

Text Analytics of the Qur'ān using Statistical and Large Language Models

by

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Contents

Title Page	1
1 Introduction	6
1.1 Background	6
1.2 Rationale of the Study	12
1.3 Objectives	15
1.4 Significance of the Study	15
1.5 Scope of the Study	15
1.6 Thesis Organization	16
2 Literature Review	17
3 Background on Probability and Statistics	20
3.1 Descriptive Statistics	20
3.2 Probability Theory	21
3.3 Statistical Graphs	28
3.3.1 Box, Density, and Histogram Plots	28
4 Methodology	30
4.1 Topic Modeling	30
4.1.1 Latent Dirichlet Allocation	30
4.1.2 Large Language Models	30
4.2 Retrieval-Augmented Generation	31
4.3 Julia Code Setup	31
4.4 Python Code Setup	31
5 Results and Discussions	32
5.1 Descriptive Statistics	32
5.1.1 Verses	34

5.2 Morphological Analysis	34
5.3 Structural Analysis	34
5.3.1 Concentric Structure	34
5.3.2 Mathematical Structure	34
5.3.3 Discussions on Islamic Philosophy of Qur’ān’s Structural Analysis	34
5.4 Topic Modeling	35
5.4.1 Latent Dirichlet Allocation	35
5.4.2 Bidirectional Encoder Representation from Transformer	35
5.4.3 Generative Pre-Trained Transformer	35
5.5 Relating to other Islamic Texts and Analyses	35
5.5.1 Retrieval-Augmented Generation Approach	35
5.6 Limitations of the Models	35
6 Conclusion and Recommendation	36
References	37

List of Figures

1.1	Statistics of the words and <i>ayāt</i> آيات (verses) of the Qur'ān	7
1.2	20th Century Qur'ān (left) in its fully featured orthographies vs Birmingham Qur'ān dated between 568 and 645 CE (right) in its basic consonantal skeleton. Image from Wikipedia (2015).	10
3.1	Statistics of the words and <i>ayāt</i> آيات (verses) of the Qur'ān	29
5.1	Statistics of the words and <i>ayāt</i> آيات (verses) of the Qur'ān	33
5.2	Statistics of the words and <i>ayāt</i> آيات (verses) of the Qur'ān according to revelation order	34

Abstract

The interest of the paper is to provide a comprehensive text analytics of the Qur'an. This is by utilizing Statistical and Machine Learning methods to computationally analyze the said scripture. Specifically, the following procedures have been done: descriptive analyses of the structure of the Qur'an, morphological analyses of the Qur'an. Further, the data used for the Qur'anic Arabic corpus is the one in QuranTree.jl by Asaad (2022). The computational software used is Julia programming language.

Chapter 1

Introduction

The use of scientific computing to studying the Qur'ān is still in its early stage in the fields of Islamic Studies and Statistical and Machine Learning applications. This study will indeed benefit not only researchers from Islamic Studies but also Statisticians and Machine Learning researchers who are into text analytics. Having said that, it is therefore necessary to provide context to audiences of these disciplines to provide background on the state of Qur'ānic studies and the increasing adoption of scientific methodology to studying humanities.

1.1 Background

The Qur'ān or *al-qur'ān* القرآن meaning *the recitation*, the holy book of Islam, is revered by 1.9 billion (according to 2020 projection of Cooperman et al. (2011, p. 13)) Muslims across the globe as the literal words of God. Muslims believed that the Qur'ān was gradually revealed (Qur'ān 25:32) to Prophet Muhammad ﷺ through angel ḡibrīl جبريل or Gabriel (Qur'ān 2:97). The Qur'ān contains 77,429 Arabic words in total, which covers only 56 percent of the Greek New Testament which has 138,020 words in total (Sinai, 2017, p. 11).

The Qur'ān is divided into *sūrahs* سور which are the equivalent of chapters, each containing *ayāt* آيات (meaning *signs*), which are the equivalent of verses. The *sūrahs* سور are not arranged in chronological order as in the Bible's books and chapters, but rather arranged in monotonically decreasing length of number of verses after the first *sūrah* سورة (see Figure 1.1). The *sūrah* سورة of the Qur'ān can be categorized into two types: the *makkīyya* مكية (Meccan) and *madaniyya* مدانية (Medinan). The categories refer to the geographical location of where the *sūrah* سورة was revealed. Figure 1.1 shows the grouping of the *sūrahs* سور. Note that some of the *sūrahs* سور have mixed geographical locations¹, that is, a few of the *ayāt* آيات in it were revealed in

¹see list of the location in https://tanzil.net/docs/revelation_order

other geographical location apart from the geographical location of the rest of the *ayāt* آيات. Therefore, the categorization in Figure 1.1 highlights the geographical location of the majority of the *ayāt* آيات in the *sūrah* سورة.

The Qur'ān (meaning *the recitation*) was revealed *orally* by angel *ġibrīl* جبريل to Prophet Muhammad ﷺ and passed onto other believers through oral tradition (reciting the Qur'ān to students repeatedly so as to memorize it, instead of writing it down and let the believers read it and memorize it). Memorizing 77,429 Arabic words of the Qur'ān through oral transmission can be a difficult task, but what aids this memorization is the rhythm feature of the Qur'ān. According to one Orientalist, Sinai (2017), "rhyme, however, or rather a periodically recurrent word-final assonance, is a feature of the Qur'ān throughout, and it naturally partitions the

