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RFC 9474 RSA Blind Signatures

Abstract

This document specifies an RSA-based blind signature protocol. RSA blind signatures were first introduced by Chaum for untraceable payments. A signature that is output from this protocol can be verified as an RSA-PSS signature.

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1. Introduction

Originally introduced in the context of digital cash systems by Chaum for untraceable payments [Chaum83], RSA blind signatures turned out to have a wide range of applications ranging from privacy-preserving digital payments to authentication mechanisms [GoogleVPN] [ApplePrivateRelay] [PrettyGoodPhonePrivacy].

Recently, interest in blind signatures has grown to address operational shortcomings from applications that use Verifiable Oblivious Pseudorandom Functions (VOPRFs) [VOPRF], such as Privacy Pass [PRIVACY-PASS]. Specifically, VOPRFs are not necessarily publicly verifiable, meaning that a verifier needs access to the VOPRF private key to verify that the output of a VOPRF protocol is valid for a given input. This limitation complicates deployments where it is not desirable to distribute private keys to entities performing verification. Additionally, if the private key is kept in a Hardware Security Module, the number of operations on the key is doubled compared to a scheme where only the public key is required for verification.

In contrast, digital signatures provide a primitive that is publicly verifiable and does not require access to the private key for verification. Moreover, [JKK14] shows that one can realize a VOPRF in the random oracle model by hashing a (message, signature) pair, where the signature is computed using a deterministic blind signature protocol.

This document specifies (1) a protocol for computing RSA blind signatures using RSA-PSS encoding and (2) a family of variants (Section 5) for this protocol, denoted RSABSSA (RSA Blind Signature with Appendix). In order to facilitate deployment, it is defined in such a way that the resulting (unblinded) signature can be verified with a standard RSA-PSS library.

This document represents the consensus of the Crypto Forum Research Group (CFRG). It is not an IETF product and is not a standard.

2. Requirements Notation

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "NOT RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in BCP 14 [RFC2119] [RFC8174] when, and only when, they appear in all capitals, as shown here.

3. Notation

The following terms, which describe different protocol operations, are used throughout this document:

bytes_to_int and int_to_bytes:

Convert a byte string to and from a non-negative integer. bytes_to_int and int_to_bytes are implemented as OS2IP and I2OSP -- as described in [RFC8017] -- respectively. Note that these functions operate on byte strings in big-endian byte order.

random_integer_uniform(M, N):

Generate a random, uniformly distributed integer R between M inclusive and N exclusive, i.e., $M \le R \le N$.

bit_len(n):

Compute the minimum number of bits needed to represent the positive integer n.

inverse_mod(x, n):

Compute the multiplicative inverse of x mod n or fail if x and n are not co-prime.

is_coprime(x, n):

Return true if x and n are co-prime, and false otherwise.

len(s):

The length of a byte string, in bytes.

random(n):

Generate n random bytes using a cryptographically secure random number generator.

concat(x0, ..., xN):

Concatenation of byte strings. For example, concat(0x01, 0x0203, 0x040506) = 0x010203040506.

slice(x, i, j):

Return bytes in the byte string x starting from offset i and ending at offset j, inclusive. For example, slice(0x010203040506, 1, 5) = 0x0203040506.

4. Blind Signature Protocol

The RSA Blind Signature Protocol is a two-party protocol between a client and server where they interact to compute sig = Sign(sk, input_msg), where input_msg = Prepare(msg) is a prepared version of the private message msg provided by the client, and sk is the private signing key provided by the server. See Section 6.2 for details on how sk is generated and used in this protocol. Upon completion of this protocol, the server learns nothing, whereas the client learns sig. In particular, this means the server learns nothing of msg or input_msg and the client learns nothing of sk.

The protocol consists of four functions -- Prepare, Blind, BlindSign, and Finalize -- and requires one round of interaction between client and server. Let msg be the client's private input message, and let (sk, pk) be the server's private and public key pair.

The protocol begins by the client preparing the message to be signed by computing:

```
input_msg = Prepare(msg)
```

The client then initiates the blind signature protocol by computing:

```
blinded_msg, inv = Blind(pk, input_msg)
```

The client then sends blinded_msg to the server, which then processes the message by computing:

```
blind_sig = BlindSign(sk, blinded_msg)
```

The server then sends blind_sig to the client, which then finalizes the protocol by computing:

```
sig = Finalize(pk, input_msg, blind_sig, inv)
```

The output of the protocol is <code>input_msg</code> and <code>sig</code>. Upon completion, correctness requires that clients can verify signature <code>sig</code> over the prepared message <code>input_msg</code> using the server public key pk by invoking the RSASSA-PSS-VERIFY routine defined in Section 8.1.2 of [RFC8017]. The Finalize function performs this check before returning the signature. See Section 4.5 for more details about verifying signatures produced through this protocol.

Shown graphically, the protocol runs as follows:

In the remainder of this section, we specify the Prepare, Blind, BlindSign, and Finalize functions that are used in this protocol.

4.1. Prepare

Message preparation, denoted by the Prepare function, is the process by which the message to be signed and verified is prepared for input to the blind signing protocol. There are two types of preparation functions: an identity preparation function and a randomized preparation function. The identity preparation function returns the input message without transformation, i.e., msg = PrepareIdentity(msg).

The randomized preparation function augments the input message with fresh randomness. We denote this process by the function PrepareRandomize(msg), which takes as input a message msg and produces a randomized message input_msg. Its implementation is shown below.

```
PrepareRandomize(msg)
Inputs:
- msg, message to be signed, a byte string
Outputs:
- input_msg, a byte string that is 32 bytes longer than msg
Steps:
1. msg_prefix = random(32)
2. input_msg = concat(msg_prefix, msg)
3. output input_msg
```

4.2. Blind

The Blind function encodes an input message and blinds it with the server's public key. It outputs the blinded message to be sent to the server, encoded as a byte string, and the corresponding inverse, an integer. RSAVP1 and EMSA-PSS-ENCODE are as defined in Sections 5.2.2 and 9.1.1 of [RFC8017], respectively.

If this function fails with a "blinding error" error, implementations **SHOULD** try the function again. The probability of one or more such errors in sequence is negligible. This function can also fail with an "invalid input" error, which indicates that one of the inputs (likely the public key) was invalid. Implementations **SHOULD** update the public key before calling this function again. See Section 6.1 for more information about dealing with such errors.

Note that this function invokes RSAVP1, which is defined to throw an optional error for invalid inputs. However, this error cannot occur based on how RSAVP1 is invoked, so this error is not included in the list of errors for Blind.

```
Blind(pk, msg)
Parameters:
- modulus_len, the length in bytes of the RSA modulus n
- Hash, the hash function used to hash the message
MGF, the mask generation functionsalt_len, the length in bytes of the salt (denoted sLen
  in RFC 8017)
Inputs:
- pk, server public key (n, e)
- msg, message to be signed, a byte string
Outputs:
- blinded_msg, a byte string of length modulus_len
- inv, an integer used to unblind the signature in Finalize
- "message too long": Raised when the input message is too long
  (raised by EMSA-PSS-ENCODE)
  "encoding error": Raised when the input message fails encoding
(raised by EMSA-PSS-ENCODE)
- "blinding error": Raised when the inverse of r cannot be found
- "invalid input": Raised when the message is not co-prime with n
1. encoded_msg = EMSA-PSS-ENCODE(msg, bit_len(n))
   with Hash, MGF, and salt_len as defined in the parameters
2. If EMSA-PSS-ENCODE raises an error, re-raise the error and stop
3. m = bytes_to_int(encoded_msg)
4. c = is\_coprime(m, n)
5. If c is false, raise an "invalid input" error and stop
6. r = random_integer_uniform(1, n)
7. inv = inverse_mod(r, n)
8. If inverse_mod fails, raise a "blinding error" error and stop
9. x = RSAVP1(pk, r)
10. z = (m * x) \mod n
11. blinded_msg = int_to_bytes(z, modulus_len)
12. output blinded_msg, inv
```

The blinding factor r **MUST** be randomly chosen from a uniform distribution. This is typically done via rejection sampling.

4.3. BlindSign

BlindSign performs the RSA private key operation on the client's blinded message input and returns the output encoded as a byte string. RSASP1 is as defined in Section 5.2.1 of [RFC8017].

```
BlindSign(sk, blinded_msg)
Parameters:
- modulus_len, the length in bytes of the RSA modulus n
Inputs:
- sk, server private key
- blinded_msg, encoded and blinded message to be signed, a
  byte string
Outputs:
- blind_sig, a byte string of length modulus_len
Errors:
- "signing failure": Raised when the signing operation fails
- "message representative out of range": Raised when the
  message representative to sign is not an integer between \boldsymbol{\theta}
  and n - 1 (raised by RSASP1)
1. m = bytes_to_int(blinded_msg)
2. s = RSASP1(sk, m)
3. m' = RSAVP1(pk, s)
4. If m != m', raise a "signing failure" error and stop 5. blind_sig = int_to_bytes(s, modulus_len)
output blind_sig
```

4.4. Finalize

Finalize validates the server's response, unblinds the message to produce a signature, verifies it for correctness, and outputs the signature upon success. Note that this function will internally hash the input message as is done in Blind.

```
Finalize(pk, msg, blind_sig, inv)
Parameters:
- modulus_len, the length in bytes of the RSA modulus n
- Hash, the hash function used to hash the message
MGF, the mask generation functionsalt_len, the length in bytes of the salt (denoted sLen
  in RFC 8017)
Inputs:
- pk, server public key (n, e)
- msg, message to be signed, a byte string
- blind_sig, signed and blinded element, a byte string of
  length modulus_len
- inv, inverse of the blind, an integer
Outputs:
- sig, a byte string of length modulus_len
- "invalid signature": Raised when the signature is invalid
- "unexpected input size": Raised when a byte string input doesn't
  have the expected length
Steps:
1. If len(blind_sig) != modulus_len, raise an "unexpected input size"
   error and stop
2. z = bytes_to_int(blind_sig)
3. s = (z * inv) \mod n
4. sig = int_to_bytes(s, modulus_len)
5. result = RSASSA-PSS-VERIFY(pk, msg, sig) with
   Hash, MGF, and salt_len as defined in the parameters
6. If result = "valid signature", output sig, else raise an "invalid signature" error and stop
```

4.5. Verification

As described in Section 4, the output of the protocol is the prepared message input_msg and the signature sig. The message that applications consume is msg, from which input_msg is derived. Clients verify the msg signature using the server's public key pk by invoking the RSASSA-PSS-VERIFY routine defined in Section 8.1.2 of [RFC8017] with (n, e) as pk, M as input_msg, and S as sig.

