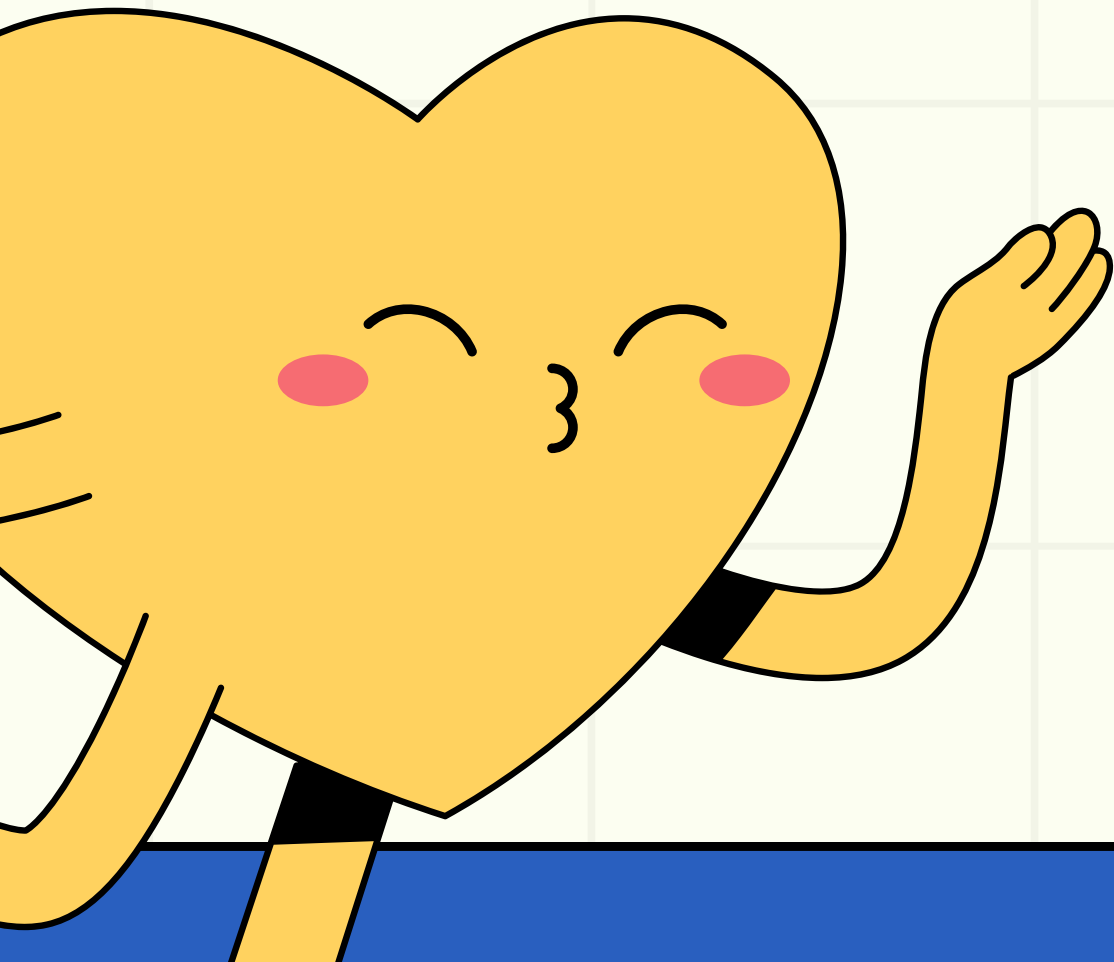
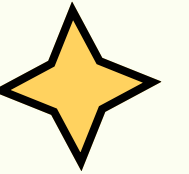


MINI PROJECT

Bayesian Data Analysis



Aldo Oktavianus - 2702234081
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William - 2702225373

