



# Meta-Analysis with R

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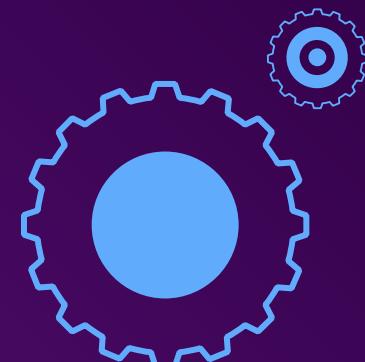
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Multi-Level, Structural Equation,  
Network, and Bayesian Method





01

# Systematic Review

Introduction to Systematic Review and Meta-Analysis

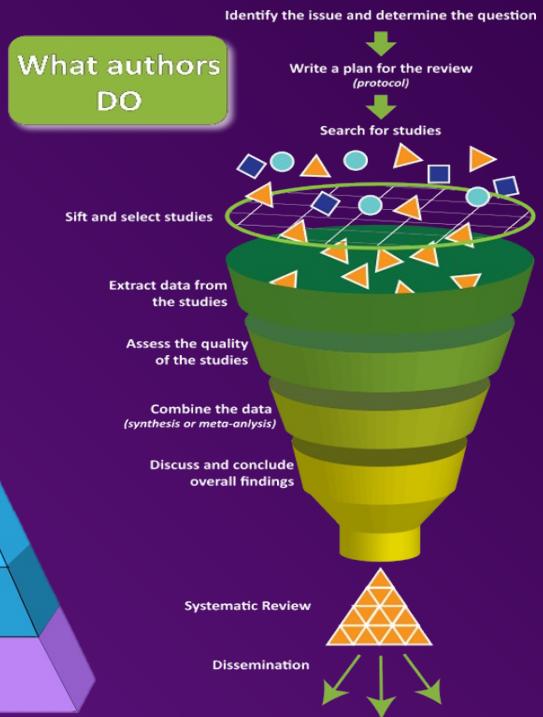




"A systematic review attempts to collate all empirical evidence that fits pre-specified eligibility criteria in order to answer a specific research question. It uses explicit, systematic methods that are selected with a view to minimizing bias, thus providing more reliable findings from which conclusions can be drawn and decisions made."