Verification and the message that applications consume therefore depend on which preparation function is used. In particular, if the PrepareIdentity function is used, then the application message is input_msg. In contrast, if the PrepareRandomize function is used, then the application message is slice(input_msg, 32, len(input_msg)), i.e., the prepared message with the message randomizer prefix removed.

5. RSABSSA Variants

In this section, we define different named variants of RSABSSA. Each variant specifies EMSA-PSS options Hash, MGF, and sLen as defined in Section 9.1.1 of [RFC8017], as well as the type of message preparation function applied (as described in Section 4.1). Each variant uses the mask generation function 1 (MGF1) defined in Appendix B.2.1. of [RFC8017]. Future specifications can introduce other variants as desired. The named variants are as follows:

RSABSSA-SHA384-PSS-Randomized:

This named variant uses SHA-384 as the EMSA-PSS Hash option, MGF1 with SHA-384 as the EMSA-PSS MGF option, and 48 as the EMSA-PSS sLen option (48-byte salt length); it also uses the randomized preparation function (PrepareRandomize).

RSABSSA-SHA384-PSSZERO-Randomized:

This named variant uses SHA-384 as the EMSA-PSS Hash option, MGF1 with SHA-384 as the EMSA-PSS MGF option, and 0 as the EMSA-PSS sLen option (0-byte salt length); it also uses the randomized preparation function (PrepareRandomize).

RSABSSA-SHA384-PSS-Deterministic:

This named variant uses SHA-384 as the EMSA-PSS Hash option, MGF1 with SHA-384 as the EMSA-PSS MGF option, and 48 as the EMSA-PSS sLen option (48-byte salt length); it also uses the identity preparation function (PrepareIdentity).

RSABSSA-SHA384-PSSZERO-Deterministic:

This named variant uses SHA-384 as the EMSA-PSS Hash option, MGF1 with SHA-384 as the EMSA-PSS MGF option, and 0 as the EMSA-PSS sLen option (0-byte salt length); it also uses the identity preparation function (PrepareIdentity). This is the only variant that produces deterministic signatures over the client's input message msg.

The **RECOMMENDED** variants are RSABSSA-SHA384-PSS-Randomized or RSABSSA-SHA384-PSSZERO-Randomized.

Not all named variants can be used interchangeably. In particular, applications that provide high-entropy input messages can safely use named variants without randomized message preparation, as the additional message randomization does not offer security advantages. See [Lys22] and Section 7.3 for more information. For all other applications, the variants that use the randomized preparation function protect clients from malicious signers. A verifier that accepts randomized messages needs to remove the random component from the signed part of messages before processing.

Applications that require deterministic signatures can use the RSABSSA-SHA384-PSSZERO-Deterministic variant, but only if their input messages have high entropy. Applications that use RSABSSA-SHA384-PSSZERO-Deterministic **SHOULD** carefully analyze the security implications, taking into account the possibility of adversarially generated signer keys as described in Section 7.3. When it is not clear whether an application requires deterministic or randomized signatures, applications **SHOULD** use one of the variants with randomized message preparation.

6. Implementation and Usage Considerations

This section documents considerations for interfaces to implementations of the protocol defined in this document. This includes error handling and API considerations.

6.1. Errors

The high-level functions specified in Section 4 are all fallible. The explicit errors generated throughout this specification, along with the conditions that lead to each error, are listed in the definitions for Blind, BlindSign, and Finalize. These errors are meant as a guide for implementors. They are not an exhaustive list of all the errors an implementation might emit. For example, implementations might run out of memory.

Moreover, implementations can handle errors as needed or desired. Where applicable, this document provides guidance for how to deal with explicit errors that are generated in the protocol. For example, a "blinding error" error is generated in Blind when the client produces a prime factor of the server's public key. Section 4.2 indicates that implementations **SHOULD** retry the Blind function when this error occurs, but an implementation could also handle this exceptional event differently, e.g., by informing the server that the key has been factored.

6.2. Signing Key Generation and Usage

The **RECOMMENDED** method for generating the server signing key pair is as specified in FIPS 186-5 [DSS].

A server signing key **MUST NOT** be reused for any other protocol beyond RSABSSA. Moreover, a server signing key **MUST NOT** be reused for different RSABSSA encoding options. That is, if a server supports two different encoding options, then it **MUST** have a distinct key pair for each option.

If the server public key is carried in an X.509 certificate, it **MUST** use the id-RSASSA-PSS OID [RFC5756]. It **MUST NOT** use the rsaEncryption OID [RFC5280].

7. Security Considerations

Lysyanskaya proved one-more-forgery polynomial security of RSABSSA variants in the random oracle model under the one-more-RSA assumption; see [Lys22]. This means the adversary cannot output n+1 valid message and signature tuples, where all messages are distinct, after interacting with the server (signer) as a client only n times, for some n that is polynomial in the protocol's security parameter. Lysyanskaya also proved that the RSABSSA variants, which use the PrepareRandomize function, achieve blindness (see version B of the protocol and related proofs in [Lys22]). Blindness means that the malicious signer learns nothing about the client input and output after the protocol execution. However, additional assumptions on the message inputs are required for blindness to hold for RSABSSA variants that use the PrepareIdentity function; see Section 7.3 for more discussion on those results.

7.1. Timing Side Channels and Fault Attacks

BlindSign is functionally a remote procedure call for applying the RSA private key operation. As such, side-channel resistance is paramount to protect the private key from exposure [RemoteTimingAttacks]. Implementations SHOULD implement some form of side-channel attack mitigation, such as RSA blinding as described in Section 10 of [TimingAttacks]. Failure to apply such mitigations can lead to side-channel attacks that leak the private signing key.

Moreover, we assume that the server does not initiate the protocol and therefore has no knowledge of when the Prepare and Blind operations take place. If this were not the case, additional side-channel mitigations might be required to prevent timing side channels through Prepare and Blind.

Beyond timing side channels, [FAULTS] describes the importance of implementation safeguards that protect against fault attacks that can also leak the private signing key. These safeguards require that implementations check that the result of the private key operation when signing is correct, i.e., given s = RSASP1(sk, m), verify that m = RSAVP1(pk, s), as is required by BlindSign. Applying this (or an equivalent) safeguard is necessary to mitigate fault attacks, even for implementations that are not based on the Chinese remainder theorem.

7.2. Message Robustness

An essential property of blind signature protocols is that the signer learns nothing of the message being signed. In some circumstances, this may raise concerns regarding arbitrary signing oracles. Applications using blind signature protocols should take precautions to ensure that such oracles do not cause cross-protocol attacks. Ensuring that the signing key used for RSABSSA is distinct from other protocols prevents such cross-protocol attacks.

An alternative solution to this problem of message blindness is to give signers proof that the message being signed is well structured. Depending on the application, zero-knowledge proofs could be useful for this purpose. Defining such proofs is out of scope for this document.

Verifiers should check that, in addition to signature validity, the signed message is well structured for the relevant application. For example, if an application of this protocol requires messages to be structures of a particular form, then verifiers should check that messages adhere to this form.

7.3. Message Entropy

As discussed in [Lys22], a malicious signer can construct an invalid public key and use it to learn information about low-entropy input messages. Note that some invalid public keys may not yield valid signatures when run with the protocol, e.g., because the signature fails to verify. However, if an attacker can coerce the client to use these invalid public keys with low-entropy inputs, they can learn information about the client inputs before the protocol completes.

A client that uses this protocol might be vulnerable to attack from a malicious signer unless it is able to ensure that one of the following conditions is satisfied:

(1) The client has proof that the signer's public key is honestly generated. [GRSB19] presents some (non-interactive) honest-verifier zero-knowledge proofs of various statements about the public key.

(2) The input message has a value that the signer is unable to guess. That is, the client has added a high-entropy component that was not available to the signer prior to them choosing their signing key.

The named variants that use the PrepareRandomize function -- RSABSSA-SHA384-PSS-Randomized and RSABSSA-SHA384-PSSZERO-Randomized -- explicitly inject fresh entropy alongside each message to satisfy condition (2). As such, these variants are safe for all application use cases. In contrast, the named variants that use the PrepareIdentity function do not inject fresh entropy and therefore could be a problem with low-entropy inputs.

Note that these variants effectively mean that the resulting signature is always randomized. As such, this interface is not suitable for applications that require deterministic signatures.

7.4. Randomness Generation

All random values in the protocol, including the salt, message randomizer prefix (msg_prefix; see Appendix A), and random blind value in Blind, MUST be generated from a cryptographically secure random number generator [RFC4086]. If these values are not generated randomly or are otherwise constructed maliciously, it might be possible for them to encode information that is not present in the signed message. For example, the PSS salt might be maliciously constructed to encode the local IP address of the client. As a result, implementations SHOULD NOT allow clients to provide these values directly.

Note that malicious implementations could also encode client information in the message being signed, but since clients can verify the resulting message signature using the public key, this can be detected.

7.5. Key Substitution Attacks

RSA is well known for permitting key substitution attacks, wherein an attacker generates a key pair (skA, pkA) that verifies some known (message, signature) pair produced under a different (sk, pk) key pair [WM99]. This means it may be possible for an attacker to use a (message, signature) pair from one context in another. Entities that verify signatures must take care to ensure that a (message, signature) pair verifies with a valid public key from the expected issuer.

7.6. Alternative RSA Encoding Functions

This document uses PSS encoding as specified in [RFC8017] for a number of reasons. First, it is recommended in recent standards, including TLS 1.3 [RFC8446], X.509 [RFC4055], and even PKCS #1 itself. According to [RFC8017], "Although no attacks are known against RSASSA-PKCS1-v1_5, in the interest of increased robustness, RSASSA-PSS is **REQUIRED** in new applications." While RSA-

PSS is more complex than RSASSA-PKCS1-v1_5 encoding, ubiquity of RSA-PSS support influenced the design decision in this document, despite PKCS #1 v1.5 having equivalent security properties for digital signatures [JKM18].

