

Times:

Part A:

$$t_1 = 5.52$$

$$t_2 = 5.58$$

$$t_3 = 5.39$$

$$t_{avg} = 5.50$$

Part B:

$$t_1 = 5.65$$

$$t_2 = 5.75$$

$$t_3 = 5.68$$

$$t_{avg} = 5.69$$

Part A calculations: $t = 5.50 \text{ s}$; $m_1 = 0.448 \text{ kg}$; $r = 0.155 \text{ m}$

$$F_c = \frac{4\pi^2 mr}{T^2} = \frac{4\pi^2 (0.448)(0.155)}{(0.55)^2} \quad T_1 = \frac{5.50}{10} = 0.55$$

$$= 9.06 \text{ N}$$

$$F_{spring} = mg = (0.966)(9.8) = 9.4 \text{ N}$$

Part B calculations: $t = 5.69 \text{ s}$ $m_2 = 0.5487 \text{ kg}$

$$T_2 = \frac{5.69}{10} = 0.569 \text{ N}$$

$$\frac{m_1}{T_1^2} = \frac{m_2}{T_2^2} = T_2 = \sqrt{\frac{m_2}{m_1} \cdot T_1^2}$$

$$= \sqrt{\frac{0.5487}{0.4487} \cdot 0.55^2}$$

$$T_2 = 0.608 \text{ N}$$

Part C calculations:

XA: Distance from center of vertical rotating shaft to point A (top of string): 15.5 cm

AM: Distance from point A to the center of mass: 17.5 cm

XC: Distance from center of vertical rotating shaft to vertical pointer: 22.4 cm

$y_A - y_C$: Vertical distance from point A to pointer: 20.9 cm

$$\theta = \tan^{-1} \left(\frac{x_C - x_A}{y_A - y_C} \right) = \tan^{-1} \left(\frac{22.4 \text{ cm} - 15.5 \text{ cm}}{20.9 \text{ cm}} \right) = \tan^{-1} \left(\frac{6.9 \text{ cm}}{20.9 \text{ cm}} \right) = 18.27^\circ$$

$$r = x_A + AM \sin \theta = 0.155 \text{ m} + (0.175 \text{ m}) \sin(18.27^\circ) \approx 0.21 \text{ m}$$

$$T = \frac{15.2}{10} = 1.521 \quad ; \quad F_c = g \tan(18.27^\circ) = 3.52 \text{ N}$$

$$F_c = \frac{4\pi^2 (0.21)}{(1.521)^2} = 3.58 \text{ N}$$