-Antman 1992, Oxman 1993

# The EBM Pyramid



# 02

## Meta-Analysis

When and How To Conduct Meta-Analysis



# Why To Have a Meta-Analysis



## Inconsistency

Inconsistent results  
between the previously  
conducted studies



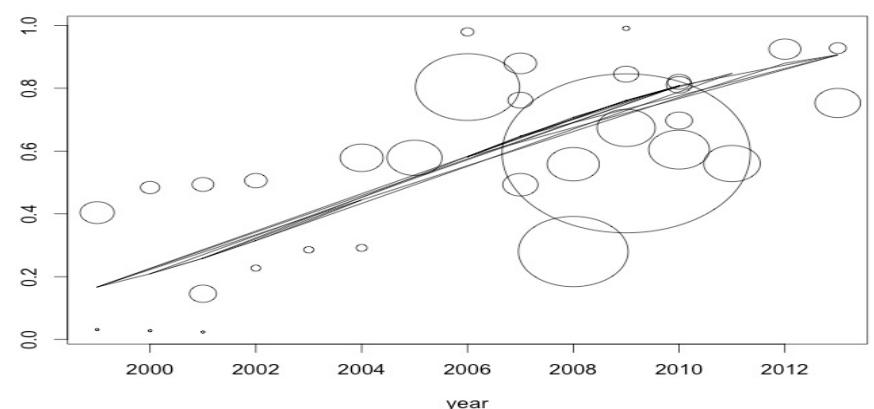
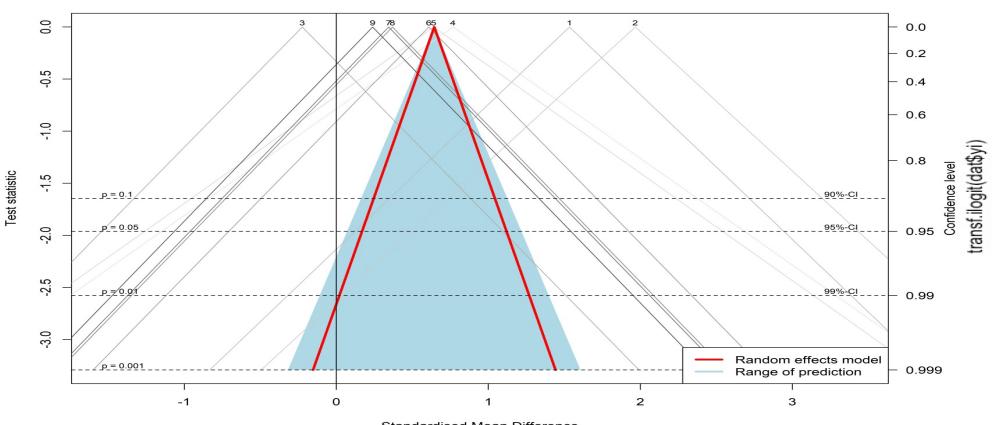
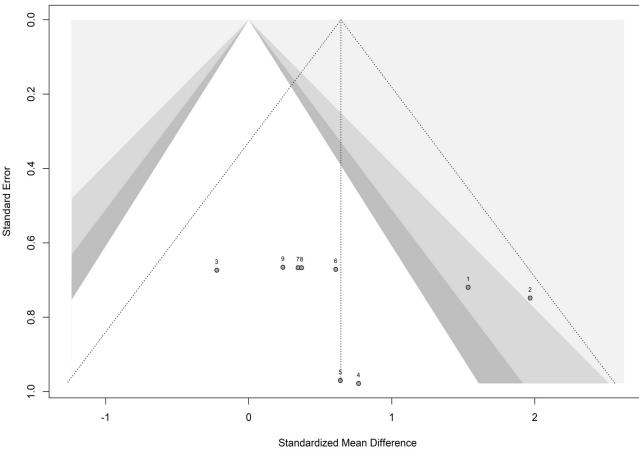
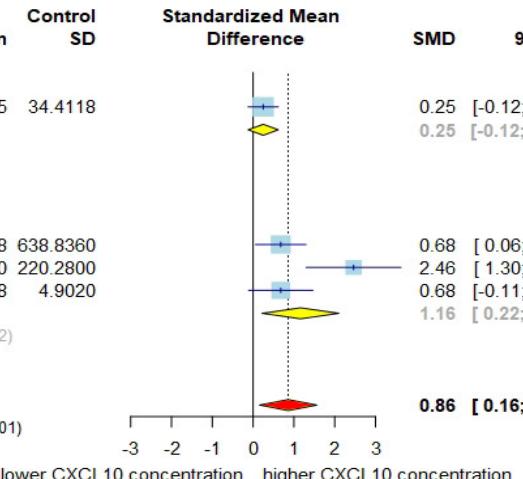
## Better Presentation

Quantitative data helps to present  
the result of the study in a more  
understandable way

