

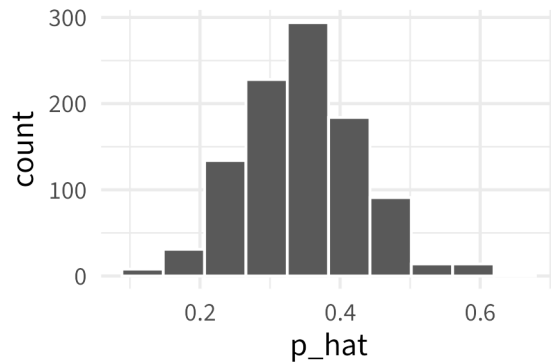
# NOTES 11: CONFIDENCE INTERVALS + INTRO TO THE BOOTSTRAP

Stat 120 | Fall 2025

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Let's begin with the class proportion from last time: 36.7% of Carleton students are "from the Midwest", while \_\_\_\_% of our class (who were in attendance) are from the Midwest.



The mean and standard deviation of the sampling distribution are:

```
# A tibble: 1 x 2
  xbar    se
<dbl> <dbl>
1 0.349 0.0879
```

Standard Error:  
Standard deviation of a statistic or a sampling distribution

In a random class of 32 students, how many would we expect to be from the Midwest?

### Confidence Interval

An interval computed from sample data by a method that will capture the parameter for a specified percentage of all samples

95% confidence interval using the standard error:

### Margin of Error

Example: Percent of each country with internet access (StatKey)

### CI Misinterpretations

- A 95% CI contains 95% of the data from the population
- I am 95% sure that the mean of the sample will be in CI
- The probability that the parameter is in the CI is 95%

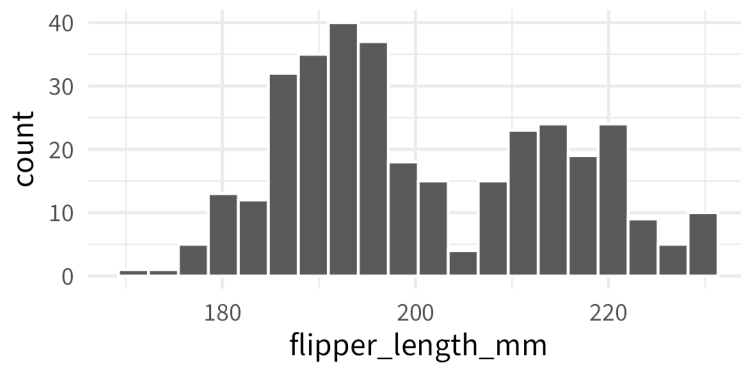
Structure of a CI:

1. I am \_\_\_\_ % confident
2. that the [population parameter in context]
3. is between \_\_\_\_ and \_\_\_\_ [units]

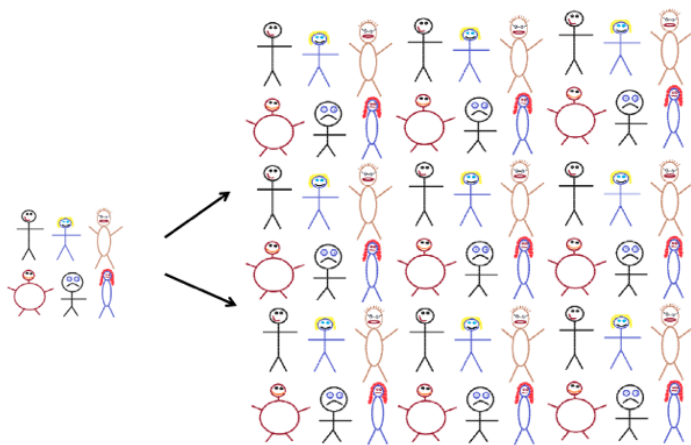
## 1 The Bootstrap

So far, we've used the population to generate samples and construct sampling distributions. For most situations, this is unrealistic.

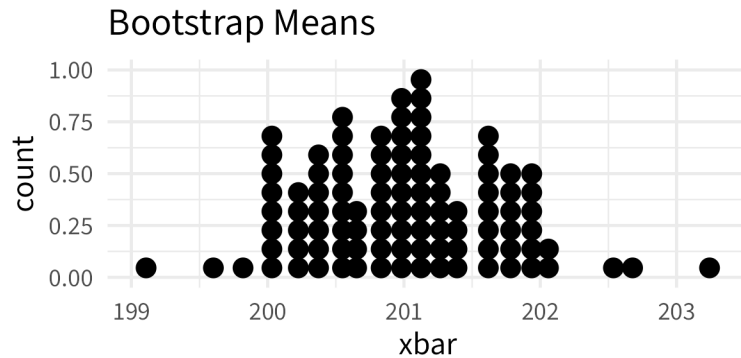
Example: Let's consider our penguin friends. I'm interested in finding a 95% confidence interval for the mean flipper length of all Palmer Archipelago penguins. The mean flipper length is 200.9152 and the standard deviation is 14.0617.



Idea:



Let's return to our penguins. I've made 100 bootstrap samples and found the mean for each one:



The mean of this distribution is 200.9947 and the standard deviation is 0.6988.

Bootstrap confidence interval:

The magic of the bootstrap is that it works for any statistic we can compute from our sample! We simply have to follow these steps:

1. Generate bootstrap samples:
  - Sample from the original sample with replacement
  - Use the same sample size as original sample
2. Compute the statistic of interest for each bootstrap sample
3. Collect the statistics for many bootstrap samples to create the bootstrap distribution
4. Treat the bootstrap distribution as the sampling distribution to estimate the standard error

⚠ What happens when the bootstrap distribution is not symmetric?