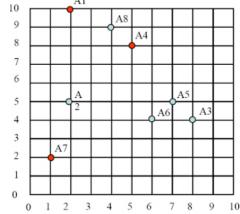
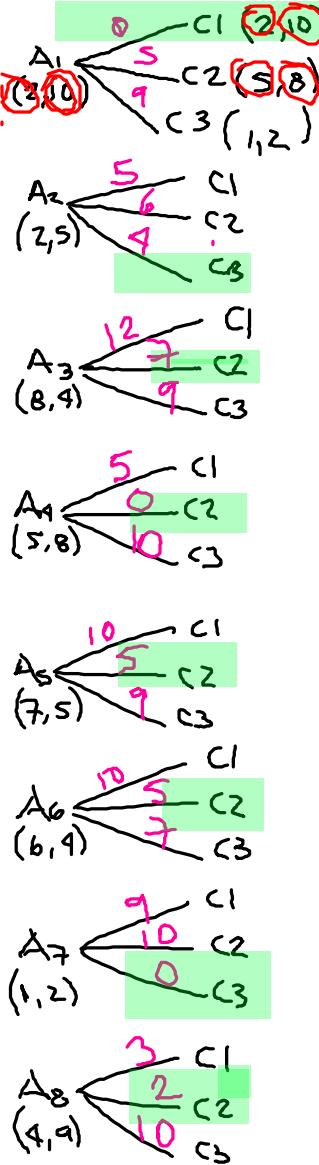


Ejercicio K-Means

- Distancia Manhattan $|x_2 - x_1| + |y_2 - y_1|$
- Centroídes iniciales A_1, A_2, A_4



1er ITERACIÓN



CLUSTERS

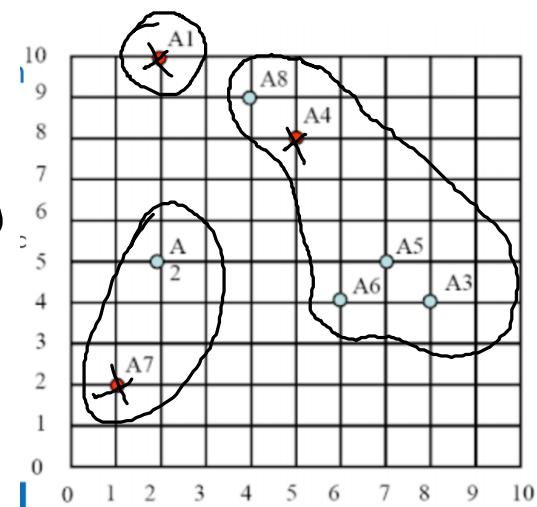
| $C_1(2,10)$ | $C_2(5,8)$ | $C_3(1,2)$ |
|-------------|--|--------------------------|
| $A_1(2,10)$ | $A_3(8,4)$ $A_4(5,8)$ $A_5(7,5)$ $A_6(6,4)$ $A_9(6,9)$ | $A_2(2,5)$ $A_7(1,2)$ |