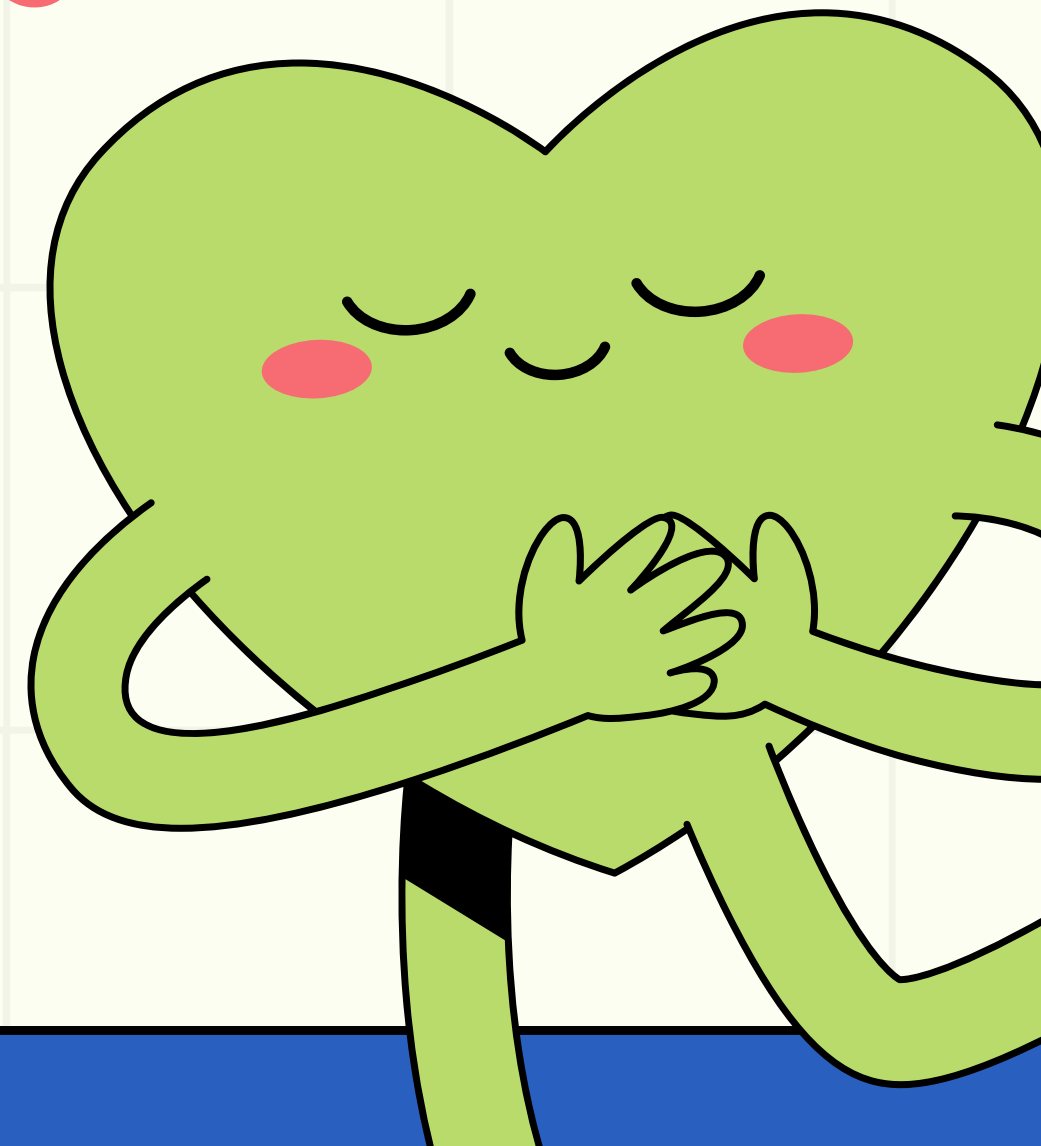


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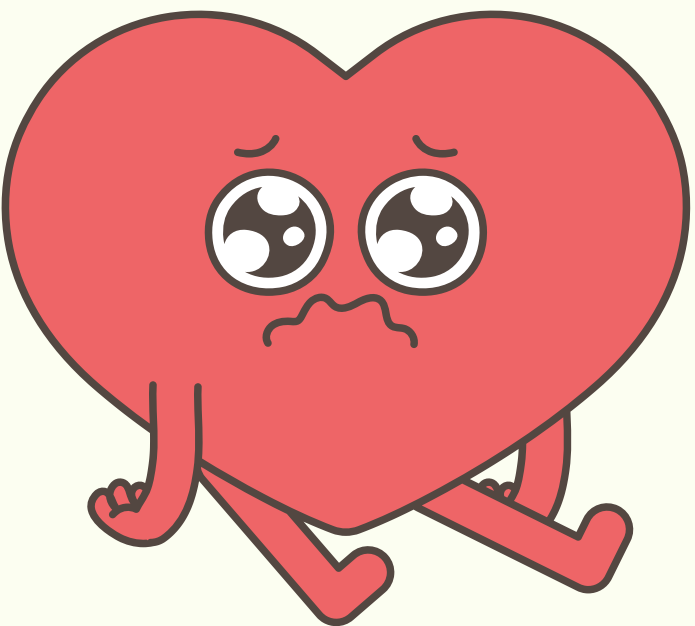
2. Goals

3. Models

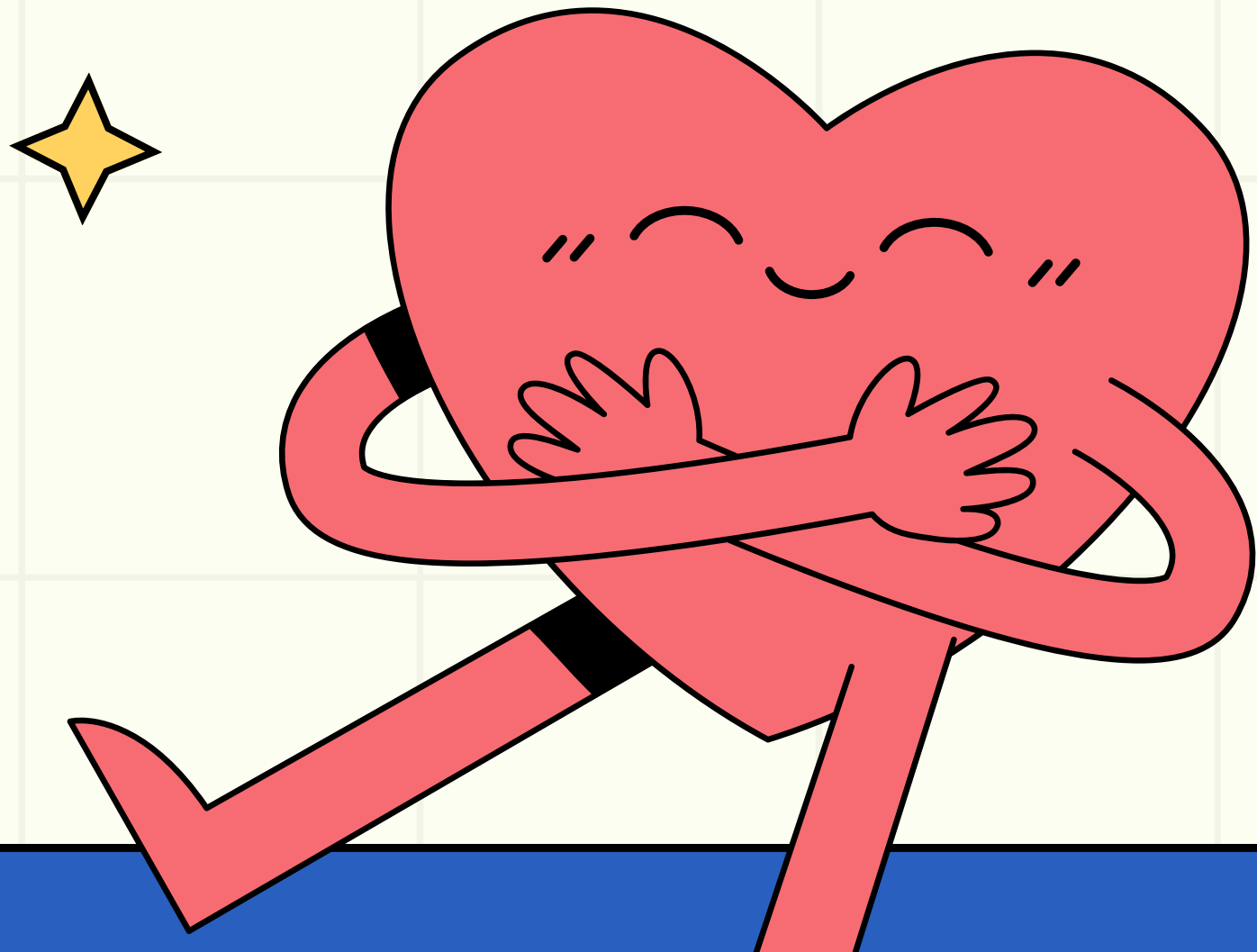
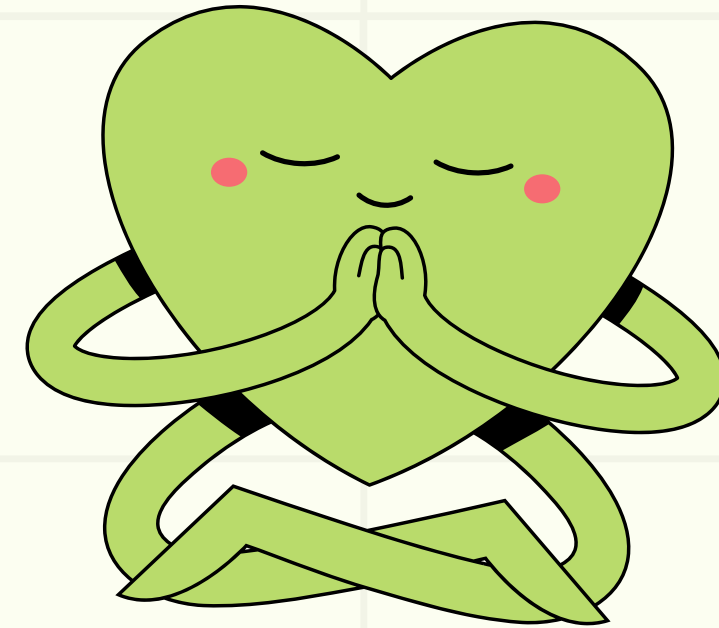
4. Algorithm

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INTRODUCTION

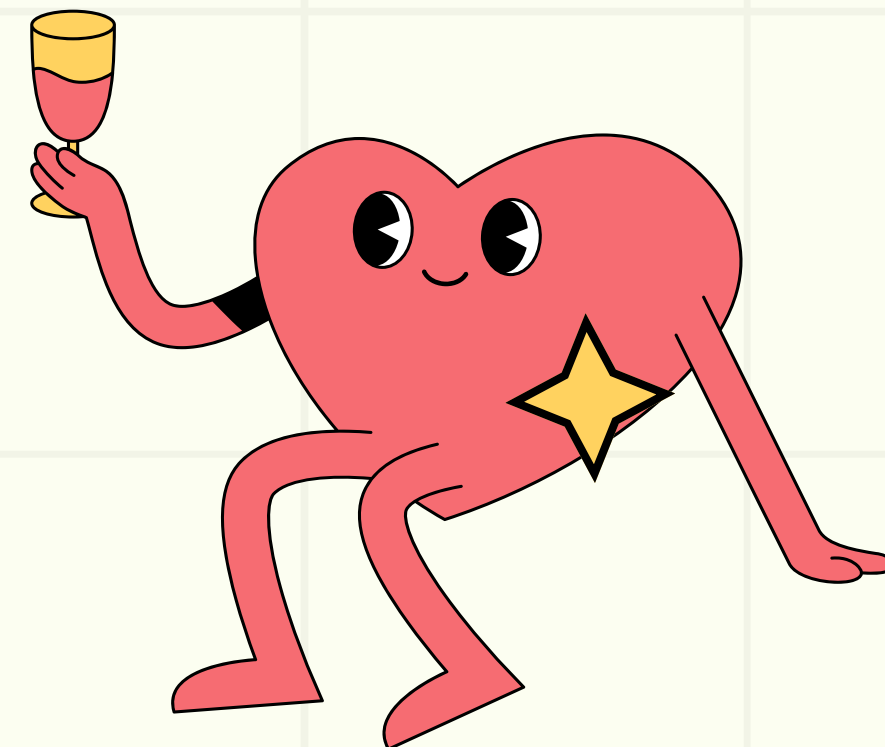
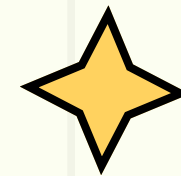