Full Domain Hash (FDH) encoding [RSA-FDH] is also possible. This variant provides security equivalent to that of PSS [KK18]. However, FDH is less standard and is not used widely in related technologies. Moreover, FDH is deterministic, whereas PSS supports deterministic and probabilistic encodings.

7.7. Post-Quantum Readiness

The blind signature protocol specified in this document is not post-quantum ready, since it is based on RSA. Shor's polynomial-time factorization algorithm readily applies.

8. IANA Considerations

This document has no IANA actions.

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Appendix A. Test Vectors

This section includes test vectors for the blind signature protocol defined in Section 4. The following parameters are specified for each test vector:

p, q, n, e, d:

RSA private and public key (sk and pk) parameters, each encoded as a hexadecimal string.

msg:

Input message being signed, encoded as a hexadecimal string. The hash is computed using SHA-384.

msg_prefix:

Message randomizer prefix, encoded as a hexadecimal string. This is only present for variants that use the randomization preparation function.

prepared_msg:

The message actually signed. If the variant does not use the randomization preparation function, this is equal to msg.

salt:

Randomly generated salt used when computing the signature. The length is either 48 or 0 bytes.

encoded_msg:

EMSA-PSS encoded message. The mask generation function is MGF1 with SHA-384.

inv:

The message blinding inverse, encoded as a hexadecimal string.

blinded_msg, blind_sig:

The protocol values exchanged during the computation, encoded as hexadecimal strings.

sig:

The output message signature.

A.1. RSABSSA-SHA384-PSS-Randomized Test Vector

 $\begin{array}{ll} p = e1f4d7a34802e27c7392a3cea32a262a34dc3691bd87f3f310dc756734889305\\ 59c120fd0410194fb8a0da55bd0b81227e843fdca6692ae80e5a5d414116d4803fca\\ 7d8c30eaaae57e44a1816ebb5c5b0606c536246c7f11985d731684150b63c9a3ad9e\\ 41b04c0b5b27cb188a692c84696b742a80d3cd00ab891f2457443dadfeba6d6daf10\\ 8602be26d7071803c67105a5426838e6889d77e8474b29244cefaf418e381b312048\\ b457d73419213063c60ee7b0d81820165864fef93523c9635c22210956e53a8d9632\\ 2493ffc58d845368e2416e078e5bcb5d2fd68ae6acfa54f9627c42e84a9d3f277401\\ 7e32ebca06308a12ecc290c7cd1156dcccfb2311 \end{array}$

 $\begin{array}{ll} q = c601a9caea66dc3835827b539db9df6f6f5ae77244692780cd334a006ab353c8\\ 06426b60718c05245650821d39445d3ab591ed10a7339f15d83fe13f6a3dfb20b945\\ 2c6a9b42eaa62a68c970df3cadb2139f804ad8223d56108dfde30ba7d367e9b0a7a8\\ 0c4fdba2fd9dde6661fc73fc2947569d2029f2870fc02d8325acf28c9afa19ecf962\\ daa7916e21afad09eb62fe9f1cf91b77dc879b7974b490d3ebd2e95426057f35d0a3\\ c9f45f79ac727ab81a519a8b9285932d9b2e5ccd347e59f3f32ad9ca359115e7da00\\ 8ab7406707bd0e8e185a5ed8758b5ba266e8828f8d863ae133846304a2936ad7bc7c\\ 9803879d2fc4a28e69291d73dbd799f8bc238385 \end{array}$

n = aec4d69addc70b990ea66a5e70603b6fee27aafebd08f2d94cbe1250c556e047a928d635c3f45ee9b66d1bc628a03bac9b7c3f416fe20dabea8f3d7b4bbf7f963be3 35d2328d67e6c13ee4a8f955e05a3283720d3e1f139c38e43e0338ad058a9495c533 77fc35be64d208f89b4aa721bf7f7d3fef837be2a80e0f8adf0bcd1eec5bb040443a 2b2792fdca522a7472aed74f31a1ebe1eebc1f408660a0543dfe2a850f106a617ec6 685573702eaaa21a5640a5dcaf9b74e397fa3af18a2f1b7c03ba91a6336158de420d 63188ee143866ee415735d155b7c2d854d795b7bc236cffd71542df34234221a0413 e142d8c61355cc44d45bda94204974557ac2704cd8b593f035a5724b1adf442e78c5 42cd4414fce6f1298182fb6d8e53cef1adfd2e90e1e4deec52999bdc6c29144e8d52 a125232c8c6d75c706ea3cc06841c7bda33568c63a6c03817f722b50fcf898237d78 8a4400869e44d90a3020923dc646388abcc914315215fcd1bae11b1c751fd52443aa c8f601087d8d42737c18a3fa11ecd4131ecae017ae0a14acfc4ef85b83c19fed33cf d1cd629da2c4c09e222b398e18d822f77bb378dea3cb360b605e5aa58b20edc29d00 0a66bd177c682a17e7eb12a63ef7c2e4183e0d898f3d6bf567ba8ae84f84f1d23bf8 b8e261c3729e2fa6d07b832e07cddd1d14f55325c6f924267957121902dc19b3b329 48bdead5

e = 010001

d = 0d43242aefe1fb2c13fbc66e20b678c4336d20b1808c558b6e62ad16a2870771 80b177e1f01b12f9c6cd6c52630257ccef26a45135a990928773f3bd2fc01a313f1d ac97a51cec71cb1fd7efc7adffdeb05f1fb04812c924ed7f4a8269925dad88bd7dcf bc4ef01020ebfc60cb3e04c54f981fdbd273e69a8a58b8ceb7c2d83fbcbd6f784d05 2201b88a9848186f2a45c0d2826870733e6fd9aa46983e0a6e82e35ca20a439c5ee7 b502a9062e1066493bdadf8b49eb30d9558ed85abc7afb29b3c9bc644199654a4676 681af4babcea4e6f71fe4565c9c1b85d9985b84ec1abf1a820a9bbebee0df1398aae 2c85ab580a9f13e7743afd3108eb32100b870648fa6bc17e8abac4d3c99246b1f0ea 9f7f93a5dd5458c56d9f3f81ff2216b3c3680a13591673c43194d8e6fc93fc1e37ce 2986bd628ac48088bc723d8fbe293861ca7a9f4a73e9fa63b1b6d0074f5dea2a624c 5249ff3ad811b6255b299d6bc5451ba7477f19c5a0db690c3e6476398b1483d10314 afd38bbaf6e2fbdbcd62c3ca9797a420ca6034ec0a83360a3ee2adf4b9d4ba29731d 131b099a38d6a23cc463db754603211260e99d19affc902c915d7854554aabf608e3 ac52c19b8aa26ae042249b17b2d29669b5c859103ee53ef9bdc73ba3c6b537d5c34b 6d8f034671d7f3a8a6966cc4543df223565343154140fd7391c7e7be03e241f4ecfe b877a051

 $\label{eq:msg} \begin{array}{ll} \text{msg} &= 8 \text{f} 3 \text{d} \text{c} 6 \text{f} b 8 \text{c} 4 \text{a} 02 \text{f} 4 \text{d} 6352 \text{e} \text{d} f 0907822 \text{c} 1210 \text{a} 9 \text{b} 32 \text{f} 9 \text{b} \text{d} \text{d} 4 \text{c} 45 \text{a} 698 \text{c} 80023 \text{a} \\ \text{a} 6 \text{b} 59 \text{f} 8 \text{c} \text{f} \text{e} \text{c} 5 \text{f} \text{d} \text{b} \text{b} 36331372 \text{e} \text{b} \text{e} \text{f} \text{e} \text{d} \text{a} \text{e} 7 \text{d} \\ \end{array}$

msg_prefix = 8417e699b219d583fb6216ae0c53ca0e9723442d02f1d1a34295527e7d929e8b

prepared_msg = 8417e699b219d583fb6216ae0c53ca0e9723442d02f1d1a342955
27e7d929e8b8f3dc6fb8c4a02f4d6352edf0907822c1210a9b32f9bdda4c45a698c8
0023aa6b59f8cfec5fdbb36331372ebefedae7d

 $\verb|salt| = 051722b35f458781397c3a671a7d3bd3096503940e4c4f1aaa269d60300ce \\ 449555cd7340100df9d46944c5356825abf \\$

 $encoded_msg = 2be01c5669eb676cb3f0002eb636427d61568f3f0579da5b998279$ a7eb3ab784e5617319376d04809d83e72bef9f0738e7324af3fd1b4f0a35f4f58058 ab329495406bdb5ff31a0274be2d137c735ab0d5a591b3129a6cc46fcecc4b41dbc6 84c965cb30e3eb4864ef18cc8d95b4d6a2002607c821d4d8a7e026ae7bb1f6b4c7c9 3d1b58e9cd87864d6094b0d8f7e2b5f966473703634fb58c774dd4a24376e0eb262a 24b58e3a0b4da4f36ef75651627561ff2ecee9dcbfe1d728cc31a7b46030f7a2815a e9edf9a2a5c0c6d8dbab1b33b9c3bbda5c083670a3550f7d74c4263aad09f8ed1d43 5fc6295ca4d51fc02c7de9ae28ffd53372c3fa864521b27560daa11ab9daad8d0d74 7661718d2f79c59d0661b09c74863fa32bdcb1c408d3bd24569c57aecae6e06c0c9d eb7303c5b7b1240960fd2413d61b2e3829af8c09874fdba0fe84ca6aa7e7d533f9b0 ddfe508f562b132ca2d325f1e73f91a8a6b831a2fd9bc0bd5bfa5ea3a1dee16bd9b2 64174b9553a4c0c0d62373353355c05b35824e4bae702f49e5a6bf83eaff65af4990 45bcef1470a0e58ddb21856034af0db96f8636d4a6f1591f34c7224e0c0293e3d3be 2139f2797c5ed8b65473ac2f83c52b87f8cf8754ac2f55f5e41e105df1d079a647fb 1aa591526295667f37db1129752d024eb03bfe506a43665072118423351ef9b86633 76f9fc073141e1e7bc

