can sometimes be used. For example the market can be looked at in a long time horizon, possibly for portfolios that only rebalance rarely, where the only time jumps of note are days, months or years, then time may progress discretely in chunks relating to the desired time step. Conversely very small time scales may be investigated, this is the case that pertains to HFTs market microstructure. Looking at very short time gaps it can be seen that the market actually operates at discrete intervals only progressing in very short time steps. This phenomenon is due to the use of electronic markets, since all markets that HFTs trade on are controlled by a computer they operate at a time set be the computers internal clock. Though computers can have a large amount of precision their clocks do not operate continuously and are in fact using discrete time prescribed by the change in voltage of an internal system clock, done by creating a square-wave oscillating voltage. Hence all trading on electronic markets, whether or not it started in continuous time, was sent by a human, will be curtailed into discrete time by the exchanges computers.

To a human this will still appear as a continuous time scale, however HFTs operate at such small time scales that this discrete time is comparable and therefore important to modelling them.

2.2.6 Message Ordering

Due to the speed at which HFTs trade, the order in which events happen becomes very important. For example if two orders sent to an exchange are processed in the wrong order this could cause or destroy a feedback loop, hence making meaningful analysis impossible. Therefore a fine-grained approach which keeps track of both timings of interactions and ordering of messages between entities is required; modelling and storage of the precise order of message-passing and the messages is hence needed. To correctly order messages delays also have to be taken into account, these can be from constant elements such as how long it takes messages to pass through the cables between computers, or varying elements for instance the time taken for an exchange to process an order, which can increase with large traffic [8]. Hence the approach to modelling a market in this detail requires the correct storage of message-passing, arrival order (that can be altered with different delays) and content.

2.2.7 Agents

It has been shown that yes, simple models of the financial markets can produce complex emergence. For example bull and bear markets created from the interaction between two traders, operating different simple trading strategies, and a market maker [13].

To create InterDyne, a modelling technique on which to build the simulator had to be decided upon. This technique had to satisfy the previously discussed requirements for market microstructure modelling; discrete time, message-passing, arrival order and storage of messages. The chosen technique for the InterDyne project was agent-based modelling [14]

An agent-based model [REF] provides an attractive fit to modelling interaction dynamics in a System of Systems, since each component can be modelled by a separate agent or by a group of agents with varying levels of detail, with private communication within a group; furthermore, messaging and discrete time are handled naturally, and numerical solutions can be obtained for large problems that are analytically intractable. However, we were initially wary of this approach because of the limitations that cause agent-based models to be not widely accepted by economists, as described for example by Gould et al [REF 2013] and Leombruni and Richiardi [REF]. For our purposes, the most important limitations appear to be: ? Although each agent is fully specified, the model as a whole may lack a formal definition. ? It can be difficult to track how a specified input parameter affects the output, and parameter-estimation may be achieved in a way that is not representative of all possible outcomes the model can produce. ? Finding a set of agent rules that produces a specific high-level behaviour provides no guarantee that it is the only set of rules to do so. Leombruni and Richiardi [REF] resolved the first of these problems by providing a formal specification of an agent-based model in terms of a set of recurrence relations. This has the added advantage that the recurrence relations are easily understandable by non-programmers. They also showed how to ameliorate the second problem by analysis of the sensitivity of outcomes to parameter selections. The third problem remains, yet it is a problem shared by a wide range of models [REFS? HMMs?].

based model [REF] provides an attractive fit to a SoS, since each component system can be modelled by a separate agent or by a group of agents with private communication within a group (perhaps using a hierarchical agent-based model [REF]); furthermore, messaging and discrete time are handled naturally, and numerical solutions can be obtained for large problems that are analytically intractable. However, we were initially wary of this approach because of the limitations that cause agent-based models to be not widely accepted by