Stroke is a medical condition characterized by a sudden disruption of blood flow to the brain, leading to cell damage. It is a leading cause of death and disability worldwide, with various risk factors such as hypertension, heart disease, age, and lifestyle choices. Early identification of stroke risk factors is crucial for prevention and improving patient outcomes.

The dataset used in this project comprises 5,110 rows and 12 columns which consist:

- **id**: Unique identifier for each patient.
- **gender**: Gender of the patient (Male/Female).
- **age**: Age of the patient.
- **hypertension**: Presence of hypertension (0 = No, 1 = Yes).
- **heart_disease**: Presence of heart disease (0 = No, 1 = Yes).
- **ever_married**: Marital status (Yes/No).
- **work_type**: Type of occupation (e.g., Private, Self-employed, Govt job).
- **Residence_type**: Living environment (Urban/Rural).
- **avg_glucose_level**: Average glucose level in the blood.
- **bmi**: Body Mass Index.
- **smoking_status**: Smoking habits (e.g., never smoked, formerly smoked, smokes).
- **stroke**: Stroke occurrence (1 = Yes, 0 = No).

Dataset Overview



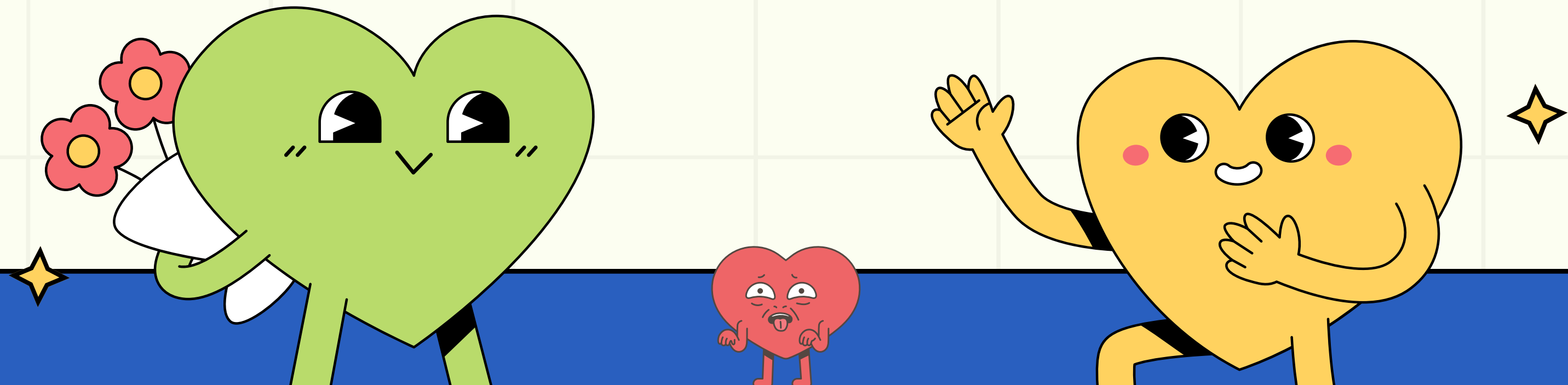
Models

01

**BAYESSIAN LOGISTIC REGRESSION
with ALL FEATURES**

02

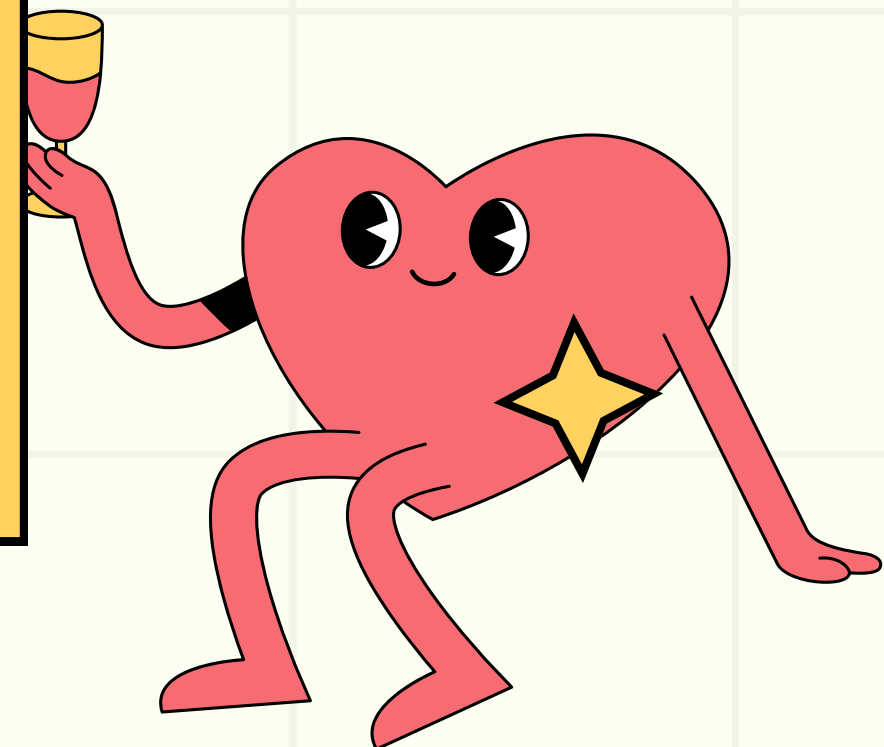
**BAYESSIAN LOGISTIC REGRESSION
with SELECTED FEATURES**



ENCODING

label encoding:

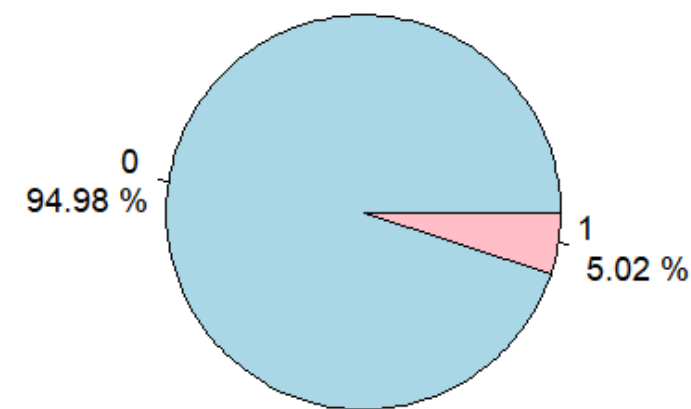
- gender
- ever_married
- work_type
- smoking_statys
- residence_type