Recalcular centroides

$$C_1 = \frac{(2,10) + (5,8) + (7,5) + (6,4) + (4,9)}{5} = (6,6)$$

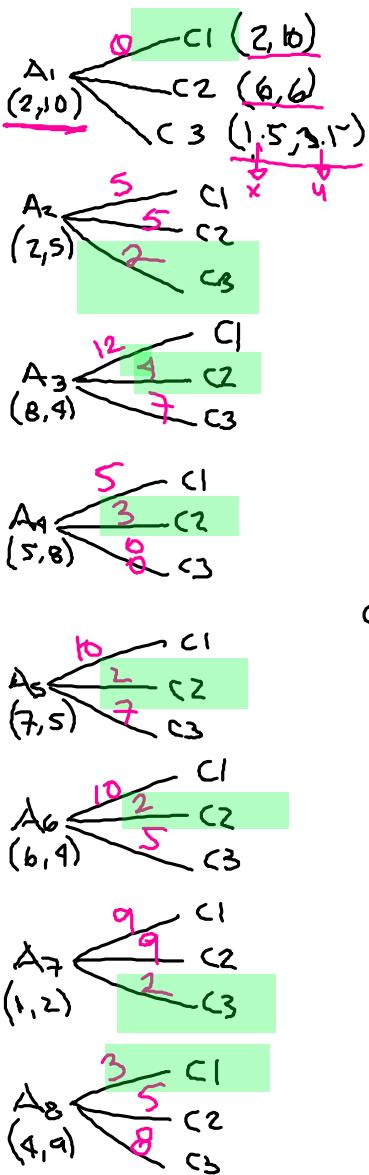
Nuevos centroides

$$C_1 = (2,10)
C_2 = (6,6)
C_3 = (1.5,3.5)$$



2^a ITERACIÓN

CLUSTERS

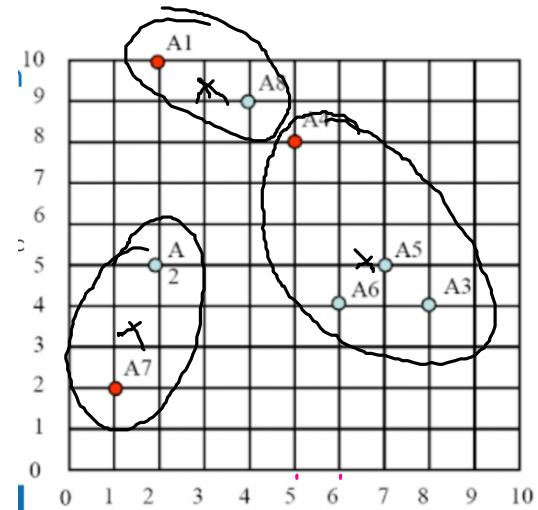


| $C_1(2,10)$ | $C_2(6,6)$ | $C_3(1.5,3.5)$ |
|---------------------------|--|--------------------------|
| $A_1(2,10)$ $A_8(4,9)$ | $A_3(8,4)$ $A_4(5,8)$ $A_5(7,5)$ $A_6(6,4)$ | $A_2(2,5)$ $A_7(1,2)$ |
| | | |

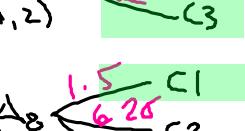
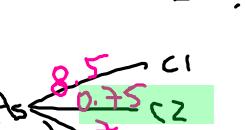
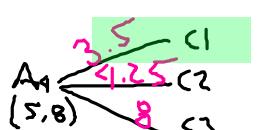
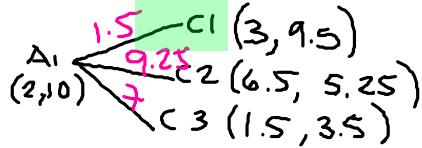
Recalcular centroides

$$\begin{array}{ccc}
 C_1 & C_2 & C_3 \\
 \begin{matrix} (2,10) \\ (4,9) \end{matrix} & \begin{matrix} (8,4) \\ (5,8) \\ (7,5) \\ (6,4) \end{matrix} & \begin{matrix} (1,2) \\ (1,2) \end{matrix} \\
 2\sqrt{(6,19)} = & 4\sqrt{(24,21)} = & 2\sqrt{3.75} = \\
 C_1 = (3,9.5) & C_2 = (6.5,5.25) & C_3 = (1.5,3.5)
 \end{array}$$

