

#P4

$$u'' = e^{\sin(x)}, \quad u'(0) = 0, \quad u'(1) = \alpha.$$

integrate:

$$u' = \int_0^x e^{\sin t} dt + C, \quad \text{since } u'(0) = 0, \quad C = 0.$$

$$\alpha = u'(1) = \left(\int_0^1 e^{\sin t} dt \right)$$

integrate again.

$$u = \int_0^x \int_0^s e^{\sin t} dt ds + C.$$