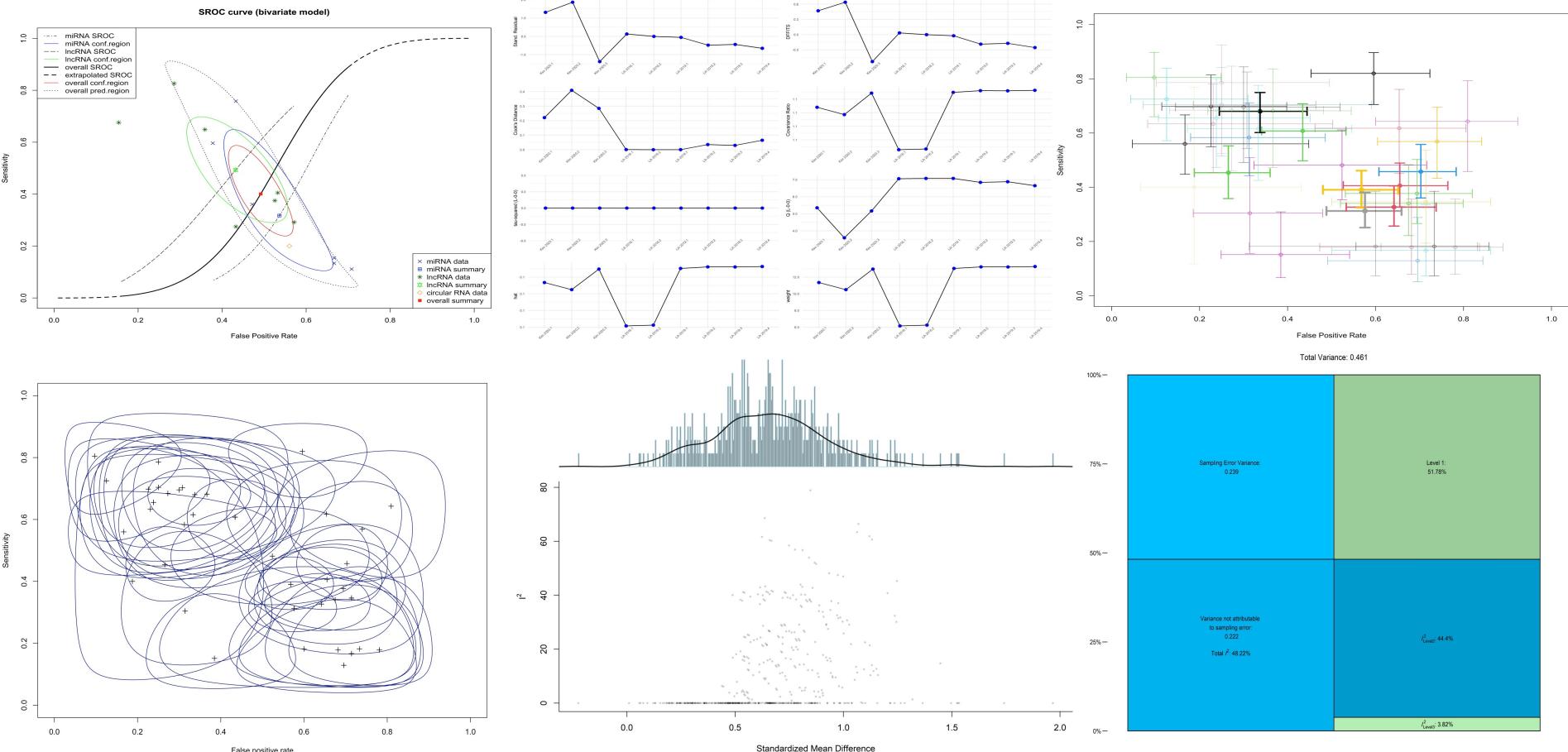


# Some Figures You Usually See When Looking at Meta-Analyses

Study	Experimental						Control	Standardized Mean Difference	SMD	95%-CI	Weight
	Total	Mean	SD	Total	Mean	SD					
<b>autoimmune</b>											
Jiang, X. Y. 2020	147	317.33	1329.83	35	19.75	34.41	118		0.25	[-0.12; 0.62]	31.3%
<b>Random effects model</b>											
Heterogeneity: not applicable	147			35					0.25	[-0.12; 0.62]	31.3%
Test for effect in subgroup: $z = 1.31$ ( $p = 0.19$ )											
<b>infectious</b>											
Maric, L. S. 2018	23	5948.57	10879.91	20	438.38	638.83	60		0.68	[0.06; 1.30]	27.1%
Zajkowska, J. 2011	15	9359.80	4322.54	8	338.00	220.28	00		2.46	[1.30; 3.62]	17.7%
Lepej, S. Z. 2007	19	467.02	802.57	11	9.78	4.90	20		0.68	[-0.11; 1.47]	23.9%
<b>Random effects model</b>											
	57			38					1.16	[0.22; 2.10]	68.7%
Heterogeneity: $\tau^2 = 74\%$ , $\chi^2 = 0.5035$ [0.0450; 34.8551], $\gamma^2 = 7.72$ ( $p = 0.02$ )											
Test for effect in subgroup: $z = 2.41$ ( $p = 0.02$ )											
<b>Random effects model</b>											
	204			73					0.86	[0.16; 1.56]	100.0%
Heterogeneity: $\tau^2 = 77\%$ , $\chi^2 = 0.3747$ [0.0943; 10.2103], $\gamma^2 = 13.25$ ( $p < 0.01$ )											
Test for overall effect: $z = 2.40$ ( $p = 0.02$ )											
Test for subgroup differences: $\gamma^2 = 3.13$ , df = 1 ( $p = 0.08$ )											



# Some Figures You **Cannot** Usually See When Looking at Meta-Analyses



# What is General Idea Behind Meta-Analysis?

It is Weighted Mean of Effect sizes



# Effect Size

the effect size is a measure of the magnitude of the relationship or difference between two groups or conditions. It is used to quantitatively summarize the results of multiple studies and determine whether there is a consistent effect across studies.

