

REAL ESTATE MODELLING & FORECASTING

EXPLAINING ISTANBUL HOUSING PRICE WITH ECONOMIC INDICATORS & FORECASTING UNIT PRICES CHANGE

ALPARSLAN YARIKTAS 516171003

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1. Introduction

I. Problem Question

- 1. How The Economic Indicators Affect on Housing Unit Price at Istanbul?
- 2. Which indicators more dominant on the prices?
- 3. What must be the equation for Istanbul Unit Housing Price?
- 4. What will be the housing price for 6 months?

II. Literature Review

- The construction industry and other related sub industries are the most crucial aspects of the economy The Turkish housing industry has achieved fast growth in the past fifteen years The macroeconomic importance of the construction industry arises from its multiplier effect It sets 250 sub industries in motion with impacts on both growth and employment.
- Housing and related interests make up a significant portion of the construction industry in our country. The industry's growth rate is influenced by booms/stagnation observed in housing demand and sales. The industry's sensitivity to the total national growth is also high.
- As well the price of a home in the housing sector is determined by the balance of housing supply and demand In the short term, the supply of housing is for the most part fixed, meaning that the main variable in determining housing prices is the rise or decline in demand Consequently, in the short term, rising demand for housing causes prices to increase and declining demand causes them to fall.

In this study Section - 1 includes "The Regression Analysis" to explain the dependent variable which is **Unit Housing Price in Istanbul** with independent variables below in the table and tried to find **the highest and most effective model** that explaining unit housing price. In Section B, "The ARIMA Analysis" used for forecasting the "Housing Price Changes In Istanbul" for six months. The summary of study as in the below following chart.

Section 1 - Cross Section	Section 2 - Time Series
Regression Analysis	Auto Regressive Integrated Moving Average Analysis
Explaining Istanbul Housing Unit Price	Forecasting Istanbul Housing Price's Change Next Month

Some variables and description in the below chart.

VARIABLES	DESCRIPTION
DATE	Monthly Date from 2013 to 2019
IST_RPPI	Istanbul Residential Property Price Index
IST_PRC	Istanbul Housing Unit Price TL/m ²
IST_CNST_PRMT	Construction Permits
IST_OCCP_PRMT	Occupational Permits
MG_RT	Mortgage Credit Rates
IST_FGR_SL	Istanbul Housing Sales to Only Foreigners
IST_PRP_SL	Istanbul Total Housing Sales
IST_MRTG_SL	Istanbul Housing Sales by Using Mortgage Loan
CNSTR_TRST	Construction Trust Index
IST_CPI	Istanbul Consumer Price Index
TR_PPI	Turkey Producer Price Index
USD_RT	USD Buying Exchange Rate
RNT_CPI	IST Rent Consumer Price Index
NEMP_RT	Unemployment Rate

Notes: IST_CNST_PRMT - IST_OCCP_PRMT forward some different periods 2,3,4,6,9 etc.

For the reason why using both *Price Index* and *Unit Prices* main purpose of the using both Price Index and Prices on the data set in order to see the correlation between Monthly Price Index and Unit Prices and cross check our Property observations. It can easilv expect the correlation coefficient aproximately The main value of Housing Prices Index and Unit Prices would be the expecting correlation coefficient which is approximately 0.96 but the monthly percentage changes between them wouldn't be the bigger than 80%. This study also prove this on the next paragraphs.

2. Cross Section

III. Setting The Libraries

Before start the study, the libraries should be import to get rid of the errors and help to analyze all in one for study.

```
library(readr)
library(ggplot2)
library(mlbench)
## Warning: package 'mlbench' was built under R version 3.5.3
library(corrplot)
## Warning: package 'corrplot' was built under R version 3.5.3
## corrplot 0.84 loaded
library(Amelia)
## Warning: package 'Amelia' was built under R version 3.5.3
## Loading required package: Rcpp
## ##
## ## Amelia II: Multiple Imputation
## ## (Version 1.7.5, built: 2018-05-07)
## ## Copyright (C) 2005-2019 James Honaker, Gary King and Matthew Blackwell
## ## Refer to http://gking.harvard.edu/amelia/ for more information
## ##
library(caret)
## Warning: package 'caret' was built under R version 3.5.3
## Loading required package: lattice
```

```
library(plotly)
##
## Attaching package: 'plotly'
## The following object is masked from 'package:ggplot2':
##
##
       last plot
## The following object is masked from 'package:stats':
##
##
       filter
## The following object is masked from 'package:graphics':
##
       layout
library(caTools)
library(reshape2)
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
library(knitr)
## Warning: package 'knitr' was built under R version 3.5.3
library(ggplot2)
library(forecast)
## Warning: package 'forecast' was built under R version 3.5.3
library(tseries)
## Warning: package 'tseries' was built under R version 3.5.3
library(astsa)
## Attaching package: 'astsa'
## The following object is masked from 'package:forecast':
##
##
       gas
library(readr)
```

IV. Data Import

This project include different studies that divide main values and percentage change according to the previous months.

IST_RPPI_MODEL_CG

Main Value of All variables Monthly Percentage Changes Values(%)

V. Data Type Observation

All the variables according to data type is "dbl" that is related with numeric values except "Date". The study is not going to include **dates** in any model at Section-1 on Regression Analysis. Seeing the data types and first 5 column is also important for the data set what imported correctly.

```
head(IST_RPPI_MODEL)
## # A tibble: 6 x 23
                IST PRC IST RPPI MG RT IST FGR SL IST PRP SL IST MRTG SL
##
     DATE
                                                         <db1>
     <date>
                  <dbl>
                            <dbl> <dbl>
                                              <dbl>
                                                                     <db1>
## <u>1</u> 2013-01-01
                  2064.
                             47.8 9.78
                                               138
                                                         18235
                                                                      8423
## 2 2013-02-02
                  2114.
                             48.8
                                   9.58
                                               120
                                                         18971
                                                                       8836
## 3 2013-03-03
                  2157.
                             49.9 9.31
                                               198
                                                         21570
                                                                     10164
## 4 2013-04-04
                  2186.
                             50.9 9.06
                                                209
                                                         20791
                                                                       9726
## 5 2013-05-05
                             51.6 8.77
                                               188
                  2218.
                                                         22030
                                                                     10805
## 6 2013-06-06
                  2263.
                             52.4 8.3
                                               155
                                                         19357
                                                                       9762
## # ... with 16 more variables: CNSTR TRST <dbl>, RNT CPI <dbl>,
       IST_CPI <dbl>, TR_PPI <dbl>, USD_RT <dbl>, NEMP_RT <dbl>,
       IST_CNST_PT <dbl>, IST_OCCP_PT <dbl>, IST_CNST_PT_2 <dbl>,
       IST OCCP PT 2 <dbl>, IST CNST PT 3 <dbl>, IST OCCP PT 3 <dbl>,
```

VI. Understanding Data

In order to understand and examine data generally use five number summary. *Five Number Summary* shows *median*, *mean*, *min-max* and *Q1 & Q3* values. This may help us to mining and eliminating and understanding the structure of data and classifying the observations.

For example:

- Housing Unit Prices in Istanbul has minimum value which is 2064; Mean Value is 3708 and also the Median Value is 3922. Q3 is 4562 and Max. value 5123. It can be easily understanding this data classified with a good range because there is not any extreme observation.
- Istanbul Unit Price Changes min.value -1.266, max.value 3.756, mean 1.285, median 1.366
- Total Istanbul Housing Sales min.value 11903, max.value 27156, mean value 19512, median value 19305. 3rd Quartile value is 21213 This value shows us there is not any extreme circumstances.
- When it comes to mortgage rates,

```
      Min.
      1st Q.
      Median
      Mean
      3rd Q.
      Max.

      8.30
      11.00
      12.20
      13.11
      13.93
      28.99
```

The situation about the outliers will be scrutinized next paragraphs.

1. Unit Housing Price

```
summary(IST_RPPI_MODEL$IST_PRC)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 2064 2775 3922 3708 4562 5123
```

2. Residential Housing Price Index

```
summary(IST_RPPI_MODEL$IST_RPPI)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 47.81 63.26 86.48 81.55 100.39 103.19
```

3. Property Sales

```
summary(IST_RPPI_MODEL$IST_PRP_SL)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 11903 17398 19305 19512 21213 27156
```

4. Foreigner Sales

```
summary(IST_RPPI_MODEL$IST_FGR_SL)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 120.0 403.2 540.5 608.1 646.0 2283.0
```

5. Sales by Mortgage

```
summary(IST_RPPI_MODEL$IST_MRTG_SL)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 987 6230 7150 7109 8672 10805
```

6. Occupational Permits forward 9 months

```
summary(IST_RPPI_MODEL$IST_OCCP_PT_9)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 552.0 966.2 1121.5 1147.3 1318.5 2024.0
```

7. Consumer Price Index

```
summary(IST_RPPI_MODEL$IST_CPI)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 220.9 248.1 278.4 285.7 316.6 403.7
```

8. Mortgage Rates

```
summary(IST_RPPI_MODEL$MG_RT)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 8.30 11.00 12.20 13.11 13.93 28.99
```

9. Construction Permits

```
summary(IST_RPPI_MODEL$IST_CNST_PT)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 322.0 967.8 1322.5 1371.3 1597.0 4845.0
```

10. Rent Consumer Price Index

```
summary(IST_RPPI_MODEL$RNT_CPI)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 297.5 327.1 366.3 373.8 415.1 477.5
```

11. Turkey Producer Price Index

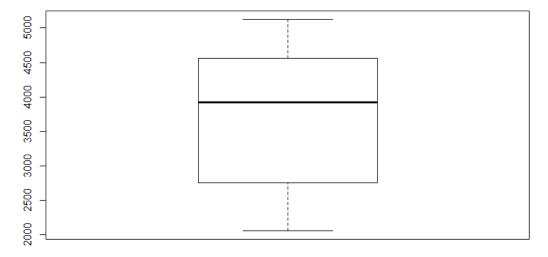
```
summary(IST_RPPI_MODEL$TR_PPI)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 206.7 234.6 250.9 271.8 296.1 443.8
```

12. USD Currency Rates

```
summary(IST_RPPI_MODEL$USD_RT)
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 1.770 2.217 2.920 3.055 3.663 6.380
#summary(IST_RPPI_MODEL)
```

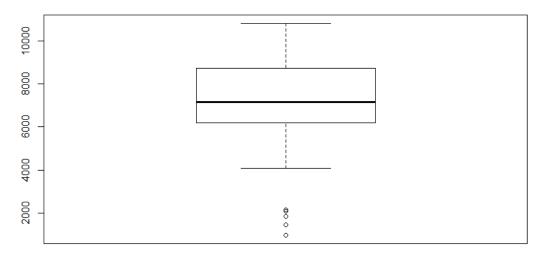
The values with box plot In addition to numeric table, Housing Sales also be showed with box plot.