Agent based models (ABMs) are a kind of model which can be used for simulations. These simulations work by having a number of independent agents who each have their own behaviour interacting via messages sent between them, this system created by these interacting agents is the model. Because ABMs take a radically different approach to the modelling of systems the difference equations, using a number of interacting agents each with their own behaviour that could be described as grouped difference equations instead of that large block of logic, which is inherent in difference equations, they

can tackle some of the issues in a very different way. ABMs also have the ability to be run at a far faster pace than difference equations under the right circumstances, this is because they can be run in parallel computing architecture setups, allowing multiple calculations to be run simultaneously on different machines. They also tend to require far less recomputation than their difference equation counterparts due to the way, which they are set up and then run. These features make this method far more efficient for very large systems that otherwise could take a very large amount of computation time. ABMs operate in a step-by-step way making it very natural to create an ABM that has discrete time as each step. This means that at each step all the agents will send out their messages to other agents telling them their interactions at that particular time interval, this is a similar behaviour to how the real financial market operates. The exact time interval can be chosen by deciding upon the smallest time unit which will be used in the simulation and having everything else operate at integer multiples of this base time.

Discrete time is also used in coarse-grained models, where in different models an individual time step may represent an intraday period, a day, or perhaps a month (see for example [REF Huang et al] [REF YanClack, etc]). An important characteristic of discrete-time models is that each time step represents an equal amount of time; the extent of each time step may be defined (e.g. as a number of seconds, minutes, hours or days), though in some models (e.g. [REF Huang et al]) the extent is left unstated in the model and may then be instantiated in a numerical simulation.

2.3 InterDyne Detail Operation

2.4 Examples

Day and Huang [Day, R. And Huang, W., "Bulls, Bears and Market Sheep", Journal of Economic Behaviour and Organisation, 1990] for example have demonstrated how interactions between two simple but different trading strategies and a market-maker can cause complex emergent features of stock market prices such as alternating periods of rising ("bull market") and falling ("bear market") with sudden switching between the two at irregular intervals. Further, Lyons [Lyons, R.K. "A Simultaneous Trade Model of the Foreign Exchange Hot Potato", Journal of International Economics 42 (1997) 275-298] has shown how a feedback loop can emerge between foreign exchange dealers, causing them to repeatedly transfer inventory between themselves. Yet these are simple models of interaction. Our aim is to develop a framework for modelling and analysing more complex emergent behaviour that arises from the dynamics of interaction, and in the context of our case study to analyse behaviour that may increase risk to the stability of the financial markets.

2.4.1 Hot Potato

This feedback effect has been shown, in the InterDyne simulator, to create instabilities in market prices and even lead to crashes [15].

2.4.2 Flash Crash

A flash crash is defined as a quick drop and then recovery in securities prices, with the most infamous crash occurring on the 6th of May 2010 and lasting for around 20 minutes in which time almost one trillion dollars of market value was lost [16].

There is no consensus on the exact cause of the flash crash, however a number of theories exist. The theory that InterDyne models is that the flash crash was caused by an interaction effect between High Frequency Trader Market Makers, known as the hot potato effect [12].

There are numerous examples of emergent behaviour in the financial markets caused by interaction dynamics within the SoS, here we will look at how the US markets "Flash Crash" of May 6th 2010 [CFTC-SEC, 2010. "Findings regarding the market events of May 6, 2010"] may have been caused by these interaction dynamics. The term "Flash Crash" here is used to describe an event within a financial market where the price of commodities plummets extremely quickly before rapidly