# Types of Effect Sizes



## Mean

- Single Group Mean
- Standardized Mean difference
  - Cohen's d
  - Hedges' g
  - Etc.



## Fractions

- Proportions
- Ratios
  - Odds
  - Risk
- Incidence Rate Ratio



## Correlation

- Pearson Correlation
  - Usually is transformed into Fisher's Z





# Brief Insight on Calculation of Effect sizes

## Hedges's SMD

$$d = (M_1 - M_2) / S_{dpooled}$$

$$S_{dpooled} = \sqrt{(SD_1^2 + SD_2^2) / 2}$$

$$g = d * (1 - 3/(4*N-9))$$

## Log Odds Ratio

$$\ln(OR)$$

## Fisher's Z-Transform

$$r = \frac{\sum[(X_i - \bar{x})(Y_i - \bar{y})]}{\sqrt{\sum(X_i - \bar{x})^2} \sqrt{\sum(Y_i - \bar{y})^2}}$$

$$SE(r) = \sqrt{(1 - r^2) / (n - 2)}$$

$$z = 0.5 * \ln[(1 + r) / (1 - r)]$$

$$SE(z) = 1/\sqrt{n-3}$$

# Types of Meta-Analysis



## Fixed-Effect Model



A fixed-effect meta-analysis assumes that all studies included in the analysis share a common true effect size, and any variation in the observed effect sizes is due to sampling error or chance.

## Random-Effect Model

A random-effects meta-analysis, on the other hand, assumes that the true effect size may vary across studies, and any observed differences in effect sizes are due to both sampling error and true variation in the effect sizes across studies.



# Questions



# Whoa!

Let's take a plunge into what we can practically do ...



# 03

## Practice with R

Hands-on Practice on Doing Meta-Analysis with [R](#)

# Four Sample Analyses

	Type	Data	Multiple Groups
Task 1	Percentage	dat.baker2009	✗
Task 2	SMD	SuicidePrevention	✓
Task 3	OR	DepressionMortality	✓
Task 4	Correlation	HealthWellbeing	✗

# Usual Packages for the Meta-Analysis

- ❖ **meta**

A comprehensive package to conduct meta-analysis and present and visualize the results.

- ❖ **metafor**

A thorough package that provide tools to calculate various effect sizes, conduct meta-analysis, and visualize results.

- ❖ **MAd**

A comprehensive package for calculating and converting effect sizes.

- ❖ **rmeta**

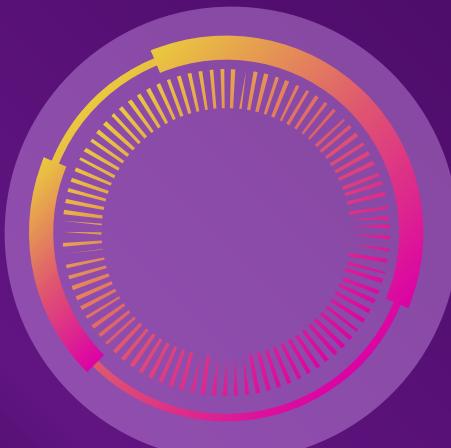
A package that provide tools to visualize meta-analysis results.

- ❖ **dmetar**

Package guide of the “Doing Meta-Analysis in R” book.

- ❖ **netameta**

A package for conducting network meta-analysis.





## How to Calculate Effect Sizes

- `escalc()` function from `metafor` package could be used for calculation of various effect sizes. This function gets the results statistics of studies and `return` the `TE` and `seTE`. Types of given data are:
  - Dichotomous data:
    - RR
    - OR
    - RD
    - AS (*arcsine square root transformed risk difference*)
    - PETO
  - If the data is not dichotomous, but it is a dichotomized version of quantitative data:
    - "PBIT" for the *probit transformed risk difference* as an estimate of the standardized mean difference,
    - "OR2DN" for the *transformed odds ratio* as an estimate of the standardized mean difference (assuming normal distributions),
    - "OR2DL" for the *transformed odds ratio* as an estimate of the standardized mean difference (assuming logistic distributions).