inv = 80682c48982407b489d53d1261b19ec8627d02b8cda5336750b8cee332ae26 0de57b02d72609c1e0e9f28e2040fc65b6f02d56dbd6aa9af8fde656f70495dfb723 ba01173d4707a12fddac628ca29f3e32340bd8f7ddb557cf819f6b01e445ad96f874 ba235584ee71f6581f62d4f43bf03f910f6510deb85e8ef06c7f09d9794a008be7ff 2529f0ebb69decef646387dc767b74939265fec0223aa6d84d2a8a1cc912d5ca25b4 e144ab8f6ba054b54910176d5737a2cff011da431bd5f2a0d2d66b9e70b39f4b050e 45c0d9c16f02deda9ddf2d00f3e4b01037d7029cd49c2d46a8e1fc2c0c17520af1f4 b5e25ba396afc4cd60c494a4c426448b35b49635b337cfb08e7c22a39b256dd032c0 0adddafb51a627f99a0e1704170ac1f1912e49d9db10ec04c19c58f420212973e0cb 329524223a6aa56c7937c5dffdb5d966b6cd4cbc26f3201dd25c80960a1a111b3294 7bb78973d269fac7f5186530930ed19f68507540eed9e1bab8b00f00d8ca09b3f099 aae46180e04e3584bd7ca054df18a1504b89d1d1675d0966c4ae1407be325cdf623c f13ff13e4a28b594d59e3eadbadf6136eee7a59d6a444c9eb4e2198e8a974f27a39e b63af2c9af3870488b8adaad444674f512133ad80b9220e09158521614f1faadfe85 05ef57b7df6813048603f0dd04f4280177a11380fbfc861dbcbd7418d62155248dad 5fdec0991f

blinded_msg = aa3ee045138d874669685ffaef962c7694a9450aa9b4fd6465db9b 3b75a522bb921c4c0fdcdfae9667593255099cff51f5d3fd65e8ffb9d3b3036252a6 b51b6edfb3f40382b2bbf34c0055e4cbcc422850e586d84f190cd449af11dc65545f 5fe26fd89796eb87da4bda0c545f397cddfeeb56f06e28135ec74fd477949e7677f6 f36cfae8fd5c1c5898b03b9c244cf6d1a4fb7ad1cb43aff5e80cb462fac541e72f67 f0a50f1843d1759edfaae92d1a916d3f0efaf4d650db416c3bf8abdb5414a78cebc9 7de676723cb119e77aea489f2bbf530c440ebc5a75dccd3ebf5a412a5f346badd61b ee588e5917bdcce9dc33c882e39826951b0b8276c6203971947072b726e935816056 ff5cb11a71ca2946478584126bb877acdf87255f26e6cca4e0878801307485d3b7bb 89b289551a8b65a7a6b93db010423d1406e149c87731910306e5e410b41d4da32346 24e74f92845183e323cf7eb244f212a695f8856c675fbc3a021ce649e22c6f0d053a 9d238841cf3afdc2739f99672a419ae13c17f1f8a3bc302ec2e7b98e8c353898b715 0ad8877ec841ea6e4b288064c254fefd0d049c3ad196bf7ffa535e74585d0120ce72 8036ed500942fbd5e6332c298f1ffebe9ff60c1e117b274cf0cb9d70c36ee4891528 996ec1ed0b178e9f3c0c0e6120885f39e8ccaadbb20f3196378c07b1ff22d10049d3 039a7a92fe7efdd95d

blind_sig = 3f4a79eacd4445fca628a310d41e12fcd813c4d43aa4ef2b81226953 248d6d00adfee6b79cb88bfa1f99270369fd063c023e5ed546719b0b2d143dd1bca4 6b0e0e615fe5c63d95c5a6b873b8b50bc52487354e69c3dfbf416e7aca18d5842c89 b676efdd38087008fa5a810161fcdec26f20ccf2f1e6ab0f9d2bb93e051cb9e86a9b 28c5bb62fd5f5391379f887c0f706a08bcc3b9e7506aaf02485d688198f5e22eefdf 837b2dd919320b17482c5cc54271b4ccb41d267629b3f844fd63750b01f5276c79e3 3718bb561a152acb2eb36d8be75bce05c9d1b94eb609106f38226fb2e0f5cd5c5c39 c59dda166862de498b8d92f6bcb41af433d65a2ac23da87f39764cb64e79e74a8f4c e4dd567480d967cefac46b6e9c06434c3715635834357edd2ce6f105eea854ac126c cfa3de2aac5607565a4e5efaac5eed491c335f6fc97e6eb7e9cea3e12de38dfb3152 20c0a3f84536abb2fdd722813e083feda010391ac3d8fd1cd9212b5d94e634e69ebc c800c4d5c4c1091c64afc37acf563c7fc0a6e4c082bc55544f50a7971f3fb97d5853 d72c3af34ffd5ce123998be5360d1059820c66a81e1ee6d9c1803b5b62af6bc87752 6df255b6d1d835d8c840bebbcd6cc0ee910f17da37caf8488afbc08397a1941fcc79 e76a5888a95b3d5405e13f737bea5c78d716a48eb9dc0aec8de39c4b45c6914ad4a8 185969f70b1adf46

sig = 191e941c57510e22d29afad257de5ca436d2316221fe870c7cb75205a6c071c2735aed0bc24c37f3d5bd960ab97a829a508f966bbaed7a82645e65eadaf24ab5e6 d9421392c5b15b7f9b640d34fec512846a3100b80f75ef51064602118c1a77d28d93 8f6efc22041d60159a518d3de7c4d840c9c68109672d743d299d8d2577ef60c19ab4 63c716b3fa75fa56f5735349d414a44df12bf0dd44aa3e10822a651ed4cb0eb6f47c 9bd0ef14a034a7ac2451e30434d513eb22e68b7587a8de9b4e63a059d05c8b22c7c5 1e2cfee2d8bef511412e93c859a13726d87c57d1bc4c2e68ab121562f839c3a3d233 e87ed63c69b7e57525367753fbebcc2a9805a2802659f5888b2c69115bf865559f10 d906c09d048a0d71bfee4b33857393ec2b69e451433496d02c9a7910abb954317720 bbde9e69108eafc3e90bad3d5ca4066d7b1e49013fa04e948104a1dd82b12509ecb1 46e948c54bd8bfb5e6d18127cd1f7a93c3cf9f2d869d5a78878c03fe808a0d799e91 0be6f26d18db61c485b303631d3568368fc41986d08a95ea6ac0592240c19d7b2241 6b9c82ae6241e211dd5610d0baaa9823158f9c32b66318f5529491b7eeadcaa71898 a63bac9d95f4aa548d5e97568d744fc429104e32edd9c87519892a198a30d333d427 739ffb9607b092e910ae37771abf2adb9f63bc058bf58062ad456cb934679795bbdf cdfad5e0f2

A.2. RSABSSA-SHA384-PSSZERO-Randomized Test Vector

 $\begin{array}{ll} p = e1f4d7a34802e27c7392a3cea32a262a34dc3691bd87f3f310dc756734889305\\ 59c120fd0410194fb8a0da55bd0b81227e843fdca6692ae80e5a5d414116d4803fca\\ 7d8c30eaaae57e44a1816ebb5c5b0606c536246c7f11985d731684150b63c9a3ad9e\\ 41b04c0b5b27cb188a692c84696b742a80d3cd00ab891f2457443dadfeba6d6daf10\\ 8602be26d7071803c67105a5426838e6889d77e8474b29244cefaf418e381b312048 \end{array}$

b457d73419213063c60ee7b0d81820165864fef93523c9635c22210956e53a8d96322493ffc58d845368e2416e078e5bcb5d2fd68ae6acfa54f9627c42e84a9d3f2774017e32ebca06308a12ecc290c7cd1156dcccfb2311

 $\begin{array}{ll} q = c601a9caea66dc3835827b539db9df6f6f5ae77244692780cd334a006ab353c8\\ 06426b60718c05245650821d39445d3ab591ed10a7339f15d83fe13f6a3dfb20b945\\ 2c6a9b42eaa62a68c970df3cadb2139f804ad8223d56108dfde30ba7d367e9b0a7a8\\ 0c4fdba2fd9dde6661fc73fc2947569d2029f2870fc02d8325acf28c9afa19ecf962\\ daa7916e21afad09eb62fe9f1cf91b77dc879b7974b490d3ebd2e95426057f35d0a3\\ c9f45f79ac727ab81a519a8b9285932d9b2e5ccd347e59f3f32ad9ca359115e7da00\\ 8ab7406707bd0e8e185a5ed8758b5ba266e8828f8d863ae133846304a2936ad7bc7c\\ 9803879d2fc4a28e69291d73dbd799f8bc238385 \end{array}$

n = aec4d69addc70b990ea66a5e70603b6fee27aafebd08f2d94cbe1250c556e047a928d635c3f45ee9b66d1bc628a03bac9b7c3f416fe20dabea8f3d7b4bbf7f963be3 35d2328d67e6c13ee4a8f955e05a3283720d3e1f139c38e43e0338ad058a9495c533 77fc35be64d208f89b4aa721bf7f7d3fef837be2a80e0f8adf0bcd1eec5bb040443a 2b2792fdca522a7472aed74f31a1ebe1eebc1f408660a0543dfe2a850f106a617ec6 685573702eaaa21a5640a5dcaf9b74e397fa3af18a2f1b7c03ba91a6336158de420d 63188ee143866ee415735d155b7c2d854d795b7bc236cffd71542df34234221a0413 e142d8c61355cc44d45bda94204974557ac2704cd8b593f035a5724b1adf442e78c5 42cd4414fce6f1298182fb6d8e53cef1adfd2e90e1e4deec52999bdc6c29144e8d52 a125232c8c6d75c706ea3cc06841c7bda33568c63a6c03817f722b50fcf898237d78 8a4400869e44d90a3020923dc646388abcc914315215fcd1bae11b1c751fd52443aa c8f601087d8d42737c18a3fa11ecd4131ecae017ae0a14acfc4ef85b83c19fed33cf d1cd629da2c4c09e222b398e18d822f77bb378dea3cb360b605e5aa58b20edc29d00 0a66bd177c682a17e7eb12a63ef7c2e4183e0d898f3d6bf567ba8ae84f84f1d23bf8 b8e261c3729e2fa6d07b832e07cddd1d14f55325c6f924267957121902dc19b3b329 48bdead5