rebounding. This kind of behaviour tends to go hand and hand with commodities becoming disconnected from their fundamental value, such as stocks for companies trading at far lower prices despite the fact that mothering has change about the company in question. The crash in question occurred within the E-mini SP 500 market, EXPLAIN WHAT THIS MARKET IS, lasting approximately thirty minutes [REF] with the prices for some stocks falling as low as a penny a share [REF]. FIGURE OF FLASH CRASH??? There has been a large amount of speculation about the cause of this crash with blame levelled at a large sale by a mutual fund, spoofing by a independent trader and the hot potato effect between High Frequency Traders (HFTs), it is the later that we are interested in here. HFTs are algorithmic traders who use equipment that allows them to operate at nanosecond speeds [REF], this means huge amounts of trading can occur between HFTs before a human can process what has happened. Not sure how to phrase this but want to say that a lot can go wrong before a human realises HFTs often operate as a Market Maker, these are entities that both buy and sell with the market under a set of rules, such as having to always have a bid and ask on the order book, they are then rewarded by having discounts applied to their trades. Market Makers make their profit of the difference in price between buying and selling assets and not of the fluctuation in price of an asset over time. They would not buy assets with the aim of selling them in a few days as they think the price would increase, instead they buy and sell the assets normally within a few milliseconds. As such having a large inventory of any asset is considered to be risky by the Market Maker and they will normally have thresholds on their stock, if these thresholds are passed, they have more stock then they want, they will enter an aggressive selling phase, quickly reducing their stock back below their thresholds. When this occurs the HFT is said to be in a panic state, the inventory at which this panic state occurs can be dynamic, changing demanding on the perceived risk within the market and how the Market Maker is trying to preform. Since HFTs can place orders so quickly and make their profit of buying and selling they will normally have orders near or at the touch, the best bid and ask. This means that if you trade on the market you are likely to execute your trade with a market maker first SAY WHAT PERCENTAGE OF TRADES THE MARKET MAKERS ARE RESPONSIBLE FOR [REF]. This means that if a Market Maker goes into panic it is likely to sell its stock to another Market Maker; this creates links between the Market Makers as they will buy and sell to each other during panic states. There are a number of methods used for exiting a panic state, enough inventory can be solid to bring the Market Maker back to exactly its limit, more can be solid to bring it below its limit by a set amount or all the inventory can be solid to reduce the risk to the Market Maker to zero. Each of these different options changes how much stock will be passed on to another Market Maker during the panic state. The question then arises, what happens if the Market Maker who buys this excesses stock is already near its inventory limit? In this case the receiving Market Maker can also enter panic, causing it to sell its inventory back to the market. As can be imagined in the right market conditions, this inventory can be picked up by another Market Maker who is also close to their limit and hence the processes can continue. If this inventory passing between the Market Makers forms a feed bank loop, where the initial Market Maker receives the stock again before selling it on for a second time, it can be said that ?Hot Potato? effect is occurring, this is simply the processes of passing inventory around traders in a loop. There are a number of reason a Market Maker could be near its limits or go into panic, it could be already near its limits and then be forced to buy more inventory by the exchange rules. It could dynamically shift its risk limits changing its inventory boundaries causing it to go into panic or at least approach its limits or it could make a number of assumptions about its sell orders which may be incorrect. A reason assumption are made is because of time delays with in the system.

3 Description and analysis of the problem

3.1 Why InterDyne is not enough

3.1.1 One-to-Many Problem

3.1.2 Semantics of the System

3.1.3 Inverse Function Problem?

3.2 Difference equations

Leombruni and Richiardi [REF] have shown how a discrete-time agent-based model of the dynamic microstructure of financial markets can be expressed as a set of recurrence relations. In their formulation, each agent is well described by a state variable given by x_i,t where i is the agent identity ($i \in 1, \dots, n$) LC- in a n agent problem and t is time, and where each $x_{i,t+1}$