Housing Prices



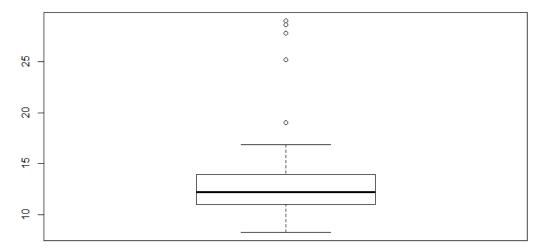
Outlier rows:

Housing Sales By Using Loan



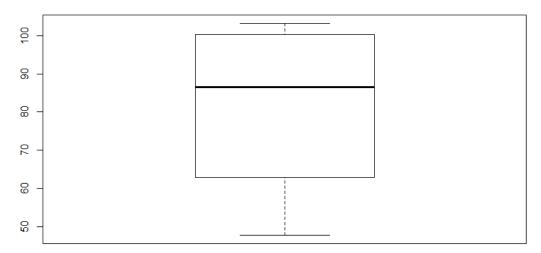
Outlier Rows: 2567

Mortgage Rates



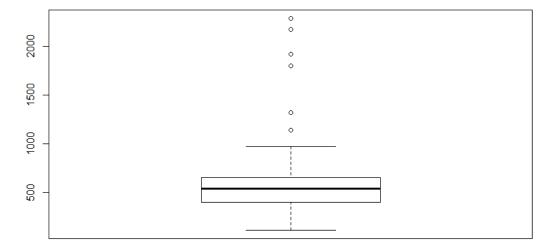
Outlier Rows: 29.69

Property Price Index



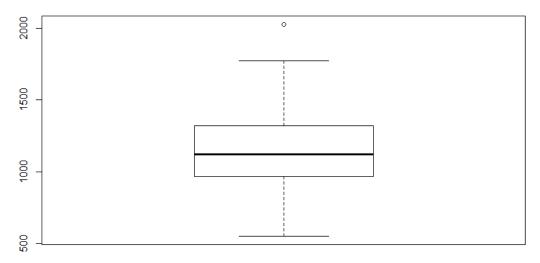
Outlier Rows:

Foreigner Sales



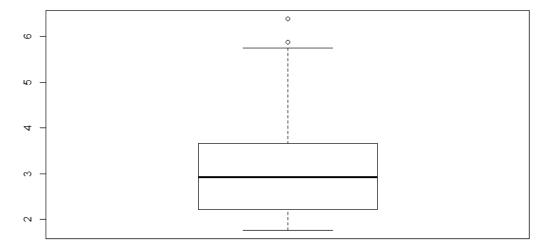
Outlier Rows: 2200

Occupational Permits forward 9 months



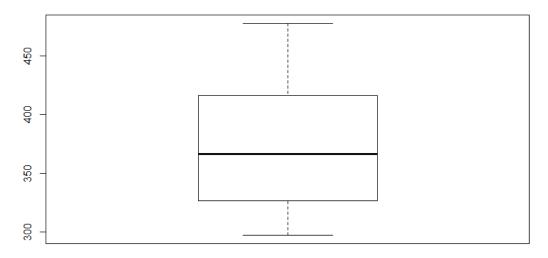
Outlier Rows: 2024

USD Exchange Rate



Outlier Rows: 6.88

Rent Consumer Price Index



Outlier Rows:

```
MG RT OUT <- boxplot.stats(IST RPPI MODEL$MG RT)$out
MRTG_SL_OUT <- boxplot.stats(IST_RPPI_MODEL$IST_MRTG_SL)$out</pre>
data.frame(MG_RT_OUT, MRTG_SL_OUT)
     MG RT OUT MRTG SL OUT
##
         19.02
## 1
                       2082
## 2
         25.19
                       1863
## 3
         28.99
                       2164
## 4
         28.63
                        987
## 5
         27.82
                       1461
IST_FGR_SL_OUT <- boxplot.stats(IST_RPPI_MODEL$IST_FGR_SL)$out</pre>
IST OCCP PT 9 OUT <- boxplot.stats(IST RPPI MODEL$IST OCCP PT 9)$out
USD_RT_OUT <- boxplot.stats(IST_RPPI_MODEL$USD_RT)$out</pre>
data.frame(IST_FGR_SL_OUT, IST_OCCP_PT_9_OUT, USD_RT_OUT)
##
     IST FGR SL OUT IST OCCP PT 9 OUT USD RT OUT
## 1
                1321
                                   2024
                                               6.38
## 2
                                               5.87
                1141
                                   2024
## 3
                1799
                                   2024
                                               6.38
## 4
                2283
                                   2024
                                               5.87
## 5
                1922
                                   2024
                                               6.38
## 6
                                               5.87
                2170
                                   2024
```

Mortgage Rates and Mortgage Sales have <u>5 outliers</u>, Foreigner Sales <u>6</u>, Occupational permits <u>1 and 2 outliers</u> in Usd Exchange Rates.

The outliers distracting model confidence, others should remove from dataset. In the study outliers used because of the size.

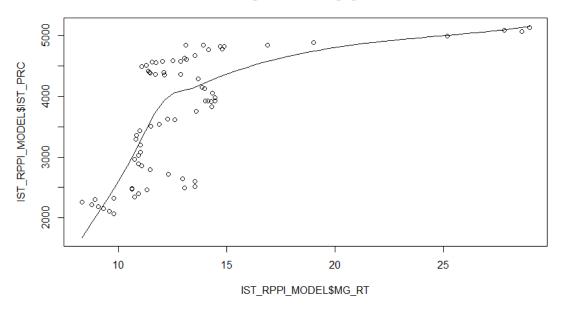
An alternative solution may offer remove the outliers and **fill with median value** of column.

When It comes to *dependent - independent variables*, It can be easily showing distribution in scatter plot.

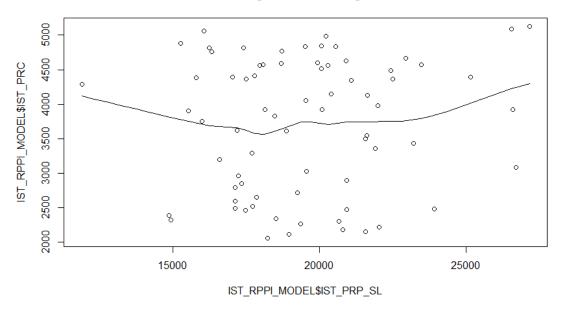
For example:

Some distrubitons about Housing Price and other variables showing with the scatter plot.

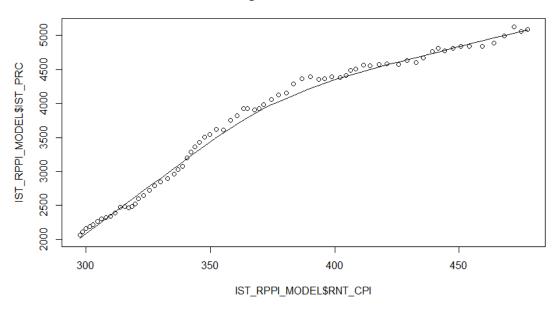
Housing Price ~ Mortgage Rates



Housing Price ~ Housing Sales



Housing Price ~ Rent Price Index

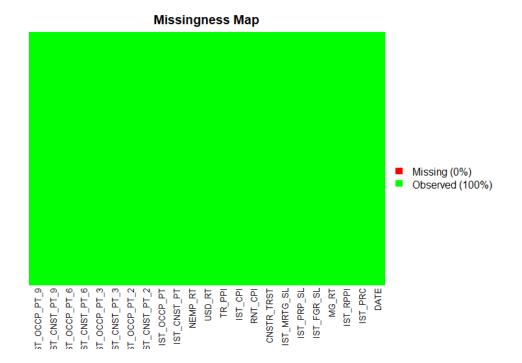


This plot also sort out to correlation. The relation between price & mortgage rates also
positive correlation but taking into consideration that supply and demand equilibrium,
expecting when mortgage rates down prices would be higher because of the demand
would increasing.

- When it comes to Turkey considering that there is an imbalance situation. People always wanting to get a housing neither mortgage rates increase nor mortgage rates decrease.
- The study emphasis this situation on next paragraphs at the Correlation.

In order to see the missing observations, easily get this code by using *Amelia Package*. In this study, any missing value the model including.

VII. See The Missing Values



Note: The study doesn't consist any missing observations. On the some literature text that filling the missing values with median value of the variables.

