## z-p Isomorphism

Ocean (z coordinates)

 $z \leftrightarrow p$ 

Atmosphere (p coordinates)

$$\begin{aligned} d_{\underline{t}}\underline{v} + f \times \underline{v} + \underline{\nabla}_{z}P &= \underline{F} & P \leftrightarrow \Phi \\ g\rho + \partial_{z}P &= 0 & \rho \leftrightarrow \alpha \\ \underline{\nabla}_{h} \cdot \underline{v} + \partial_{z}w &= 0 & w \leftrightarrow \omega \\ d_{\underline{t}}\theta &= Q & \theta \\ d_{\underline{t}}s &= S & s \leftrightarrow q \\ \partial_{\underline{t}}\eta + \underline{\nabla} \cdot (\eta + H)\underline{v} &= P-E & \eta + H \leftrightarrow p_{\underline{s}} \end{aligned}$$

$$P \leftrightarrow \Phi$$

$$\rho \leftrightarrow \alpha$$

$$w \leftrightarrow \omega$$

$$\theta$$

$$s \leftrightarrow q$$

$$d_{t}\underline{v} + f \times \underline{v} + \frac{\nabla}{\rho}\Phi = \underline{F}$$

$$\alpha + \partial_{\rho}\Phi = 0$$

$$\underline{\nabla}_{p}\underline{\cdot}\underline{v} + \partial_{\rho}\omega = 0$$

$$d_{t}\theta = Q$$

$$d_{t}q = S$$

$$\partial_{t}p_{s} + \underline{\nabla}\underline{\cdot}p_{s}\underline{v} = 0$$