- Quantitative Data:
  - MD
  - SMD
  - "SMDH" for the *standardized mean difference* with heteroscedastic population variances in the two groups (Bonett, 2008, 2009),
  - "SMD1" for the *standardized mean difference* where the mean difference is divided by the standard deviation of the second group (and "SMD1H" for the same but with heteroscedastic population variances),
  - "ROM" for the *log transformed ratio of means* (Hedges et al., 1999; Lajeunesse, 2011).
- Transformed Log odds ratio from SMD:
  - "D2ORN" for the *transformed standardized mean difference* as an estimate of the log odds ratio (assuming normal distributions),
  - "D2ORL" for the *transformed standardized mean difference* as an estimate of the log odds ratio (assuming logistic distributions).
- differences between the two groups with respect to their variability:
  - "CVR" for the *log transformed coefficient of variation ratio*,
  - "VR" for the *log transformed variability ratio*.





- Event Count:
  - "IRR" for the *log incidence rate ratio*,
  - "IRD" for the *incidence rate difference*,
  - "IRSD" for the *square root transformed incidence rate difference*.
  
- Variable Association:
  - "COR" for the *raw correlation coefficient*,
  - "UCOR" for the *raw correlation coefficient* corrected for its slight negative bias (based on equation 2.3 in Olkin & Pratt, 1958),
  - "ZCOR" for *Fisher's r-to-z transformed correlation coefficient* (Fisher, 1921).





# Meta-Analysis Using **meta** package

1. Importing the data
2. Inspecting the data and choosing the effect size
3. Doing the meta-analysis
4. Drawing the forest plot
5. Drawing funnel plot
6. Checking publication bias
7. Sensitivity and influence analysis
8. Trim and fill
9. Gosh plot (**metafor**)



# Meta-Analysis Using **meta** package

1. Importing the data
2. Inspecting the data

```
121 effect <- escalc(measure = "SMD", m1i = mean.e, m2i = mean.c,
122                     sd1i = sd.e, sd2i = sd.c,
123                     n1i = n.e, n2i = n.c, data = df_SMD)
124
125 head(effect)
> head(df_meta)
# A tibble: 6 × 10
  author      n.e mean.e   sd.e   n.c mean.c   sd.c pubyear age_group control
  <chr>     <dbl>  <dbl> <dbl> <dbl>  <dbl> <dbl> <dbl> <chr>    <chr>
1 Berry et al.    90  15.0    3.29    95  15.5    4.41  2006 gen      WLC
2 DeVries et al.   77  16.2    5.35    69  20.1    7.43  2019 older    no intervention
3 Fleming et al.   30  3.01    0.87    30  3.13    1.23  2006 gen      no intervention
4 Hunt & Burke     64  19.3    6.41    65  20.2    7.62  2011 gen      WLC
5 McCarthy et al.  50  4.54    2.75    50  5.61    2.66  1997 gen      WLC
6 Meijer et al.    109 15.1    4.63   111  16.5    5.39  2000 gen      no intervention
```





# Meta-Analysis Using **meta** package

## 3. Doing Meta-Analysis

```
133 meta_model_1 <- metacont(n.e = n.e, mean.e = mean.e, sd.e = sd.e,
134                               n.c = n.c, mean.c = mean.c, sd.c = sd.c,
135                               studlab = author, data = df_meta)
136
137 summary(meta_model_1)
> summary(meta_model_1)
      MD          95%-CI %W(common) %W(random)
Berry et al. -0.5600 [-1.6773;  0.5573]    6.0     11.4
DeVries et al. -3.9200 [-6.0416; -1.7984]   1.7      4.9
Fleming et al. -0.1200 [-0.6591;  0.4191]   25.9     18.7
Hunt & Burke -0.9000 [-3.3285;  1.5285]    1.3      4.0
McCarthy et al. -1.0700 [-2.1305; -0.0095]   6.7     12.0
Meijer et al. -1.3500 [-2.6770; -0.0230]   4.3      9.5
Rivera et al.  0.0200 [-0.5527;  0.5927]   23.0     18.2
Watkins et al. -0.2800 [-0.7764;  0.2164]   30.6     19.2
Zaytsev et al. -1.1700 [-4.5947;  2.2547]   0.6      2.2

Number of studies combined: k = 9
Number of observations: o = 1147

      MD          95%-CI      z p-value
Common effect model -0.3597 [-0.6341; -0.0853] -2.57  0.0102
Random effects model -0.6467 [-1.1774; -0.1159] -2.39  0.0169

Quantifying heterogeneity:
tau^2 = 0.3175 [0.0044; 4.2610]; tau = 0.5635 [0.0662; 2.0642]
I^2 = 54.9% [4.7%; 78.7%]; H = 1.49 [1.02; 2.17]

Test of heterogeneity:
  Q d.f. p-value
17.76   8  0.0231

Details on meta-analytical method:
- Inverse variance method
- Restricted maximum-likelihood estimator for tau^2
- Q-Profile method for confidence interval of tau^2 and tau
```

