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Basic Level

define constants

```
x1 = 1.032; % inches
x2 = 0 ;
            % inches
x3 = 2.825 ; % inches
x4 = 9.0625; % inches
y1 = 5.936 ; % inches
y2 = 0 ;
            % inches
y3 = 1.16; % inches
y4 = 7.9375; % inches
pin_diameter = 0.25 ; % inches
theta = 20.577 * (pi/180); % (refers to the theta (in radians)
calculated using Pythagorean theorem)
w = 0.712; % inches
t = 0.09; % since values for arm and link are the same for simplicity
Force = 20 ; % lbf (refers to half the force applied to the handle due
 to symmetry)
FOS = 1.8; % (refers to the Factor of Safety required)
alpha = 0;
% solve for reaction forces
F1 = Force * (sin(alpha)*y4 + cos(alpha)*x4) / (sin(theta)*y3 +
cos(theta)*x3);
F3 = Force * (sin(alpha)*y4 + cos(alpha)*x4) / (sin(theta)*y3 +
cos(theta)*x3) ;
```

```
F2_x = -(Force)*(sin(alpha)*sin(theta)*y3 - sin(alpha)*sin(theta)*y4 +
 sin(alpha)*cos(theta)*x3 - sin(theta)*cos(alpha)*x4) / (sin(theta)*y3
 + cos(theta)*x3); % x-component of the force present at rivet 2
F2 y = -(Force)*(sin(alpha)*cos(theta)*y4 - sin(theta)*cos(alpha)*y3 -
 cos(alpha)*cos(theta)*x3 + cos(alpha)*cos(theta)*x4) / (sin(theta)*y3
 + cos(theta)*x3); % y-component of the force present at rivet 2
F2 = sqrt( (F2_x).^2 + (F2_y).^2 ) ;
Flink = F1;
% print reactions
fprintf('---- Basic Level (alpha=0) -----\n')
fprintf('Reaction forces:\n')
fprintf('F1 = %4.4f\n',F1)
fprintf('F2x = %4.4f\n',F2\_x)
fprintf('F2y = %4.4f\n',F2 y)
fprintf('F2 = %4.4f\n',F2)
fprintf('F3 = %4.4f\n',F3)
% rivet strength - direct shear
pin_radius_outer = 1/8 ; % inches
pin_thickness = 1/16 ; % inches
pin_radius_inner = pin_radius_outer - pin_thickness ; % inches
pin_inner_area = pi * pin_radius_inner^2 ; % inches^2
pin outer area = pi * pin radius outer^2 ; % inches^2
Area_Pin = pin_outer_area - pin_inner_area; % inches^2
Tau Pin 1 Shear = F1 / Area Pin; % psi
Tau_Pin_2_Shear = F2 / Area_Pin; % psi
Tau_Pin_3_Shear = F3 / Area_Pin; % psi
tau_rivet_critical = Tau_Pin_1_Shear;
Sy yield rivet = FOS*2*tau rivet critical;
% link strength - normal stress (axial)
Aaxial = t*(w-pin_diameter);
sigma_axial = Flink/Aaxial;
Sy yield axial = FOS*sigma axial;
% link strenght - normal stress (bearing)
Abearing = t*pin_diameter;
sigma_bearing = Flink/Abearing;
Sy_yield_bearing = FOS*sigma_bearing;
% link strength
1 = \operatorname{sqrt}((w/2)^2-(\operatorname{pin\_diameter}/2)^2);
Atearout = 2*1*t;
tau_tearout = Flink/Atearout;
Sy yield tearout = FOS*2*tau tearout;
% print yield strengths
fprintf('\nYield strengths:\n')
fprintf('Sy_yield_rivet = %4.4f\n',Sy_yield_rivet)
fprintf('Sy_yield_axial = %4.4f\n',Sy_yield_axial)