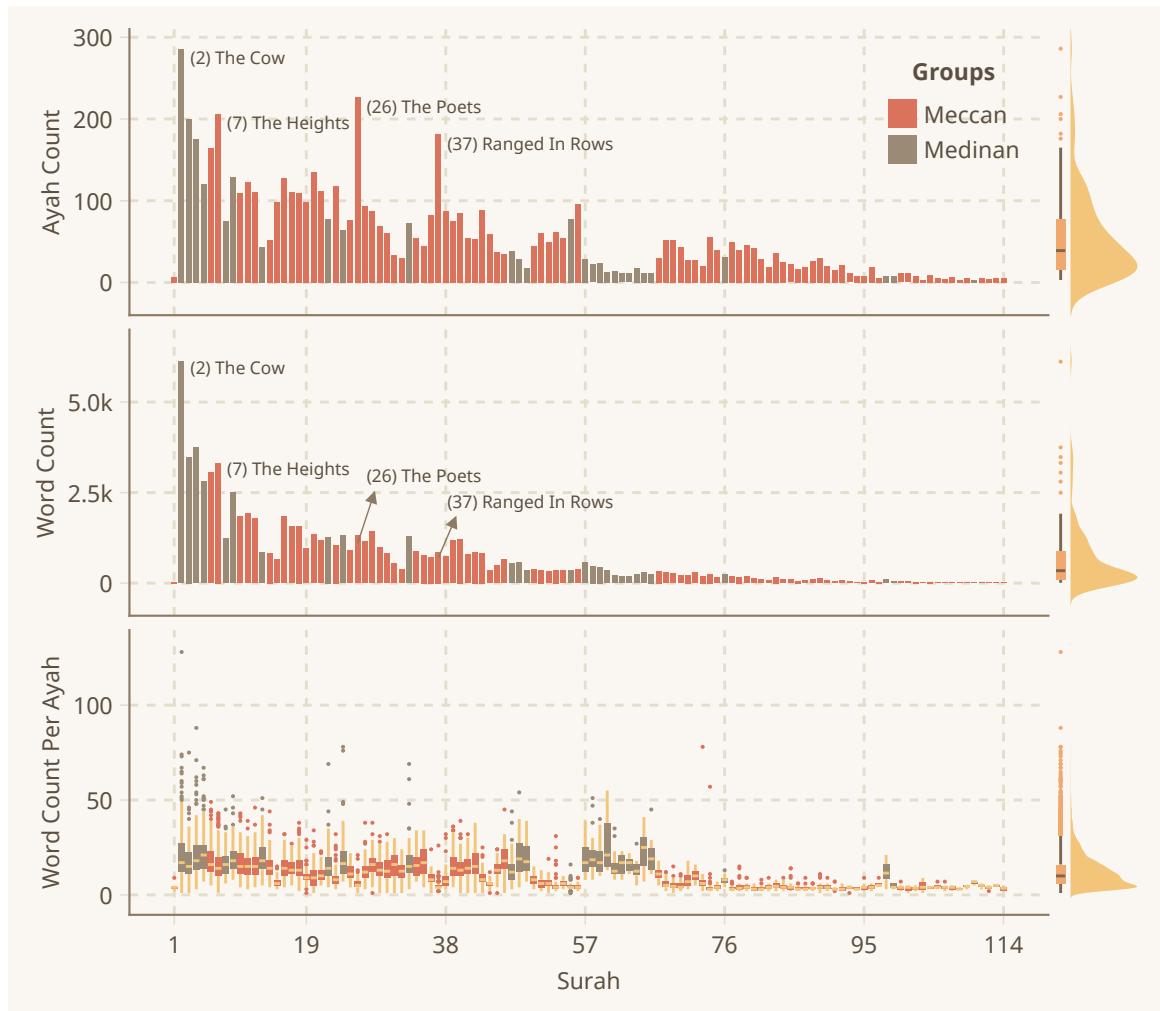


Figure 1.1: Statistics of the words and *ayāt* آيات (verses) of the Qur'ān

sūrah سُورَةٌ." Indeed, because of this feature, it makes it easy to memorize the entire Qur'ān, and the one who do so is called *hafiz* حَفِظْ meaning *one who remembers* or *keeper*. Qur'ān memorization contest is a common event in Muslim countries, the Philippine embassy has hosted one in 2022 in Saudi Arabia (Manila Bulletin, 2022).

According to the Muslim tradition, the oral transmission of passing the Qur'ān from a *hafiz* حَفِظْ to new believers was gradually put into writings as requested by the believers themselves. The idea was brought up after the battle of Yamama, where many of the Muslims who died were *qurrā'* قُرَّاءٌ (*the one who properly recite the Qur'ān*), and so fearing that their numbers will reduce in other battle fields, Umar ibn al-Khattab عمر بن الخطاب (who became the second caliph) suggested to the first caliph, Abū Bakr 'Abd Allāh ibn 'Abī Quhāfa, أبو بكر عبد الله بن أبي قحافة or short for Abū Bakr أبو بكر, to collect the Qur'ān into writing. Abū Bakr then authorized Zaid ibn Thabit زيد بن ثابت for the task. According to Zaid, he started collecting from the leafless stalks of the date-palm tree and from the pieces of leather and hides and from the stones, and from the chests of men (who had memorized the Qur'ān, i.e. the *hafiz* حَفِظْ)². Long story short, the effort was finally codified by the third caliph, Uthman ibn Affan عُثْمَانُ بْنُ عَفَّانَ in the year 645 CE, which was then recopied and distributed to the different regional capitals of the early Islamic empire of that time. The rest of the copies outside this codification were then burned³ down in order to have one standard Qur'ān. The Qur'ān nowadays is therefore assumed to be based on Uthmanic codex because of the story mentioned. That is, if indeed Uthman has ordered to burn other copies of the Qur'ān outside his codification, then what's left should only be based on his codex or archetype, and that should only be the inherited codex of the Muslims today.

The Qur'ān is believed by the Muslims to have been preserved since it was first recited by angel *gibril* جَبْرِيلْ or Gabriel to the Prophet ﷺ. Many orientalists had been skeptic about this claim, for example, John Wansbrough theorized that the Qur'ān was collected over a 200-year period (see Wansbrough, 2004, p. 101) after the death

²see <https://sunnah.com/bukhari:7191>

³see <https://sunnah.com/bukhari:4987>

of the Prophet ﷺ, instead of within a few years after the death of the Prophet ﷺ. However, recent findings through radiocarbon dating brings forward strong evidence of potential preservation of the whole Qur’ān, which the Muslims believed to be so. For example, the Birmingham Qur’ān manuscript discovered in 2015 is dated to be between 568 and 645 CE with 94.5% accuracy, making it among the oldest Qur’ānic manuscript in the world (see Birmingham University, 2015). Its predicted range of years intersects with the lifetime (570 to 632 CE) of the Prophet ﷺ. What is interesting is that the Birmingham Qur’ān is consistent with the Qur’ān today, word-by-word and letter-by-letter⁴, see Figure 1.2. This is indeed another evidence that the Qur’ān today was codified by Uthman since the discovery of the Birmingham Qur’ān manuscripts have confirm it. In addition to this, the Sana'a Palimpsest is also among the oldest Qur’ān radiocarbon dated to be between 578 CE and 669 CE with 95% accuracy (Sadeghi & Bergmann, 2010), which according to Sinai (2017), "neither does the edited portion of the Sana'a palimpsest offer evidence for additional or missing verses or for a divergent verse order within the *sūrahs* سور." Given these discoveries on the recent Quranic manuscripts, the claim of Wansbrough (2004, p. 101) is now untenable (see Sinai, 2014).

One likely reason as to why the scribes were able to preserve the Qur’ān in the two folios of the Birmingham Qur’ān manuscripts follows from the fact that the Qur’ān is firstly memorized before it was decided to be written. So that, the Topkapi manuscripts that contain 99% (only 23 verses missing)—dated around 701 to 750 CE (Karatay, 1962)⁵, that is, around 69 to 118 years after the death of the Prophet ﷺ—of the Qur’ān today was likely partly written from memory. This is possible since the Qur’ān possesses a rhythmic feature (that aids with memorization) that naturally divides its verses or *ayāt* آيات, and that the Qur’ān memorization competition is still held to this day (as in the example of Manila Bulletin, 2022), apart from

⁴The orthography of the Arabic letters in the early days had no diacritics and were written in its basic consonantal skeleton. That is, Arabic orthography and grammar were in their nascent when the Qur’ān was revealed, and therefore has to adjust and catch up, to capture and preserve the proper recitation of the Qur’ān.

⁵see also <https://corpuscoranicum.de/en/manuscripts/1977/page/1-410?sura=1&verse=1>

the fact that it needs to be recited (any chapter after the first chapter of the Qur'ān according to the choice of the worshipper) every prayer from memory. Bottomline, there are many avenues for Qur'ān recitation from memory, and these have helped in its preservation. Moreover, since there are no significant evidence of insertion or malicious intention on addition or revision in all of the extant Qur'ānic manuscripts so far, some Orientalists came up with other theories of insertions on the basis of the literary style of the Qur'ān, see for example Sinai (2017, p. 92), where verse 102 of *sūra l-sāffāt* سُورَةِ الصَّافَاتِ or The Chapter of *Ranged in Rows* is theorized as addition because it is longer compared to other verses in the said chapter, refer to Sinai (2017, p. 92) for his other reasonings. Nonetheless, the Qur'ān is indeed stable based on the extant manuscripts.

Furthermore, the vastness of the early Islamic empire meant that different Mus-



Figure 1.2: 20th Century Qur'ān (left) in its fully featured orthographies vs Birmingham Qur'ān dated between 568 and 645 CE (right) in its basic consonantal skeleton. Image from Wikipedia (2015).

lim regional capitals have covered populations with different Arabic dialects, and so to accommodate these differences, Muslims believed that there were seven variant readings of the Uthmanic codex. Variant readings are defined as different pronunciations of the same word, in this case seven Uthamnic Qur'ān for seven different pronunciations. The *hadīt* حَدِيثٌ or *narration* comes from Ubayy ibn Ka'b who reported⁶ that the Prophet ﷺ was near the tank of Banu Ghifar that ḡibrīl جِبْرِيلٌ or Gabriel came to him and said: "... Allah has commanded you to recite the Qur'ān to your people in *seven dialects*, and in whichever dialect they would recite, they would be right." Recent work of Sidky (2020) shows that the material evidence on the regional variants is in remarkable agreement with well-attested written variants documented in the traditional Muslim literature.