VIII. Show The Correlation

Correlation table including related coefficients below in the chart.

```
res_mn <- cor(select(IST_RPPI_MODEL, -DATE))</pre>
res mn <- data.frame(round(res_mn, 2))</pre>
head(res mn, n=6)
##
                IST PRC IST RPPI MG RT IST FGR SL IST PRP SL IST MRTG SL
                                   0.59
## IST PRC
                   1.00
                             1.00
                                                0.64
                                                            0.10
                                                                        -0.55
## IST_RPPI
                   1.00
                             1.00
                                    0.53
                                                0.58
                                                            0.09
                                                                        -0.50
## MG_RT
                   0.59
                             0.53
                                    1.00
                                                0.91
                                                            0.13
                                                                        -0.85
## IST FGR SL
                   0.64
                             0.58
                                    0.91
                                                1.00
                                                            0.35
                                                                        -0.69
## IST_PRP_SL
                   0.10
                             0.09
                                    0.13
                                                0.35
                                                            1.00
                                                                         0.33
                   -0.55
                            -0.50 -0.85
                                               -0.69
                                                                         1.00
## IST_MRTG_SL
                                                            0.33
##
                CNSTR TRST RNT CPI IST CPI TR PPI USD RT NEMP RT IST CNST PT
## IST_PRC
                      -0.37
                               0.96
                                        0.93
                                                0.83
                                                       0.88
                                                                0.64
                                                                            -0.16
## IST RPPI
                      -0.31
                               0.94
                                        0.90
                                                0.78
                                                       0.84
                                                                0.63
                                                                            -0.11
## MG RT
                      -0.75
                               0.68
                                        0.77
                                                0.84
                                                       0.80
                                                                0.48
                                                                            -0.32
## IST_FGR_SL
                      -0.74
                               0.72
                                        0.80
                                                0.85
                                                       0.82
                                                                0.50
                                                                            -0.20
                                                       0.13
## IST PRP SL
                      -0.23
                               0.11
                                        0.13
                                                0.13
                                                                0.11
                                                                             0.21
## IST_MRTG_SL
                       0.62
                              -0.64
                                       -0.70
                                               -0.75
                                                       -0.72
                                                               -0.42
                                                                             0.35
##
                IST_OCCP_PT IST_CNST_PT_2 IST_OCCP_PT_2 IST_CNST_PT_3
## IST PRC
                        0.23
                                      -0.12
                                                       0.22
                                                                     -0.09
## IST RPPI
                        0.24
                                      -0.07
                                                      0.24
                                                                     -0.04
## MG RT
                        0.22
                                      -0.28
                                                      0.09
                                                                     -0.23
                        0.26
## IST FGR SL
                                      -0.24
                                                      0.00
                                                                     -0.12
## IST_PRP_SL
                        0.44
                                      -0.14
                                                     -0.27
                                                                      0.20
                        0.00
                                       0.21
                                                     -0.21
## IST_MRTG_SL
                                                                      0.22
##
                IST_OCCP_PT_3 IST_CNST_PT_6 IST_OCCP_PT_6 IST_CNST_PT_9
## IST_PRC
                          0.25
                                         0.02
                                                         0.40
                                                                        0.06
## IST_RPPI
                          0.27
                                         0.04
                                                         0.41
                                                                        0.08
## MG RT
                          0.08
                                        -0.20
                                                         0.19
                                                                       -0.30
## IST_FGR_SL
                          0.02
                                        -0.17
                                                         0.29
                                                                       -0.26
## IST PRP SL
                                                         0.12
                         -0.10
                                         0.04
                                                                        0.11
## IST MRTG SL
                         -0.14
                                         0.18
                                                        -0.13
                                                                        0.35
##
                IST_OCCP_PT_9
## IST_PRC
                          0.44
## IST_RPPI
                          0.45
## MG RT
                          0.28
## IST FGR SL
                          0.33
## IST PRP SL
                          0.19
## IST_MRTG_SL
                         -0.26
```

This table show us the correlation coefficients between Istanbul Unit Housing Prices and the other variables.

The best correlation equivalent in order to explain the housing unit prices:

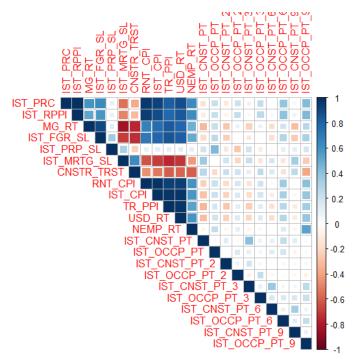
```
1. RNT_CPI: 0.96
```

- 2. IST_CPI: 0.93
- 3. USD_RT: 0.88
- 4. TR_PPI: 0.83
- 5. NEMP_RT: 0.64
- 6. IST_FGR_SL: 0.64
- 7. MG RT: 0.59
- 8. IST_MRTG_SL: -0.55
- 9. IST_OCCP_PT_9: 0.44
- 10. CNSTR_TRST: -0.37
- 11. IST_CNST_PT:-0.16

The Index which are Rent Consumer Price Index, Istanbul Consumer Price Index, USD Rate and Turkey Producer Price Index affecting The Housing Unit Prices very strongly correlated. So that try to find the best model in this study, include strong correlated variables in the model on next paragraphs.

```
res cg<- cor(select(IST RPPI MODEL CG, -DATE))</pre>
res_cg <- data.frame(round(res_cg, 2))</pre>
head(res cg, n=1)
           IST PRC IST RPPI MG RT IST FGR SL IST PRP SL IST MRTG SL
                                                      0.02
## IST PRC
                        0.62 -0.05
                                          0.07
           CNSTR_TRST_RNT_CPI_IST_CPI_TR_PPI_USD_RT_NEMP_RT_IST_CNST_PT
                                   0.08
## IST PRC
                  0.06
                         -0.17
                                         -0.07
                                                 -0.11
           IST_OCCP_PT IST_CNST_PT_2 IST_OCCP_PT_2 IST_CNST_PT_3
                                 -0.26
                                               -0.01
## IST_PRC
                  -0.15
                                                               -0.13
           IST OCCP PT 3 IST CNST PT 6 IST OCCP PT 6 IST CNST PT 9
## IST_PRC
                                   -0.18
                                                  -0.01
                     0.04
           IST_OCCP_PT_9
## IST PRC
```

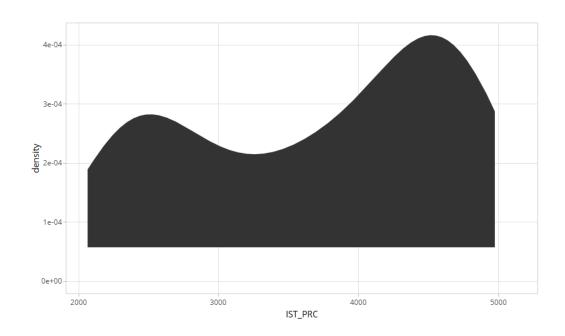
This study also proved that the marker of Price and Price Index is positive correlated but first case Unit Price and Price Index correlated equal, The correlation coefficient between Unit Price Changes and Property Price Index Changes nearly 0.62, different from each others.

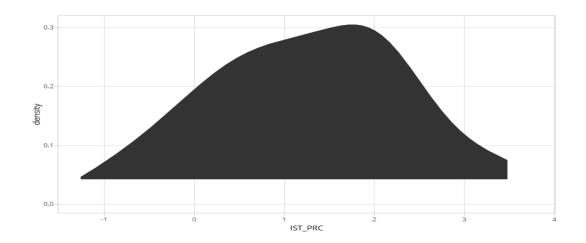


```
#corrplot(cor(select(IST_RPPI_MODEL_CG, -DATE)),
# method = "square", addrect = 2, sig.level = .01, type #= "upper")
```

- 1. The main value's correlation coefficient was ~ 1.00 but in this case the monthly changes different than each others when considered the actual values, the monthly change's coefficients different from main values. First, we look up the Unit Price and Property Price Index's coefficient is approximately $\sim 100\%$ but we look the monthly change of the both variables coefficient is $\sim 62\%$, So when we consider why the monthly changes different than main values.
 - This two main dependent variables is the same. It can be explained that Price Index is publishing after The Unit Prices maybe 1-2 month, Price Index can be influenced by the other things. According to housing market the index publishing after 1 and 2 months published unit prices and Index be affecting from other main Index like Rent, CPI, PPI etc.
- 2. Secondly, we should look the Construction-Occupational Permits the best correlation with Housing Prices is
- The direct and not postponed value of Construction Permits \sim -16%
- Held over value for 9 months of Occupational Permits ~ 44%
 So, It would be think that when a construction start and all permits be get, how long will this pre-construction and construction process extend or when this new supply get in the market? The study also show that Housing Market Prices, much more influenced by Occupational Permits which published data forward for 9 months.

IX. Showing The Density





The Property Price has two major range -bimodal distribution- one of the between 55-60, the other is 95-100 because of the time process .

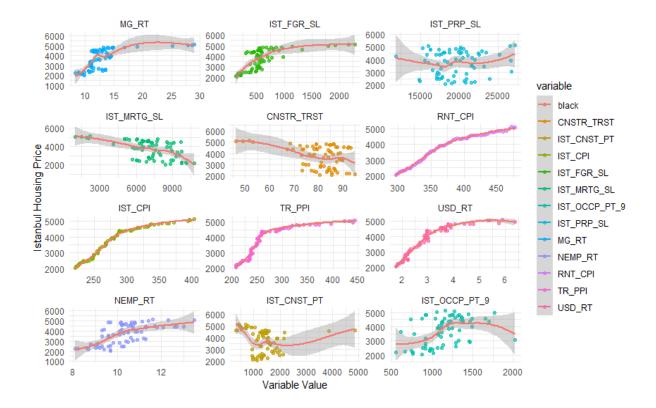
Prices always getting increase time to time and also the monthly price changes have one modal distribution. It can be easily reach mod, median, mean values show in "Five Number Summary section".

Istanbul Housing Price monthly change has one modal, normal distribution. Showing The Five Number Summary of Price and Price Change belowing chart.

```
summary(IST_RPPI_MODEL$IST_PRC)
##
      Min. 1st Qu.
                    Median
                              Mean 3rd Qu.
                                              Max.
##
      2064
              2775
                      3922
                              3708
                                      4562
                                              5123
summary(IST RPPI MODEL CG$IST PRC)
##
      Min. 1st Qu.
                    Median
                              Mean 3rd Qu.
                                              Max.
   -1.266 0.463 1.336
                             1.285 2.084
                                             3.758
```

X. Seeing The Correlation Plot

In order to plot all variables related with the Housing Prices :



The correlation between all variables *Positive & Negative Correlation* would easily showed above a plot with Istanbul Housing Prices.

Positive Corelation Negative Correlation

Mortgage Rates Construction Trust Index
Foreigner Sales Mortgage Sales
Rent CPI
USD Rate
TR PPI
IST CPI
NEMP Rate

UNEMP rate is also expecting negative correlation because the purchasing power is decreasing so anyone would not want to buy a house this means demand will decrease and price should be expecting down. In this case this not go through what we expecting.