Our Assumption

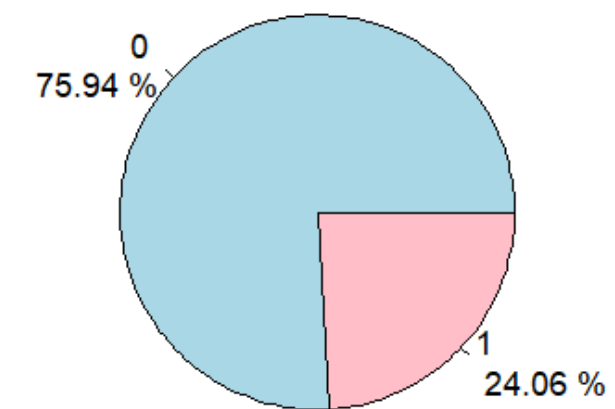
Severe Class Imbalance

Class Proportion of Stroke in Training Set

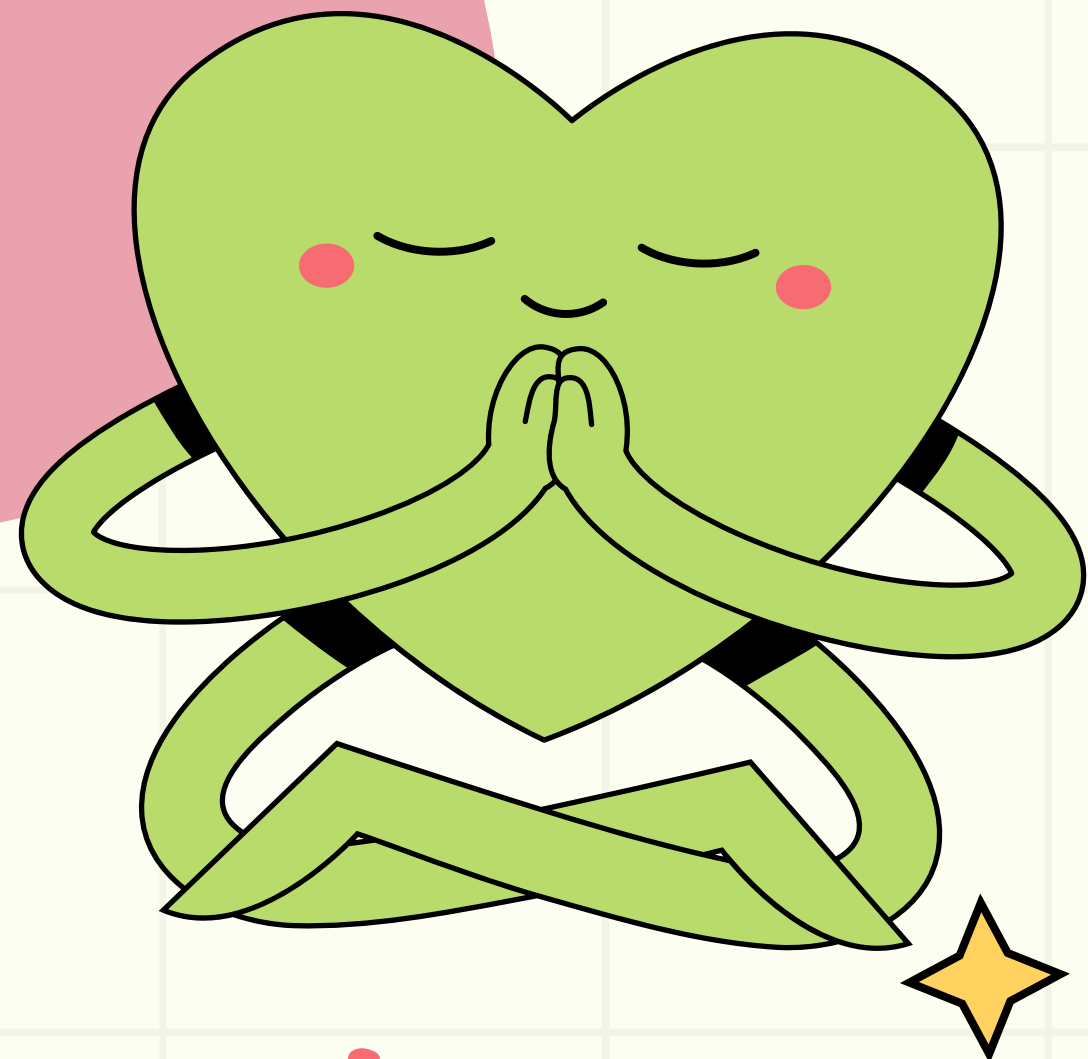


Before SMOTE

Class Proportion of Stroke in Training Set



After SMOTE



Model 1

All Features

LIKELIHOOD:

Bernoulli Distribution

$Y[i] \sim \text{dbern}(pi[i])$

Reasonings:

- Binary output
- Compatible with logit relationship
- Fits independent events

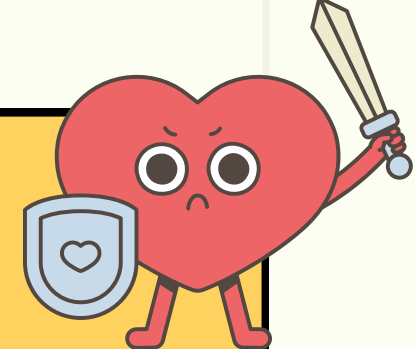
PRIOR:

Normal Distribution

- Coeficients ($\beta[j]$): $\beta[j] \sim \text{dnorm}(0,0.01)$
- Intercept (α): $\alpha \sim \text{dnorm}(0,0.01)$

Reasonings:

- Uninformative priors
- Flexibility



Model 2:

Selected Features

LIKELIHOOD:

Bernoulli Distribution

$y[i] \sim \text{dbern}(\pi[i])$

Reasonings:

- Binary output
- Compatible with logit relationship
- Fits independent events

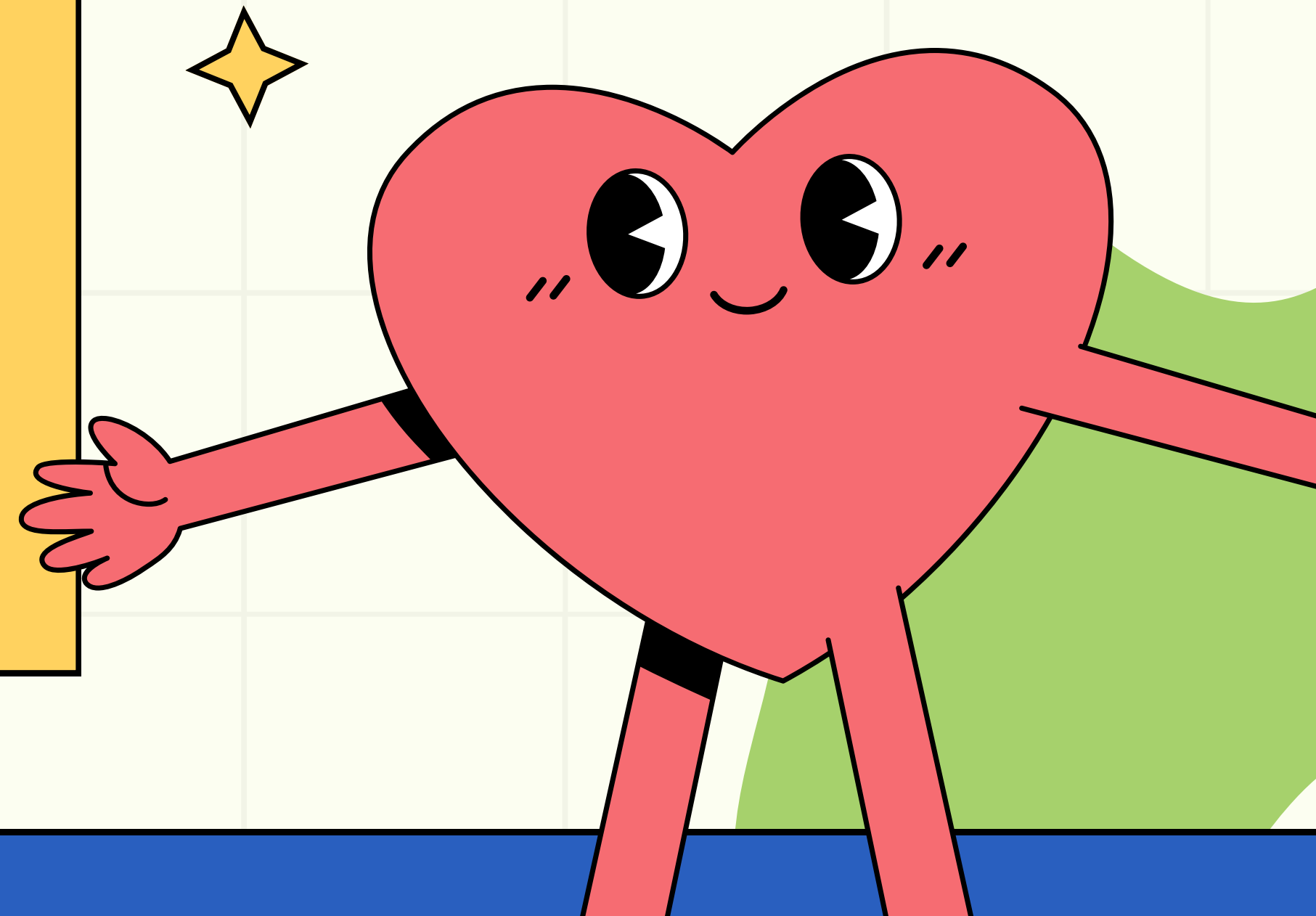
PRIOR:

Normal Distribution

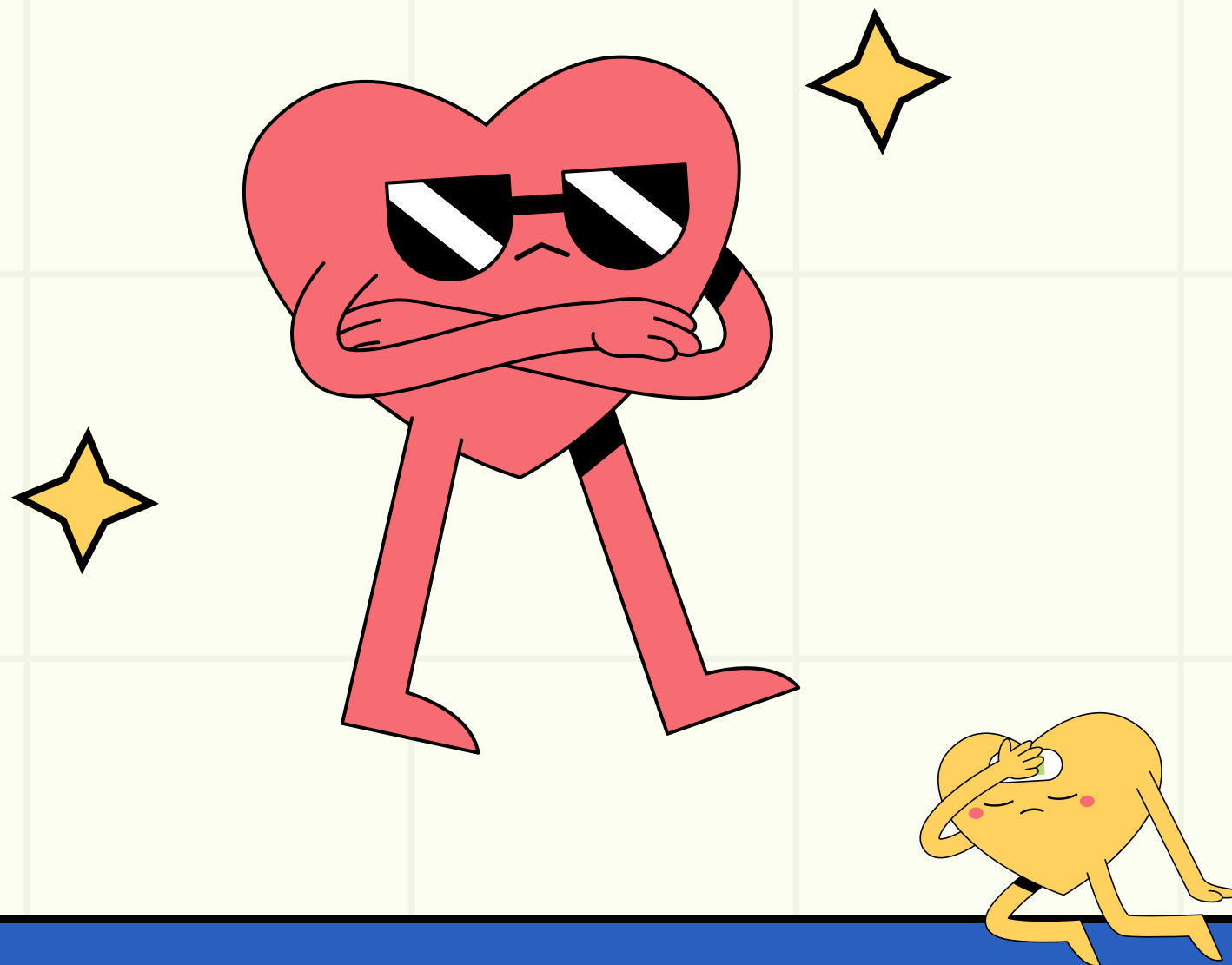
- Coefficients ($\beta[j]$): $\beta[j] \sim \text{dnorm}(0, 0.01)$
- Intercept (α): $\alpha \sim \text{dnorm}(0, 0.01)$

Reasonings:

- Uninformative priors
- Scalability



Convergence Diagnostic Model #1



Geweke

```
{r}
for (i in 1:4){
  cat("Chain", i)
  print(geewe.diag(samples_1[[i]]))
}
```

Chain 1

Fraction in 1st window = 0.1
Fraction in 2nd window = 0.5

alpha	beta[1]	beta[2]	beta[3]	beta[4]	beta[5]	beta[6]	beta[7]	beta[8]	beta[9]	beta[10]
-0.16067	-1.18517	-0.53223	-0.14597	0.42006	0.88653	-0.02353	-1.00996	-0.25424	0.43493	-0.22263

Chain 2

Fraction in 1st window = 0.1
Fraction in 2nd window = 0.5

alpha	beta[1]	beta[2]	beta[3]	beta[4]	beta[5]	beta[6]	beta[7]	beta[8]	beta[9]	beta[10]
-1.0425	-0.1859	2.1235	0.6147	-0.5594	0.0232	1.1334	0.3154	1.4952	1.0433	3.1897

Chain 3

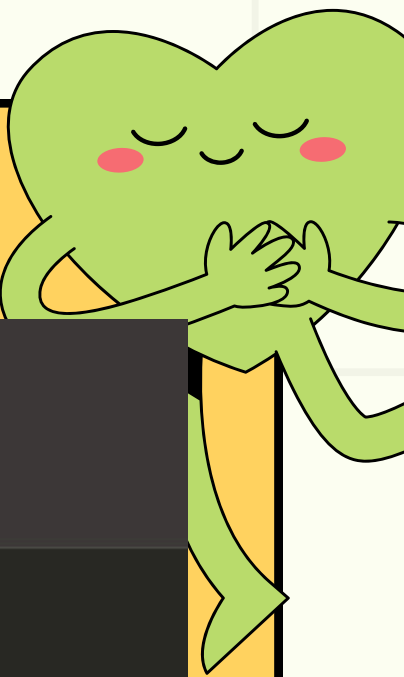
Fraction in 1st window = 0.1
Fraction in 2nd window = 0.5

alpha	beta[1]	beta[2]	beta[3]	beta[4]	beta[5]	beta[6]	beta[7]	beta[8]	beta[9]	beta[10]
0.40236	-0.83350	-0.96642	-1.05789	-0.89184	0.03266	0.26321	0.30528	0.62139	-1.50968	-1.05846