Muslim and non-Muslim scholars alike have been extremely interested in understanding the unique literary characteristics of the Qur'ān. As mentioned earlier, unlike other books like the Bible (arranged in chronological order), the Qur'ān does not follow any obvious organization. In addition to this, a *sūrah* سُورَةٌ does not fit the exact definition of a chapter. Indeed, the name attached to a *sūrah* سُورَةٌ is often decided as the unique entity mentioned in the said *sūrah* سُورَةٌ, its main purpose is to help early Muslims distinguish which *sūrah* سُورَةٌ they are talking about, this is contrary to the chapter name where the associated name is obviously the main topic of the chapter. Further, as described by Sinai (2017), "... the compositional unity of the long surahs located at the beginning of the corpus is anything but obvious: at least at first sight, they can appear a flit back and forth between different topics in a largely haphazard manner. This impression is not limited to Western readers: even pre-modern Muslim scholars have often approached their scripture as a quarry of unconnected verses and groups of verses that bear little intrinsic relation to what precedes and follows." It wasn't until Neuwirth (2007), that the compositional unity of the Qur'ān can be observed in tighter literary unities, as Neuwirth (2007) showed that the many of these texts display a tripartite structure and are often constructive

⁶source: <https://sunnah.com/muslim:821a>

around a narrative middle part (Sinai, 2017). Samples of the organizational style of the Qur’ān was shown in Sinai (2017, p. 88).

1.2 Rationale of the Study

Attempts at understanding the Qur’ān by Qur’ānic scholars were mostly done with the use of manual processes, that is, studying the scriptures by going through its content one-at-a-time manually. However, with the advent of computers, some researchers have started using it to aid in their study. The first known to have used computers for studying the Qur’ān was likely Rashad Khalifa in 1968⁷, where he studied the significance of the mysterious initials at the beginning of some *sūrāhs* سور. Rashad uploaded the Qur’ān into his computer by transliterating the Arabic letters and other Qur’ānic orthographies into Roman letters and symbols that the computer can easily parse. This approach of using computers to find new insights is more common in the field of science, and it was new to the field of Qur’ānic studies.

Indeed, to proceed with the use of scientific computing, the Qur’ān will be treated as the data that needs to be analyzed using what is called Natural Language Processing (NLP), a branch of Machine Learning (ML) that aims to understand natural languages, such as Arabic. To instruct the computer to do Statistical analyses, ML, or NLP, one needs to use a *software application* or a formal language called *programming language*. There are several programming languages that the computer can understand. The popular one for researchers in the field of sciences are Python, R, and sometimes Julia (Bezanson et al., 2017). These programming languages will be used to construct instructions for computer. Therefore, if the data is the Qur’ān, then there should be a way to interface with it using any of these programming languages. Or alternatively, there should be a way to upload it into the chosen programming language and encode the Arabic letters into something that can be easily parsed by the computer, like what Rashad Khalifa did. Having said that, there are indeed some programming languages with libraries or packages for

⁷see https://www.masjidtucson.org/quran/miracle/a_profound_miracle_sura68nun133.html

interfacing with the Qur’ān, and this is true for Python, R, and Julia. For this study, Julia programming language since its library for interfacing the Qur’ān using the QuranTree.jl⁸ has more features compared to those available in R and Python (see Asaad, 2021). QuranTree.jl is based on Tanzil⁹ for the Qur’ānic Arabic texts, and Dukes and Habash (2010) for morphological annotation, which both libraries from R and Python do not have in terms of morphological annotation from Dukes and Habash (2010).

Now that the programming language for this paper is identified, next is to understand how Statistics and Machine Learning can help in studying the Qur’ān. Statistics is a branch of Science that aims to study features or characteristics of data generated from a random phenomenon. The findings of Statistical analyses can then be used to make conclusions or predictions of the general population of the data or general characteristics of the data. Machine Learning or ML, on the other hand, is a branch of Artificial Intelligence that heavily intersects with Statistics, albeit with distinct differences as well. Both Statistics and ML aims to characterize data by learning its features, but ML research aims on complex models that are often inspired by simpler models from Statistics. Therefore, one can think of Statistics as one of the fundamentals of ML.

One of the goals of Statistics and Machine Learning is to summarize all of the learned features into a hypothesized equation or hypothesized mathematical formula whose parameters or weights are optimized to capture the most characteristics of the data. It is called hypothesized equation since the researcher is the one who decide which family of equation best describe the characteristics of the data. The said equation is called a *model*. Therefore, a model is a generic entity that can be fitted or molded to capture the features of the data. Mathematically and in general, a model can be written as:

$$\hat{y} := h(x|\theta), \quad (1.1)$$

⁸see <https://alstat.github.io/QuranTree.jl/stable/>

⁹<https://tanzil.net/download/>

which is a mapping between the sets \mathcal{X} and \mathcal{Y} where $x \in \mathcal{X}$ and $y \in \mathcal{Y}$ through a hypothesized function h . The idea of modeling is to find the optimal value of θ in such a way it will minimize the error between the actual data (represented by y below) and the predicted one \hat{y} :

$$\varepsilon := y - \hat{y} = y - h(x|\theta). \quad (1.2)$$

To help understand the concept of modeling, and relate it to the fashion industry, which the author assumes most readers are familiar with, a model in a fashion industry is responsible for representing the characteristics of the target customers (in Eq. 1.1 this is y). Therefore, for a clothing company, they hire Asian models (in Eq. 1.1, this is \hat{y} or $h(x|\theta)$) to target Asian customers (in Eq. 1.1 this is y). So that, when these models wore the clothes sold by the said company, the potential customer will more or less be able to relate to the model, and be able to imagine themselves wearing that same clothes as well, which help them incline to buying the said clothing. The model, therefore, does not necessarily have the looks of every target Asian customers, but at least in terms of height, skin tone, hair, and other common Asian features, the model will likely have it, or at least the difference is more or less minimal (in Eq. 1.1, the difference is represented by $\varepsilon := y - \hat{y}$). The question now is, what are the benefits that this model can bring to the clothing company? Well, the clothing company will be able to create products that are tailored to their Asian customers using the said model, since the company will have the right baseline measurements needed. Relating this analogy to the technical concept discussed earlier, you can think of the target customers as the real or actual data (in Eq. 1.1 this is y), and the model as the same technical term use in Machine Learning and Statistics (in Eq. 1.1 this is $h(x|\theta)$), but this time this technical model is expected to capture the characteristics of the real data analogous to fashion model that is expected to capture the characteristics of the target customer. This Statistical or Machine Learning model brings the following benefit: researchers will be able to study the real data by simply using the model to answer questions that are not

available in the sampled real data.

In this paper, the aim is to make use of the Statistical or Machine Learning modeling to understand the characteristics of the Qur'ān in terms of the morphologies of its canonical text in its modern orthography. More specifically, the following are the general objectives:

1.3 Objectives

The objective of the paper is to answer the following research questions:

1. What are the thematic themes of the surah that can be extracted by a Large Language Model?
2. What other insights that can be extracted by a Statistical and Machine Learning models in terms of the Qur'ānic morphology?
3. How does this combination of Statistical, Machine Learning, and Artificial Intelligence (AI) with the Muslim's traditional literatures help in understanding the Qurān, especially with the advent of Generative AI?