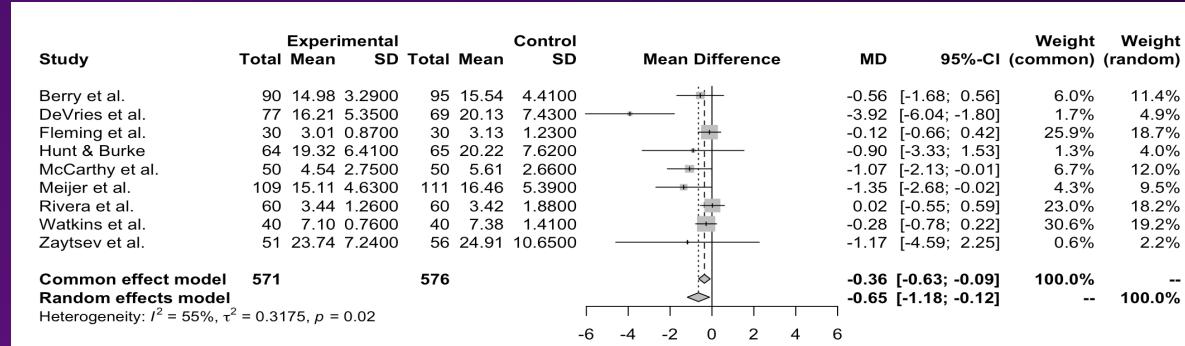




# Meta-Analysis Using **meta** package

## 4. Forest Plot

```
140 | meta::forest(meta_model_1)
```

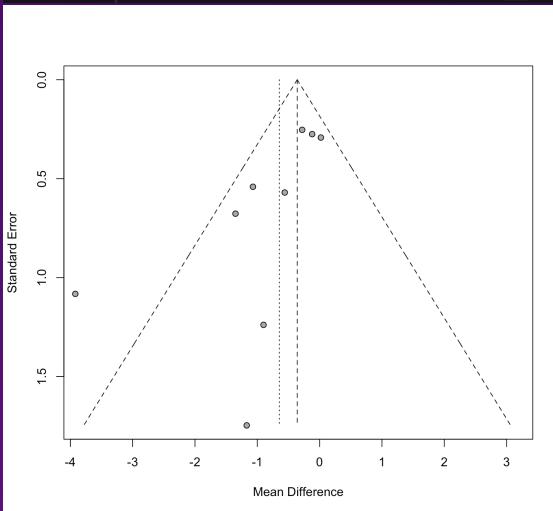




# Meta-Analysis Using **meta** package

## 4. Funnel Plot

```
141 meta::funnel(meta_model_1)
```

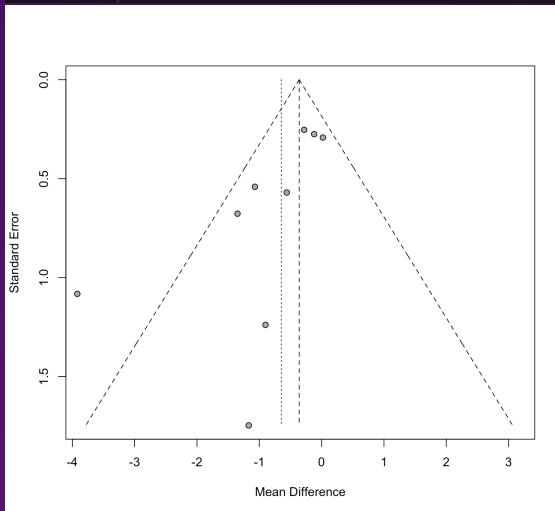




## Meta-Analysis Using **meta** package

### 5. Funnel Plot

```
141 | meta::funnel(meta_model_1)
```





# Meta-Analysis Using **meta** package

## 6. Publication Bias

```
> meta::metabias(meta_model_1)
Warning message:
Number of studies (k=9) too small to test for small study effects (k.min=10). Change argument 'k.min' if appropriate.
145 | meta::metabias(meta_model_1, k.min = 3)
> meta::metabias(meta_model_1, k.min = 3)
Linear regression test of funnel plot asymmetry

Test result: t = -2.95, df = 7, p-value = 0.0215

Sample estimates:
      bias se.bias intercept se.intercept
-2.0352  0.6908    0.3737     0.2901