Nuevos centroides



3^{ra} ITERACIÓN



CLUSTERS

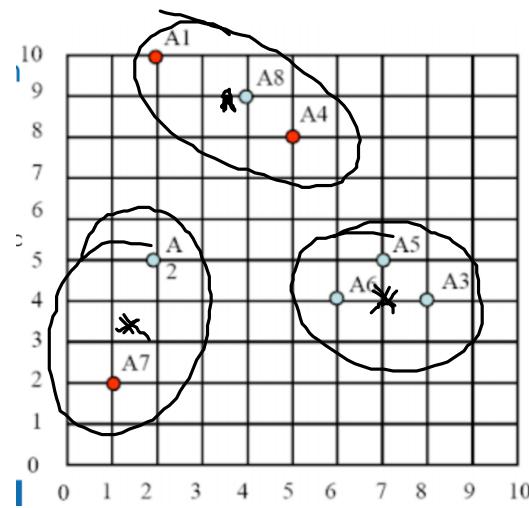
| C ₁ (3,9.5) | C ₂ (6.5,5.25) | C ₃ (1.5,3.5) |
|------------------------|---------------------------|--------------------------|
| A ₁ (2,10) | A ₅ (5,8) | A ₂ (2,5) |
| A ₄ (7,5) | A ₆ (6,4) | A ₇ (1,2) |
| A ₈ (4,9) | | |

Recalcular centroides

$$\begin{array}{l} \text{C}_1 = \frac{(2,10) + (5,8) + (4,9)}{3} = (5,8) \\ \text{C}_2 = \frac{(7,5) + (6,4)}{2} = (6.5,5.25) \\ \text{C}_3 = \frac{(1,2)}{1} = (1.5,3.5) \end{array}$$

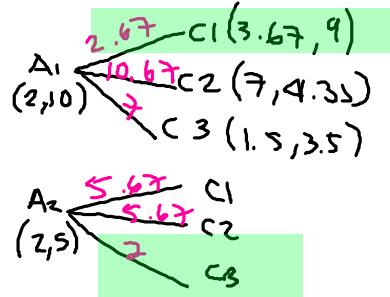
Nuevos centroides

$$\begin{aligned} \text{C}_1 &= (3.67, 9) \\ \text{C}_2 &= (7, 4.33) \\ \text{C}_3 &= (1.5, 3.5) \end{aligned}$$



4ta ITERACIÓN

CLUSTERS



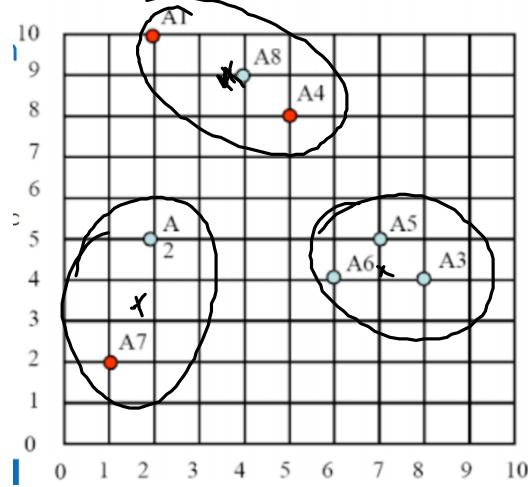
| $C_1(3.67, 9)$ | $C_2(7, 4.33)$ | $C_3(1.5, 3.5)$ |
|----------------|----------------|-----------------|
| $A_1(2,10)$ | $A_3(8,4)$ | $A_2(2,5)$ |
| $A_4(5,8)$ | $A_5(7,5)$ | $A_7(1,2)$ |
| $A_6(6,4)$ | | |

Recalcular centroides

$$\begin{array}{l}
 \begin{array}{c} C_1 \\ (2,10) \\ (5,8) \\ (4,9) \end{array} \\
 \hline
 3 \overline{(11,77)}
 \end{array}
 \quad
 \begin{array}{c} C_2 \\ (8,4) \\ (7,5) \\ (6,9) \end{array} \\
 \hline
 3 \overline{(21,13)}
 \end{array}
 \quad
 \begin{array}{c} C_3 \\ (1,2) \\ (1,2) \end{array} \\
 \hline
 2 \overline{(3,7)}
 \end{array}$$

Nuevos centroides

$$\boxed{
 \begin{aligned}
 C_1 &= (3.67, 9) \\
 C_2 &= (7, 4.33) \\
 C_3 &= (1.5, 3.5)
 \end{aligned}
 }$$