1.4 Significance of the Study

While the Qur'ān has been extensively studied by Muslims and non-Muslims scholars alike, especially in the topic of Meccan and Medinan surahs, there is still a lot to uncover from the perspective of Computational Statistics. Hence, the significance of this study is that it brings forward new ways of extracting insights from the Qur'ān by leveraging Computations, Statistics, Machine Learning, and AI, that is still in its early stage in the field of Qur'ānic Studies. Therefore, this new perspective or process of studying the scripture not only aids the scholars of the Islamic Studies, but may also contribute indirectly to community development and policy makers who use Qur'ān as part of their decision making.

1.5 Scope of the Study

The paper will cover all chapters of the Qur'ān both for the Morphological and Topic Modeling analyses, but it will only present the results of *sūrahs* سُورَاتٍ with at

least 1000 words. The rest of the result will be part of the web application that can be used to query the Qur'ān. It will also not delve into the *tafsir* تفسير of each of the verses, but only when necessary for further context.

1.6 Thesis Organization

The paper is organized as follows: Chapter 2 will discuss the related literatures, Chapter 3 will discuss the methodology, Chapter 4 will present the results and discussions, and finally Chapter 5 will contain the conclusion and recommendation. The references and appendices are placed after the Chapter 5.

Chapter 2

Literature Review

As mentioned in the previous chapter, the earliest work in Qur'ānic studies using computer was likely the work of Rashad Khalifa in 1968¹, which led to one of his book entitled 'The Computer Speaks: God's Message to the World' (see Khalifa (1981)). While the work of Rashad started at studying the mystery letters in the beginning of some *sūrahs* سور (for example Qur'ān 2:1, 3:1, 7:1, etc.), it quickly went on to cover what he calls other *mathematical miracles*, all of which are covered in Khalifa (1981). His findings led him to generalize the claim that God revealed His words through this mathematical patterns throughout the Qur'ān, and that those verses that were off and did not conform to this discovered mathematical patterns led him to extensive investigation of the said verses, and concluded that those could be or surely be an insertion that should not have been in the Qur'ān in the first place. There are two verses that were off according to Rashad, and he called these verses as *false verses*², these are the last two *ayāt* آيات of *sūra l-tāwba* سورة التوبة or The Chapter of *Repentance*. These two verses were removed in Rashad's Qur'ān translation³. Rashad believed so much on his findings that he self-proclaimed himself to be a messenger⁴ with this new findings and that the Qur'ān nowadays should conform to his found mathematical patterns. This self-proclamation led to his assassination.

Fast forward to 20th century, among the pioneers to creating a stemmer system for the Qur'ān is the work of Thabet (2004). A stemmer system is a system for trimming inflected words into its basic form, which grammatically mean its the root form. For example, in English language the root word for *computational*, *computer*, *computation*, and *computerize* is *compute*. Therefore, from the root of the word forms different stems representing the different words. Hence, the idea of stemming is to

¹https://www.masjidtucson.org/quran/miracle/a_profound_miracle_sura68nun133.html

²<https://submission.org/App24.html>

³<https://www.masjidtucson.org/quran/frames/>

⁴https://www.masjidtucson.org/submission/faq/rashad_khalifa_summary.html

trim these words into its basic form, so that it would be easy to do word clustering or grouping through word similarity. According to Thabet (2004), the rich morphology of the Qur'ānic language or the Classical Arabic makes it even more difficult to do word stemming. Moving on, Thabet (2005) builds on this stemming system, and used it for tokenization of the Qur'ānic words. Tokenization is the process of listing all of the words in a sentence, and Thabet (2005) makes use of Thabet (2004) to further cleanse the noise from these tokens brought by the morphological variants of the Classical Arabic words. After cleansing the data, Thabet (2005) makes use of a statistical methodology for clustering or grouping the chapters of the Qur'ān, in particular the statistical methodology used is the Agglomerative Hierarchical Clustering based on the Euclidean distance of the adjusted word frequency of the *sūrah* سورة.

The work of Thabet (2004) and Thabet (2005) makes use of the Qur'ān corpus transliterated to Roman letters and symbols. Indeed, with interest growing on studying the Qur'ān from the lense of Data Analysis and Natural Language Processing, more work have been put in place into creating digital corpi of the Qur'ān that captures the different aspects of its linguistic styles. Hence, a series of work by Sharaf and Atwell led to the following publications: Sharaf and Atwell (2009) studied knowledge representation of the Qur'ānic verb valences using FrameNet frames, the output of which is a lexical database of the corpus of Qur'ān verbs. Further, the work of Sharaf and Atwell (2012a) came up with corpus for the annotations of the Qur'ānic pronouns, the authors named it as QurAna. Building on this work, Sharaf and Atwell (2012b) came up with a corpus for studying Qur'ānic relatedness based on the commentary of Ibn Kathir ابن كثیر, the authors named this corpus as QurSim.

Moving on, an unpublished work by Nassourou (2011) used a Support Vector Machine (SVM) to predict the classification of the place of revelation of the Qur'ānic *sūrahs* سور. The idea was to use *sūrahs* سور with well attested place of revalation as the training set, and then train an SVM to predict the remainings of the chapters.

Furthermore, the work of Shahzadi, ur Rahman, and Sawar (2012) developed a simple classifier based on the frequency distribution of words in *ayāt* آیات and the corresponding words in *sūrahs* سور.

Moving on, the work of

Chapter 3

Background on Probability and Statistics

This chapter will discuss some statistical concepts that will be used to understand and build up the ideas behind the methodology of this paper, which is presented in the next chapter. With that said, the discussions are organized as follows: Section 3.1 will present the concept of Descriptive Statistics; Section 3.2 will discuss the Probability Theory; and, Section 3.3 will discuss the Statistical graphs or plots.

Further, the topics discussed here may be self-explanatory for Statisticians, ML researchers or those with Mathematical background. However, for the benefit of readers coming from humanities background, the paper will present the methodology as follows: mathematical formulas are formalized for purpose of brevity through Definition, Proposition, and Corollary, but immediate to these are explanations or examples aimed to be simple enough for non-statistician readers. As a guide, statisticians or ML researchers can simply read the Definition, Proposition, and/or Corollary. Whereas for humanities readers, the reading shouldn't not stress too much on the said mathematical formalities, and instead proceed to the discussions or examples immediate to it to aid with the understanding.

3.1 Descriptive Statistics

Among the basic statistical methodologies for summarizing information or data is what is known as Descriptive Statistics. From the name itself, these statistics are meant to convey simple descriptions of the data. For example, *mean* and *variance* are common statistics used for describing the data. The formulas for these statistics are given in the following definitions:

Definition 3.1.1 (Mean). Let $x_i, i \in \{1, \dots, n\}$ where $n \in \mathbb{N}$, then the *mean* of x_i s is defined as follows:

$$\bar{x} = \sum_{i=1}^n x_i, \quad \text{where } x_i \in \mathbb{R}. \quad (3.1)$$

Definition 3.1.2 (Variance). Let $x_i, i \in \{1, \dots, n\}$ where $n \in \mathbb{N}$ and let \bar{x} be the mean defined in Defn. 3.1.1 then the *variance* of x_i s is defined as follows:

$$\text{Var}(x) = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2, \quad \text{where } x_i \in \mathbb{R}. \quad (3.2)$$

Definition 3.1.3 (Standard Deviation). Let σ^2 be the variance, then the standard deviation, denoted by σ , is defined as $\sigma := \sqrt{\sigma^2}$, that is, square root of the variance.

The mean is simply the average of the data points, while the variance is a single number that measures or summarizes the distances of the data points from the mean. The variance therefore measures how spread or varied the data points are. In practice, however, standard deviation is more popular for measure of variability since it doesn't get big easily due to the square root operator. Standard deviation is also the preferred metric for this paper.