XI. Building A Model (Train-Test)

Setting a Seed Random Number

Seed number should be selected to determine the same results, accuracy, errors every run command. In this study, 2019 is specified.

```
#set.seed(2019)
#split <- sample.split(IST_RPPI_MODEL, SplitRatio = 0.70)
#train_mn <- subset(IST_RPPI_MODEL, split == FALSE)
#test_mn <- subset(IST_RPPI_MODEL, split == FALSE)
#set.seed(2019)
#split <- sample.split(IST_RPPI_MODEL_CG, SplitRatio = 0.70)
#train_cg <- subset(IST_RPPI_MODEL_CG, split == TRUE)
#test_cg <- subset(IST_RPPI_MODEL_CG, split == FALSE)</pre>
```

Split is meaning the portion of the training data. For a study train set determined 0.70 of all data set this should be increase in small data sets as well test set specified 0.30

Notes : Split and seed number didn't use for the model why the model is weak for observations ~ 72

Building Different Models and See Residuals

```
model1 mn <- lm(IST_PRC ~ MG_RT + IST_FGR_SL +
                    IST_MRTG_SL + CNSTR_TRST +
                    RNT_CPI + USD_RT +
                    IST_CNST_PT + IST_OCCP_PT_9 ,
                data = IST RPPI MODEL)
summary(model1 mn)
##
## Call:
## lm(formula = IST_PRC ~ MG_RT + IST_FGR_SL + IST_MRTG_SL + CNSTR_TRST +
       RNT CPI + USD RT + IST CNST PT + IST OCCP PT 9, data = IST RPPI MODEL)
##
## Residuals:
      Min
##
                10 Median
                                30
                                       Max
## -474.41 -183.41 -54.82 173.76 450.79
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
                 -4.953e+03 7.345e+02 -6.743 5.6e-09 ***
## (Intercept)
## MG RT
                 2.651e+01 2.520e+01
                                       1.052
                                                  0.297
## IST FGR SL
                                                  0.394
                 -1.726e-01 2.013e-01
                                        -0.858
                                       1.347
## IST_MRTG_SL
                 3.880e-02 2.880e-02
                                                  0.183
```

```
3.926e+00 4.885e+00 0.804
                                                0.425
## CNSTR_TRST
## RNT_CPI
                 2.169e+01 1.901e+00 11.414
                                              < 2e-16 ***
## USD RT
                -1.857e+02 1.159e+02
                                      -1.603
                                                0.114
## IST CNST PT
                 7.382e-02 4.622e-02
                                        1.597
                                                0.115
## IST OCCP PT 9 1.591e-01 1.215e-01
                                       1.310
                                                0.195
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 232.7 on 63 degrees of freedom
## Multiple R-squared: 0.9483, Adjusted R-squared: 0.9417
## F-statistic: 144.4 on 8 and 63 DF, p-value: < 2.2e-16
```

Model's P-values not good what expecting, Model-1 says us only Rent CPI is affecting Price, The data including both one digit numbers and four&five digit numbers. An alternative solution to get rid of big numbers to start logarithm process for big numbers. Built a new one more model which is **Model-2 with logarithm process.**

```
model2 mn <- lm(log10(IST PRC) ~ MG RT + log10(IST FGR SL) +
                    log10(IST_MRTG_SL) + CNSTR_TRST + RNT_CPI + USD_RT +
                    log10(IST CNST PT) + log10(IST OCCP PT 9) ,
                data = IST RPPI MODEL)
summary(model2 mn)
##
## Call:
## lm(formula = log10(IST PRC) ~ MG RT + log10(IST FGR SL) +
log10(IST_MRTG_SL) +
      CNSTR_TRST + RNT_CPI + USD_RT + log10(IST_CNST_PT) +
log10(IST_OCCP_PT_9),
##
      data = IST_RPPI_MODEL)
##
## Residuals:
                   10
                         Median
                                       3Q
  -0.077355 -0.026468 -0.003827 0.024054 0.083776
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
                                               6.294 3.34e-08 ***
## (Intercept)
                        1.8108140 0.2877130
## MG RT
                        0.0006012 0.0035592
                                               0.169
                                                       0.8664
## log10(IST_FGR_SL)
                        0.0738485 0.0331655
                                               2.227
                                                       0.0296 *
                        0.0595833 0.0620361
## log10(IST_MRTG_SL)
                                               0.960
                                                       0.3405
## CNSTR TRST
                        0.0005521 0.0007025
                                               0.786
                                                       0.4349
                        0.0026682 0.0002929
                                               9.110 4.17e-13 ***
## RNT CPI
## USD RT
                       -0.0322541 0.0169629 -1.901
                                                       0.0618 .
## log10(IST_CNST_PT)
                       0.0560448 0.0250875
                                               2.234
                                                       0.0290 *
## log10(IST OCCP PT 9) 0.0624600 0.0476259
                                               1.311
                                                       0.1945
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
## Residual standard error: 0.03452 on 63 degrees of freedom
## Multiple R-squared: 0.9298, Adjusted R-squared: 0.9208
## F-statistic: 104.2 on 8 and 63 DF, p-value: < 2.2e-16
```

Model-2 increased the p-value of variables. When looking model-2, there are four different variables in confidence p-values as well USD Rate close to line. In Model-2 used logarithm on three or more digit values.

```
model3 mn <- lm(log10(IST_PRC) ~ log10(MG_RT) + log10(IST_FGR_SL) +
                    log10(IST MRTG SL) + log10(CNSTR TRST) +
                    log10(RNT_CPI) + log10(USD_RT) +
                   log10(IST_CNST_PT)
                data = IST RPPI MODEL)
summary(model3 mn)
##
## Call:
  lm(formula = log10(IST PRC) ~ log10(MG RT) + log10(IST FGR SL) +
       log10(IST_MRTG_SL) + log10(CNSTR_TRST) + log10(RNT_CPI) +
##
       log10(USD_RT) + log10(IST_CNST_PT), data = IST_RPPI_MODEL)
## Residuals:
         Min
                   1Q
                         Median
                                       3Q
                                                Max
  -0.059546 -0.021530 -0.001008 0.017957 0.082533
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      -2.45896
                                 0.69953 -3.515 0.000813 ***
## log10(MG RT)
                      0.17492
                                 0.11004 1.590 0.116859
                                 0.02995 0.905 0.369053
## log10(IST FGR SL)
                      0.02709
## log10(IST MRTG SL) 0.13435
                                 0.05131 2.618 0.011015 *
## log10(CNSTR_TRST)
                      0.09797
                                 0.09546 1.026 0.308622
## log10(RNT CPI)
                                 0.29121 6.501 1.39e-08 ***
                      1.89303
## log10(USD RT)
                      0.03683
                                 0.14308 0.257 0.797697
                                 0.02128 2.539 0.013571 *
## log10(IST CNST PT) 0.05401
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.02972 on 64 degrees of freedom
## Multiple R-squared: 0.9471, Adjusted R-squared: 0.9413
## F-statistic: 163.8 on 7 and 64 DF, p-value: < 2.2e-16
```

In Model-3, all variables reduced with logarithm so that decrease digits but in this model there isn't enough confidence than Model-2. So keep continuous with Model-2 and remove the highest p-value which is mortgage rates plus mortgage sales. Add the property sales rather than mortgage sales.

```
model4_mn \leftarrow lm(log10(IST_PRC) \sim log10(IST_FGR_SL) + log10(IST_FG
                                                    log10(IST_PRP_SL) + CNSTR_TRST + RNT_CPI + USD_RT +
                                                    log10(IST_CNST_PT) + log10(IST_OCCP_PT_9) ,
                                         data = IST RPPI MODEL)
summary(model4 mn)
##
## Call:
## lm(formula = log10(IST PRC) ~ log10(IST FGR SL) + log10(IST PRP SL) +
                  CNSTR_TRST + RNT_CPI + USD_RT + log10(IST_CNST_PT) +
log10(IST_OCCP_PT_9),
                  data = IST RPPI MODEL)
##
##
## Residuals:
                       Min
                                                                   Median
                                                   10
                                                                                                       30
                                                                                                                              Max
## -0.079379 -0.023790 -0.006316 0.029584 0.051114
## Coefficients:
                                                                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                                                2.4238074 0.3063565 7.912 4.61e-11 ***
                                                               0.0867433 0.0294176
## log10(IST_FGR_SL)
                                                                                                                            2.949 0.00445 **
## log10(IST PRP SL)
                                                              -0.1132032 0.0668606 -1.693 0.09530 .
## CNSTR TRST
                                                               0.0007370 0.0006209 1.187 0.23957
## RNT CPI
                                                              ## USD_RT
## log10(IST CNST PT)
                                                            0.0719461 0.0244949 2.937 0.00460 **
## log10(IST_OCCP_PT_9) 0.0652729 0.0461248 1.415 0.16188
## Signif. codes: 0 '*** 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.03394 on 64 degrees of freedom
## Multiple R-squared: 0.931, Adjusted R-squared: 0.9235
## F-statistic: 123.4 on 7 and 64 DF, p-value: < 2.2e-16
```

When considered the Construction Trust Index's p-value so higher than others. It can be remove from model, try to find more accuracy model in Model-5.

```
Min
                   10
                         Median
                                                Max
                                       3Q
## -0.083918 -0.024270 -0.006217
                                 0.031252 0.051470
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                        2.5382655 0.2917025
                                               8.702 1.66e-12 ***
## log10(IST FGR SL)
                        0.0804707 0.0290301 2.772 0.007260 **
## log10(IST_PRP_SL)
                       -0.1238142   0.0664687   -1.863   0.067018
## RNT CPI
                        0.0028985 0.0002451 11.824 < 2e-16 ***
                       -0.0500706 0.0134835 -3.713 0.000427 ***
## USD RT
## log10(IST_CNST_PT)
                       0.0801521 0.0235731 3.400 0.001156 **
## log10(IST_OCCP_PT_9) 0.0490817 0.0442006 1.110 0.270905
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.03404 on 65 degrees of freedom
## Multiple R-squared: 0.9295, Adjusted R-squared: 0.923
## F-statistic: 142.9 on 6 and 65 DF, p-value: < 2.2e-16
```

Model-5 good correlated to explain the prices but It is not enough because of the big p-values. In model-6, get rid of the Occupational Permits.

```
model6 mn <- lm(log10(IST PRC) \sim log10(IST FGR SL) +
                   log10(IST_PRP_SL) + RNT_CPI + USD_RT +
                   log10(IST_CNST_PT)
               data = IST RPPI MODEL)
summary(model6 mn)
##
## Call:
  lm(formula = log10(IST_PRC) ~ log10(IST_FGR_SL) + log10(IST_PRP_SL) +
##
      RNT_CPI + USD_RT + log10(IST_CNST_PT), data = IST_RPPI_MODEL)
##
## Residuals:
                 10
                     Median
                                  30
                                          Max
  -0.07949 -0.02566 -0.00592 0.03070 0.05494
##
## Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
                                           9.726 2.27e-14 ***
## (Intercept)
                      2.6541108 0.2728896
## log10(IST_FGR_SL)
                    0.0888126 0.0280907
                                          3.162 0.002370 **
## log10(IST PRP SL) -0.1250391 0.0665768 -1.878 0.064784
## RNT CPI
                     0.0029514 0.0002409 12.253 < 2e-16 ***
## USD RT
                     ## log10(IST_CNST_PT) 0.0811789 0.0235965 3.440 0.001012 **
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.0341 on 66 degrees of freedom
```

```
## Multiple R-squared: 0.9282, Adjusted R-squared: 0.9227
## F-statistic: 170.6 on 5 and 66 DF, p-value: < 2.2e-16
```

