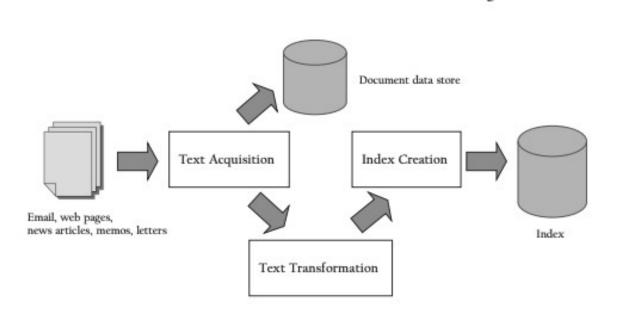
BOOLEAN AND VECTOR SPACE RETRIEVAL MODELS

Chapter 1,2 (IR Overview)

Chapter 7 (Boolean/Vector-Space Models)

Search Engine Architecture

- Search Engine has two main components:
 - Indexing process: build structures onto of the document collection to enable searching
 - Query process: uses those structures and the user query to produce a ranked list of documents.



Search Engine Architecture (Cont.)

- Text acquisition identifies the documents that will be searched.
 - This may include crawling or scanning the Web or identifying a subset of documents in a given collection.
- Index Creation creates the data structures (indexes) that enable fast searching.
 - Index creation must be efficient in terms of time and space and be efficiently updated when new documents are acquired.
 - Inverted indexes are the most common form of index used for search.



Search Engine Architecture (Cont.)

- Text transformation transforms documents into index terms or features.
 - Index terms can be words, phrases, names of people, dates, etc.
 - This process can involve :
 - 1. Removing stop words (common words from the document) since they contribute little to the description of the document content. Ex. "for", "to", "and", etc.
 - 2. Grouping words that are derived from a common stem (called stemming). Ex. Grouping the words "fish", "fishes", and "fishing" to just "fish" is just one example.
 - 3. Strip unwanted characters/markup (e.g. HTML tags, punctuation, numbers, etc.).
- •Ranking component transforms the user's query into terms and generates a ranked list of documents using scores based on the retrieval model.
 - Evaluation (using log data that records query execution time and user behavior) is used to evaluate the retrieval model.

Index Creation

- Index creation is the heart of the retrieval model.
- Not every term or feature should be used to build the index however, plus, we need some way to rank documents based on term importance.
- Document statistics: document statistics are stored in lookup tables
 - Records the counts of index terms in each document.
 - The <u>position</u> occurrence of index terms in each document,
 - Aggregated occurrence count of index terms in the document collection.
- Weighting: reflects the relative importance of words in documents which is then used in computing scores for ranking.
 - TF-IDF: Term Frequency Inverse Document Frequency

User Query

- Usually there is a query interface that parses the user query and transforms the query to standardize and extract relevant terms.
- Query Transformation: several techniques are used to improve the initial query such as spell checking, query suggestion, stemming, stop-word removal, etc.

Ranking

- Ranking (or query processing), calculates scores for documents.
- The most basic ranking algorithm is aggregating the score of all terms in the collection.

Retrieval Models

- Boolean Model (or Exact-Match)
- Vector-Space Model (ranking by query similarity)
- Probabilistic Ranking
- PageRank (ranking using link analysis document rank)
- Combination of various methods

Boolean Model (or Exact-Match Retrieval)

- A document is represented as a set of keywords (or features)
- Queries are Boolean expressions of keywords, connected by AND, OR, and NOT, including the use of brackets to indicate scope.
 - [[Rio & Brazil] | [Hilo & Hawaii]] & hotel & !Hilton], or
 - "William" AND "Shakespeare" AND NOT ("Marlowe" OR "bacon")
- The output of the Boolean model is a collection of documents that are relevant
 - Note: this does not support partial matches or ranking

Boolean Model (or Exact-Match Retrieval)

Advantages

- Popular retrieval model because it is easy to understand and explain to users.
- Reasonably efficient implementations possible for normal queries.