3.2 Probability Theory

Statistics is built around the concept of Probability Theory. Hence, it is important to understand how this mathematical theory behind the statistical concepts work. Probability theory is a discipline in itself. It is a branch of mathematics that aims at studying realizations or observations from random phenomena. It does this by using algorithms and models (see discussion in Chapter 1 for understanding the model). These probability models are mathematical formula design to characterize or describe the patterns of data points. The simplest form of these models is the univariate probability density functions. However, before discussing these models, the idea behind it should be build up from ground up so that humanities readers can appreciate it. To do this, the discussion will proceed with the concept of probability.

Definition 3.2.1 (Probability). A probability is a mathematical concept that measures the likelihood or chance of some event to happen.

Indeed, this idea of probability is well known or is easily understood by many.

So that, the probability that someone will die is 1, meaning 100%, since that's how natures and biology work. Further, the probability of selecting one *ayāt* from *sūra l-fātihiati* سُورَةُ الْفَاتِحَةُ through a random draw is one out of seven, assuming each *ayāt* has equal chances of being drawn.

Now, to gradually formalize the concept into mathematics, the succeeding definitions will be discussed to build up the definition of a probability distribution.

Definition 3.2.2 (Sample Space). Let $\omega_1, \dots, \omega_n, \forall n \in \mathbb{N}$ be the list of all possible outcomes of a random event or a phenomena, then the sample space, denoted by Ω , is defined as the collection of all these possible outcomes including the empty set denoted by \emptyset . □

Example 3.2.1. Consider the random phenomenon or event where someone randomly picks a verse from the Qur'ān, what is the probability that it will be a Meccan مكّية or a Medinan مدّنية verse?

The possible output for such random event is either Meccan or Medinan. Suppose, we let Meccan to be denoted by ω_1 and Medinan to be denoted ω_2 , then the sample space, which is the collection of all possible output is denoted as follows:

$$\Omega := \{\text{مكّية}, \text{مدّنية}\} = \{\text{Meccan}, \text{Medinan},\} = \{\omega_1, \omega_2,\} \quad (3.3)$$

It should be understood that \emptyset is also included in Ω , but is not written for brevity. □

Definition 3.2.3 (Event). Let $\Omega = \{\omega_1, \dots, \omega_n\}, \forall n \in \mathbb{N}$, be the sample space, then an event, denoted here as \mathcal{A} , is defined as the subset of the sample space, i.e., $\mathcal{A} \subseteq \Omega$. □

Example 3.2.2. From Ex. 3.2.1, consider drawing two samples from the Qur'an, what is the sample space and give an example of a possible event?

Solution: The sample space is given below:

$$\Omega = \{(\text{مَكِّيَةَ}, \text{مَكِّيَةَ}), (\text{مَكِّيَةَ}, \text{مَدِّيَةَ}), (\text{مَدِّيَةَ}, \text{مَكِّيَةَ})\} \\ = \{(\text{Meccan}, \text{Meccan}), (\text{Meccan}, \text{Medinan}), \quad (3.4)$$

$$(\text{Medinan}, \text{Meccan}), (\text{Medinan}, \text{Medinan})\} \quad (3.5)$$

$$= \{(\omega_1, \omega_1), (\omega_1, \omega_2), (\omega_2, \omega_1), (\omega_2, \omega_2)\} \quad (3.6)$$

So that, if \mathcal{A} is the event of drawing two *ayāt* آيات from the Qur'ān, then a possible event is given by

$$\mathcal{A} := \{\text{مَكِّيَةَ}, \text{مَدِّيَةَ}\} = \{\text{Medinan}, \text{Meccan}\} = \{\omega_2, \omega_1\} \quad (3.7)$$

Therefore, $\mathcal{A} \subseteq \Omega$, read as \mathcal{A} is a subset of Ω . □

Now, going back to the discussion on the concept of probability above and reflect on the example given, that the probability that someone will die is 1; and that the probability of selecting one *ayāt* آيات from *sūra l-fātiḥati* سُورَةُ الْفَاتِحَةِ through a random draw is one out of seven. It therefore begs the following questions: how does one solve this? Like how does it translate into a formal mathematical computation?

Indeed, to appreciate the motivation of the succeeding definitions, it is important to devise a logical approach to computing probability mathematically, and this should explain why the following definitions are defined the way they are.

Probability as already defined in Defn. 3.2.1 is a measure. Indeed, this is analogues to measuring an object's size using a tape measure. So, when someone attempts to measure an object's size, there are conditions for the object to be measurable. That is, it is necessary to defined the space where the measurement will be performed. This space is of course the object's body area. For any object's surface area, the area or the space or the field should have the following properties:

- The object's area can be broken down into smallest pieces, and that the collection of all possible collections of these pieces include:

1. The 0 size piece, that is, the object's measurement should start at 0;
2. The remainings of the pieces given the pieces already measured;
3. The union of the pieces.

Definition 3.2.4 (σ -algebra). Let $\Omega := \{\omega_1, \dots, \omega_n\}, \forall n \in \mathbb{N}$, then the collections of all disjoint partitions, which are the events, are defined as the σ -algebra or σ -field, denoted here as \mathfrak{F} , and should satisfy the following conditions:

1. The empty set $\emptyset \in \mathfrak{F}$
2. If $\mathcal{A} \in \mathfrak{F}$, then the complement $\Omega \setminus \mathcal{A}$ is also an element of \mathfrak{F}
3. If $\mathcal{A}_1, \mathcal{A}_2, \dots$ is a countable sequence of sets in \mathfrak{F} , then the $\bigcup_{i=1}^{\infty} \mathcal{A}_i$ is also an element of \mathfrak{F}

□

Example 3.2.3. Given the sample space $\Omega := \{\text{Meccan, Medinan}\}$, the σ -algebra is $\mathfrak{F} = \{\{\text{Meccan}\}, \{\text{Medinan}\}, \Omega, \emptyset\}$. □

Definition 3.2.5 (Probability Measure). Let Ω be the *sample space*, \mathfrak{F} be the σ -algebra, \mathbb{P} be the probability measure, then the probability of a set $\mathcal{A}, \mathcal{A} \in \mathfrak{F}$, on the probability space $(\Omega, \mathfrak{F}, \mathbb{P})$, denoted by $\mathbb{P}(\mathcal{A})$, satisfies the following properties:

1. Non-negativity: For any set $\mathcal{A}, \mathbb{P}(\mathcal{A}) \geq 0$
2. Normalization: $\mathbb{P}(\Omega) = 1$
3. Countable additivity: For any sequence of disjoint sets $\mathcal{A}_1, \mathcal{A}_2, \dots$ in \mathfrak{F} , such that the union $\bigcup_{i \in \mathbb{N}} \mathcal{A}_i$ is also in \mathfrak{F} , we have: $\mathbb{P}\left(\bigcup_{i \in \mathbb{N}} \mathcal{A}_i\right) = \sum_{i \in \mathbb{N}} \mathbb{P}(\mathcal{A}_i)$

□

Basically, the idea of Defn. 3.2.5 is to define the concept of "measure" in general sense, although above is a special measure called probability measure. One can think of this probability measure like a tape measure in simple sense. This tape

measure has some properties that should be expected for a measurement tool. The first property or condition is that the probability measure has to be positive. Indeed, if we use any tape measure for measuring length, never will someone get a negative measure like -2cm length. It always has to be positive. Further, the second condition to expect is that for this type of tape measure called probability measure, the total measure of all objects available in the given space should be equal to 1. That is, the total is normalized to 1. Think of this like 100% coverage if we measure all of the objects. Lastly, for any object, this tape measure should be able to measure the object through partitions, such that the measure of the union of these partitions is equal to the sum of the measure of each partition. All of these conditions are logical criteria for a general idea of "measure," although the normalization part above is unique for probability measure. Note that, the concept of probability measure here is should not be confined to measuring length as in the analogy, it should generalize to measuring volume and complex objects in general.

