

January 10, 2023

1

```
library(coga,quietly=TRUE)
```

```
.Sus = 1  
.Lat = 2  
.Asy = 3  
.Pre = 4  
.Mld = 5  
.Svr = 6  
.RecS = 7  
.RecA = 8  
.NStates = .RecA
```

```
.U = 1  
.V = 2  
.W = 3  
.X = 4  
.Y = 5  
.Z = 6
```

deltaParams()

A function to make a data structure holding parameters to model the Delta SARS-CoV-2 variant.

```
deltaParams = function()  
{  
  msus = 1000  
  
  list (  Psymp = 0.5,  
          Psevere = 0.1,  
          Msus = msus,  
          Vsus = msus^2,  
          Mlat = 5.1,  
          Vlat = 7.5,  
          Masy = 7,  
          Vasy = 7.5,  
          Mpre = 3,  
          Vpre = 1.0,  
          Mmld = 5,  
          Vmld = 45.5,  
          Msev = 11,  
          Vsev = 45.5  
  )  
}
```

`omicronParams()`

A function to make a data structure holding parameters to model the Omicron SARS-CoV-2 variant.

```
omicronParams = function()
{
  ommod = 0.6
  ommod2 = 0.9
  msus = 1000

  list( Psymp = 0.5,
        Psevere = 0.1,
        Msus = msus,
        Vsus = msus^2,
        Mlat = 5.1 * ommod,
        Vlat = 7.5 * ommod^2,
        Masy = 7 * ommod2,
        Vasy = 7.5 * ommod2^2,
        Mpre = 3 * ommod2,
        Vpre = 1.0 * ommod2^2,
        Mmld = 5 * ommod2,
        Vmld = 45.5 * ommod2^2,
        Msev = 11 * ommod2,
        Vsev = 45.5 * ommod2^2,
        ommod = ommod,
        ommod2 = ommod2
  )
}
```

`makeModel()`

A function to convert a SARS-CoV-2 model specified by means and variances into a collection of Gamma shape and rate parameters, with associated path splitting probabilities.

```
makeModel = function(Q)
{
  means = c(Q$Msus, Q$Mlat, Q$Mpre, Q$Masy, Q$Msev, Q$Mmld)
  vars = c(Q$Vsus, Q$Vlat, Q$Vpre, Q$Vasy, Q$Vsev, Q$Vmld)
  list(q=Q$Psymp, r=Q$Psevere, shape=means^2/vars, rate=means/vars)
}
```

FF()

A function calling `pcoga()` to calculate the cumulative distribution function of a sum selected Gamma random variables.

```
FF = function(x,P,use)
{
  pcoga(x,P$shape[use],P$rate[use])
}
```

StateProbs01()

A function to calculate the state probabilities for a vector of times `x`, using the parameters in the model `M` and depending on an indicator `transmission` of whether a transmission occurred at time 0.

```
StateProbs01 = function(x,M,transmission)
{
  s = matrix(0,nrow=NSStates,ncol=length(x))
  if (transmission)
  {
    s[.Sus,] = 0
    fv = FF(x,M,c(.V))
    s[.Lat,] = 1-fv
    fvx = FF(x,M,c(.V,.X))
    s[.Asy,] = (1-M$q)*(fv-fvx)
    fvw = FF(x,M,c(.V,.W))
    s[.Pre,] = M$q*(fv-fvw)
    fvwz = FF(x,M,c(.V,.W,.Z))
    s[.Mld,] = M$q*(1-M$r)*(fvw-fvwz)
    fvwY = FF(x,M,c(.V,.W,.Y))
    s[.Svr,] = M$q*M$r*(fvw-fvwY)
    s[.RecS,] = M$q*M$r*fvwY+M$q*(1-M$r)*fvwz
    s[.RecA,] = (1-M$q)*fvx
  }
  else
  {
    fu = FF(x,M,c(.U))
    s[.Sus,] = 1-fu
    fuv = FF(x,M,c(.U,.V))
    s[.Lat,] = fu-fuv
    fuvx = FF(x,M,c(.U,.V,.X))
    s[.Asy,] = (1-M$q)*(fuv-fuvx)
    fuvw = FF(x,M,c(.U,.V,.W))
    s[.Pre,] = M$q * (fuv - fuvw)
  }
}
```

```

        fuvwz = FF(x,M,c(.U,.V,.W,.Z))
        s[.Mld,] = M$q*(1-M$r) * (fuvw - fuvwz)
        fuvwy = FF(x,M,c(.U,.V,.W,.Y))
        s[.Svr,] = M$q*M$r * (fuvw - fuvwy)
        s[.RecS,] = M$q*M$r * fuvwy + M$q*(1-M$r) * fuvwz
        s[.RecA,] = (1-M$q) * fuvx
    }
    s
}

```

StateProbs()

A function to calculate the state probabilities for a vector of times **x**, using model **M**, with probability **p** that a trasmission occured at time 0.

```

StateProbs = function(x,p,M)
{
    p * StateProbs01(x,M,TRUE) + (1-p) * StateProbs01(x,M,FALSE)
}

```

Conditioning events

Vectors and functions specifying vectors that give the probabilities of events given the underlying states. Used to calculate, by Bayes rule, the probabilities of the underlying states given the observed events. The events include:

- **Unconditional**: no observation.
- **NoSymptoms**: no symptoms are observed.
- **Infected**: the individual is infected.
- **PcrTest()**: a NEGATIVE PCR test with specified sensitivity and specificity is observed.
- **AntigenTest()**: a NEGATIVE antigen test with specified sensitivity and specificity is observed.

```

Unconditional = c(1,1,1,1,1,1,1,1)
NoSymptoms = c(1,1,1,1,0,0,0,1)
Infected = c(0,1,1,1,1,1,0,0)

PcrTest = function(sens,spec=1)
{

```

```

        c(spec,spec,1-sens,1-sens,1-sens,1-sens,1-sens,1-sens)
    }

    AntigenTest = function(sens,spec=1)
    {
        c(spec,spec,1-sens,1-sens,1-sens,1-sens,spec,spec)
    }

```

ProbInfected()

A function to calculate the probability that an individual is infected at a vector of times **x** following exposure, where the probability of transmission is **p**, the SARS-CoV-2 model is specified by the structure **M**. The probabilities are conditional given the observations specified by the vector **observation**.

```

ProbInfected = function(x,p,observation,M)
{
    probs = StateProbs(x,p,M)
    bot = observation %*% probs
    top = (Infected * observation) %*% probs
    top/bot
}

```

PostProbTransmission()

A function to calculate the posterior probability that a transmission occurred at time 0, given an observation specified by **observation** at times **x**. The prior probability of transmission is specified by **p**, and the model by **M**.

```

PostProbTransmission = function(x,p,observation,M)
{
    q1 = observation %*% StateProbs01(x,M,T)
    q0 = observation %*% StateProbs01(x,M,F)
    q1 * p / (q1 * p + q0 * (1-p))
}

```

ConditionalStateProbs()

A function to calculate the conditional state probabilities for an individual at a vector of times **x** following exposure, where the probability of transmission is **p**, the SARS-CoV-2 model is specified by the structure **M**. The probabilities are conditional given the observations specified by the vector **observation**.

```
ConditionalStateProbs = function(x,p,M,observation)
{
  y = p * StateProbs01(x,M,TRUE) + (1-p) * StateProbs01(x,M,FALSE)
  for (j in 1:length(y[1,]))
  {
    y[,j] = y[,j]*observation
    y[,j] = y[,j]/sum(y[,j])
  }
  y
}
```

Functions to plot a pile up of state probabilities

First a function to draw a frame suitable for plotting probabilities.

```
frame = function(x,xl="Days from exposure",yl="Probability")
{
  plot(x,x,type="n",ylim=c(0,1), ylab=yl, xlab=xl)
}
```

Then a function to find the first index into a vector where the value is the maximum of the vector.

```
maximizer = function(x)
{
  (1:length(x))[x==max(x)][1]
}
```

Then a function to draw the pileup given the vector of times, the state probabilities, some colours and labels.

```
skeletonPileup = function(x,ss,stateCols,stateNames)
{
  frame(x,yl="Cumulative probability")
  s = apply(ss,2,cumsum)
  lns = rev(1:length(s[,1]))
  for (i in lns)
  {
    lines(x,s[i,])
    polygon(c(x,max(x),0),c(s[i,],0,0),col=stateCols[i],border=NA)
  }

  for (i in lns)
  {
```

```

        zz = ss[i,]
        if (i > 1)
            z = s[i-1,]
        else
            z = rep(0,length(ss))

        if (max(ss) > 0)
        {
            whj = maximizer(ss)
            whx = x[whj]
            whx = min(c(whx,0.90*max(x)))
            whx = max(c(whx,0.05*max(x)))
            why = z[whj] + ss[whj]/2
            text(whx,why,stateNames[i])
        }
    }
}

```

A function to draw a pileup of all the states.

```

pileUp = function(x,ss)
{
    stateCols = c("green","yellow","pink","orange","magenta","red","cyan","cyan")
    stateNames = c("Sus","Lat","Asy","Pre","Mld","Svr","RecS","RecA")
    skeletonPileup(x,ss,stateCols,stateNames)
}

```

A function to draw a pileup with some states combined.

```

pileup = function(x,sss,opt=2)
{
    ss = matrix(0,ncol=ncol(sss),nrow=nrow(sss)-2)

    if (opt == 2)
    {
        stateCols = c("green","yellow","pink","orange","red","cyan")
        stateNames = c("Sus","Lat","Asy","Pre","Sym","Rec")
        ss[1:4,] = sss[1:4,]
        ss[5,] = sss[5,] + sss[6,]
        ss[6,] = sss[7,] + sss[8,]
    }

    if (opt == 1)
    {
        stateCols = c("yellow","pink","orange","red","cyan","green")
    }
}

```



```

        stateNames = c("Lat", "Asy", "Pre", "Sym", "Rec", "Sus")
        ss[1:3,] = sss[2:4,]
        ss[4,] = sss[5,] + sss[6,]
        ss[5,] = sss[7,] + sss[8,]
        ss[6,] = sss[1,]
    }

    skeletonPileup(x,ss,stateCols,stateNames)
}

```