Disadvantages

- A document is typically represented by a bag of words/terms (unordered words with frequencies) and hence the effectiveness of this approach depends on the user's query and their inclusion of good "terms".
- Difficult to add relevance or limit number of documents returned.

Example

- Assume the following fragments comprise your document collection:
- Assume the following are stopwords: an, and, do, in, not
 - **Doc 1:** Interest in real estate speculation
 - Doc 2: Interest rates and rising home costs
 - Doc 3: Kids do not have an interest in banking
 - Doc 4: Lower interest rates, hotter real estate market
 - Doc 5: Feds interest in raising interest rates rising

	Doc1	Doc2	Doc3	Doc4	Doc5
bankin g					
costs				-	
estate					
feds					
have					
home					
hotter					

Construct the term-document index

What documents are returned to query:

- interest NOT rates
- (interest AND rates) NOT (rising OR kids)

Vector Space Model

- Instead of Boolean retrieval, lets rank the document based on relevance.
 - Measures similarity, and does not assume exact match
- <u>Problem:</u> Given two text documents (query is a special type of document), how similar are they?
- First, we need to extract features or tokens from documents.
- Example
 - D₁ the cat is blue
 - D₂ the cat is blue and the dog is green
 - Q cat dog
- Can use "Bag of Words" method in which words are extracted from text and thrown into a "bag" without order.
 - So, for D₁ "the cat is blue" is indistinguishable from "blue cat is the"

Vector-Space Model

- Both documents and queries are represented by a vector of index terms.
- For example document D_i is represented by a vector of index terms.
 - $D_i = (w_{i1}, w_{i2}, w_{i3}, \ldots, w_{ij})$,
 - where w_{ij} represents the weight of the jth term
 - zero means the term has no significance or does not exist in the document.
- A collection of *n* documents can be represented in the vector space model by a term-document matrix.
- Queries are represented in the same method.

Incidence matrix (Binary Weighting)

	text	terms
d ₁	The cat is green	<the, cat,="" green="" is,=""></the,>
d_2	The cat is red, the dog is green	<the, car,="" dog,="" green="" is,="" red,=""></the,>
Q	I want a green cat	<i, ,="" a="" cat="" green,="" want,=""></i,>

3 vectors in 9dimentional term vector space

	the	is	cat	dog	red	green	L	want	а
d ₁	1	1	1			1			
d_2	1	1	1	1	1	1			
Q			1			1	1	1	1

Weights: w_{ii} = 1 if document I contains term j and zero otherwise

What about non-binary weights? Well, we will talk about TF-IDF later

Vector-Space Model (Cont.)

- Ranking is done by computing the distance between each document and the query.
- A similarity measure is used (rather than a distance or dissimilarity measure), so that the documents with the highest scores are the most similar to the query.
- Using a similarity measure between the query and each document:
 - It is possible to rank the retrieved documents in the order of presumed relevance.
 - It is possible to enforce a certain threshold so that the size of the retrieved set can be controlled.

Similarity Measure - Inner Product

• Similarity between vectors for the document d_i and query q can be computed as the vector inner product (a.k.a. dot product):

$$sim(d_j, q) = d_j \cdot q = \sum_{i=1}^t w_{ij} w_{iq}$$

- •where \mathbf{w}_{ij} is the weight of term i in document j and \mathbf{w}_{iq} is the weight of term i in the query
- For binary vectors, the inner product is the number of matched query terms in the document (size of intersection).
- For weighted term vectors, it is the sum of the products of the weights of the matched terms.

Properties of Inner Product

- The inner product is unbounded.
- Favors long documents with a large number of unique terms.
- Measures how many terms matched but not how many terms are not matched.