Definition 3.2.6 (Random Variable). Let Ω be the sample space, and \mathbb{R} be the set of all real numbers, then a random variable X is a function defined as $X : \Omega \rightarrow \mathbb{R}$. \square

Example 3.2.4. Consider the example of drawing a random verse or *ayāt* again, what is the probability that it will be an *ayāt* from *sūrah l-baqara's ayāt* آية سورة البقرة or the Chapter of Cow?

The answer to this is 4.59% probability, this is because there are 286 *ayāt* and there are 6236 verses in the Qur'ān, so that the probability is $\frac{286}{6236} = 0.04586$. \square

Example 3.2.5. To apply the concept so far, consider again Ex. 3.2.4, what is the probability of getting 5 *sūrah l-baqara's ayāt* آية سورة البقرة if we randomly pick 20 *ayāt* آيات in total from the Qur'ān?

Solution. The following are given:

- $n = 20$ independent trials of drawing $x = 5$ آيات from the Qur'ān
- Each trial has two possible outcomes: *na'am* نعم meaning Yes or *lā* لَا meaning No. That is, if the *ayāt* آيات is from the *sūrah l-baqara* سورة البقرة then its نعم,

otherwise \nexists .

Now, the sample space consists of all possible sequences of 20 \nexists and \exists . That is,

$$\Omega = \{(\exists, \nexists, \nexists, \dots, \nexists), \quad (3.8)$$

$$(\nexists, \nexists, \nexists, \dots, \nexists), \quad (3.9)$$

$$\vdots \quad (3.10)$$

$$(\exists, \exists, \exists, \dots, \exists)\}. \quad (3.11)$$

In total, there are $20^2 = 400$ possible samples in the sample space Ω . Further, from Ex. 3.2.4, the probability of getting a *sūrah l-baqara's ayāt* is 0.0459 or 4.59%. Therefore, if we assign \exists and \nexists as either 0 or 1, respectively, then mathematically $\mathbb{P}(X = 1) = 0.0459$. In addition, the probability of getting an *ayāt* from other *sūrah* would be $\mathbb{P}(X = 0) = 1 - \mathbb{P}(X = 1) = 1 - 0.0459 = 0.9541$.

Further, let Z be the random variable for the event of getting $n \nexists$ from 20 trials, then the problem is equivalent to finding the number of ways to choose 5 positions out of 20 in the collection or set. This can be solved using *combination* formula as shown below:

$$\binom{n}{x} = \frac{n!}{r!(n-r)!} \Rightarrow \binom{20}{5} = \frac{20!}{5!(20-5)!} = 15,504. \quad (3.12)$$

That is, there are 15,504 possible cases with 5 positions for \nexists in a 20 trial. Moreover, in each of these samples 5 has a probability of $\mathbb{P}(X = 1) = 0.0459$, while the remaining 15 has a probability of $\mathbb{P}(X = 0) = 0.9541$. So that,

$$\begin{aligned} \mathbb{P}(Z = 5) &= 184,756 \times \mathbb{P}(X = 1)^5 \times \mathbb{P}(X = 1)^{20-5} \\ &= 15,504 \times 0.0459^5 \times 0.9541^{20-5} \\ &= 0.0016. \end{aligned} \quad (3.13)$$

Hence, there is a 0.16% probability of getting 5 *sūrah l-baqara's ayāt* when

randomly drawing 20 سُورَةً from the Qur'ān. \square

Note that Ex. 3.2.5 can be solved using a known formula in probability called *Binomial* mass function. The general concept of probability distribution is defined in the following definitions.

Definition 3.2.7 (Normal Density Function). Let Y be a random variable and let $\mu \in \mathbb{R}$ and $\sigma \in \mathbb{R}$ be the mean and variance parameters, if y is the random value, then the *Gaussian* or *Normal* density function is given below:

$$\mathbb{P}(Y = y) := \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left\{-\frac{(y - \mu)^2}{\sigma^2}\right\}, \quad \text{where } -\infty < y < \infty \quad (3.14)$$

Definition 3.2.8 (Dirichlet Density Function). Let \mathbf{Y} be a vector random variable with a random value $\mathbf{y} := [y_1, \dots, y_k]^T$ and let $\boldsymbol{\alpha} := [\alpha_1, \dots, \alpha_k]^T$ be the parameters, then the *Dirichlet* density function is defined as

$$\mathbb{P}(\mathbf{X} = \mathbf{x}; \boldsymbol{\alpha}) := \frac{1}{B(\boldsymbol{\alpha})} \prod_{i=1}^k x_i^{\alpha_i-1}, \quad (3.15)$$

where,

$$B(\boldsymbol{\alpha}) := \frac{\prod_{i=1}^k \Gamma(\alpha_i)}{\Gamma\left(\sum_{i=1}^k \alpha_i\right)} \quad (3.16)$$

\square

Definition 3.2.9 (Multinomial Mass Function). Let \mathbf{X} be a vector random variable with a random value $\mathbf{x} := [x_1, \dots, x_k]^T$ such that $x_i \geq 0, \forall i \in [1, k]$, let $\mathbf{p} := [p_1, \dots, p_k]^T$ and n be the parameters, the probability mass function of a Multi-

nomial distribution is

$$\begin{aligned}
 f(x_1, \dots, x_k; n, p_1, \dots, p_k) &:= \mathbb{P}(X_1 = x_1 \text{ and } \dots \text{ and } X_k = x_k) \\
 &= \begin{cases} \frac{n!}{x_1! \cdots x_k!} p_1^{x_1} \times \cdots \times p_k^{x_k}, & \text{when } \sum_{i=1}^k x_i = n \\ 0 & \text{otherwise,} \end{cases}
 \end{aligned} \tag{3.17}$$

3.3 Statistical Graphs

Graphs or plots are data visualization tools that are useful for exploratory data analysis apart from the Descriptive Statistics discussed above. It supplements the Descriptive Statistics findings through shapes visualized in the graphs. Among the popular statistical graphs is the bar graph. An example of this is given in Figure 1.1. Other graphs used are the box plots and the density plots which is also in Figure 1.1

3.3.1 Box, Density, and Histogram Plots

While most statistical plots are easy to understand like bar graphs and scatter plots, others like Box, Density, and Histogram plots may not be easy to comprehend for someone with no Statistical background. This section will discuss how it is interpreted. Let's use Figure 1.1, Figure 3.1 for easy reference in this section.

As shown in Figure 3.1, both the Box and Density plots are tied to each other. This is indeed the case because both are describing the same information but presented in different style of visualization. In fact, Histogram is also used to describe the same information as the Box and Density, and the three are therefore related. So much so, that the three can be put into one graph. As to how to interpret these, readers are referred to for further details [to add reference].