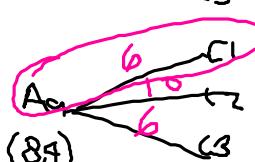
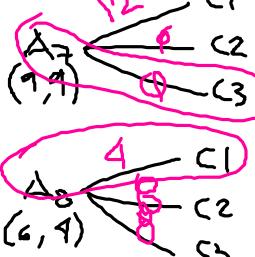
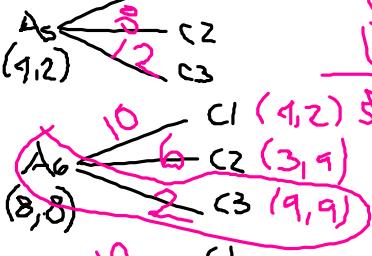
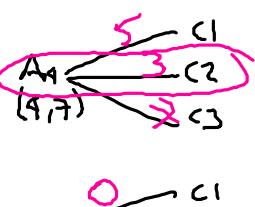
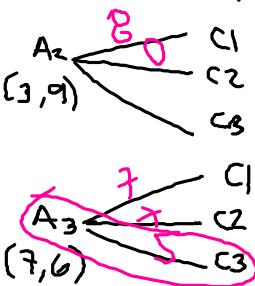
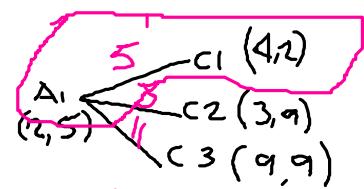


Los nuevos centroides
son iguales a los anteriores,
∴ el alg. termina

SOLUCIÓN EXAMEN 2do PARCIAL

Solución 1

1^{ta} ITERACIÓN



Distancia Manhattan $|x_1 - x_2| + |y_1 - y_2|$

CLUSTERS

| $C_1(4,2)$ | $C_2(3,9)$ | $C_3(9,9)$ |
|----------------|------------|------------|
| $A_1(2,5)$ | $A_2(3,9)$ | $A_3(7,6)$ |
| $A_5(4,2)$ | $A_9(4,7)$ | $A_6(8,8)$ |
| $A_8(6,4)$ | | $A_7(9,9)$ |
| $A_9(8,1)$ | | |
| $A_{10}(7,12)$ | | |

Recalcular centroides

$$\begin{array}{l} C_1 \\ \quad (2,5) \\ \quad (4,2) \\ \quad (6,4) \\ \quad (8,1) \\ \quad (7,12) \end{array} \quad \begin{array}{l} C_2 \\ \quad (3,9) \\ \quad (4,7) \\ \quad (8,8) \\ \quad (9,9) \end{array}$$

$$\frac{2(7,16)}{2} = (3.5, 8)$$

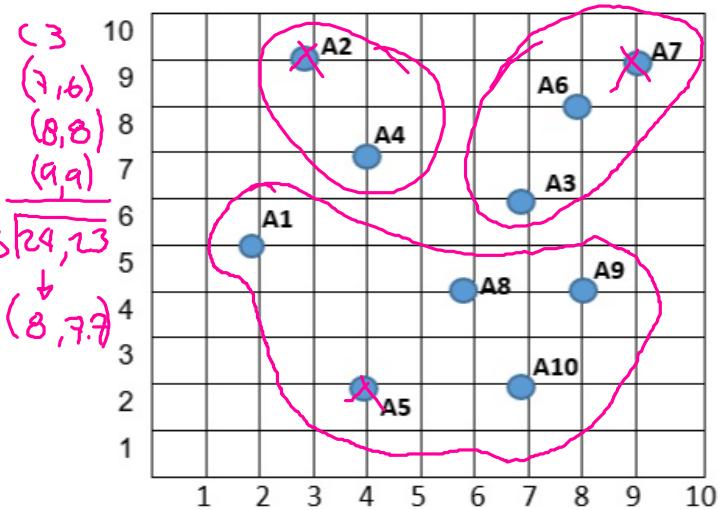
$$\begin{array}{l} C_3 \\ \quad (1,6) \\ \quad (8,8) \\ \quad (9,9) \end{array}$$