e = 010001

d = 0d43242aefe1fb2c13fbc66e20b678c4336d20b1808c558b6e62ad16a287077180b177e1f01b12f9c6cd6c52630257ccef26a45135a990928773f3bd2fc01a313f1d ac97a51cec71cb1fd7efc7adffdeb05f1fb04812c924ed7f4a8269925dad88bd7dcf bc4ef01020ebfc60cb3e04c54f981fdbd273e69a8a58b8ceb7c2d83fbcbd6f784d05 2201b88a9848186f2a45c0d2826870733e6fd9aa46983e0a6e82e35ca20a439c5ee7 b502a9062e1066493bdadf8b49eb30d9558ed85abc7afb29b3c9bc644199654a4676 681af4babcea4e6f71fe4565c9c1b85d9985b84ec1abf1a820a9bbebee0df1398aae 2c85ab580a9f13e7743afd3108eb32100b870648fa6bc17e8abac4d3c99246b1f0ea 9f7f93a5dd5458c56d9f3f81ff2216b3c3680a13591673c43194d8e6fc93fc1e37ce 2986bd628ac48088bc723d8fbe293861ca7a9f4a73e9fa63b1b6d0074f5dea2a624c 5249ff3ad811b6255b299d6bc5451ba7477f19c5a0db690c3e6476398b1483d10314 afd38bbaf6e2fbdbcd62c3ca9797a420ca6034ec0a83360a3ee2adf4b9d4ba29731d 131b099a38d6a23cc463db754603211260e99d19affc902c915d7854554aabf608e3 ac52c19b8aa26ae042249b17b2d29669b5c859103ee53ef9bdc73ba3c6b537d5c34b 6d8f034671d7f3a8a6966cc4543df223565343154140fd7391c7e7be03e241f4ecfe b877a051

 $\label{eq:msg} \mbox{ = 8f3dc6fb8c4a02f4d6352edf0907822c1210a9b32f9bdda4c45a698c80023aa6b59f8cfec5fdbb36331372ebefedae7d}$

msg_prefix = 84ea86c8cf3beedfed73beceabd792027c609d1100bf041fdd60d826a718130d

prepared_msg = 84ea86c8cf3beedfed73beceabd792027c609d1100bf041fdd60d 826a718130d8f3dc6fb8c4a02f4d6352edf0907822c1210a9b32f9bdda4c45a698c8 0023aa6b59f8cfec5fdbb36331372ebefedae7d

salt =

encoded_msg = 37f4ea66054b3570f2c46f43125a8df8d751a81db1003edcc70e98 88cb3d0fa71bb7634437a779c1bf9e84e88b3479894490ee41cd69fc8e911478326f e8460d1699f96abedde22ba0ba25a02f78bae77eb039decd41e6cd40fecc28f301c9 4d5644eb3e55b316569e2bec3ccf8e33b06eb6defca5fe672613d33ea60f84daa560 ded4c1c5e65613fb19e090d0fc96a1394e29dfad6a7644362bf30bdc90c7ca0a0651 90f5a099b5c33ae787b872518a724d9aa139229656eb21053bbe86c38f6d03b4c6fa 37a900935d9b8d19e0c394be4af6af028680996e3fd533b6698ce9e2ed6a9f96d4d3a682027ae5240040e55d75017dc303b7142c1f7e17b79778a94431398d21dc0cc7ae454cc0d6cf4db4d588d3fd15fd7f71576052fd2a52d688f99790dfb13808ecb24b6b9e9a43a8c0105670ec3ad8d6318a9c6a9cef9eb99b36d74b8e83dbacf6e8100e135b609850b34a4b01091b263678d7cd9905af2ffda801a2888d863a25211903b43cb5e59f5dba6bc18713ce4f028f1774c593664912f1d181d4544a13a1da354332d8595f59cf5af260a8aaf21a6bc948b5d5d4a520c1f72c216259dc12a33c2a3bd4d32ff2bf3de2ffe76e51f8af030b40fadc5899e740da20be1dd5a50f701292ceaee51fa35d9a047f3efc6543dc583fb3f23abeade39c2a5b5b352de26d7a11267435be7bffa8f2292e139fad923dbaf863bc

inv = 80682c48982407b489d53d1261b19ec8627d02b8cda5336750b8cee332ae26 0de57b02d72609c1e0e9f28e2040fc65b6f02d56dbd6aa9af8fde656f70495dfb723 ba01173d4707a12fddac628ca29f3e32340bd8f7ddb557cf819f6b01e445ad96f874 ba235584ee71f6581f62d4f43bf03f910f6510deb85e8ef06c7f09d9794a008be7ff 2529f0ebb69decef646387dc767b74939265fec0223aa6d84d2a8a1cc912d5ca25b4 e144ab8f6ba054b54910176d5737a2cff011da431bd5f2a0d2d66b9e70b39f4b050e 45c0d9c16f02deda9ddf2d00f3e4b01037d7029cd49c2d46a8e1fc2c0c17520af1f4 b5e25ba396afc4cd60c494a4c426448b35b49635b337cfb08e7c22a39b256dd032c0 0adddafb51a627f99a0e1704170ac1f1912e49d9db10ec04c19c58f420212973e0cb 329524223a6aa56c7937c5dffdb5d966b6cd4cbc26f3201dd25c80960a1a111b3294 7bb78973d269fac7f5186530930ed19f68507540eed9e1bab8b00f00d8ca09b3f099 aae46180e04e3584bd7ca054df18a1504b89d1d1675d0966c4ae1407be325cdf623c f13ff13e4a28b594d59e3eadbadf6136eee7a59d6a444c9eb4e2198e8a974f27a39e b63af2c9af3870488b8adaad444674f512133ad80b9220e09158521614f1faadfe85 05ef57b7df6813048603f0dd04f4280177a11380fbfc861dbcbd7418d62155248dad 5fdec0991f

blinded_msg = 4c1b82d9b97b968b2ce0754e326abd49e3d723ed937d84bead34b6 a834483b43d510bf62ca47683ed366d94d3d357b270a85cf2cc2ddd171141b45d754 9d5373cf67d14f6f462c14ebded906793144faba37f129c0f3172854ec0f854e5555 52eec5a30c87788f1039814594f04348709e26a883be82affff207b1886b75c037f4 3f847f45d89bcbf210c22ffcdf8118ce8a526b3723e6209c26319f8f5d2adcf0b637 031c9fdf53470a915c587e30287ba88ed4f1cd5e93cf3d4990acf31fffdbfddec80a e0b728d5b4c612a396fd81acaa65566a4dc1c24624f44fd10cdba05f3d0bed2e69bba05f4d0bed2e69bba05f4d0bed2e69bba05f4d0bed2e69bba05f4d0bed2e69bba05f4d0bed2e69bba05f4d0b0d13d41a9f1b4e67aa566520778733ced5e6260f4d1982f63bb835442acffe3cb87f 5f8ec6bb84226e0eab787159d08e57604b13557ceea97f2c4ad0631accf898f302df 86f0b64354ec0b3bdf1b4e2a4deb4d38f655ea8d80de4cc19aa06ffcd56e348faf89 4c8774c53235ddcc152d80cf66b417eee4d182781bab8c979937a3c7502d8f39c57c 4f09884de5a7247f2539910a96e4b15f9a3df88edc21a13030af357467a99dca50db a4afe4a6185a240ac8f1d8aab2e83443025f94e1af930f56f78661369cc6790701f3 1b83aec40f96a72c7f7ba13b4ebdd8e24e7351f4ffba0a7c072cb28f13aff06cd023 68491044fcc536213b2e3b1cf6ca81cf2097b7b19d2b36bd246f390f53768f1c2e56 113ea91b33c7cfa647

blind_sig = 4894f64d7214c216282d9842cbf7e7cccd9c0dcb1f4294a6bdeccd4c 4c2446160d7cac7892f01b70dfa69f533891d2fbb447f7cf7541d1b504a2d46fc1bb 6de26b345972aada8ebce280b906f3a10a13208f77ef896fbe6bc4504327fd4c5c8f 03211d45ae9672e9f4be0f4900762ba2a7177a58b90d6dd1263faf2b7a5f15d50a7b 00e733742c1b6a1ea4eb5fbfb407abf14496ab26b50cf1a5a56dea616b7a6a559577 7400571a751c682b9fdd6badb3f72292f314f4ba2ba0f394f91676a4bb12e60ea08c 977f7082be6357c1ca82fe3301fe5fb4128609bee2410db0481aea3a5737fb0bce93 81272c2202644f662e99f64bf1190d66e230cc0371ec33fe32fe725dfd872041914d 39462a909414a780c9aab394af443199eba56c83986d22d57d4421b41ff8e5bec537 d271223adb34d26c64989048a88d8f352a06a7cc153e216a6bed9548bb38d2a1600b 2f3403289df6df74aec525ef9e413b7140a7c1a914dedd74a336f1beed39a8e5e2ce f76cac094df0dbb3fa55d4b7ee781c74bed3bd8bc7aa6ef3f1dbfa4674945720ec93 dafa6d0650229ab75e3fae687327fac081cf4bb376e02a2b73314c54c12f88572c28 980f13aba5731bc5a3a60575ea116c8ea2fe5009168deb1255026c9310783ff7f644 255d3e1691e194db1babd7780b9a5dc0cb3de2b700d12f49cbe4db51ca2f3c8a58b0 9e854cc71e8070ab

sig = 195363ba25e4bf763f6538c86865785f93f4ea6092da3ad200d41b99eb0eb0869fa792df619fd8fa5923d5d03d5882faae6d25054118deef5e4a6a252dd5afb0da c262b74c391090b1575fbafd959d26bc294f47fb45a2c1c209932c4f94b24394eded 91fbdd015e1a85dde63c9e77a0283f812cad1192d86432c51331e46fd4f3771bbafb 929f847a19cb05e5f79b6b519d67e8f005951e53656be97cb612d2f506618b366403 b34648451d6fbc7318c2f3f583cc6fa17bf2108398f9284e0602187904406a9322f1 e7b8016ca9ad11b835756df862c465c420535e25faa48bf341f7ee8192be47fa8757 91f32f56d5e631d237060688f052426dee5b0b2b74ca5f830e82a453379eedb541fa 4fcdaa19dae6509401e3cdd4c40f5c9243db3f6d7115c4e8cd6db8290723ab01d9d0 d7e355a97a01547800e43f11736668c3f8908848d759c33a67a2f506abc3f6871cbe 625b1bc71eb06d785a59501396712c581a60d6ccc450d2f4eb4cf08ae0dbfa45c286 0425be90cc4cd4c989495bbd2963e19c59ae5d90d1ca884e80d654b5f2cd6a80c358 8b514ee91c802736f594c340397b316a97e9c70b0609955b6c3ee06f4760d9377f07 97a0411a244db395bb8b711ef79fbcb5589226174029be79a72dcd6f4ca566b7b1b9 a27e43b5c02a9a579d60bdda183398d66d76e0e8eceb1af2f27633589d043bcdc041 683b31f7f1