Dot Product Example (Binary Weights)

	VV ₁	w ₂	w ₃	vv ₄	vv ₅	νν ₆	vv ₇	vv ₈	W ₉
	the	is	cat	dog	red	green	I	want	а
d ₁	1	1	1			1			
d_2	1	1	1	1	1	0			
Q			1			1	1	1	1

Same applies to non-binary weights

•
$$sim(d_1, Q) = d_1 \cdot Q$$

$$= w_{11}w_{Q1} + w_{12}w_{Q2} + w_{13}w_{Q3} + w_{14}^*w_{Q4} + w_{15}^*w_{Q5} + w_{16}^*w_{Q6} + w_{17}^*w_{Q7} + w_{18}w_{Q8} + w_{19}w_{Q9}$$

$$= 1*0 + 1*0 + 1*1 + 0*0 + 0*0 + 1*1 + 0*1 + 0*1 + 0*1 = 2$$

•
$$sim(d_1, Q) = d_2 \cdot Q =$$

$$= W_{21}W_{Q1} + W_{22}W_{Q2} + W_{23}W_{Q3} + W_{24}^*W_{Q4} + W_{25}^*W_{Q5} + W_{26}^*W_{Q6} + W_{27}^*W_{Q7} + W_{28}W_{Q8} + W_{29}W_{Q9}$$

$$= 1*0 + 1*0 + 1*1 + 1*0 + 1*0 + 0*1 + 0*1 + 0*1 + 0*1 = 1$$

Inner Product -- Examples

• Binary:

•
$$sim(D, Q) = 3$$

• Weighted:

•
$$D_1 = \langle 2, 3, 5 \rangle$$

•
$$D_2 = <3, 7, 1>$$

• Q =
$$<0, 0, 2>$$

• 0 means corresponding term not found in document or query

$$\cdot sim(D_1, Q) = 2*0 + 3*0 + 5*2 = 10$$

$$\cdot sim(D_2, Q) = 3*0 + 7*0 + 1*2 = 2$$

Cosine similarity

- The cosine correlation measures the cosine of the angle between the query and the document vectors.
- Note, the vectors must be normalized so all documents are represented by vectors of equal length.
- Given normalized vectors, the cosine angle between
 - two identical vectors is 1 (the angle is zero), and
 - two vectors that don't share any common terms, the cosine is 0 (the angle is 90).

Quick Review

- Given d = (x1, x2, x3, ..., xn) is a vector in an n-dimentional vector space.
- Length of x is given by

•
$$|d|^2 = x_1^2 + x_2^2 + x_3^2 + \dots + x_n^2$$

•
$$|d| = \sqrt{x_1^2 + x_2^2 + x_3^2 + \dots + x_n^2}$$

- If d₁ and d₂ are document vectors:
 - Dot product is given by

$$d_1 \cdot d_2 = w_{11} \cdot w_{21} + w_{12} w_{22} + w_{13} w_{23} + \dots + w_{1n} * w_{2n}$$

Cosine angle between d1 and d2 determine doc similarity

$$\bullet \cos(\theta) = \frac{d_1 \cdot d_2}{|d_1||d_2|}$$

Cosine Similarity Measure

- Cosine similarity measures the cosine of the angle between two vectors.
- Inner product normalized by the vector lengths.

$$CosSim(d_i,Q) = \frac{d_1 \cdot d_2}{|d_1||d_2|} = \frac{\sum_{i=1}^{t} (w_{ij}w_{iQ})}{\sqrt{\sum_{i=1}^{t} w_{ij}^2 \sum_{i=1}^{t} w_{iQ}^2}}$$

$$D_1 = \langle 2, 3, 5 \rangle$$

 $D_2 = \langle 3, 7, 1 \rangle$
 $Q = \langle 0, 0, 2 \rangle$

$$CosSim(d_1, Q) = \frac{d_1 \cdot Q}{|d_1||Q|} = \frac{0 \cdot 2 + 0 \cdot 3 + 2 \cdot 5}{\sqrt{(2^2 + 3^2 + 5^2) \cdot (0^2 + 0^2 + 2^2)}} = 0.81$$

$$CosSim(d_2,Q) = \frac{d_2 \cdot Q}{|d_2||Q|} = \frac{0*3 + 0*7 + 2*1}{\sqrt{(3^2 + 7^2 + 1^2)*(0^2 + 0^2 + 2^2)}} = 0.13$$

 D_1 is 6 times better than D_2 using cosine similarity but only 5 times better if we were to use dot product.