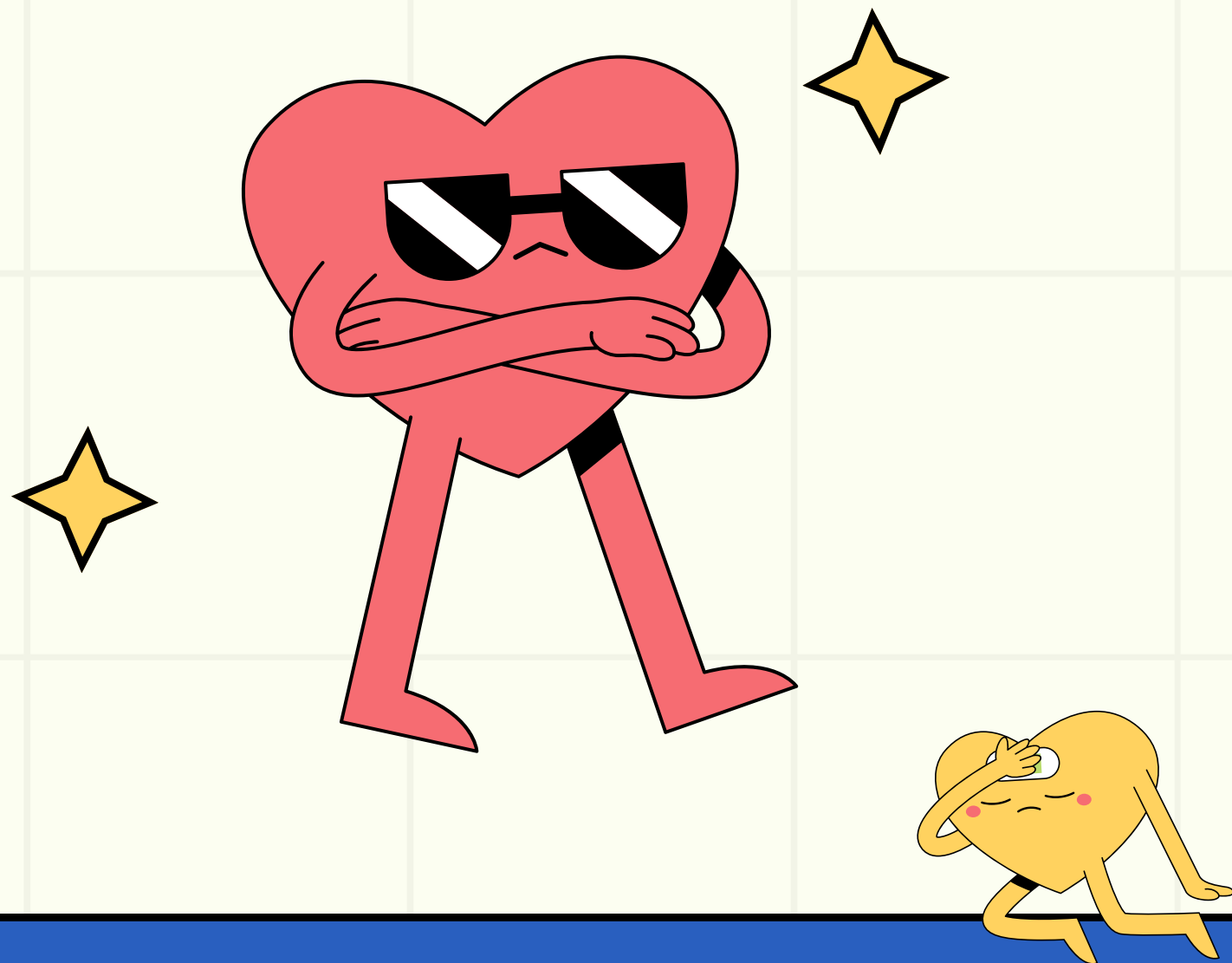
Chain 4

Fraction in 1st window = 0.1
Fraction in 2nd window = 0.5

alpha	beta[1]	beta[2]	beta[3]	beta[4]	beta[5]	beta[6]	beta[7]	beta[8]	beta[9]	beta[10]
-0.3310	0.4681	-1.9156	0.1613	1.5628	0.6460	0.2953	0.1653	0.4382	-1.0712	-0.1300



Convergence Diagnostic Model #1



Gelman Rubin

```
##{r}  
gelman.diag(samples_1)
```

Potential scale reduction factors:

	Point est.	Upper C.I.
alpha	1	1.01
beta[1]	1	1.00
beta[2]	1	1.00
beta[3]	1	1.00
beta[4]	1	1.00
beta[5]	1	1.00
beta[6]	1	1.00
beta[7]	1	1.00
beta[8]	1	1.00
beta[9]	1	1.00
beta[10]	1	1.00

Multivariate psrf

1



Geweke

```
```{r}
for (i in 1:4){
 cat("Chain", i)
 print(geeweke.diag(samples_2[[i]]))
}
```
```

Chain 1

Fraction in 1st window = 0.1
Fraction in 2nd window = 0.5

| alpha | beta[1] | beta[2] | beta[3] | beta[4] | beta[5] | beta[6] | beta[7] | beta[8] |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| -0.5156 | -0.7651 | -1.6092 | -0.1360 | -0.4885 | 0.1186 | 0.8997 | -0.5297 | 0.4353 |

Chain 2

Fraction in 1st window = 0.1
Fraction in 2nd window = 0.5

| alpha | beta[1] | beta[2] | beta[3] | beta[4] | beta[5] | beta[6] | beta[7] | beta[8] |
|--------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1.6682 | 2.6231 | 1.9678 | 0.3208 | -0.2572 | -1.6442 | -2.3266 | -0.6556 | -0.8705 |

Chain 3

Fraction in 1st window = 0.1
Fraction in 2nd window = 0.5

| alpha | beta[1] | beta[2] | beta[3] | beta[4] | beta[5] | beta[6] | beta[7] | beta[8] |
|---------|---------|----------|---------|---------|----------|----------|---------|---------|
| 0.68758 | 0.99238 | -0.17962 | 0.26204 | 0.02625 | -0.18472 | -1.83409 | 0.07535 | 1.15544 |

Chain 4

Fraction in 1st window = 0.1
Fraction in 2nd window = 0.5

| alpha | beta[1] | beta[2] | beta[3] | beta[4] | beta[5] | beta[6] | beta[7] | beta[8] |
|--------|---------|---------|---------|---------|---------|---------|---------|---------|
| 1.6212 | 1.9683 | 3.1209 | -1.2501 | -0.5724 | -2.2786 | -1.9046 | -1.3303 | -2.3774 |