$$\frac{3(24,23)}{3} \downarrow (8,7.7)$$

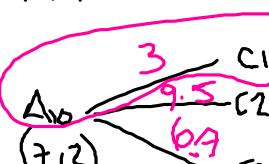
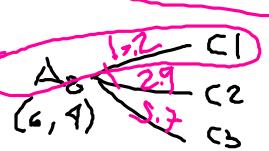
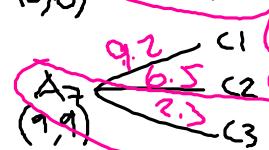
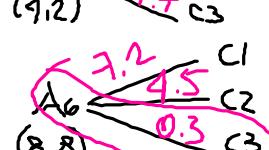
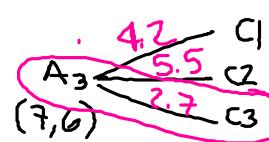
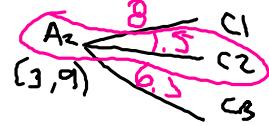
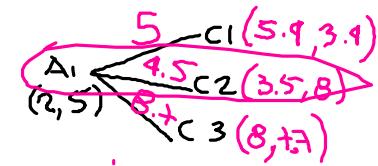
Nuevos centroides

$$C_1(5.4, 3.4)$$

$$C_2(3.5, 8)$$

$$C_3(8, 7.7)$$


2da ITERACIÓN



Distancia Manhattan $|x_1 - x_2| + |y_1 - y_2|$

CLUSTERS

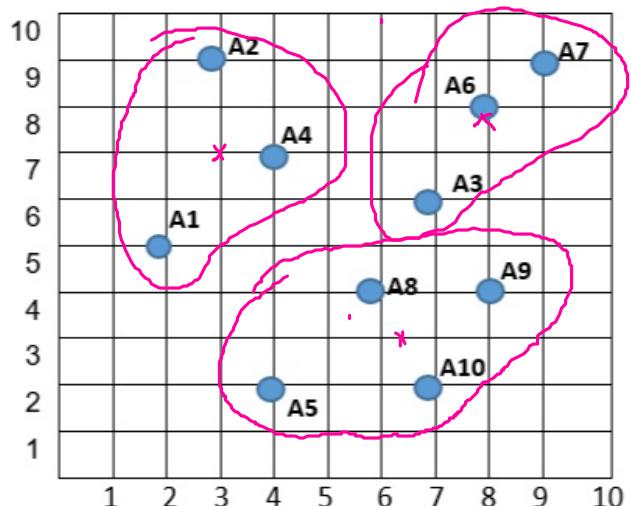
| C ₁ (5.9, 3.9) | C ₂ (3.5, 8) | C ₃ (8, 7.7) |
|---|---|---|
| A ₅ (4, 2) A ₈ (6, 4) A ₉ (8, 1) A ₁₀ (7, 2) | A ₂ (3, 9) A ₁ (4, 7) A ₁ (2, 5) | A ₃ (7, 6) A ₆ (8, 8) A ₇ (9, 9) |

