

## Problem 1.

Specify new operations as follows:

For an initial environment  $\rho$ .

minus: accepts a number and returns its negation (also a number)

```
(value-of (minus-exp exp)  $\rho$ )  
= (num-val (- (expval->num (value-of exp  $\rho$ ))))
```

double: accepts a number and returns its double (also a number)

```
(value-of (double-exp exp)  $\rho$ )  
= (num-val (* 2 (expval->num (value-of exp  $\rho$ ))))
```

gcd: accepts 2 numbers, and returns their gcd (also a number)

```
(value-of (gcd-exp exp1 exp2)  $\rho$ )  
= (num-val (calc-gcd (expval->num (value-of exp1  $\rho$ ))  
                     (expval->num (value-of exp2  $\rho$ ))))
```

prime?: accepts a number and tests if it's a prime (a boolean)

```
(value-of (prime?-exp exp)  $\rho$ )  
= (bool-val (test-prime (expval->num (value-of exp  $\rho$ ))))
```

“calc-gcd” => simple recursive gcd calculator (the euclidean algorithm)  
“test-prime” => reasonably fast, iterative prime tester (slower than  
fermat test, but simpler code-wise)

Extend language grammar in “define-the-grammar” in lang.rkt as follows:

```
; example: minus(-6) => (minus-exp <<-6>>)  
(expression  
  ("minus" "(" expression ")")  
  minus-exp)  
  
; example: double(3) => (double-exp <<3>>)  
(expression  
  ("double" "(" expression ")")  
  double-exp)  
  
; example: gcd(10,3) => (gcd-exp <<10>> <<3>>)  
(expression  
  ("gcd" "(" expression "," expression ")")  
  gcd-exp)  
  
; example: prime?(11) => (prime?-exp <<11>>)  
(expression  
  ("prime?" "(" expression ")")  
  prime?-exp)
```

Extend the interpreter by adding to “value-of” in interp.rkt as follows:

```
(minus-exp (exp)
  (let ((val (value-of exp env)))
    (let ((num (expval->num val)))
      (num-val (- num))))))

(double-exp (exp)
  (let ((val (value-of exp env)))
    (let ((num (expval->num val)))
      (num-val (* 2 num)))))

(gcd-exp (exp1 exp2)
  (let ((val1 (value-of exp1 env))
        (val2 (value-of exp2 env)))
    (let ((num1 (expval->num val1))
          (num2 (expval->num val2)))
      (num-val
       (calc-gcd num1 num2)))))

(prime?-exp (exp)
  (let ((val (value-of exp env)))
    (let ((num (expval->num val)))
      (bool-val (test-prime num)))))
```