Convergence Diagnostic Model #2



Gelman Rubin

```
## {r}  
gelman.diag(samples_2)
```

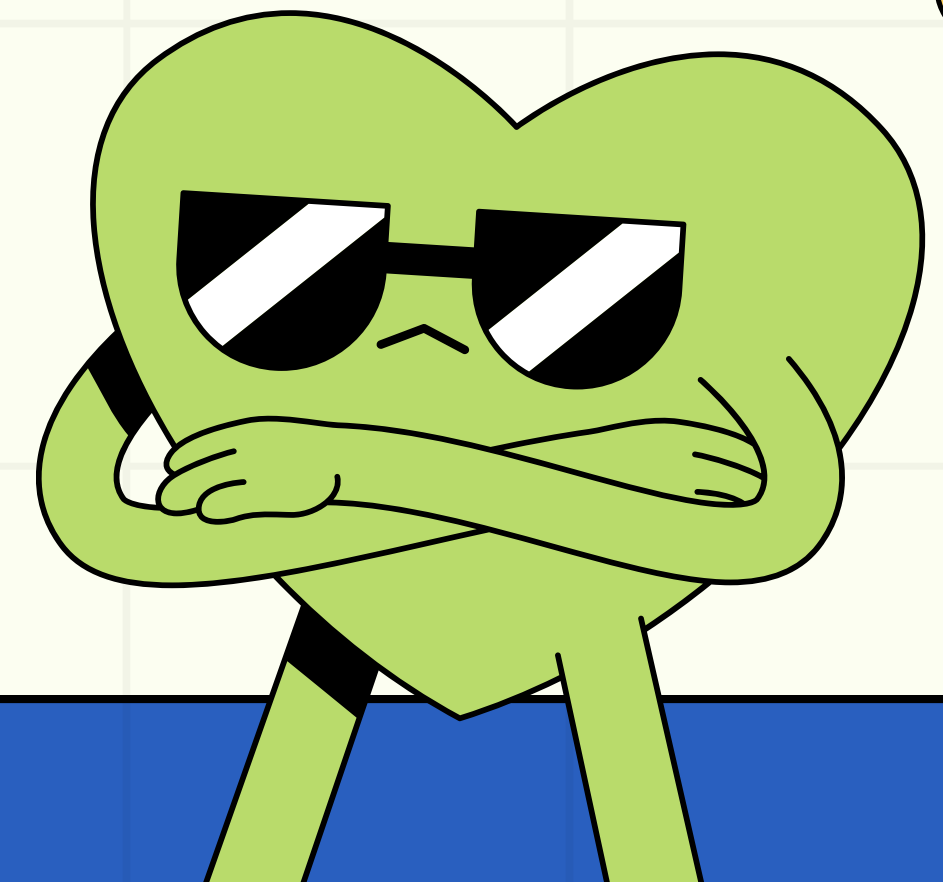
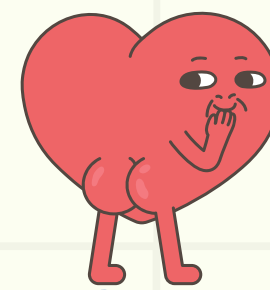
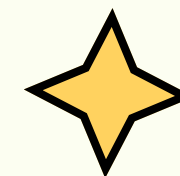
Potential scale reduction factors:

| | Point est. | Upper C.I. |
|---------|------------|------------|
| alpha | 1.03 | 1.10 |
| beta[1] | 1.00 | 1.00 |
| beta[2] | 1.00 | 1.00 |
| beta[3] | 1.00 | 1.01 |
| beta[4] | 1.00 | 1.00 |
| beta[5] | 1.00 | 1.01 |
| beta[6] | 1.03 | 1.08 |
| beta[7] | 1.00 | 1.01 |
| beta[8] | 1.00 | 1.01 |

Multivariate psrf

1.03

Convergence Diagnostic Model #2



Model Comparison

DIC & WAIC (Model 1)

```
```{r}
dic1
```
```

| | | |
|---------------------|------------|------------|
| Mean deviance: | 3978 | |
| penalty | 11.03 | |
| Penalized deviance: | 3989 | |
| | Estimate | SE |
| | <S3: AsIs> | <S3: AsIs> |
| elpd_loo | -1994.8 | 37.4 |
| p_loo | 10.9 | 0.3 |
| looic | 3989.5 | 74.8 |

3 rows

DIC & WAIC (Model 2)

```
```{r}
dic2
```
```

| | | |
|---------------------|------------|------------|
| Mean deviance: | 4048 | |
| penalty | 8.928 | |
| Penalized deviance: | 4057 | |
| | Estimate | SE |
| | <S3: AsIs> | <S3: AsIs> |
| elpd_loo | -2028.4 | 37.6 |
| p_loo | 8.9 | 0.2 |
| looic | 4056.9 | 75.1 |

3 rows

Deviance Information Criterion (DIC)

Mean Deviance: goodness of fit of the model

Penalty: complexity of the model

Penalized Deviance: combination of fit and penalty

Model 1 is preferable overall because it has a lower DIC and better data fit (lower mean deviance), despite being slightly more complex than Model 2.

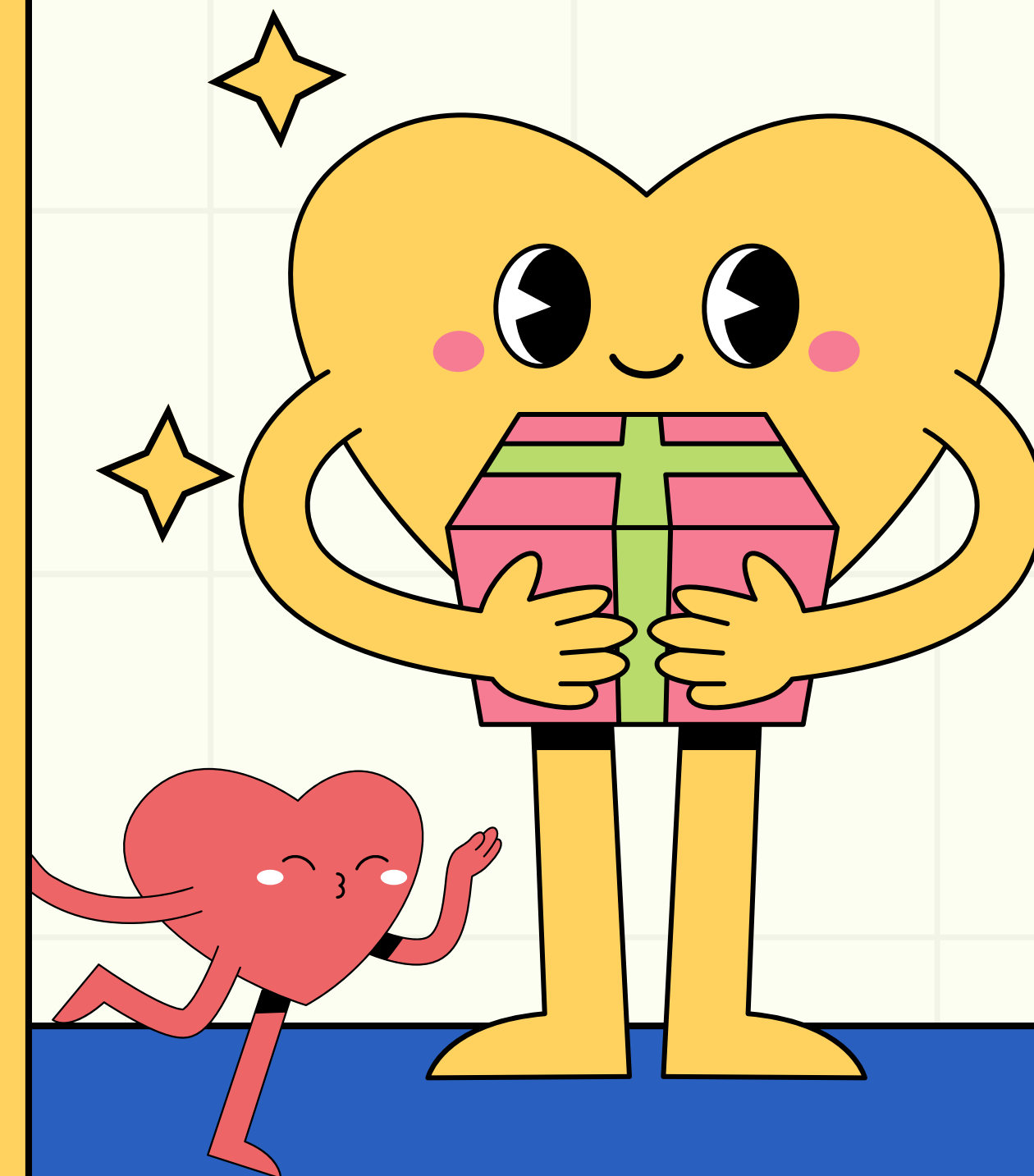
Watanabe-Akaike Information Criterion (WAIC)

