gw02-sols

```
library(bayesrules) # R package for our textbook
library(tidyverse) # Collection of packages for tidying and plotting data
library(janitor) # Helper functions like tidy and tabyl
```

1 BR Exercise 2.13

See handwritten

<int>

1

2

2 BR Exercise 2.18

The smallest Y where $P(\pi = .6|Y) > .4$ is 6

<dbl>

0.0299

0.0877

<dbl>

0 0.000105

1 0.00157

<dbl>

0.000877

0.00449

```
5
     4 0.111
                     0.175
                             0.159
6
      5 0.201
                     0.157
                             0.319
7
     6 0.251
                     0.120
                             0.523
8
    7 0.215
                     0.0752
                             0.715
                     0.0356
9
     8 0.121
                             0.850
10
    9 0.0403
                    0.0109
                             0.928
11
    10 0.00605
                     0.00156 0.966
```

3 BR Exercise 2.17

```
# Define possible trees
trees <- data.frame(type = c("mold", "not mold"))</pre>
# Define the prior model
prior <- c(0.18, .82)
# Simulate 10000 trees
set.seed(84735)
trees_sim <- sample_n(trees, size = 10000,</pre>
                         weight = prior, replace = TRUE)
trees_sim <- trees_sim %>%
  mutate(data_model = case_when(type == "mold" ~ 0.8,
                                 type == "not mold" \sim 0.1)
# Define tree species
data <- c("maple", "not maple")</pre>
# Simulate species
trees_sim <- trees_sim %>%
  group_by(1:n()) %>%
  mutate(species = sample(data, size = 1,
                         prob = c(data_model, 1-data_model)))
trees_sim %>%
  filter(species == "maple") %>%
  tabyl(type) %>%
  adorn_totals("row")
```

type n percent mold 1482 0.6327925

not mold 860 0.3672075 Total 2342 1.0000000

4 MLE

If $Y \sim \text{Binom}(n, \pi)$, show that $\hat{\pi}_{MLE} = \frac{Y}{n}$ (see handwritten)

5 BR Exercise 3.1

For each part, use plot_beta and/or summarize_beta to justify your answer

6 BR Exercise 3.12

7 Choice of prior

I am interviewing Carleton students about whether or not they have used (knowingly) used ChatGPT on coursework in a non-approved way. I think the proportion has a 90% chance of being less than .25.

(a) Choose an informative prior that you think is reasonable for this belief

I then ask 20 students this question and 15 respond "yes". Find the posterior using the prior from above, then using the 3 non/weakly informative priors below:

- (a) Unif(0,1) prior
- (b) Beta(2,2) prior
- (c) "Reference" prior Beta(.5, .5)

Compare the posteriors for each of the priors above. Do results change if we instead observe 150/200 students responding "yes"?

8 BR 4.13

(see handwritten)