A.3. RSABSSA-SHA384-PSS-Deterministic Test Vector

 $\begin{array}{ll} p = e1f4d7a34802e27c7392a3cea32a262a34dc3691bd87f3f310dc756734889305\\ 59c120fd0410194fb8a0da55bd0b81227e843fdca6692ae80e5a5d414116d4803fca\\ 7d8c30eaaae57e44a1816ebb5c5b0606c536246c7f11985d731684150b63c9a3ad9e\\ 41b04c0b5b27cb188a692c84696b742a80d3cd00ab891f2457443dadfeba6d6daf10\\ 8602be26d7071803c67105a5426838e6889d77e8474b29244cefaf418e381b312048\\ b457d73419213063c60ee7b0d81820165864fef93523c9635c22210956e53a8d9632\\ 2493ffc58d845368e2416e078e5bcb5d2fd68ae6acfa54f9627c42e84a9d3f277401\\ 7e32ebca06308a12ecc290c7cd1156dcccfb2311 \end{array}$

 $\begin{array}{ll} q = c601a9caea66dc3835827b539db9df6f6f5ae77244692780cd334a006ab353c8\\ 06426b60718c05245650821d39445d3ab591ed10a7339f15d83fe13f6a3dfb20b945\\ 2c6a9b42eaa62a68c970df3cadb2139f804ad8223d56108dfde30ba7d367e9b0a7a8\\ 0c4fdba2fd9dde6661fc73fc2947569d2029f2870fc02d8325acf28c9afa19ecf962\\ daa7916e21afad09eb62fe9f1cf91b77dc879b7974b490d3ebd2e95426057f35d0a3\\ c9f45f79ac727ab81a519a8b9285932d9b2e5ccd347e59f3f32ad9ca359115e7da00\\ 8ab7406707bd0e8e185a5ed8758b5ba266e8828f8d863ae133846304a2936ad7bc7c\\ 9803879d2fc4a28e69291d73dbd799f8bc238385 \end{array}$

n = aec4d69addc70b990ea66a5e70603b6fee27aafebd08f2d94cbe1250c556e047a928d635c3f45ee9b66d1bc628a03bac9b7c3f416fe20dabea8f3d7b4bbf7f963be3 35d2328d67e6c13ee4a8f955e05a3283720d3e1f139c38e43e0338ad058a9495c533 77fc35be64d208f89b4aa721bf7f7d3fef837be2a80e0f8adf0bcd1eec5bb040443a 2b2792fdca522a7472aed74f31a1ebe1eebc1f408660a0543dfe2a850f106a617ec6 685573702eaaa21a5640a5dcaf9b74e397fa3af18a2f1b7c03ba91a6336158de420d 63188ee143866ee415735d155b7c2d854d795b7bc236cffd71542df34234221a0413 e142d8c61355cc44d45bda94204974557ac2704cd8b593f035a5724b1adf442e78c5 42cd4414fce6f1298182fb6d8e53cef1adfd2e90e1e4deec52999bdc6c29144e8d52 a125232c8c6d75c706ea3cc06841c7bda33568c63a6c03817f722b50fcf898237d78 8a4400869e44d90a3020923dc646388abcc914315215fcd1bae11b1c751fd52443aa c8f601087d8d42737c18a3fa11ecd4131ecae017ae0a14acfc4ef85b83c19fed33cf d1cd629da2c4c09e222b398e18d822f77bb378dea3cb360b605e5aa58b20edc29d00 0a66bd177c682a17e7eb12a63ef7c2e4183e0d898f3d6bf567ba8ae84f84f1d23bf8 b8e261c3729e2fa6d07b832e07cddd1d14f55325c6f924267957121902dc19b3b329 48bdead5

e = 010001

 $\label{eq:defended} \begin{array}{ll} d = 0d43242aefe1fb2c13fbc66e20b678c4336d20b1808c558b6e62ad16a287077180b177e1f01b12f9c6cd6c52630257ccef26a45135a990928773f3bd2fc01a313f1dac97a51cec71cb1fd7efc7adffdeb05f1fb04812c924ed7f4a8269925dad88bd7dcfbc4ef01020ebfc60cb3e04c54f981fdbd273e69a8a58b8ceb7c2d83fbcbd6f784d05\\ \end{array}$

2201b88a9848186f2a45c0d2826870733e6fd9aa46983e0a6e82e35ca20a439c5ee7b502a9062e1066493bdadf8b49eb30d9558ed85abc7afb29b3c9bc644199654a4676681af4babcea4e6f71fe4565c9c1b85d9985b84ec1abf1a820a9bbebee0df1398aae2c85ab580a9f13e7743afd3108eb32100b870648fa6bc17e8abac4d3c99246b1f0ea9f7f93a5dd5458c56d9f3f81ff2216b3c3680a13591673c43194d8e6fc93fc1e37ce2986bd628ac48088bc723d8fbe293861ca7a9f4a73e9fa63b1b6d0074f5dea2a624c5249ff3ad811b6255b299d6bc5451ba7477f19c5a0db690c3e6476398b1483d10314afd38bbaf6e2fbdbcd62c3ca9797a420ca6034ec0a83360a3ee2adf4b9d4ba29731d131b099a38d6a23cc463db754603211260e99d19affc902c915d7854554aabf608e3ac52c19b8aa26ae042249b17b2d29669b5c859103ee53ef9bdc73ba3c6b537d5c34b6d8f034671d7f3a8a6966cc4543df223565343154140fd7391c7e7be03e241f4ecfeb877a051

msg = 8f3dc6fb8c4a02f4d6352edf0907822c1210a9b32f9bdda4c45a698c80023a a6b59f8cfec5fdbb36331372ebefedae7d

msg_prefix =

prepared_msg = 8f3dc6fb8c4a02f4d6352edf0907822c1210a9b32f9bdda4c45a6 98c80023aa6b59f8cfec5fdbb36331372ebefedae7d

salt = 051722b35f458781397c3a671a7d3bd3096503940e4c4f1aaa269d60300ce
449555cd7340100df9d46944c5356825abf

encoded_msg = 6e0c464d9c2f9fbc147b43570fc4f238e0d0b38870b3addcf7a421 7df912ccef17a7f629aa850f63a063925f312d61d6437be954b45025e8282f9c0b11 31bc8ff19a8a928d859b37113db1064f92a27f64761c181c1e1f9b251ae5a2f8a404 7573b67a270584e089beadcb13e7c82337797119712e9b849ff56e04385d144d3ca9 d8d92bf78adb20b5bbeb3685f17038ec6afade3ef354429c51c687b45a7018ee3a69 66b3af15c9ba8f40e6461ba0a17ef5a799672ad882bab02b518f9da7c1a962945c2e 9b0f02f29b31b9cdf3e633f9d9d2a22e96e1de28e25241ca7dd04147112f57897340 3e0f4fd80865965475d22294f065e17a1c4a201de93bd14223e6b1b999fd548f2f75 9f52db71964528b6f15b9c2d7811f2a0a35d534b8216301c47f4f04f412cae142b48 c4cdff78bc54df690fd43142d750c671dd8e2e938e6a440b2f825b6dbb3e19f1d7a3 c0150428a47948037c322365b7fe6fe57ac88d8f80889e9ff38177bad8c8d8d98db4 2908b389cb59692a58ce275aa15acb032ca951b3e0a3404b7f33f655b7c7d83a2f8d 1b6bbff49d5fcedf2e030e80881aa436db27a5c0dea13f32e7d460dbf01240c2320c 2bb5b3225b17145c72d61d47c8f84d1e19417ebd8ce3638a82d395cc6f7050b6209d 9283dc7b93fecc04f3f9e7f566829ac41568ef799480c733c09759aa9734e2013d76 40dc6151018ea902bc

inv = 80682c48982407b489d53d1261b19ec8627d02b8cda5336750b8cee332ae26 0de57b02d72609c1e0e9f28e2040fc65b6f02d56dbd6aa9af8fde656f70495dfb723 ba01173d4707a12fddac628ca29f3e32340bd8f7ddb557cf819f6b01e445ad96f874 ba235584ee71f6581f62d4f43bf03f910f6510deb85e8ef06c7f09d9794a008be7ff 2529f0ebb69decef646387dc767b74939265fec0223aa6d84d2a8a1cc912d5ca25b4 e144ab8f6ba054b54910176d5737a2cff011da431bd5f2a0d2d66b9e70b39f4b050e 45c0d9c16f02deda9ddf2d00f3e4b01037d7029cd49c2d46a8e1fc2c0c17520af1f4 b5e25ba396afc4cd60c494a4c426448b35b49635b337cfb08e7c22a39b256dd032c0 0adddafb51a627f99a0e1704170ac1f1912e49d9db10ec04c19c58f420212973e0cb 329524223a6aa56c7937c5dffdb5d966b6cd4cbc26f3201dd25c80960a1a111b3294 7bb78973d269fac7f5186530930ed19f68507540eed9e1bab8b00f00d8ca09b3f099 aae46180e04e3584bd7ca054df18a1504b89d1d1675d0966c4ae1407be325cdf623c f13ff13e4a28b594d59e3eadbadf6136eee7a59d6a444c9eb4e2198e8a974f27a39e b63af2c9af3870488b8adaad444674f512133ad80b9220e09158521614f1faadfe85 05ef57b7df6813048603f0dd04f4280177a11380fbfc861dbcbd7418d62155248dad 5fdec0991f