Term Weights: Term Frequency

- But how to compute the weight of terms?
- The term frequency component, tf, reflects the importance of a term in a document d_i.
 - f_{ij} = frequency of term i in document j

Where,

- tf_{ik} is the term frequency weight of term k in document D_i , and
- f_{ik} is the number of occurrences of term k in the document.

Term Weights: Inverse Document Frequency

- Terms that appear in many different documents are less indicative of overall topic, hence, term-frequency alone may not be the best weight.
- The inverse document frequency component (idf) reflects the importance of the term in the collection of documents.
- The more documents that a term occurs in, the less discriminating the term is between documents and, consequently, the less useful it will be in retrieval.

$$idf_k = \log \frac{N}{n_k}$$
 Usually written as 1+n_k

Where,

- Where idf_k is the inverse document frequency weight for term k,
- N is the number of documents in the collection, and
- n_k is the number of documents in which term k occurs.
- Log used to dampen the effect relative to tf.

Tf-IDF weighting

Tf-IDF weighting is the most common term frequency weighting scheme.

$$w_{ij} = tf_{ij} *idf_{i}$$

- A term occurring frequently in the document but rarely in the rest of the collection is given high weight.
- The effects of these two weights are combined by multiplying them (hence the name tf.idf).
- The reason for combining them this way is mostly empirical (developed by intuition and experiment).

Computing TF-IDF -- An Example

Given a document containing terms with given frequencies:

$$tf(d) = \langle t_1, t_2, t_3 \rangle = \langle 3, 2, 1 \rangle$$

 Assume collection contains 10,000 documents and document frequencies of these terms are:

$$tf(D) = \langle t_1, t_2, t_3 \rangle = \langle 50, 1300, 250 \rangle$$

Then:

```
• tf_a = 3/3; idf_a = log2(10000/50) = 7.6; tf-idf = 7.6

• tf_b = 2/3; idf_b = log2(10000/1300) = 2.9; tf-idf = 2.0

• tf_c = 1/3; idf_c = log2(10000/250) = 5.3; tf-idf = 1.8
```

Problems with Vector Space Model

Advantages

- Simple, mathematically based approach.
- Considers both local (tf) and global (idf) word occurrence frequencies.
- Provides partial matching and ranked results.
- Tends to work quite well in practice despite obvious weaknesses.
- Allows efficient implementation for large document collections.

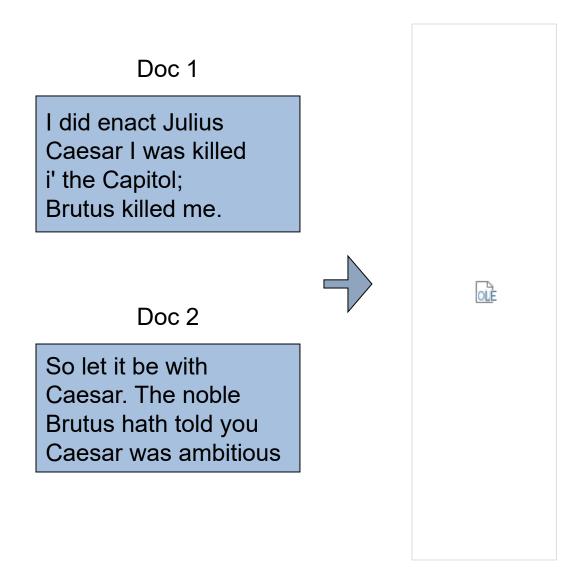
Disadvantages

- Missing semantic information (e.g. word sense).
- Missing syntactic information (e.g. phrase structure, word order, proximity information).
- Assumption of term independence (e.g. ignores synonomy).
- Lacks the control of a Boolean model (e.g., requiring a term to appear in a document).
- Doesn't deal with conditions such as :
 - synonyms (ex. Car and automobile) or
 - Polysems, words that have multiple meanings (ex. Java)

