

# 07: EXPONENTIAL FAMILIES

Rice 8.8.1

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## 1 Exponential Families

Many “nice” distributions that we’ve spent a lot of time with are members of the **exponential family**.

### Exponential Family

One-parameter members of the exponential family have density functions of the form:

Writing densities in this form requires a bit of work.

**Example:** Poisson distribution

BUT, the payoff is that once we write the pdf in *exponential form*, we can immediately identify a sufficient statistic:

We also have the following results:

### **Sufficiency and the MLE**

### **Mean and Variance of Exponential Families**

### **Conjugate priors**

**Example:** Poisson distribution

**k-parameter exponential family**

**Example:**  $X_1, \dots, X_n \sim N(\mu, \sigma^2)$

## 1.1 More distributions