Recalcular centroides

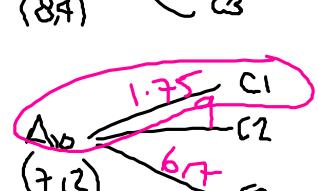
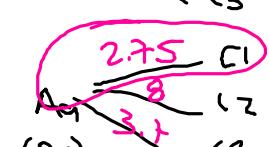
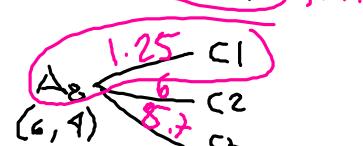
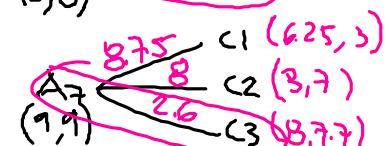
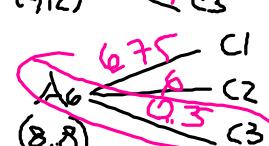
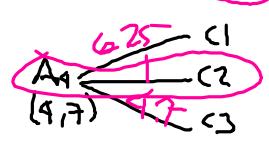
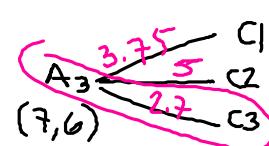
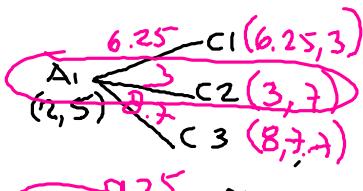
C₁ (6.25, 3)
C₂ (3, 7)

C₃ (8, 7.7)

Nuevos centroides



3^a ITERACIÓN



\downarrow Termina

Distancia Manhattan $|x_1 - x_2| + |y_1 - y_2|$

CLUSTERS

| $C_1(6.25, 3)$ | $C_2(3, 7)$ | $C_3(8, 7.7)$ |
|----------------|----------------|----------------|
| $A_1(2, 5)$ | $A_4(4, 2)$ | $A_3(7, 6)$ |
| $A_2(3, 9)$ | $A_5(6, 9)$ | $A_6(7, 7)$ |
| $A_3(7, 6)$ | $A_7(9, 7)$ | $A_8(8, 4)$ |
| $A_4(9, 7)$ | $A_{12}(4, 2)$ | $A_{13}(7, 7)$ |
| $A_5(6, 9)$ | $A_{14}(6, 9)$ | $A_{15}(8, 8)$ |
| $A_6(7, 7)$ | $A_{16}(9, 7)$ | $A_{17}(8, 4)$ |
| $A_7(9, 7)$ | $A_{18}(7, 7)$ | $A_{19}(8, 8)$ |
| $A_8(8, 4)$ | $A_{20}(6, 9)$ | $A_{21}(8, 8)$ |
| $A_9(8, 8)$ | | |
| $A_{10}(7, 6)$ | | |
| $A_{11}(9, 9)$ | | |

Recalcular centroides

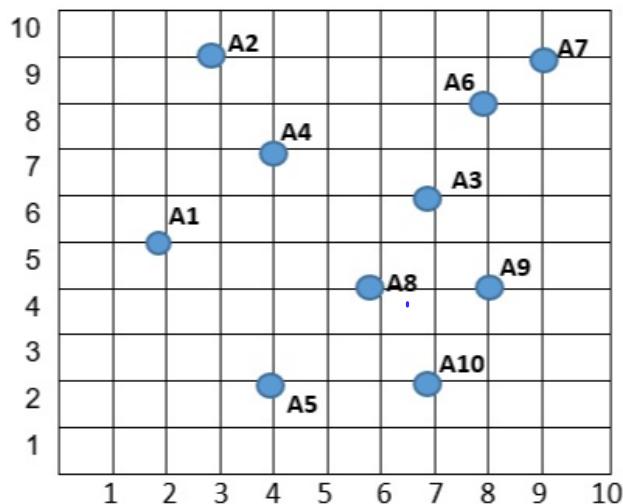
$$C_1 \overline{6.25, 3} \quad C_2 \overline{3, 7} \quad C_3 \overline{8, 7.7}$$