When Supply-Demand Equilibrium considered: Property Sales expecting increase, Price would be get higher. Because of the confidence level of Property Sales the variable's marker say us the negative situation. In Model-7, removed the Property Sales.

```
model7 mn <- lm(log10(IST PRC) \sim log10(IST FGR SL) +
                   RNT CPI + USD RT +
                   log10(IST CNST PT)
               data = IST_RPPI_MODEL)
summary(model7 mn)
##
## Call:
## lm(formula = log10(IST_PRC) ~ log10(IST_FGR_SL) + RNT_CPI + USD_RT +
      log10(IST_CNST_PT), data = IST_RPPI_MODEL)
##
## Residuals:
                   10
                        Median
                                      3Q
  -0.083967 -0.027947 -0.005618 0.030005 0.069826
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     2.1745802 0.0981212 22.162 < 2e-16
## log10(IST_FGR_SL) 0.0722039 0.0271606 2.658 0.009810 **
## RNT CPI
                     0.0029860 0.0002447 12.204 < 2e-16 ***
                     ## USD RT
## log10(IST_CNST_PT) 0.0732571 0.0236503 3.098 0.002850 **
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.03474 on 67 degrees of freedom
## Multiple R-squared: 0.9243, Adjusted R-squared: 0.9198
## F-statistic: 204.7 on 4 and 67 DF, p-value: < 2.2e-16
```

Model-7 is final outcome in which more comprehensive and meaningfully than other models. The model prove that :

- If Total Foreigner Sale increase than Price would be higher
- If Rent Consumer Price Index would be higher than Price get increase
- When it come to USD Rate, considered the Housing Market at this moment. USD currency extremely high and Housing Prices getting decrease. So this model actually prove that.
- Construction Permits affecting housing prices positive.
- Another different model for explaining Mortgage Sales :

```
model8 mn <- lm(log10(IST_MRTG_SL) ~ MG_RT + log10(IST_FGR_SL) +
                  log10(IST_PRC) + IST_RPPI +
                  CNSTR_TRST + RNT_CPI + IST_CPI +
                  TR PPI + USD RT + NEMP RT +
                  log10(IST CNST PT) +
                   log10(IST_OCCP_PT_9) ,
               data = IST RPPI MODEL)
summary(model8 mn)
##
## Call:
## lm(formula = log10(IST MRTG_SL) ~ MG_RT + log10(IST_FGR_SL) +
      log10(IST_PRC) + IST_RPPI + CNSTR_TRST + RNT_CPI + IST_CPI +
##
      TR_PPI + USD_RT + NEMP_RT + log10(IST_CNST_PT) + log10(IST_OCCP_PT_9),
##
      data = IST RPPI MODEL)
##
## Residuals:
##
                  10
                        Median
                                              Max
                                     3Q
  -0.169169 -0.023805 -0.000374
                               0.046476 0.182193
## Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
                                 3.320589
                                           2.120 0.03822 *
## (Intercept)
                       7.039615
## MG RT
                      -0.046521
                                 0.006010 -7.740 1.5e-10 ***
                      0.107414 0.080741 1.330 0.18852
## log10(IST_FGR_SL)
                      -1.037223 1.043871 -0.994 0.32446
## log10(IST PRC)
## IST RPPI
                      0.004044 0.009811 0.412 0.68167
## CNSTR_TRST
                      -0.001159 0.001750 -0.662 0.51025
## RNT CPI
                      ## IST CPI
                      ## TR PPI
                      -0.006651 0.003196 -2.081 0.04180 *
## USD RT
                       0.019703 0.065725
                                          0.300 0.76540
## NEMP RT
                      -0.017519 0.013246 -1.323 0.19107
## log10(IST_CNST_PT) 0.062833
                                 0.056462 1.113 0.27029
## log10(IST_OCCP_PT_9) 0.106697
                                 0.103936
                                           1.027 0.30881
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06588 on 59 degrees of freedom
## Multiple R-squared: 0.8997, Adjusted R-squared: 0.8793
## F-statistic: 44.1 on 12 and 59 DF, p-value: < 2.2e-16
```

The model can't explain what the study want. Remove the high p-values which are IST_RPPI and CNSTR TRST from model.

```
log10(IST_CNST_PT) +
                  log10(IST_OCCP_PT_9) ,
              data = IST RPPI MODEL)
summary(model9 mn)
##
## Call:
## lm(formula = log10(IST_MRTG_SL) ~ MG_RT + log10(IST_FGR_SL) +
      log10(IST PRC) + RNT CPI + IST CPI + TR PPI + USD RT + NEMP RT +
##
      log10(IST_CNST_PT) + log10(IST_OCCP_PT_9), data = IST_RPPI_MODEL)
## Residuals:
                  10
                       Median
                                    3Q
  -0.178090 -0.027195 -0.001252 0.040338 0.189463
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                               1.307289 4.440 3.84e-05 ***
                     5.804990
## MG RT
                     -0.044687
                                0.005255 -8.504 6.00e-12 ***
## log10(IST FGR SL)
                     0.116321 0.075503 1.541 0.12858
## log10(IST_PRC)
                     -0.710977   0.494219   -1.439   0.15538
## RNT CPI
                     ## IST CPI
                      ## TR PPI
                     ## USD_RT
                     0.040256 0.051781 0.777 0.43991
## NEMP RT
                     -0.012860 0.010775 -1.193 0.23731
## log10(IST_CNST_PT)
                     0.064872 0.049501 1.311 0.19493
## log10(IST_OCCP_PT_9) 0.105658
                                0.102583 1.030 0.30709
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.06506 on 61 degrees of freedom
## Multiple R-squared: 0.8988, Adjusted R-squared: 0.8823
## F-statistic: 54.21 on 10 and 61 DF, p-value: \langle 2.2e-16 \rangle
```

Remove from model USD RT, NEMP RT, CNST & OCCP Permits, RNT CPI

```
## Residuals:
                       Median
##
        Min
                  10
                                    30
                                            Max
  -0.187080 -0.039010 0.002511 0.045031 0.221918
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
                              1.022878 5.430 8.7e-07 ***
                   5.554099
## (Intercept)
                            0.004293 -9.546 4.7e-14 ***
## MG RT
                   -0.040984
## log10(IST FGR SL) 0.203193 0.062403 3.256 0.00178 **
## log10(IST PRC)
                   ## IST_CPI
                   0.005162
                              0.002764
                                       1.868 0.06627 .
## TR_PPI
                   -0.004112
                              0.001765 -2.330 0.02288 *
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06659 on 66 degrees of freedom
## Multiple R-squared: 0.8854, Adjusted R-squared: 0.8767
## F-statistic: 102 on 5 and 66 DF, p-value: < 2.2e-16
```

Final step IST_PRC and IST_CPI are not in confidence p-value, remove from model.

```
model11 mn <- lm(log10(IST_MRTG_SL) ~ MG_RT + log10(IST_FGR_SL) +</pre>
                  TR PPI,
              data = IST RPPI_MODEL)
summary(model11 mn)
##
## Call:
## lm(formula = log10(IST_MRTG_SL) ~ MG_RT + log10(IST_FGR_SL) +
      TR PPI, data = IST RPPI MODEL)
##
## Residuals:
                       Median
        Min
                 10
                                    3Q
                                            Max
  ##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   4.0644591 0.0999960 40.646 < 2e-16 ***
                   -0.0447582 0.0037657 -11.886 < 2e-16 ***
## MG_RT
## log10(IST FGR SL) 0.1971191 0.0520759
                                        3.785 0.000327 ***
## TR PPI
                   ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.0677 on 68 degrees of freedom
## Multiple R-squared: 0.8779, Adjusted R-squared: 0.8725
## F-statistic: 163 on 3 and 68 DF, p-value: < 2.2e-16
```

Final outcome show us Property Sales with Mortgage is highly negative correlated with Mortgage Rates what It is easily expected. Turkey Producer Price Index also negative correlated with Mortgage Sales but Foreigner Sales strongly correlated with Foreigner Sales. When Foreigner Sales increase, Mortgage Sales also increasing.

For this study created and built different models. First of all in Model-1 include all variables which have logical correlation coefficients.

Housing Price Model

- Created model with the most logical variables in Model-1
- Eliminated one by one according to the P-Value.
- Housing Price Model

$$R^2 = 0.91$$

 $log10(HousingPrice) \\ = 0.07xlog10(FRGNRSL) + 0.003xRentCPI - 0.05xUSDRate + 0.07xlog10(CNSTPRMT) \\ + 2.175$

Mortgage Sale Model

- 1. Model 11 is explaining the **Housing Sales By Using Loan**, all big numbers like thousand reduced with log10. To many irrelevant p-values observed in model 8. Related Index numbers removed from model.
- 2. P-values which is bigger than 0.05 eliminated one by one and the final model.
- 3. Final model

$$R^2 = 0.83$$

log10(Sales) = 0.197xlog10(FRGNRSL) - 0.045xMGRT - 0.0007xTRPPI + 4.064

```
###### 9.3. Residential Property Price Index Monthly Changes - Creating
Different Models and See Residuals -
#model1_cg <- lm(IST_PRC ~ MG_RT + IST_FGR_SL + IST_PRP_SL + IST_MRTG_SL +
CNSTR_TRST + RNT_CPI + IST_CPI + TR_PPI + USD_RT + NEMP_RT + IST_CNST_PT +
IST_OCCP_PT_9 , data = train_cg)
#summary(model1_cg)

#model2_cg <- lm(IST_PRC ~ MG_RT + IST_FGR_SL + IST_PRP_SL + IST_MRTG_SL +
CNSTR_TRST + RNT_CPI + IST_CPI + TR_PPI + USD_RT + NEMP_RT + IST_CNST_PT +
IST_OCCP_PT_9 , data = train_cg)
#summary(model2_cg)

#model3_cg <- lm(IST_PRC ~ IST_FGR_SL + IST_PRP_SL + IST_MRTG_SL + RNT_CPI +
IST_CPI + TR_PPI + IST_CNST_PT + IST_OCCP_PT_9 , data = train_cg)
#summary(model3_cg)

#model4_cg <- lm(IST_PRC ~ RNT_CPI + IST_FGR_SL , data = train_cg)
#summary(model4_cg)

#This model include the change rates of Housing Unit Prices and other
variables. So try to explain Unit Prices with different undependent
variables.</pre>
```