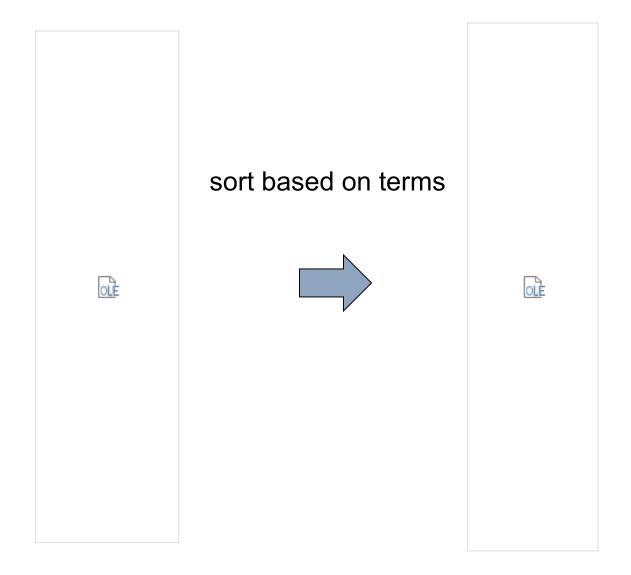
Fast TF-IDF

- Assume we are computing Cosine Similarity using TF-IDF weights
- One approach
 - Traverse entries calculating the product
 - Accumulate the vector lengths and divide at the end
- But how do we do this faster when we have a very sparse representation?

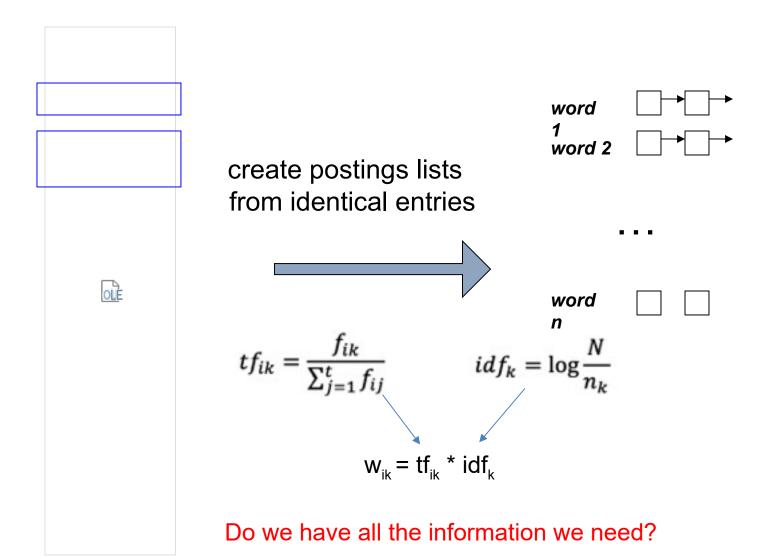
Index construction: collect documentIDs



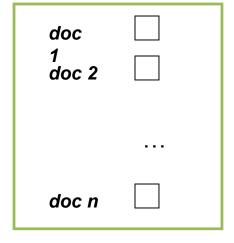
Index construction: sort dictionary



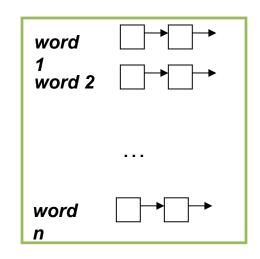
Index construction: create postings list



Index construction: Document Length



Document Length Index



Posting List

$$tf_{ik} = \frac{f_{ik}}{\sum_{j=1}^{t} f_{ij}} \qquad idf_k = \log \frac{N}{n_k}$$
$$w_{ik} = tf_{ik} * idf_k$$

Computing Cosine Scores

*Function CosineScore (q):

```
scores[N] \leftarrow 0 (cosine scores)
length[N] \leftarrow doc length list
postings[T] \leftarrow term frequency list
```

for each query term t do calculate $w_{t,q}$ and fetch postings list for t for each pair (d, $tf_{t,d}$) in postings list do Scores[d] += $w_{t,d}$ * $w_{t,q}$

for each document d in Length do Scores[d] = Scores[d] / Length[d]

return top k components of Scores[]