Announcements

Wednesday: Quiz 2 / HW 10 arro due (compression)
Today: Review

OH . 4-day 11:30 -12:30

recondune wed out to trusday 3-4:15 or s

Friday: ctars new stroll, proper

$$\hat{\theta}_{1} \rightarrow E(X_{1}) = \frac{1}{N} \sum X_{1}$$

$$\hat{\theta}_{2} = X$$

$$\hat{\theta}_{2} \rightarrow E(X_{1})^{2} = \frac{1}{N} \sum X_{1}^{2}$$

$$\lambda + \lambda^{2} = \frac{1}{N} \sum X_{1}^{2}$$

$$\rightarrow \text{Solve for } \lambda$$

$$V(x_i) = E(x_i^2) - E(x_i)^2$$

$$\Rightarrow E(x_i^2) = V(x_i) + E(x_i)^2$$

$$= \lambda + \lambda^2$$

$$= \theta^{(x_i)} - \theta$$

(D) 109 - NX - POI((D)

(a) $E(x_i) = \lambda = v(x_i)$

(b) ((0) = 1) (0) (0)

= 6 2 A: 6 - NO 1 3

 $(c) I(\theta) = -E\left(\frac{3^2 I}{3\theta^2}\right) - E\left(\frac{-\Sigma Y^2}{\theta^2}\right) = \frac{1}{\theta^2} \sum E(Y)$ $= \frac{1}{\theta^2} - \frac{\Sigma Y^2}{\theta^2}$

T (ince we did & In (6)

V(x) = V(It;) = 12 n. 0 = 0 > x muck CRUB

ld) CPLB exposies (support(f) does not depend on 0, \$ (ê)=0)

lle)= Ey: In & -no In e

Var (B) = 1 IND = 1 IND = 0

 $\frac{\partial f}{\partial \theta} = \frac{\sum y_i}{\theta} - n = 0$

 $\frac{1}{\theta^2} \cdot n\theta = \frac{N}{\theta}$

 $\lambda + |\lambda^2| = \frac{1}{16} \sum_{i=1}^{n} X_i^2$ > solve An 2

(b)
$$f(X) = \alpha \beta = \frac{\alpha}{2} = \overline{X}$$

 $\Rightarrow \alpha = 2\overline{X}$

$$funma(nd, \frac{1}{2})$$
, then $E(\hat{a})$

$$tumma(nd, \frac{1}{3})$$
, then $E($

$$V(\widehat{a}) = V(\frac{1}{n} \sum_{i=1}^{n} \chi_{i}^{i}) = \frac{2^{n}}{n^{2}} \cdot n \cdot V(\chi_{i}) = \frac{4}{n} \cdot x \cdot \frac{1}{4}$$

(A) By ROO-Blackwell, X not a function of T= TIX:

=) d" = E(X/T=t) will have strictly

~ N(2d, =)

(e) $b_1 w_1^2 + v = 0 + \left(\frac{w}{2}\right)^2 = \frac{w_2}{w_2}$

By delta method,
$$2\bar{x} \sim N(2\alpha, 4\frac{\alpha}{m})$$







asymp. various (same as exact in









3 (a)
$$l(\lambda) = \prod_{i=1}^{n} \lambda^{2} x_{i}^{-2} e^{-\lambda/\lambda i}$$

(b)
$$L(\lambda) = \lambda^{2n} e^{-\lambda \sum \frac{1}{x_i}}$$
. $\prod \frac{1}{x_i^2}$ \forall (an also find via exponential family. Not necessarily = but should be a function of $\sum \frac{1}{x_i}$.

By fact theorem. $\sum k^{-1}$ sull for λ

$$|||||| = 2n \text{ in } \lambda - \lambda \sum_{i=1}^{n} \ln e_i + 2$$

(i)
$$L(\lambda) = 2n \text{ en } \lambda - \lambda \sum_{i=1}^{k} lne + \sum_{i=1}^{k} ln \sum_{i=1}^{k} ln e + \sum_{i=1}^{k} ln \sum_{i=1}^{k} ln e + \sum_{i=1}^{k}$$

(d) MUE has large sumpre diet N(&, I(0))

(1) By mvariance of MLB.

 $I(\gamma) = E\left(\frac{3\gamma_0}{3\sqrt{1}}\right) = -E\left(-\frac{\gamma_0}{5m}\right) = \frac{\gamma_0}{5m} \quad \text{in} \quad \gamma = \frac{\gamma_0}{3m}$

$$\lambda$$
) = 2n en $\lambda - \lambda \sum \frac{1}{2}$; lne + \sum

=
$$2n \ln \lambda - \lambda \sum_{i} \ln e + i$$

$$\frac{\partial l}{\partial \lambda} = \frac{2n}{\lambda} - \sum \frac{1}{x} = 0$$

) = 2n = 2n

PIMLE = log (\hat{\hat{\chi}}_{mlb}) = log (\frac{2h}{\subsection{\chi}{\sin}{\sin\eta}}\simen\chi}{\sin\eta}}}}}}}}}}}} \right)

(a) Face. MLF 15 asymptoxically unbineed

(b) Farce LCW tehr us & -> pr que ansitraring close to pe, but not

(6) Falce - X is consistent for p., so only the of E(Xi) = 0

(d) CRLB: V(B) & TE(B)

$$V(\overline{X}) = V(\frac{1}{n} \overline{Z}X;) = \frac{1}{n^2} \cdot n \cdot V(X;) = \frac{0^{-2}}{n}$$

X meets LRIB, so it is mulib.
Us and is unbiased.

· True:

act. of CRIB