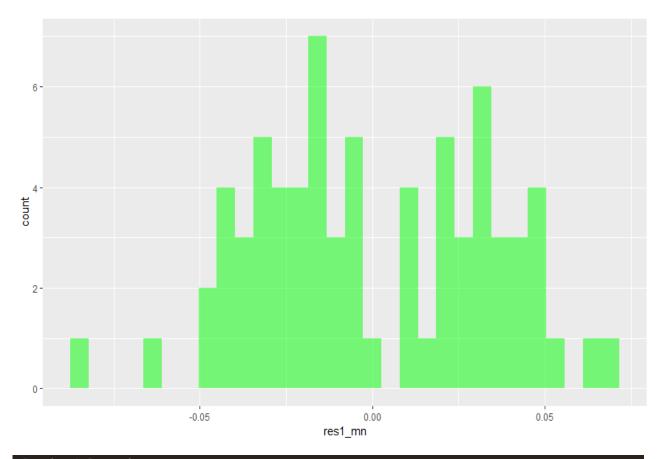
XII. Residuals - Outliers

For all model errors below in the table according to AIC & BIC.

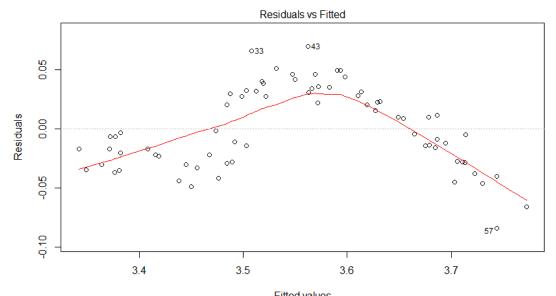
```
library(stats)
AIC(model1_mn,
    model2_mn,
    model3_mn,
    model4_mn,
    model5_mn,
    model6_mn,
    model7_mn,
    model8_mn,
    model9_mn,
    model10_mn,
    model11_mn)
```

```
df
                        AIC
## model1_mn
              10
                  999.4975
## model2_mn
              10 -270.0226
## model3 mn
               9 - 292.4694
## model4 mn
               9 -273.3428
## model5 mn
               8 -273.7747
               7 -274.4216
## model6 mn
## model7_mn
               6 -272.6729
## model8 mn
              14 -173.6773
## model9 mn
              12 -177.0729
## model10 mn
              7 -178.0671
## model11_mn
               5 -177.5276
BIC(model1_mn,
    model2 mn,
    model3_mn,
    model4_mn,
    model5_mn,
    model6_mn,
    model7 mn,
    model8 mn,
    model9 mn,
    model10_mn,
    model11 mn)
##
              df
                        BIC
              10 1022.2642
## model1_mn
## model2_mn
              10 -247.2560
## model3_mn
               9 -271.9794
## model4 mn
               9 -252.8529
## model5 mn
               8 -255.5613
## model6_mn
               7 -258.4850
## model7_mn
               6 -259.0129
## model8_mn
              14 -141.8039
## model9_mn
              12 -149.7529
## model10_mn
              7 -162.1304
## model11_mn 5 -166.1443
```

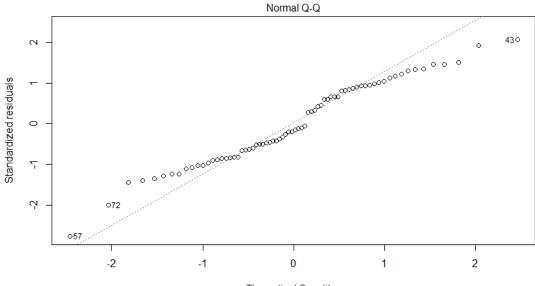
Related with Model-7 Residuals, Outliers showed on the plot.



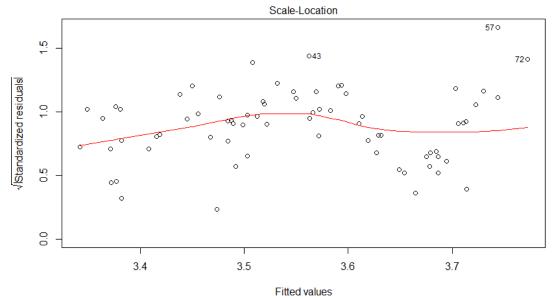
plot(model7_mn)



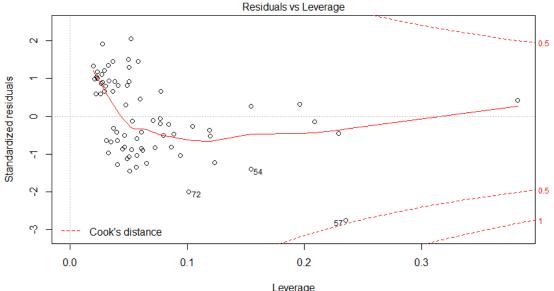
 $\label{eq:fitted} Fitted \ values $$ Im(log10(IST_PRC) \sim log10(IST_FGR_SL) + RNT_CPI + USD_RT + log10(IST_CNST_P \dots PROMOTE + INT_CPI +$



 $\label{log10} Theoretical Quantiles $$ Im(log10(IST_PRC) \sim log10(IST_FGR_SL) + RNT_CPI + USD_RT + log10(IST_CNST_P \dots NST_P) $$ and $$ Im(log10(IST_PRC) \sim log10(IST_PRC) + log10(IST_PRC) $$ and $$ Im(log10(IST_PRC) \sim log10(IST_PRC) $$ and $$ and $$ Im(log10(IST_PRC) \sim log10(IST_PRC) $$ and $$ Im(log10(IST_PRC) \sim log10(IST$

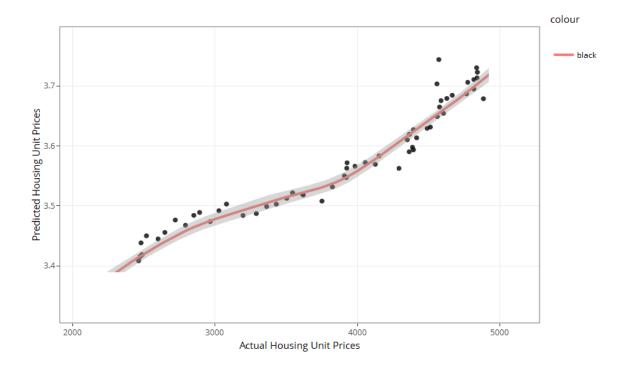


Im(log10(IST_PRC) ~ log10(IST_FGR_SL) + RNT_CPI + USD_RT + log10(IST_CNST_P ...



 $Leverage $$ Im(log10(IST_PRC) \sim log10(IST_FGR_SL) + RNT_CPI + USD_RT + log10(IST_CNST_P \dots + log10(IST_CNST_P + log10(IST_CNST$

```
##model2
## res2 <- residuals(model2)
##
## res2 <- as.data.frame(res2)
##
## ggplot(res2, aes(res2)) + geom_histogram(fill = 'green', alpha = 0.5)
##
## plot(model2)</pre>
```



XIII. Errors

Root Mean Square Error of Model-7:

```
error <- log10(IST_RPPI_MODEL$IST_PRC-IST_RPPI_MODEL$predicted.IST_PRC)
rmse <- sqrt(mean(error)^2)
data.frame(error)

## error
## 1 3.313962
## 2 3.324350
## 3 3.333263
## 4 3.339033</pre>
```

```
## 5 3.345260
## 6 3.354024
## 7 3.361043
## 8 3.364759
## 9 3.369697
## 10 3.378417
## 11 3.392814
## 12 3.394049
## 13 3.391059
## 14 3.395388
## 15 3.400648
## 16 3.414459
## 17 3.422334
## 18 3.434210
## 19 3.445506
## 20 3.454532
## 21 3.460680
## 22 3.471628
## 23 3.480521
## 24 3.488120
## 25 3.504160
## 26 3.516639
## 27 3.526142
## 28 3.534838
## 29 3.543987
## 30 3.549053
## 31 3.558151
## 32 3.557635
## 33 3.573646
## 34 3.582072
## 35 3.592887
## 36 3.593561
## 37 3.591520
## 38 3.593327
## 39 3.599627
## 40 3.607498
## 41 3.614967
## 42 3.617730
## 43 3.632097
## 44 3.639345
## 45 3.642284
## 46 3.638012
## 47 3.639483
## 48 3.642314
## 49 3.641572
## 50 3.644485
## 51 3.651632
## 52 3.653857
## 53 3.658556
## 54 3.658292
```

```
## 55 3.660048
## 56 3.660989
## 57 3.659547
## 58 3.664869
## 59 3.662634
## 60 3.668403
## 61 3.677587
## 62 3.682265
## 63 3.678380
## 64 3.682320
## 65 3.684525
## 66 3.684302
## 67 3.684049
## 68 3.688326
## 69 3.697681
## 70 3.709240
## 71 3.703702
## 72 3.706080
data.frame(rmse)
##
         rmse
## 1 3.552557
```

Tried for each observations to estimate the real and predicted value in Model-7 In this case, using logarithm process for the errors because of the model include Housing Price with Log10. So this errors say us differences between Real Housing Price and The model which built to explain housing price.

3. Time Series

Autoregressive Integrated Moving Average

In statistics and econometric, and in particular in time series analysis, an auto regressive integrated moving average (ARIMA) model is a generalization of an auto regressive moving average (ARMA) model. Both of these models are fitted to time series data either to better understand the data or to predict future points in the series (forecasting). ARIMA models are applied in some cases where **data show evidence of non-stationarity**, where an **initial differencing step** (corresponding to the "integrated" part of the model) can be applied one or more times to eliminate the non-stationary.

The AR part of ARIMA indicates that the evolving variable of interest is **regressed on its own lagged** (i.e., prior) values. The MA part indicates that the **regression error** is actually a linear combination of *error terms* whose values occurred contemporaneously and at various times in the past. The I (for "integrated") indicates that the data values have been replaced with the difference between their values and the previous values (and this difference process may have been performed more than once). The purpose of each of these features is to make the model fit the data as well as possible.