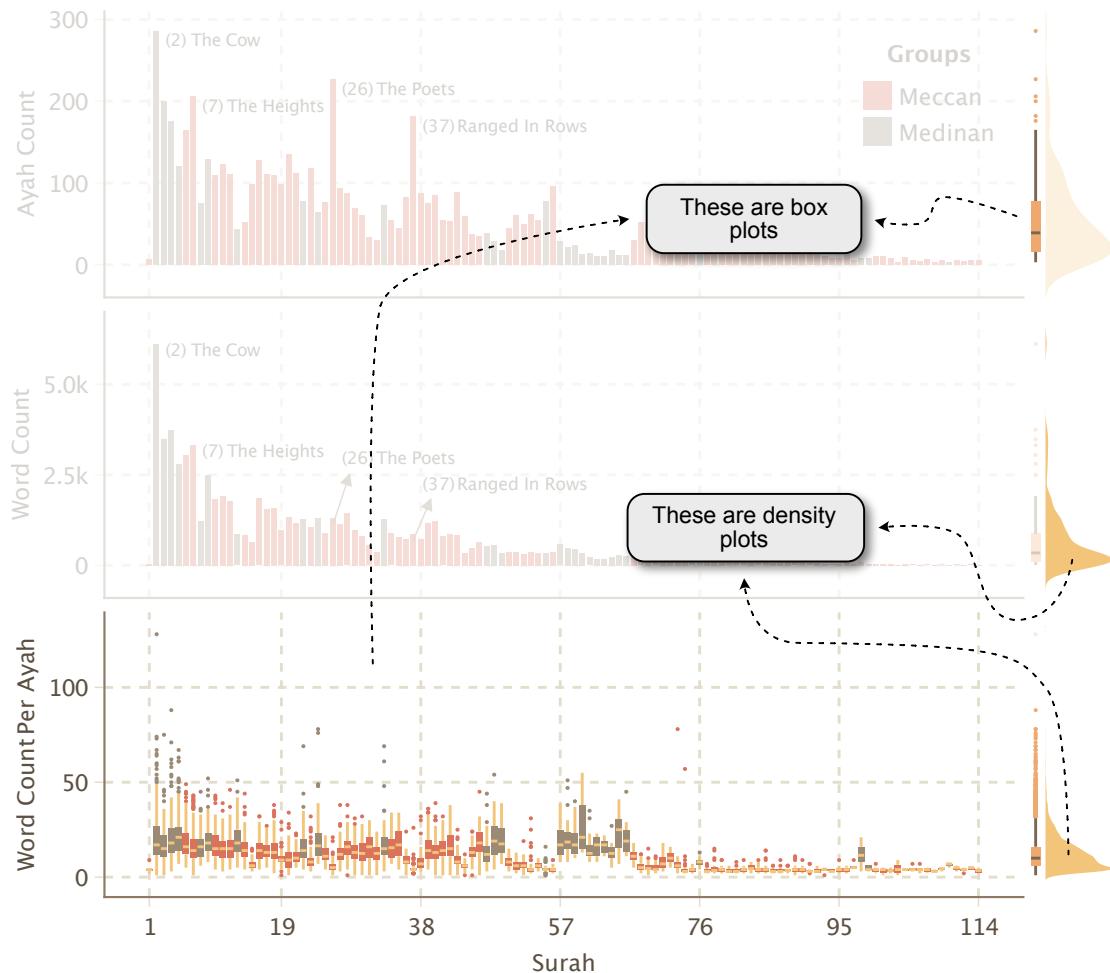


Figure 3.1: Statistics of the words and *ayāt* (verses) of the Qur'ān

Chapter 4

Methodology

This chapter is organized as follows: Section 4.1 will discuss the concept of Topic Modeling, Section 4.1.2 will discuss the concept of Large Language Models, and finally Section 4.3 will discuss how to implement this in Julia programming language.

4.1 Topic Modeling

As presented in Chapter 1, the first objective is to extract the thematic themes of *sūrahs* سور with at least 1000 words. In Statistics and Machine Learning, this task is called Topic Modeling. There are several ways to do this, but the popular methodology is to use the Latent Dirichlet Allocation (LDA) discussed in the next section.

4.1.1 Latent Dirichlet Allocation

Latent Dirichlet Allocation (LDA) is a Statistical methodology that is based on Bayesian inference (Bayes, 1763; Laplace, 1986). It is a generative probabilistic model for collection of discrete data such as text corpora (Blei, Ng, & Jordan, 2003).

The main formula is defined below:

Definition 4.1.1 (Latent Dirichlet Allocation). Let $\mathbf{W}, \mathbf{Z}, \boldsymbol{\theta}, \boldsymbol{\varphi}$ be the random variables, and let α and β be the hyper-parameters, then the probability of generating a document is

$$\mathbb{P}(\mathbf{W}, \mathbf{Z}, \boldsymbol{\theta}, \boldsymbol{\varphi}) = \prod_{j=1}^m \mathbb{P}(\boldsymbol{\theta}_j; \alpha) \prod_{i=1}^k \mathbb{P}(\boldsymbol{\varphi}; \beta) \prod_{t=1}^n \mathbb{P}(\mathbf{Z}_{j,t} | \boldsymbol{\theta}_j) \mathbb{P}(\mathbf{W}_{j,t} | \boldsymbol{\varphi}_{\mathbf{Z}_{j,t}}) \quad (4.1)$$

4.1.2 Large Language Models

Generative Artificial Intelligence or GenAI for short has been making waves on its effectiveness to generate texts, images, audio, video, etc. It has elevated humanity to a new level of capability. However, behind this amazing capabilities is that GenAI

is by design a mathematical formula that are called *model*. There are several types of *models*, and one of those is the Large Language Model (LLM). The following section will discuss what LLM is and its mathematical formulation.

Bidirectional Encoder Representation from Transformer

Generative Pre-Trained Transformer

4.2 Retrieval-Augmented Generation

The problem with LLM is that it was only trained on huge but limited data, and is therefore not able to infer what should be the context when asked.

4.3 Julia Code Setup

This section will discuss the coding setup. As mentioned in Chapter 1, the main programming language to use is Julia. As such, it is necessary to present where the codes will be stored so that readers are able to reproduce it. All of the codes will be saved in Github repository accessible through the following link:

<https://github.com/alstat/ma-thesis/tree/main/codes>

4.4 Python Code Setup

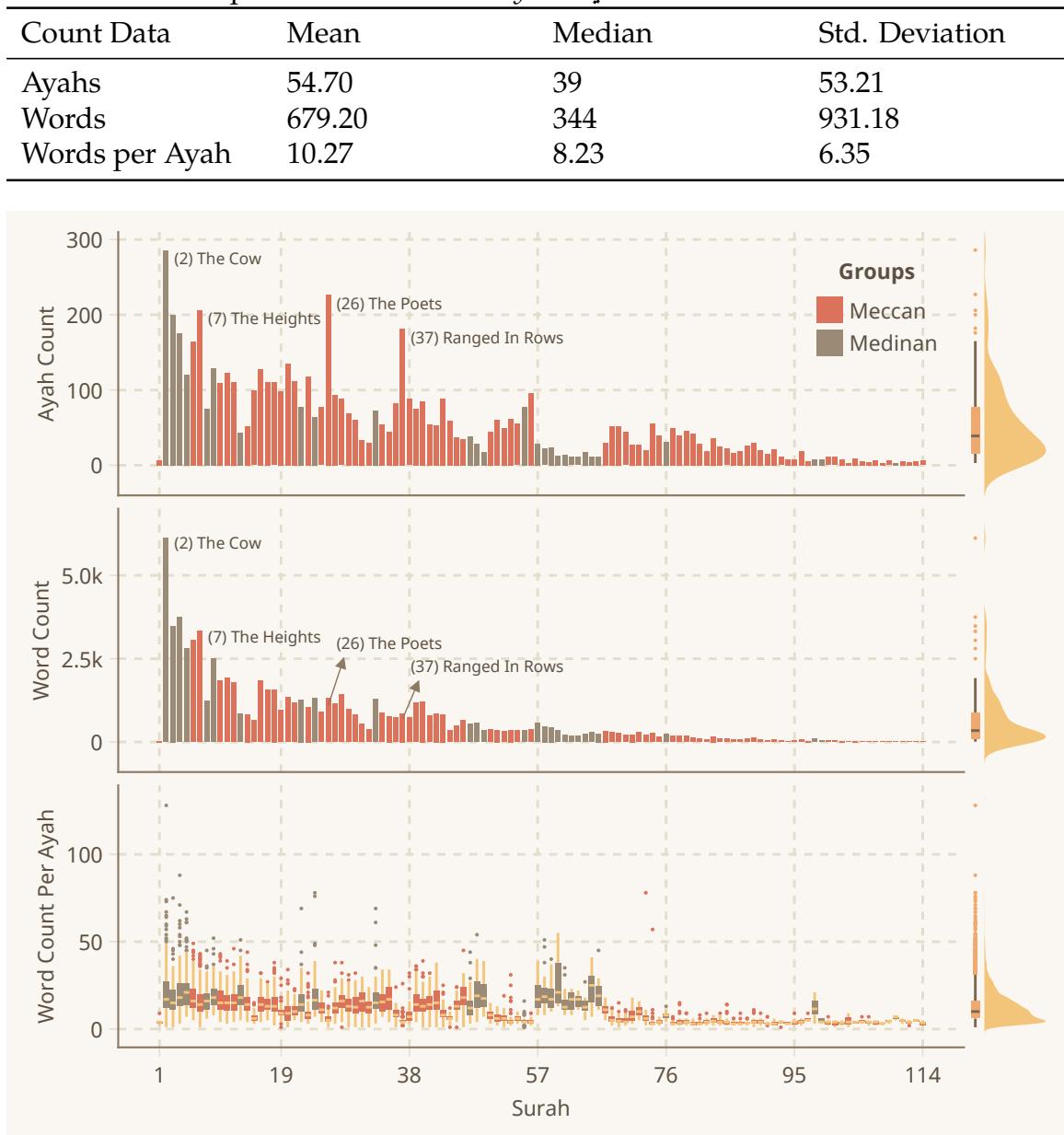
Chapter 5

Results and Discussions

This chapter is organized as follows: Section 5.1 will discuss the results of the descriptive statistics; Section 5.2 will discuss the results on the morphological analyses; Section 5.3 will discuss the structural analyses including the Mathematical structures of the Qur’ān; Section 5.4 will discuss the results for thematic analyses using both statistical and Large Language models; and finally, Section 5.5 will discuss the use of other Islamic texts that will help in adding more contexts for the Large Language models.

5.1 Descriptive Statistics

This section will focus on the results of the descriptive statistics of the Qur’ān’s *ayāt* آيات (verses) and *kalimat* كلامات or words. Figure 5.1 visualizes the frequency of the *ayāt* آيات and words of the Qur’ān using a combinations of bar, density, and box plots. The figure is divided into three main parts. The first part is the statistics of the *ayāt* آيات count. It can be seen that in terms of the number of verses, it is generally decreasing just like what the Muslims observed. Table 5.1 summarizes the necessary statistics of Figure 5.1. From the said table, there are 39 *ayāt* آيات to expect based on the median statistics, and there are about 55 *ayāt* آيات to expect per *sūrah* سورة based on the mean statistics. The reason the mean is higher than the median follows from the fact that there are surahs that can be considered outlier because of the large number of *ayāt* آيات. The annotation on the *sūrah* سورة with the highest number of *ayāt* آيات are indicated in Figure 5.1. These *sūrah* سورة pushes the mean to higher number than the median. Indeed, these *sūrahs* سور have stretched the shape of the density and the box plots to higher values, suggesting that the data points are more varied. The width of the density and the box plots is measured by the variance and the standard deviation, which is simply the square root of the variance.

Table 5.1: Descriptive statistics of the *ayāt* آيات counts and the counts of its wordsFigure 5.1: Statistics of the words and *ayāt* آيات (verses) of the Qur'ān

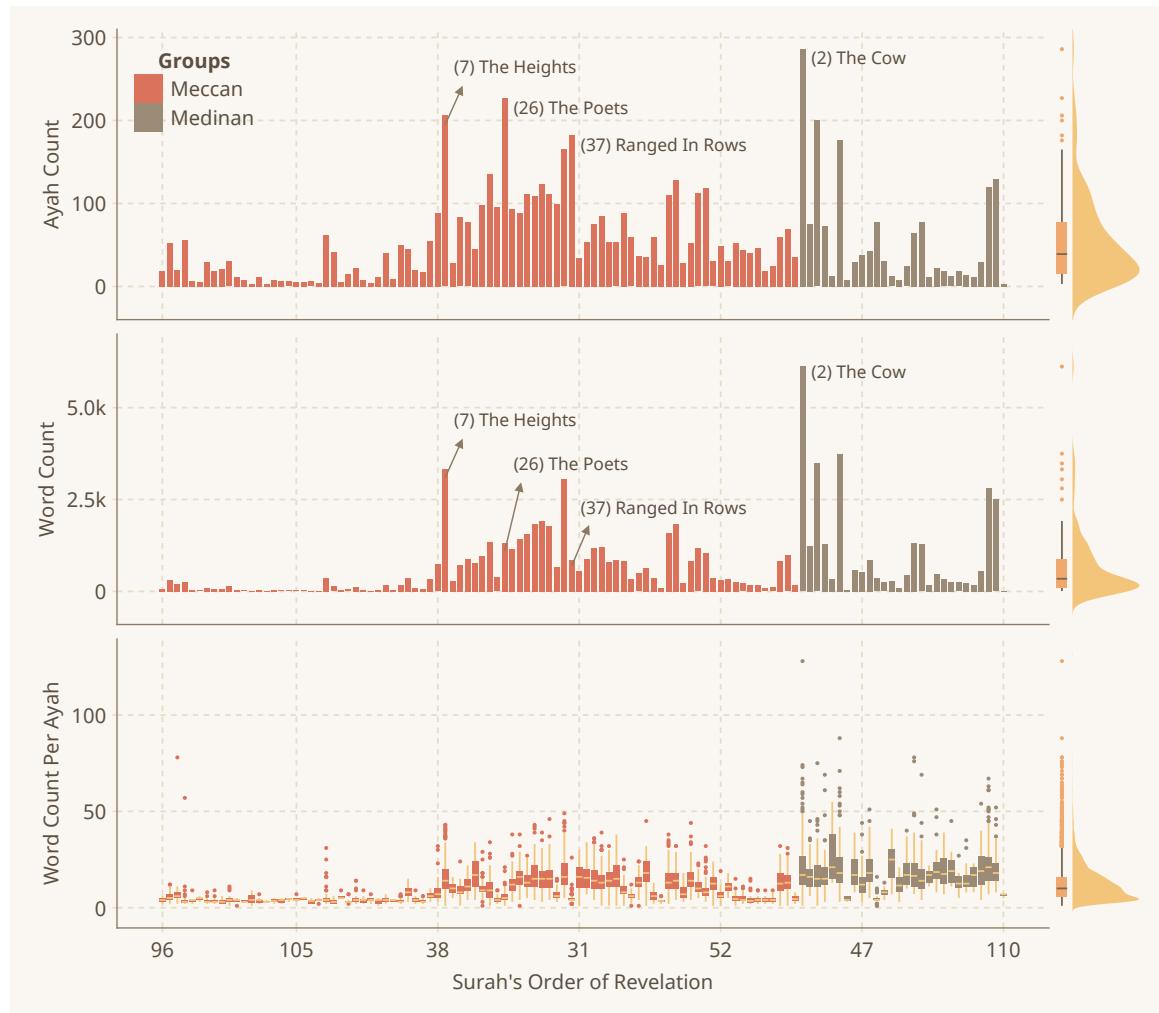


Figure 5.2: Statistics of the words and *ayāt* آیات (verses) of the Qur'ān according to revelation order

5.1.1 Verses

5.2 Morphological Analysis

5.3 Structural Analysis

5.3.1 Concentric Structure

5.3.2 Mathematical Structure

5.3.3 Discussions on Islamic Philosophy of Qur'ān's Structural Analysis

5.4 Topic Modeling

5.4.1 Latent Dirichlet Allocation

5.4.2 Bidirectional Encoder Representation from Transformer

5.4.3 Generative Pre-Trained Transformer

5.5 Relating to other Islamic Texts and Analyses

5.5.1 Retrieval-Augmented Generation Approach

5.6 Limitations of the Models

Chapter 6

Conclusion and Recommendation

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