

Algorithm: Regression Tree Alg.

- ① Begin with all data
- ② For every possible split of data
 $\langle X_L, \bar{Y}_L \rangle, \langle X_R, \bar{Y}_R \rangle$

③ Calculate

$$SSE_L = \sum (Y_{li} - \bar{Y}_L)^2$$

$$SSE_R = \sum (Y_{ri} - \bar{Y}_R)^2$$

- ③ Find split which

$$SSE_{TOT} = SSE_L + SSE_R \rightarrow \text{take the minimum.}$$

- ④ Create the split

- ⑤ ~~Recursively~~ $\langle X_L, \bar{Y}_L \rangle$ Recurse data in step 1 and do 2 steps
 $\langle X_R, \bar{Y}_R \rangle$ " " " " " "

Recurse until "STOP"

STOP # of observation in a node $\leq N_0$.

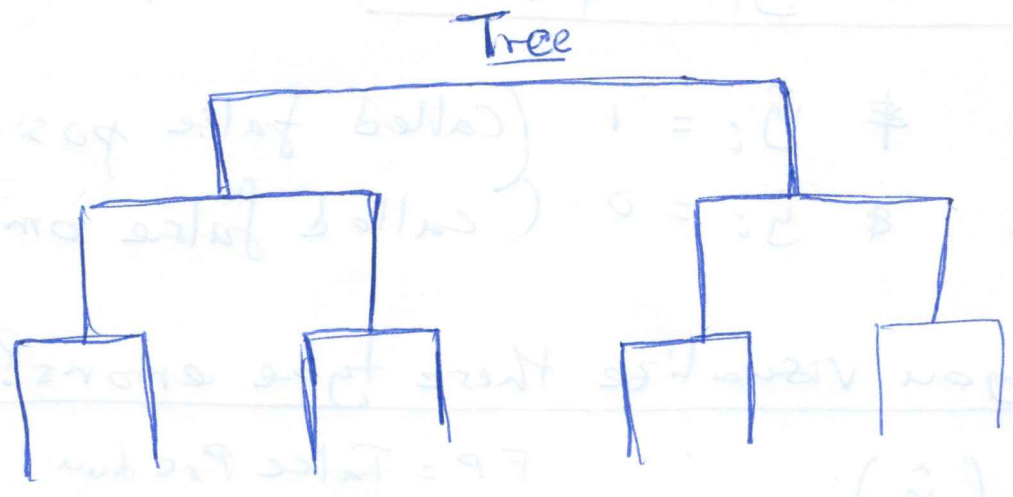
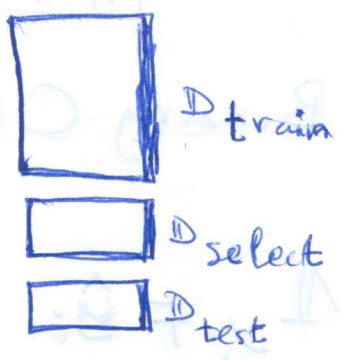
(N_0 is a hyperparameter).

~~Default~~ : N_0

Default : $N_0 = 5$

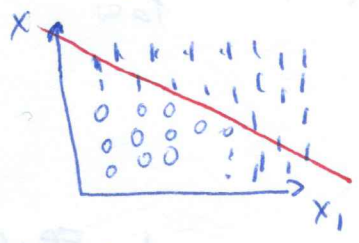
- ⑥ For all leaf nodes, assign $\hat{Y} = \bar{Y}_0$ where \bar{Y}_0 is sample avg of all y 's in node.

If default No=5
How to pick No?



$Y = \{0, 1\}$ binary classification.

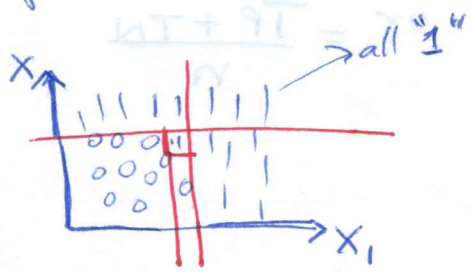
$Y = \{1, 2, \dots, k\}$ classification k -group / labels.



$$H = \{b_0 + w_1 x_1 + w_2 x_2 - \vec{w} \cdot \vec{x} \in \mathbb{R}^3\}$$

$$\phi = \arg \min \left\{ \frac{1}{n} \sum \max \left\{ 0, \frac{1}{2} - (\gamma_0 - \frac{1}{2})(\vec{w} \cdot \vec{x} - b) \right\} + \lambda \|\vec{w}\| \right\}$$

Now feed a tree



A A A	D D D
A A A	R C C
B B B	C C C
C C C	C C C