fprintf('Sy_yield_bearing = %4.4f\n',Sy_yield_bearing)
fprintf('Sy_yield_tearout = %4.4f\n',Sy_yield_tearout)
```

```
----- Basic Level (alpha=0) ------
Reaction forces:
F1 = 59.3782
F2x = 20.8694
F2y = -35.5899
F2 = 41.2574
F3 = 59.3782

Yield strengths:
Sy_yield_rivet = 5806.2847
Sy_yield_axial = 2570.4846
Sy_yield_bearing = 4750.2555
Sy_yield_tearout = 3562.6934
```

Medium Level

```
fprintf('\n----- Medium Level (alpha = 10 deg) -----\n')
alpha = 10*pi/180; %rad
% solve for reaction forces
F1 = Force * (sin(alpha)*y4 + cos(alpha)*x4) / (sin(theta)*y3 +
 cos(theta)*x3) ;
F3 = Force * (sin(alpha)*y4 + cos(alpha)*x4) / (sin(theta)*y3 +
 cos(theta)*x3);
F2 x = -(Force)*(sin(alpha)*sin(theta)*y3 - sin(alpha)*sin(theta)*y4 +
 sin(alpha)*cos(theta)*x3 - sin(theta)*cos(alpha)*x4) / (sin(theta)*y3
 + cos(theta)*x3); % x-component of the force present at rivet 2
F2_y = -(Force)*(sin(alpha)*cos(theta)*y4 - sin(theta)*cos(alpha)*y3 -
 cos(alpha)*cos(theta)*x3 + cos(alpha)*cos(theta)*x4) / (sin(theta)*y3
 + cos(theta)*x3); % y-component of the force present at rivet 2
F2 = sqrt((F2_x).^2 + (F2_y).^2);
Flink = F1;
% print reactions
fprintf('Reaction forces:\n')
fprintf('F1 = %4.4f\n',F1)
fprintf('F2x = %4.4f\n',F2\_x)
fprintf('F2y = %4.4f\n',F2_y)
fprintf('F2 = %4.4f\n',F2)
fprintf('F3 = %4.4f\n',F3)
% rivet strength - direct shear
pin_radius_outer = 1/8 ; % inches
pin_thickness = 1/16 ; % inches
pin_radius_inner = pin_radius_outer - pin_thickness ; % inches
pin_inner_area = pi * pin_radius_inner^2 ; % inches^2
pin_outer_area = pi * pin_radius_outer^2 ; % inches^2
Area_Pin = pin_outer_area - pin_inner_area; % inches^2
Tau_Pin_1_Shear = F1 / Area_Pin ; % psi
Tau_Pin_2_Shear = F2 / Area_Pin ; % psi
Tau Pin 3 Shear = F3 / Area Pin ; % psi
tau_rivet_critical = Tau_Pin_1_Shear;
Sy_yield_rivet = FOS*2*tau_rivet_critical;
```

```
% link strength - normal stress (axial)
Aaxial = t*(w-pin_diameter);
sigma axial = Flink/Aaxial;
Sy_yield_axial = FOS*sigma_axial;
% link strenght - normal stress (bearing)
Abearing = t*pin diameter;
sigma_bearing = Flink/Abearing;
Sy_yield_bearing = FOS*sigma_bearing;
% link strength
1 = \operatorname{sqrt}((w/2)^2-(\operatorname{pin diameter}/2)^2);
Atearout = 2*1*t;
tau tearout = Flink/Atearout;
Sy_yield_tearout = FOS*2*tau_tearout;
% print yield strengths
fprintf('\nYield strengths:\n')
fprintf('Sy_yield_rivet = %4.4f\n',Sy_yield_rivet)
fprintf('Sy_yield_axial = %4.4f\n',Sy_yield_axial)
fprintf('Sy_yield_bearing = %4.4f\n',Sy_yield_bearing)
fprintf('Sy_yield_tearout = %4.4f\n',Sy_yield_tearout)
----- Medium Level (alpha = 10 deg) -----
Reaction forces:
F1 = 67.5070