Non-seasonal ARIMA models are generally denoted ARIMA(p,d,q) where parameters p, d, and q are non-negative integers, p is the order (number of time lags) of the auto regressive model, d is the degree of difference (the number of times the data have had past values subtracted), and q is the order of the moving-average model. Seasonal ARIMA models are usually denoted ARIMA(p,d,q)(P,D,Q)m, where m refers to the number of periods in each season, and the uppercase P,D,Q refer to the auto regressive, difference, and moving average terms for the seasonal part of the ARIMA model.

When two out of the three terms are zeros, the model may be referred to based on the non-zero parameter, dropping "AR", "I" or "MA" from the acronym describing the model. For example, $ARIMA\ (1,0,0)$ is AR(1), ARIMA(0,1,0) is I(1), and ARIMA(0,0,1) is MA(1). ARIMA models can be estimated following the Box-Jenkins approach.

This analysis help us to understand the housing price changes will be in 6 months

XIV. Set The Libraries

Setting the libraries which will using on analyze.

```
library(ggplot2)
library(forecast)
library(tseries)
library(astsa)
library(readr)
```

XV. Data Import

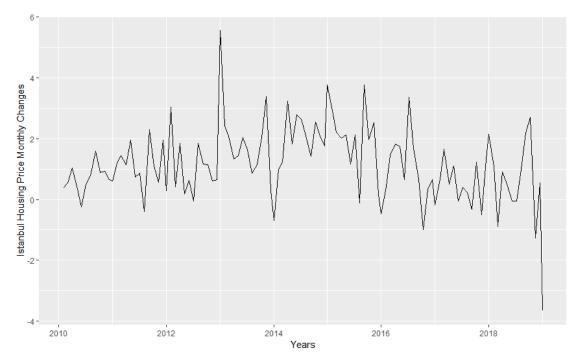
The data include monthly changes of unit housing prices at Istanbul

```
library(readr)
IST_UNTPRC_FRCST <- read_csv("IST_UNTPRC_FRCST.csv",</pre>
                             col_types = cols(DATE = col_date(format =
"%d.%m.%Y")))
head(IST_UNTPRC_FRCST)
## # A tibble: 6 x 2
     DATE IST_PRC_CG
##
     <date>
                     <dbl>
## 1 2010-02-02
                      0.37
                      0.54
## 2 2010-03-03
## 3 2010-04-04
                      1.04
## 4 2010-05-05
                      0.44
                     -0.25
## 5 2010-06-06
## 6 2010-07-07
                      0.5
```

XVI. Show The Distribution of Housing Price Index

Distribution of Monthly Housing Price Changes:

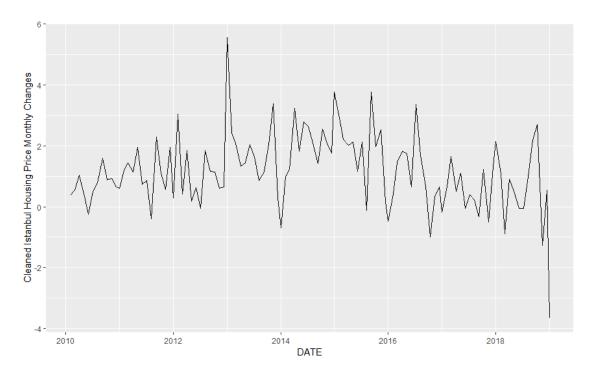
```
ggplot(IST_UNTPRC_FRCST, aes(DATE, IST_PRC_CG)) +
    geom_line() + scale_x_date('Years') +
    ylab("Istanbul Housing Price Monthly Changes") +
        xlab("")
```



XVII. Clean The Outliers with Tsclean

Cleaning the trend of monthly changes to get linear, handle with extreme outliers.

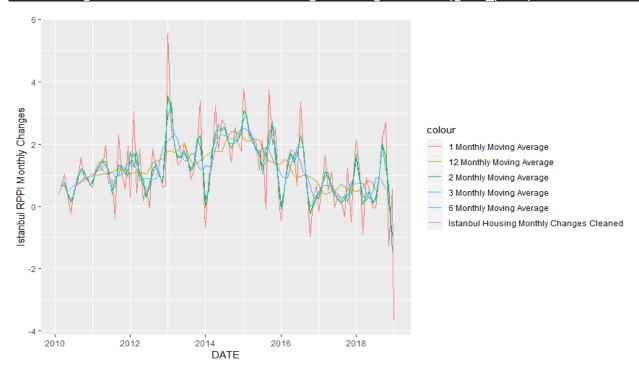
```
count_ts = ts(IST_UNTPRC_FRCST[, c('IST_PRC_CG')])
IST_UNTPRC_FRCST$clean_cnt = tsclean(count_ts)
ggplot() +
    geom_line(data = IST_UNTPRC_FRCST, aes(x = DATE, y = clean_cnt)) +
        ylab('Cleaned Istanbul Housing Price Monthly Changes')
## Don't know how to automatically pick scale for object of type ts.
Defaulting to continuous.
```



XVIII. Quarterly and Monthly Moving Averages

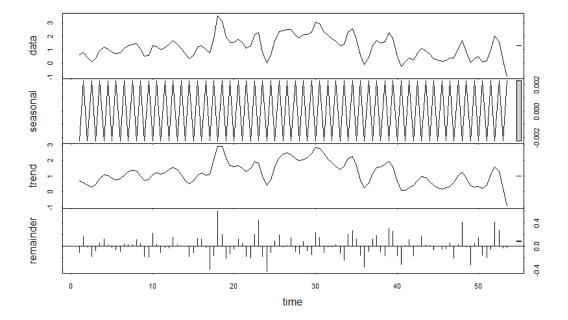
Divide into data some different periods to forecast more accuracy.

```
IST_UNTPRC_FRCST$cnt_ma1 = ma(IST_UNTPRC_FRCST$clean_cnt, order=1)
IST_UNTPRC_FRCST$cnt_ma2 = ma(IST_UNTPRC_FRCST$clean_cnt, order=2)
IST_UNTPRC_FRCST$cnt_ma3 = ma(IST_UNTPRC_FRCST$clean_cnt, order=3)
IST_UNTPRC_FRCST$cnt_ma6 = ma(IST_UNTPRC_FRCST$clean_cnt, order=6)
IST_UNTPRC_FRCST$cnt_ma12 = ma(IST_UNTPRC_FRCST$clean_cnt, order=12)
ggplot() +
  geom_line(data = IST_UNTPRC_FRCST, aes(x = DATE,
                                         y = clean_cnt,
                                         colour = "Istanbul Housing Monthly
Changes Cleaned")) +
  geom_line(data = IST_UNTPRC_FRCST, aes(x = DATE,
                                         y = cnt_ma1,
                                         colour = "1 Monthly Moving
Average")) +
  geom_line(data = IST_UNTPRC_FRCST, aes(x = DATE,
                                         y = cnt_ma2,
                                         colour = "2 Monthly Moving
Average")) +
  geom_line(data = IST_UNTPRC_FRCST, aes(x = DATE,
                                         y = cnt_ma3,
                                         colour = "3 Monthly Moving
```



XIX. Decompose - Forecasting The Data

Decomposing data to get rid of seasonality. Chooses the frequency two. This means Auto Regressive Term and Moving Avarages according to two months.



- Data: The trend isn't in balance and very variable term.
- Seasonality: Not in seasonality
- Trend: Changes are going down for the last 5-6 periods.
- Remainder: Show us the lag of data. In the 16th period.

XX. Stationarity - ADF Test

```
##
## data: count_ma
## Dickey-Fuller = -2.5629, Lag order = 4, p-value = 0.3432
## alternative hypothesis: stationary
```

Now, testing model with ADF - Augmented Dickey Fuller Test, p-value bigger than .05

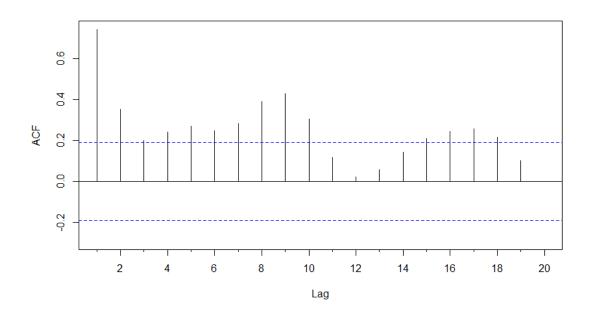
XXI. Autocorrelation and Choosing Model Order (ACF)

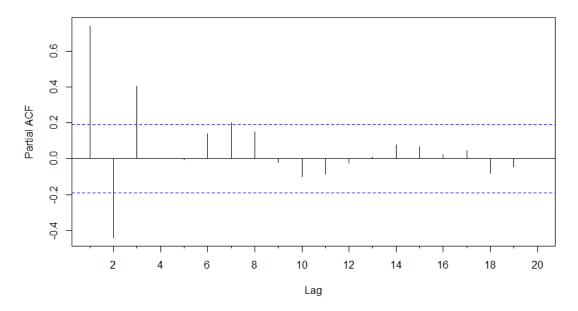
Auto correlation, also known as **serial correlation**, is the correlation of a signal with a delayed copy of itself as a function of delay. Informally, it is the similarity between observations as a function of the **time lag** between them. The analysis of auto correlation is a mathematical tool for finding repeating patterns, such as the presence of a periodic signal obscured by noise, or identifying the missing fundamental frequency in a signal implied by its harmonic frequencies. It is often used in signal processing for analyzing functions or series of values, such as time domain signals.

Different fields of study define autocorrelation differently, and not all of these definitions are equivalent. In some fields, the term is used interchangeably with autocovariance.

Unit root processes, trend stationary processes, auto regressive processes, and moving average processes are specific forms of processes with auto correlation.

```
##autocorrelation
Acf(count_ma, main ="", plot = TRUE)
```



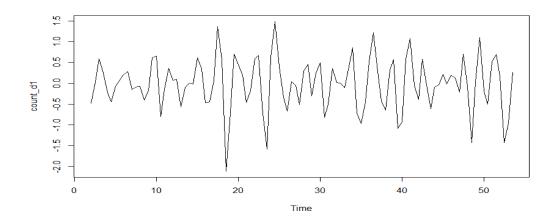


```
#Acf(count_ma, main ="", plot = FALSE)
#Pacf(count_ma, main ="", plot = FALSE)
```

There are no stationary in the model, Lags are keeping decrease untill 18th periods.