Nuevos centroides

$$C_1 \rightarrow (6.25, 3)$$

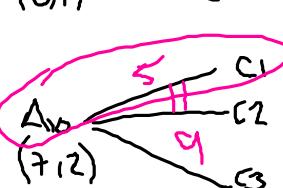
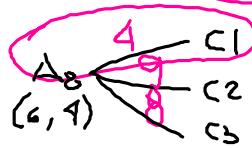
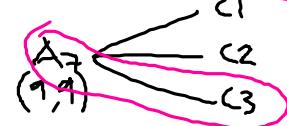
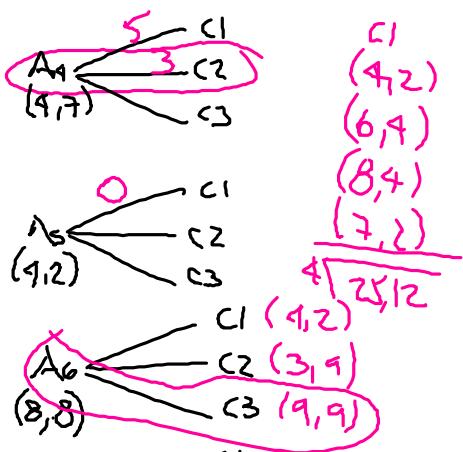
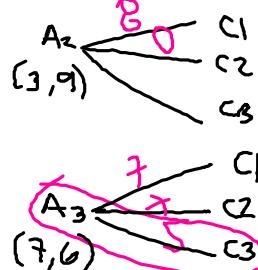
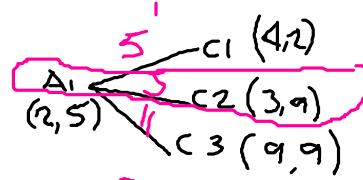
$$C_2 \rightarrow (3, 7)$$

$$C_3 \rightarrow (8, 7.7)$$



Solución 2

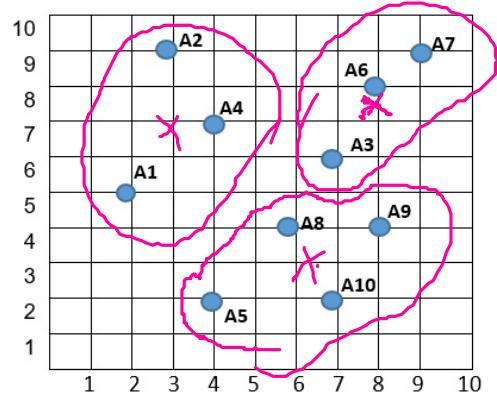
1^{ra} ITERACIÓN



Distancia Manhattan $|x_1 - x_2| + |y_1 - y_2|$

| $C_1(4,2)$ | $C_2(3,9)$ | $C_3(9,9)$ |
|---------------|------------|------------|
| , | $A_2(3,9)$ | $A_3(7,6)$ |
| $A_5(4,2)$ | $A_9(4,7)$ | $A_6(8,8)$ |
| $A_8(6,4)$ | $A_7(2,5)$ | $A_8(9,9)$ |
| $A_9(8,4)$ | | |
| $A_{10}(7,2)$ | | |

$$\begin{array}{l} C_3 \\ (1,6) \\ (8,8) \\ (9,9) \\ \hline 3 \sqrt{24,23} \\ (8,7,7) \end{array}$$



$C_1(4,2)$, $C_2(3,9)$, $C_3(8,7,7)$

Nuevos Centroides

2^{da} ITERACIÓN

Distancia Manhattan $|x_1 - x_2| + |y_1 - y_2|$

CLUSTERS

| C1 (6.25, 3) | C2 (3, 7) | C3 (8, 7.7) |
|------------------------|-----------------------|-----------------------|
| A ₅ (1, 2) | A ₁ (2, 5) | A ₃ (7, 6) |
| A ₈ (6, 4) | A ₂ (3, 9) | A ₆ (8, 8) |
| A ₁₀ (7, 2) | A ₄ (4, 7) | A ₇ (9, 9) |
| A ₉ (8, 4) | | |

Recalcular centroides

$$\begin{array}{l} C_1 \\ \hline 4 \sqrt{25, 12} \\ C_2 \\ \hline 3 \sqrt{9, 21} \\ C_3 \\ \hline 3 \sqrt{24, 23} \end{array}$$

Nuevos centroides

$$C_1 \rightarrow (6.25, 3)$$

$$C_2 \rightarrow (3, 7)$$

$$C_3 \rightarrow (8, 7.7)$$

↓ Termina