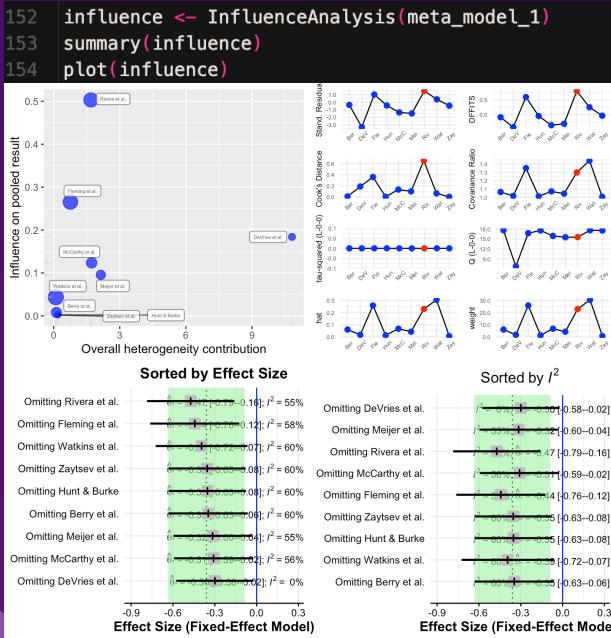
Details:
- multiplicative residual heterogeneity variance ( $\tau^2 = 1.1323$ )
- predictor: standard error
- weight: inverse variance
- reference: Egger et al. (1997), BMJ
```





# Meta-Analysis Using **meta** package

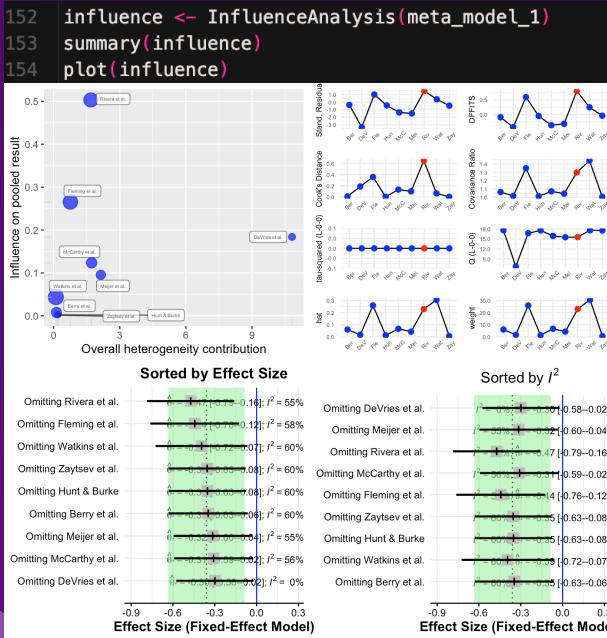
## 7. Influence Analysis





# Meta-Analysis Using **meta** package

## 7. Influence Analysis



# 04

## Advanced Methods

When and How To Conduct Meta-Analysis

Advanced Methods



# References

- Doing meta-analysis with r a hands-on guide, Mathias Harrer
- Discovering Statistics Using R, Andy Field
- Meta-analysis with r, Gerta Rücker, Guido Schwarzer, and James Carpenter
- How to perform a meta-analysis with R: a practical tutorial, Evidence-Based Mental Health, Balduzzi S, Rücker G, Schwarzer G
- onducting meta-analyses in R with the metafor package, Viechtbauer, W.



# THANKS!

Do you have any questions?

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