 $blinded_msg = 10c166c6a711e81c46f45b18e5873cc4f494f003180dd7f115585d871a28930259654fe28a54dab319cc5011204c8373b50a57b0fdc7a678bd74c523259dfe4fd5ea9f52f170e19dfa332930ad1609fc8a00902d725cfe50685c95e5b2968c9a2828a21207fcf393d15f849769e2af34ac4259d91dfd98c3a707c509e1af55647efaa31290ddf48e0133b798562af5eabd327270ac2fb6c594734ce339a14ea4fe1b9a2f81c0bc230ca523bda17ff42a377266bc2778a274c0ae5ec5a8cbbe364fcf0d2403f7ee178d77ff28b67a20c7ceec009182dbcaa9bc99b51ebbf13b7d542be337172c64$

 $74f2cd3561219fe0dfa3fb207cff89632091ab841cf38d8aa88af6891539f263adb8\\ eac6402c41b6ebd72984e43666e537f5f5fe27b2b5aa114957e9a580730308a5f5a9\\ c63a1eb599f093ab401d0c6003a451931b6d124180305705845060ebba6b0036154f\\ cef3e5e9f9e4b87e8f084542fd1dd67e7782a5585150181c01eb6d90cb9588383738\\ 4a5b91dbb606f266059ecc51b5acbaa280e45cfd2eec8cc1cdb1b7211c8e14805ba6\\ 83f9b78824b2eb005bc8a7d7179a36c152cb87c8219e5569bba911bb32a1b923ca83\\ de0e03fb10fba75d85c55907dda5a2606bf918b056c3808ba496a4d95532212040a5\\ f44f37e1097f26dc27b98a51837daa78f23e532156296b64352669c94a8a855acf30\\ 533d8e0594ace7c442$

blind sig = 364f6a40dbfbc3bbb257943337eeff791a0f290898a6791283bba581 d9eac90a6376a837241f5f73a78a5c6746e1306ba3adab6067c32ff69115734ce014 d354e2f259d4cbfb890244fd451a497fe6ecf9aa90d19a2d441162f7eaa7ce3fc4e8 9fd4e76b7ae585be2a2c0fd6fb246b8ac8d58bcb585634e30c9168a434786fe5e0b7 4bfe8187b47ac091aa571ffea0a864cb906d0e28c77a00e8cd8f6aba4317a8cc7bf3 2ce566bd1ef80c64de041728abe087bee6cadd0b7062bde5ceef308a23bd1ccc154f d0c3a26110df6193464fc0d24ee189aea8979d722170ba945fdcce9b1b4b63349980 f3a92dc2e5418c54d38a862916926b3f9ca270a8cf40dfb9772bfbdd9a3e0e089236 9c18249211ba857f35963d0e05d8da98f1aa0c6bba58f47487b8f663e395091275f8 2941830b050b260e4767ce2fa903e75ff8970c98bfb3a08d6db91ab1746c86420ee2 e909bf681cac173697135983c3594b2def673736220452fde4ddec867d40ff42dd3d a36c84e3e52508b891a00f50b4f62d112edb3b6b6cc3dbd546ba10f36b03f06c0d82 aeec3b25e127af545fac28e1613a0517a6095ad18a98ab79f68801e05c175e15bae2 1f821e80c80ab4fdec6fb34ca315e194502b8f3dcf7892b511aee45060e3994cd15e 003861bc7220a2babd7b40eda03382548a34a7110f9b1779bf3ef6011361611e6bc5 c0dc851e1509de1a

sig = 6fef8bf9bc182cd8cf7ce45c7dcf0e6f3e518ae48f06f3c670c649ac737a8b 8119a34d51641785be151a697ed7825fdfece82865123445eab03eb4bb91cecf4d69 51738495f8481151b62de869658573df4e50a95c17c31b52e154ae26a04067d5ecdc 1592c287550bb982a5bb9c30fd53a768cee6baabb3d483e9f1e2da954c7f4cf492fe 3944d2fe456c1ecaf0840369e33fb4010e6b44bb1d721840513524d8e9a3519f40d1 b81ae34fb7a31ee6b7ed641cb16c2ac999004c2191de0201457523f5a4700dd64926 7d9286f5c1d193f1454c9f868a57816bf5ff76c838a2eeb616a3fc9976f65d4371de ecfbab29362caebdff69c635fe5a2113da4d4d8c24f0b16a0584fa05e80e607c5d9a 2f765f1f069f8d4da21f27c2a3b5c984b4ab24899bef46c6d9323df4862fe51ce300 fca40fb539c3bb7fe2dcc9409e425f2d3b95e70e9c49c5feb6ecc9d43442c33d5000 3ee936845892fb8be475647da9a080f5bc7f8a716590b3745c2209fe05b17992830c e15f32c7b22cde755c8a2fe50bd814a0434130b807dc1b7218d4e85342d70695a5d7 f29306f25623ad1e8aa08ef71b54b8ee447b5f64e73d09bdd6c3b7ca224058d7c67c c7551e9241688ada12d859cb7646fbd3ed8b34312f3b49d69802f0eaa11bc4211c2f 7a29cd5c01ed01a39001c5856fab36228f5ee2f2e1110811872fe7c865c42ed59029 c706195d52

A.4. RSABSSA-SHA384-PSSZERO-Deterministic Test Vector

 $\begin{array}{ll} p = e1f4d7a34802e27c7392a3cea32a262a34dc3691bd87f3f310dc75673488930559c120fd0410194fb8a0da55bd0b81227e843fdca6692ae80e5a5d414116d4803fca7d8c30eaaae57e44a1816ebb5c5b0606c536246c7f11985d731684150b63c9a3ad9e41b04c0b5b27cb188a692c84696b742a80d3cd00ab891f2457443dadfeba6d6daf108602be26d7071803c67105a5426838e6889d77e8474b29244cefaf418e381b312048b457d73419213063c60ee7b0d81820165864fef93523c9635c22210956e53a8d96322493ffc58d845368e2416e078e5bcb5d2fd68ae6acfa54f9627c42e84a9d3f2774017e32ebca06308a12ecc290c7cd1156dcccfb2311 \\ \end{array}$

 $\begin{array}{ll} q = c601a9caea66dc3835827b539db9df6f6f5ae77244692780cd334a006ab353c8\\ 06426b60718c05245650821d39445d3ab591ed10a7339f15d83fe13f6a3dfb20b945\\ 2c6a9b42eaa62a68c970df3cadb2139f804ad8223d56108dfde30ba7d367e9b0a7a8\\ 0c4fdba2fd9dde6661fc73fc2947569d2029f2870fc02d8325acf28c9afa19ecf962\\ \end{array}$

 $\label{eq:daa7916e21afad09eb62fe9f1cf91b77dc879b7974b490d3ebd2e95426057f35d0a3c9f45f79ac727ab81a519a8b9285932d9b2e5ccd347e59f3f32ad9ca359115e7da008ab7406707bd0e8e185a5ed8758b5ba266e8828f8d863ae133846304a2936ad7bc7c9803879d2fc4a28e69291d73dbd799f8bc238385$

n = aec4d69addc70b990ea66a5e70603b6fee27aafebd08f2d94cbe1250c556e047a928d635c3f45ee9b66d1bc628a03bac9b7c3f416fe20dabea8f3d7b4bbf7f963be3 35d2328d67e6c13ee4a8f955e05a3283720d3e1f139c38e43e0338ad058a9495c533 77fc35be64d208f89b4aa721bf7f7d3fef837be2a80e0f8adf0bcd1eec5bb040443a 2b2792fdca522a7472aed74f31a1ebe1eebc1f408660a0543dfe2a850f106a617ec6 685573702eaaa21a5640a5dcaf9b74e397fa3af18a2f1b7c03ba91a6336158de420d 63188ee143866ee415735d155b7c2d854d795b7bc236cffd71542df34234221a0413 e142d8c61355cc44d45bda94204974557ac2704cd8b593f035a5724b1adf442e78c5 42cd4414fce6f1298182fb6d8e53cef1adfd2e90e1e4deec52999bdc6c29144e8d52 a125232c8c6d75c706ea3cc06841c7bda33568c63a6c03817f722b50fcf898237d78 8a4400869e44d90a3020923dc646388abcc914315215fcd1bae11b1c751fd52443aa c8f601087d8d42737c18a3fa11ecd4131ecae017ae0a14acfc4ef85b83c19fed33cf d1cd629da2c4c09e222b398e18d822f77bb378dea3cb360b605e5aa58b20edc29d00 0a66bd177c682a17e7eb12a63ef7c2e4183e0d898f3d6bf567ba8ae84f84f1d23bf8 b8e261c3729e2fa6d07b832e07cddd1d14f55325c6f924267957121902dc19b3b329 48bdead5

e = 010001

d = 0d43242aefe1fb2c13fbc66e20b678c4336d20b1808c558b6e62ad16a287077180b177e1f01b12f9c6cd6c52630257ccef26a45135a990928773f3bd2fc01a313f1d ac97a51cec71cb1fd7efc7adffdeb05f1fb04812c924ed7f4a8269925dad88bd7dcf bc4ef01020ebfc60cb3e04c54f981fdbd273e69a8a58b8ceb7c2d83fbcbd6f784d05 2201b88a9848186f2a45c0d2826870733e6fd9aa46983e0a6e82e35ca20a439c5ee7 b502a9062e1066493bdadf8b49eb30d9558ed85abc7afb29b3c9bc644199654a4676 681af4babcea4e6f71fe4565c9c1b85d9985b84ec1abf1a820a9bbebee0df1398aae 2c85ab580a9f13e7743afd3108eb32100b870648fa6bc17e8abac4d3c99246b1f0ea 9f7f93a5dd5458c56d9f3f81ff2216b3c3680a13591673c43194d8e6fc93fc1e37ce 2986bd628ac48088bc723d8fbe293861ca7a9f4a73e9fa63b1b6d0074f5dea2a624c 5249ff3ad811b6255b299d6bc5451ba7477f19c5a0db690c3e6476398b1483d10314 afd38bbaf6e2fbdbcd62c3ca9797a420ca6034ec0a83360a3ee2adf4b9d4ba29731d 131b099a38d6a23cc463db754603211260e99d19affc902c915d7854554aabf608e3 ac52c19b8aa26ae042249b17b2d29669b5c859103ee53ef9bdc73ba3c6b537d5c34b 6d8f034671d7f3a8a6966cc4543df223565343154140fd7391c7e7be03e241f4ecfe b877a051