Expected Log Predictive Density: measures model predicts unseen data

Penalized: model's complexity

Lower Overall Information Criterion: balances between model fit and complexity

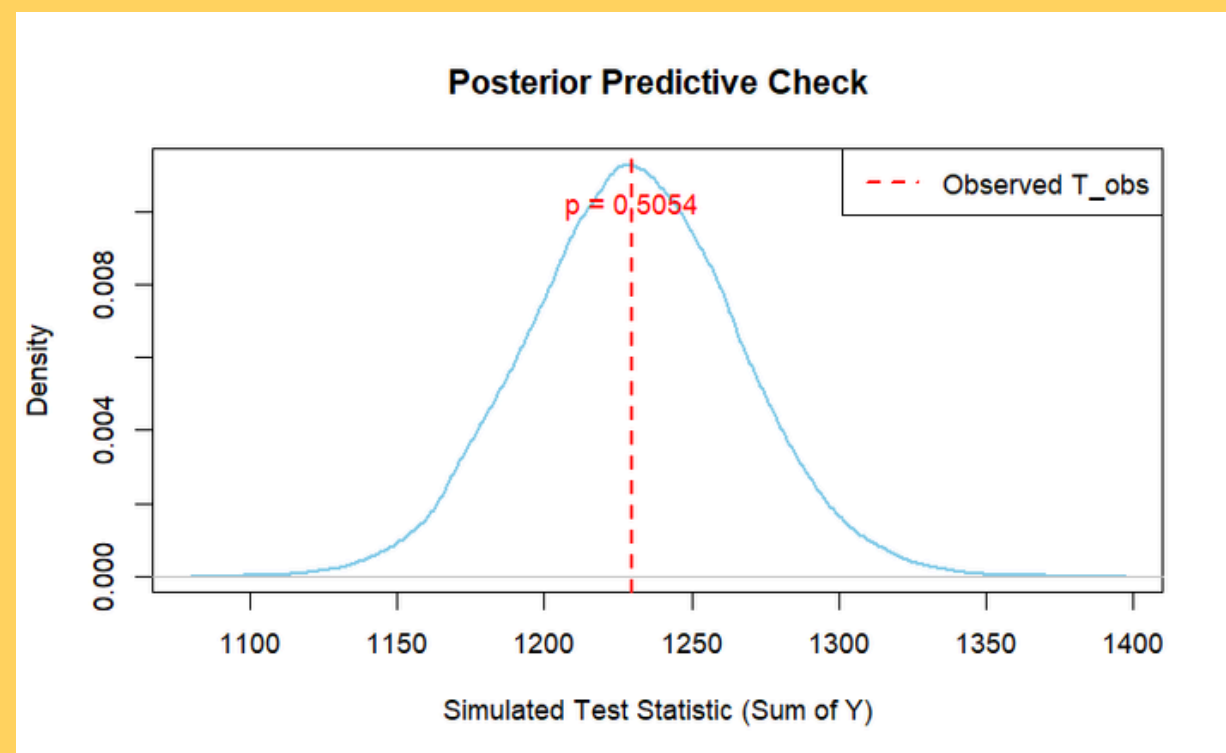
Model 1 is still preferable because has better predictive (higher) and lower overall information criterion (lower)



Posterior Predictive Checks

```
{r}  
T_obs <- sum(Y_obs)  
T_sim <- rowSums(Y_sim)  
p_value <- mean(T_sim >= T_obs)  
print(p_value)
```

```
[1] 0.5054375
```



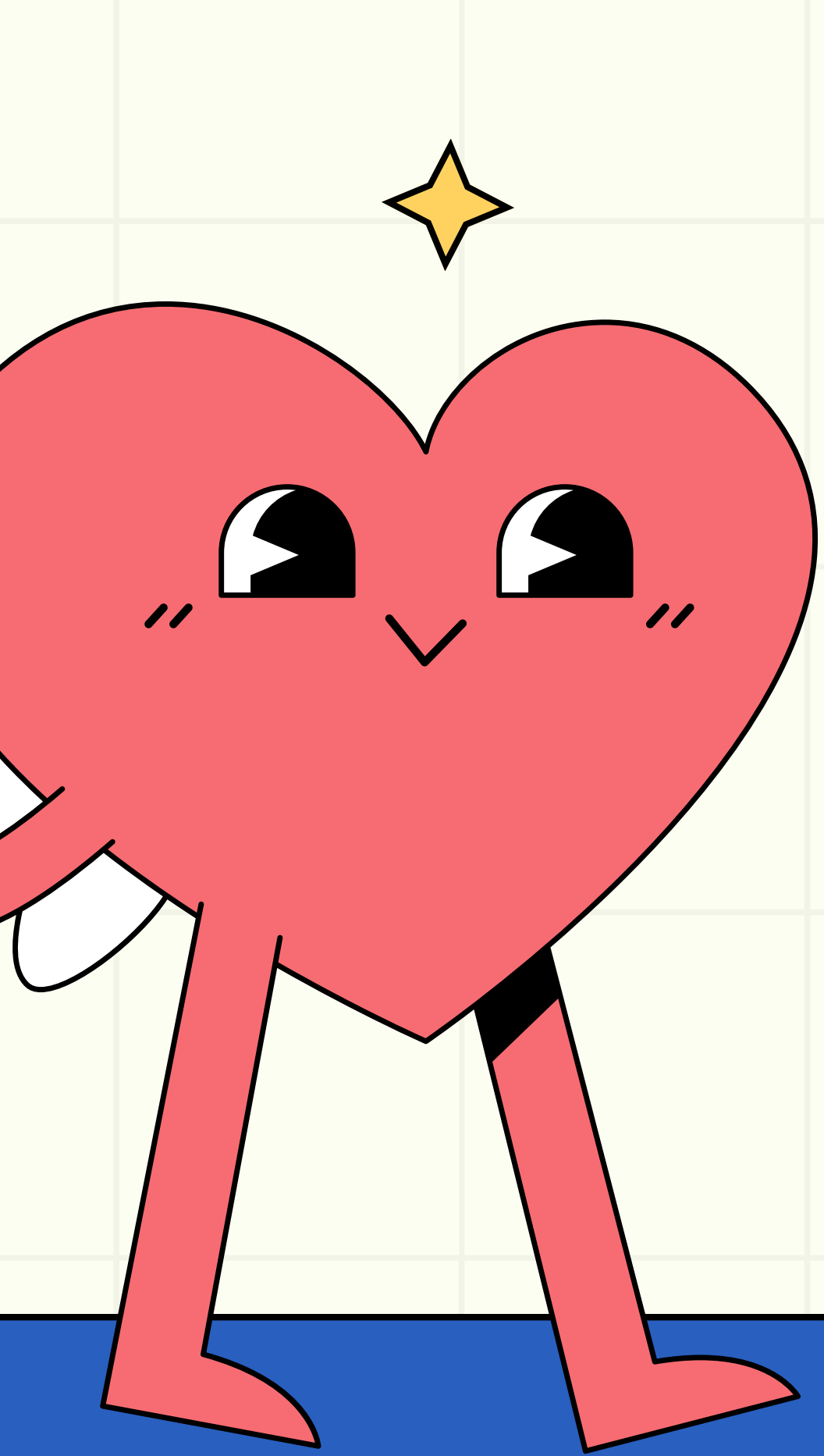
Posterior Predictive Checks

P Value:

The posterior predictive check suggests that the Bayesian logistic regression model provides a good fit to the observed data.

The Bayesian p-value of 0.5054 reflects that about 50.54% of the simulated test statistics are equal to or greater than the observed value

This balance suggests that the model captures the variability in the data well, with no evidence of systematic overestimation or underestimation. Overall, the results indicate that the model is appropriate for describing the observed data.



Thankyou
Very Much