F2x = 20.2535
F2y = -43.5040
F2 = 47.9875
F3 = 67.5070
Yield strengths:
Sy_yield_rivet = 6601.1627
Sy\_yield\_axial = 2922.3829
Sy\_yield\_bearing = 5400.5636
Sy yield tearout = 4050.4247
```

Advanced Level

```
fprintf(\n----- Advanced Level (variable alpha) -----\n')
alpha_deg = (-15:75).';
alpha = alpha_deg*(pi/180); %rad

% solve for reaction forces
F1 = Force * (sin(alpha)*y4 + cos(alpha)*x4) / (sin(theta)*y3 +
cos(theta)*x3);
F3 = Force * (sin(alpha)*y4 + cos(alpha)*x4) / (sin(theta)*y3 +
cos(theta)*x3);
F2_x = -(Force)*(sin(alpha)*sin(theta)*y3 - sin(alpha)*sin(theta)*y4 +
sin(alpha)*cos(theta)*x3 - sin(theta)*cos(alpha)*x4) / (sin(theta)*y3 +
cos(theta)*x3); % x-component of the force present at rivet 2
```

```
F2_y = -(Force)*(sin(alpha)*cos(theta)*y4 - sin(theta)*cos(alpha)*y3 -
 cos(alpha)*cos(theta)*x3 + cos(alpha)*cos(theta)*x4) / (sin(theta)*y3
 + cos(theta)*x3); % y-component of the force present at rivet 2
F2 = sqrt( (F2 x).^2 + (F2 y).^2 ) ;
Flink = F1;
% rivet strength - direct shear
pin radius outer = 1/8 ; % inches
pin thickness = 1/16 ; % inches
pin_radius_inner = pin_radius_outer - pin_thickness ; % inches
pin_inner_area = pi * pin_radius_inner^2 ; % inches^2
pin_outer_area = pi * pin_radius_outer^2 ; % inches^2
Area_Pin = pin_outer_area - pin_inner_area; % inches^2
Tau_Pin_1_Shear = F1 / Area_Pin ; % psi
Tau Pin 2 Shear = F2 / Area Pin ; % psi
Tau_Pin_3_Shear = F3 / Area_Pin ; % psi
tau_rivet_critical = Tau_Pin_1_Shear;
Sy_yield_rivet = FOS*2*tau_rivet_critical;
% link strength - normal stress (axial)
Aaxial = t*(w-pin diameter);
sigma_axial = Flink/Aaxial;
Sy_yield_axial = FOS*sigma_axial;
% link strenght - normal stress (bearing)
Abearing = t*pin diameter;
sigma_bearing = Flink/Abearing;
Sy_yield_bearing = FOS*sigma_bearing;
% link strength
Rlink = w/2;
Rrivet = pin_diameter/2;
l = sqrt((Rlink)^2-(Rrivet)^2);
Atearout = 2*1*t;
tau tearout = Flink/Atearout;
Sy_yield_tearout = FOS*2*tau_tearout;
% plot required strengths
figure(1)
plot(alpha_deg, Sy_yield_axial, '.b');
hold on
plot(alpha_deg, Sy_yield_bearing, '.g');
hold on
plot(alpha_deg, Sy_yield_tearout, '.r');
xlabel('Alpha [degrees]');
ylabel('Required Strength of Link [psi]') ;
legend('S_{y,axial}', 'S_{y,bearing}','S_{y,tearout}','Location','NORTHWEST')
figure(2)
plot(alpha_deg, Sy_yield_rivet, '.k');
xlabel('Alpha [degrees]');
ylabel('Required Strength of Rivet [psi]');
```

```
% plot crushing force
figure(3)
F_can = 2*F1.*cos(theta);
plot(alpha_deg,F_can,'.k');
xlabel('Alpha [degrees]')
ylabel('Force on Can [lb_{f}]')
% claculate max crushing forces angle
[maxF,I] = max(F_can);
alphaMaxF = alpha_deg(I);
```