 $\label{eq:msg} \begin{tabular}{ll} msg = 8f3dc6fb8c4a02f4d6352edf0907822c1210a9b32f9bdda4c45a698c80023a\\ a6b59f8cfec5fdbb36331372ebefedae7d \end{tabular}$

msq_prefix =

prepared_msg = 8f3dc6fb8c4a02f4d6352edf0907822c1210a9b32f9bdda4c45a6 98c80023aa6b59f8cfec5fdbb36331372ebefedae7d

salt =

 $\begin{array}{ll} encoded_msg = 159499b90471b496c2639ec482e99feaba525c0420c565d17dc60c\\ 1bb1f47703f04436cceaa8f69811e1bf8546fa971226c9e71421b32b571ed5ea0e03\\ 2269d4219b4404316eb17a58f277634aeed394b7f3888153b5bb163e40807e605daf\\ dd1789dd473b0846bdcb6524417bc3a35366fab4261708c0e4b4beba07a1a64bbccb\\ 4b1ac215d1350a50a501e8e96612028b535ad731abf1f117ee07d07a4de9cef3d70f\\ 5845ba84c29d5d92c6e66a1f9489a5f527b846825360fd6e90f40ed041c682e489f3\\ acde984a3ea580181418c1d15017af2657bc4b70485cdc0f1ebc3693e0d70a5d01f3\\ 7ff640993fa071274fb9ee44e0c24dcb58ffa21a9a6540d87f24379beaafcc3b4bd4\\ 2c45ec6820e03738ce98bea11c71685f31db63429fab8658bdb816f1ecccb1888f24\\ 02de0bd2f0f9646decdcad4c11b41428eec1ed25f2a86d43bb04f95726bfbd98ea34\\ ca091b7adbabd0e28f17fa0345b89542d23c3530554987508a23641bd4f9e52962b0\\ bee3ac9ffe005322d26a39941c5847774300411c69635f96903e8d593530908bd92a\\ 4fa6a2d52f88073a647a4b3894b7e4ebb80699e60227397bfa93f41b1c97e107b632\\ f68e70409372ead2f072c11cf99be4486fcbf763dde28ee156db26cd358a69fcb796\\ 44f1f2fcc166f41a4c80f5851ee08be051f14b601418d6e56e61733b9b210c6bef17\\ \end{array}$

edac121a754d19b9bc

inv = 80682c48982407b489d53d1261b19ec8627d02b8cda5336750b8cee332ae26 0de57b02d72609c1e0e9f28e2040fc65b6f02d56dbd6aa9af8fde656f70495dfb723 ba01173d4707a12fddac628ca29f3e32340bd8f7ddb557cf819f6b01e445ad96f874 ba235584ee71f6581f62d4f43bf03f910f6510deb85e8ef06c7f09d9794a008be7ff 2529f0ebb69decef646387dc767b74939265fec0223aa6d84d2a8a1cc912d5ca25b4 e144ab8f6ba054b54910176d5737a2cff011da431bd5f2a0d2d66b9e70b39f4b050e 45c0d9c16f02deda9ddf2d00f3e4b01037d7029cd49c2d46a8e1fc2c0c17520af1f4 b5e25ba396afc4cd60c494a4c426448b35b49635b337cfb08e7c22a39b256dd032c0 0adddafb51a627f99a0e1704170ac1f1912e49d9db10ec04c19c58f420212973e0cb 329524223a6aa56c7937c5dffdb5d966b6cd4cbc26f3201dd25c80960a1a111b3294 7bb78973d269fac7f5186530930ed19f68507540eed9e1bab8b00f00d8ca09b3f099 aae46180e04e3584bd7ca054df18a1504b89d1d1675d0966c4ae1407be325cdf623c f13ff13e4a28b594d59e3eadbadf6136eee7a59d6a444c9eb4e2198e8a974f27a39e b63af2c9af3870488b8adaad444674f512133ad80b9220e09158521614f1faadfe85 05ef57b7df6813048603f0dd04f4280177a11380fbfc861dbcbd7418d62155248dad 5fdec0991f

blinded_msg = 982790826556aabe6004467671a864397eea3b95740e9a11c8b80b 99ee0cf4dbc50af860bda81b601a2eceaa6943ef104f13325ad0be2e37f42030b312 0e87cfee8cfe59cde1acfb25485a43275ebe777292e2518181ae531e596f988ff16f 458daa5a42408939cbe60e7271391a21657276427d195bee6a20054101d4ceb892ec dea402ea1a866acf0e451a3336f07e7589330d96c3883fd5bc1a829a715b618b74a8 6b2a898764246ad081d4c9f1edb8ab5077e315fde2417ec2dd33cad93e120340b49b e89c18a63e62c6bb289037283d3bf18608be11ee4c823c710b0c6b89235fed3f03a7 b96ddd25a8f54f20dac37ce8905093ad8e066810f354fb1773236e3d3788ba755de2 c9bce8d340078bb1831ddc7314a5018673427ced65cb356281aae08b5e6636f3eb24 17e09d6ae476a9abcc410bc8c90813d0740e39ae75efae4c02eed49dbb7aa51258bb 71197445d17a6029bf566ba6b36282173af2c42e9b9631366f22eb6a19ef1d92bd3c e0631d3a7fb3288195b0ba380a3828d5411cefd5eba83e52198c001ac9946a333a33 d89d4d235fc833239d59837f04eaf065e9563659b00c7624a6263b727d8f2c07959b a2bb592e7ff251b8f09c85995fd2e4474e743586576b518230986b6076b762ae7708 8a37e4bffd2ef41ae68d6d4e79205290b4f76c42ef039638c41cdc6fe8af9b429c0d ee45b2942e3861da2a

blind_sig = 362ef369f9b8c1487e285514702a7cd6fe03e4a2fb854881f3d3f986 b7742a0c9bfab6562a6cd5ed71c574af67d7e77e71b33420c08ebb0ff37886b85829 7f9562fc366066c6d8e77bad1918b04756ba03f5c385d44f06759daf1b7a38b2a642 48dee95d0e3886c8afa1f74afd8ac3c56520d0f3fd206df8e0d257312756803b09a7 9d0cc38112592c3aec32de5a9bc3284c5a0a2d0808b102deafa5cc60f04e3d71c028 4cba04f17f88aa8e07d5544fe0265807d515877f79d30ed26d522b9d9c56597647b0 dbca5a69d6418f8d1b51481723f272c2a3d48f6f4fd6beeac3576c3edb00e8779964 548aeab8e004c7c4f8ef9cb6e680e2d2d49792004bb3e6974fa48f241a361ca449c0 2bd4c0ad4e66252c55e656f16049908efe59acbafa1171895dfac64d909808e54204 69d622c7253ec1de7522b41634d383bf8786bf881cbf1561627f1e62b2d93300ec30 ec0f5f0ab32036fce068bc76b0b0c6452079537f8d7f8dcee4b42bbf2d9ad7499d38 35cd93cfc7e8ebea3554ab5241e181e5d73241b7bebf0a281b63594a35f4993e2b41 6d60db966b58b648cfcba2c4bee4c2830aae4a70ff55012480298f549c13b1b26842 77bca12f592471b8a99285174f1c0ebb38fc80e74a10b3f02ec3e6682ba873f7ff0e 1e79718b470927c74ed754d4f7c3d9a55e22246e829cdb5a1c6fb2a0a6c896df3030 63c918bcf5eb0017

 $\begin{array}{lll} \text{sig} &=& 4454b6983 \text{ff01cb28545329f394936efa42ed231e15efbc025fdaca00277acf0c8e00e3d8b0ecebd35b057b8ebfc14e1a7097368a4abd20b555894ccef3d1b9528c6bcbda6b95376bef230d0f1feff0c1064c62c60a7ae7431d1fdfa43a81eed9235e363e1ffa0b2797aba6aad6082fcd285e14fc8b71de6b9c87cb4059c7dc1e96ae1e63795a1e9af86b9073d1d848aef3eca8a03421bcd116572456b53bcfd4dabb0a9691f1fabda3ed0ce357aee2cfee5b1a0eb226f69716d4e011d96eede5e38a9acb531a64336a0d5b0bae3ab085b658692579a376740ff6ce69e89b06f360520b864e33d82d029c88248a19e18e31f0ecd16fac5cd4870f8d3ebc1c32c718124152dc905672ab0b7af48bf7d1ac1ff7b9c742549c91275ab105458ae37621757add83482bbcf779e777bbd6\\ \end{aligned}$

 $1126e93686635d4766aedf5103cf7978f3856ccac9e28d21a850dbb03c811128616d\\ 315d717be1c2b6254f8509acae862042c034530329ce15ca2e2f6b1f5fd59272746e\\ 3918c748c0eb810bf76884fa10fcf749326bbfaa5ba285a0186a22e4f628dbf178d3bb5dc7e165ca73f6a55ecc14c4f5a26c4693ce5da032264cbec319b12ddb9787d0efa4fcf1e5ccee35ad85ecd453182df9ed735893f830b570faae8be0f6fe2e571a4e0d927cba4debd368d3b4fca33ec6251897a137cf75474a32ac8256df5e5ffa518b88b43fb6f63a24$

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