XXII. Tune The Model

```
count_d1 = diff(deseasonal_cnt, differences = 2)
plot(count_d1)
```



```
adf.test(count_d1, alternative = "stationary" )

## Warning in adf.test(count_d1, alternative = "stationary"): p-value smaller

## than printed p-value

##

## Augmented Dickey-Fuller Test

##

## data: count_d1

## Dickey-Fuller = -6.2587, Lag order = 4, p-value = 0.01

## alternative hypothesis: stationary
```

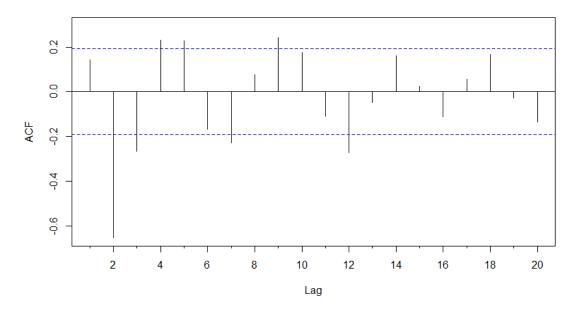
If the p value was bigger than 0.05, Differences should be use again. The model's p-value \sim .01

This process using errors to forecast previous periods.

```
## count_d2 = diff(count_d1, differences = 1)
## plot(count_d2)
## adf.test(count_d2, alternative = "stationary" )

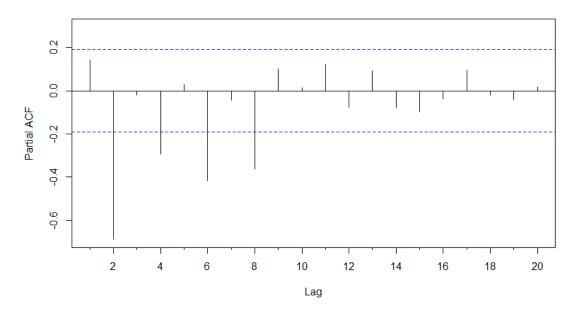
Acf(count_d1,
    main = "ACF for Differenced Series")
```

ACF for Differenced Series



```
Pacf(count_d1,
    main = "PACF for Differenced Series")
```

PACF for Differenced Series



```
#Acf(count_d1,
# main = "ACF for Differenced Series", plot = FALSE)
#Pacf(count_d1,
# main = "PACF for Differenced Series", plot = FALSE)
```

Lags can be observed in 3rd months because of the model array order is 3. To justify the model lag max should be 3. At 9th month's lag isn't in trust line. Fitting and Autoarima should be try.

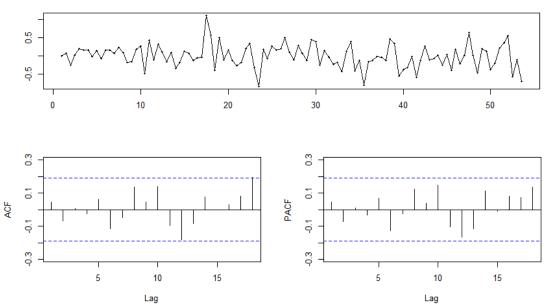
XXIII. Fitting an ARIMA Model

```
auto.arima(deseasonal_cnt, seasonal = FALSE)
## Series: deseasonal cnt
## ARIMA(2,1,2)
  Coefficients:
##
            ar1
                      ar2
                              ma1
                                       ma2
##
         0.7675
                 -0.5081
                           0.0884
                                   -0.7289
         0.0983
                  0.0912
                           0.0804
                                    0.0771
## sigma^2 estimated as 0.1038: log likelihood=-29.71
               AICc=70.03
                             BIC=82.69
   AIC=69.42
```

Auto arima say to model use Auto Regressive Term and Moving Average Two, Difference period is one.

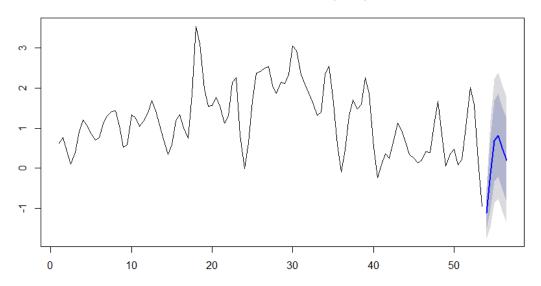
XXIV. Evaluate and Iterate

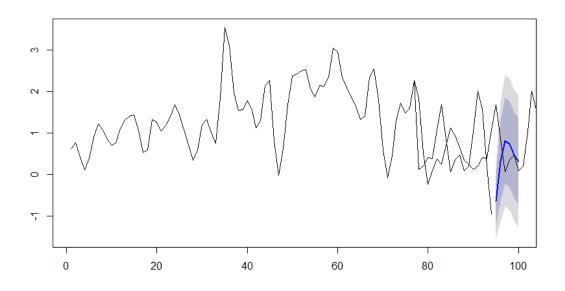
(2,1,2) Model Residuals



```
#fit2 = arima(deseasonal_cnt, order = c(1,1,1))
#fit2
#tsdisplay(residuals(fit2), lag.max = 12, main ="Seasonal Model Residuals")
fcast <- forecast(fit1, h = 6)
plot(fcast)</pre>
```

Forecasts from ARIMA(2,1,2)





```
fit_w_seasonality = auto.arima(deseasonal_cnt, seasonal=TRUE)
fit_w_seasonality
```

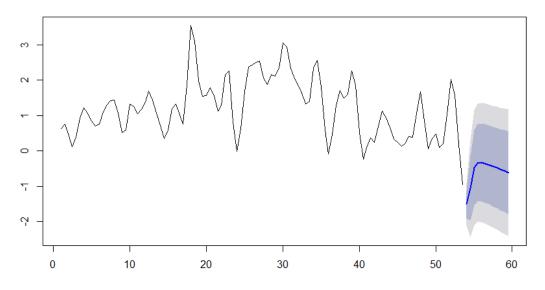
```
## Series: deseasonal cnt
## ARIMA(1,1,1)(1,0,2)[2]
  Coefficients:
##
##
            ar1
                                             sma2
                    ma1
                            sar1
                                     sma1
         0.2992
                 0.7402
                         0.9749
                                           0.9037
                                  -1.8786
         0.1703
                 0.1726
                         0.0448
                                   0.0838
                                           0.0823
##
## sigma^2 estimated as 0.09516: log likelihood=-26.99
## AIC=65.98
               AICc=66.84
```

XXV. Forecast The Istanbul Housing Price Changes

Actual Value of The Price Index

DATE	IST RPPI	CHANGE	UNIT PRICES	UNIT PRICE CHANGE
1.01.2019	100.15	-1.84	4900.15	-3.66
2.02.2019	99.63	-0.52	4702.03	-4.04
3.03.2019	99.34	-0.29	4657.59	-0.95
<pre>seas_fcast <- forecast(fit_w_seasonality, h=12)</pre>				
<pre>plot(seas</pre>	_fcast)			

Forecasts from ARIMA(1,1,1)(1,0,2)[2]



```
## Forecast method: ARIMA(1,1,1)(1,0,2)[2]
## Model Information:
## Series: deseasonal cnt
## ARIMA(1,1,1)(1,0,2)[2]
##
## Coefficients:
           ar1
                          sar1
                                           sma2
                   ma1
                                   sma1
         0.2992 0.7402 0.9749 -1.8786 0.9037
## s.e. 0.1703 0.1726 0.0448
                                 0.0838 0.0823
##
## sigma^2 estimated as 0.09516: log likelihood=-26.99
             AICc=66.84 BIC=81.9
## AIC=65.98
##
## Error measures:
                        ME
                                          MAE
                                                    MPE
                                                            MAPE
                                RMSE
                                                                      MASE
## Training set -0.02015907 0.2996248 0.2265602 -2.891127 35.16316 0.3256143
                      ACF1
## Training set 0.009417765
##
## Forecasts:
         Point Forecast
                           Lo 80
                                      Hi 80
                                                Lo 95
                                                          Hi 95
## 54.00
            -1.5099912 -1.905514 -1.1144684 -2.114891 -0.9050913
## 54.50
            -1.0575998 -1.955976 -0.1592238 -2.431547 0.3163477
## 55.00
            -0.4742754 -1.539578 0.5910271 -2.103515 1.1549642
## 55.50
            -0.3413893 -1.432975 0.7501962 -2.010825 1.3280466
## 56.00
            -0.3257026 -1.427128 0.7757226 -2.010187 1.3587819
## 56.50
            -0.3616087 -1.470237 0.7470197 -2.057109 1.3338921
## 57.00
            -0.3958208 -1.511893  0.7202516 -2.102706  1.3110646
## 57.50
            -0.4456388 -1.569952 0.6786740 -2.165127 1.2738493
## 58.00
            -0.4834252 -1.617247 0.6503963 -2.217455 1.2506051
## 58.50
            -0.5333204 -1.677822 0.6111815 -2.283685 1.2170442
## 59.00
           -0.5705563 -1.727195 0.5860823 -2.339482 1.1983697
## 59.50
          -0.6193195 -1.789356 0.5507173 -2.408736 1.1700974
```

4. The Result

The result of the study "Housing Prices in Istanbul" are more impose by **Consumer and Producer Index related with Rent, USD Currency Rate, Construction Permits and Foreigner Sales**. Some Index and Rates directly affecting Prices&Sales. The final model below with the equation:

log10(HousingPrice)

= 0.07xlog10(FRGNRSL) + 0.003xRentCPI - 0.05xUSDRate + 0.07xlog10(CNSTPRMT) + 2.175

log10(Sales) = 0.197xlog10(FRGNRSL) - 0.045xMGRT - 0.0007xTRPPI + 4.064

Regression analysis proved that the other independent variables may affecting less than consumer and procuder index.

Time Series Analysis also proved that Housing Market in Istanbul will be negative growth for 6 months as well will be decreasing The Housing Prices for 6 months.

5. References

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- 2. Linear Regression with Boston Housing Data set, Sukesh Kumar Pabba
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- 4. https://en.wikipedia.org/wiki/Autoregressive_integrated_moving_average
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