

### Problem 1.

Top-Down - reduce to base case.

Nonnegative Integer  $n$  is in  $S$  iff:

1.  $n = 0$ , or
2.  $(\sqrt{n} - 1)^2$  is in  $S$

Bottom-Up - start from base case.

$S$  is the smallest set contained in the set of nonnegative integers satisfying the following properties:

1.  $n = 0$  and ( $n$  is in  $S$ ), or
2. if ( $n$  is in  $S$ ), then  $(n + 2\sqrt{n} + 1)$  is in  $S$

Rules of Inference

Sequence of derivations (Induction Hypothesis + Inductive Step)

Base Case (always holds):

>>  $n$  is in  $S$ .

Rule of Derivation (by induction):

>> Assume  $k=m^2$  is a square number. So,  $k$  is in  $S$ .

>> Then  $(\sqrt{k}+1)^2 = (m+1)^2$  is a square number and is in  $S$ .

Proof.

$k = m^2$  (ADD  $(2*m + 1)$  to both sides)

$k + 2*m + 1 = m^2 + 2*m + 1 = (m+1)^2$ .

### Problem 2.

```
(define (repeatN lst n)
  (if (null? lst) '()
      (let ((first (car lst)) (rest (cdr lst)))
        (append (make-list n first) (repeatN rest n)))))
```

### Problem 3.

```
(define (sum-even lst) (reduce + 0 (filter even? lst)))
```

### Problem 4.

```
(define (isIn? lst n)
  (or (eqv? (car lst) n)
      (and (not (null? (cdr lst)))
            (isIn? (cdr lst) n))))

(define (myProc pred lst1 lst2 op init)
  (fold-right op init (filter (lambda (e) (pred lst2 e)) lst1)))
```