3.2.1 Benefits and Problems

3.2.2 Lack of Visualisation

3.2.3 Optimisation Problems

3.3 Two Views Approach

from book As can be seen in the previous sections there is no one perfect method for modelling the interaction dynamics and emergent behaviour within the financial system. Due to the nature of this system it has been concluded that the two most useful models are difference equations and agent based models, however these two methods give very different views of the system making it impossible to be able to claim that one single method is more useful than the other in all cases. From this problem a natural question arises: is it possible to combine these two methods and hence reap the benefits that they both have, offsetting the negatives of each other? The answer to this question we call the two-views approach, this is a way of combining both methods to tackle the same problem. The way in which we combine these two methods is to first define the problem using difference equations, allowing the benefits of this method to be used such as defining the semantics of the problem. Once the problem has been defined it is converted into an agent-based model using series of correctness preserving transformations. This allows the now agent-based version of this problem to still contain the same information that was present in its difference equation form, while now also now being able to be modelled with the benefits of the agent-based model. This method is specialised and a custom language for difference equations has been defined, that is an expansion of lambda calculus. This language has been defined in such a way that it can be used to express a problem so that the function of the agent-based model can still be fully utilised. The agent-based language that is used is designed to contain all the aspects need for expressing the financial markets: message passing, communication delays and interaction topology definition. We call this bespoke agent-based model Interdyne.

4 Converter

4.1 New Language

4.1.1 Syntax/Grammer

4.1.2 Parser

4.1.3 Examples

4.1.3.1 Simple Example

4.1.3.2 Complex Example

5 Conclusion

5.1 Further Work

6 Appendix

6.1 Appendix 1

References

- [1] Tsai-Ching Lu Hankyu Moon. Network catastrophe: Self-organized patterns reveal both the instability and the structure of complex networks. *Scientific Reports*, 2015.
- [2] Christopher D. Clack. The interdyne simulator (2011-). <http://www.resnovae.org.uk/fccsuclacuk/research>, 11 2016.
- [3] Gary O. Langford John S. Osmundson, Thomas V. Huynh. Emergent behavior in systems of systems. In *CONFERENCE ON SYSTEMS ENGINEERING RESEARCH(CSER)*, 2008.
- [4] Norman Ehrentreich. *Agent-Based Modeling: The Santa Fe Institute Artificial Stock Market Model*. Springer, 2008.
- [5] Eugene M. Izhikevich et al. Game of life. *Scholarpedia*, 10(6):1816, 2015.
- [6] Douglas C. Heggie. The classical gravitational n-body problem. astro-ph/0503600, 2005.
- [7] Anne Whitman Isaac Newton, I. Bernard Cohen. *The Principia: Mathematical Principles of Natural Philosophy*. Univ of California Press, 1999.
- [8] U.S. Securities Exchange Commission U.S. Commodity Futures Trading Commission. Findings regarding the market events of may 6, 2010. <https://www.sec.gov/news/studies/2010/marketevents-report.pdf>, September 2010.
- [9] Mehrdad Samadi Tugkan Tuzun Andrei Kirilenko, Albert S. Kyle. The flash crash: The impact of high frequency trading on an electronic market. Working Paper, SSRN. <http://ssrn.com/abstract=1686004> (accessed May 13, 2017)., 2014.
- [10] Bus Inf Syst Peter Gomber, Martin Haferkorn. High-frequency-trading. *Business Information Systems Engineering*, 5:97–99, April 2013.
- [11] Steven Krawciw Irene Aldridge. *Real-Time Risk: What Investors Should Know About FinTech, High-Frequency Trading, and Flash Crashes*. Wiley, 2017.

- [12] Elias Court. The instability of market-making algorithms. MEng Dissertation, 2013.
- [13] Weihong Huang Richard H. Day. Bulls, bears and market sheep. *Journal of Economic Behaviour and Organisation*, 1990.
- [14] Charles M. Macal Wai Kin Victor Chan, Young-Jun Son. Agent-based simulation tutorial - simulation of emergent behavior and differences between agent-based simulation and discrete-event simulation. In *Simulation Conference (WSC), Proceedings of the 2010 Winter*. IEEE, 2010.
- [15] Dmitrijs Zaparanuks Christopher D. Clack, Elias Court. Dynamic coupling and market instability. ., 2014.
- [16] Vikram Bkshi. Simulating interaction in financial markets. MSc Dissertation, 2015.