

**EXERCISES:**

1. Given the weighted and directed graph  $G = (V, E)$ , with  $V = \{a, b, c, \dots, h\}$  and  $E$  determined by the following edges list:

(a,d)	(a,f)	(d,h)	(d,f)	(h,e)	(h,g)	(e,g)	(f,g)	(f,b)	(f,c)	(b,c)
1	2	1	6	2	7	2	3	4	5	2

- Draw the graph  $G$ .
- Write the depth-first traversal over  $G$ , starting with vertex  $a$ .
- Write one topological ordering for the vertices of  $G$ .
- Draw a minimum spanning tree of the undirected underlying graph, indicating its total weight.
- Draw the tree with the shortest paths from vertex  $a$  to all other vertices of the graph, indicating for each vertex the minimum distance calculated.

2. Given the weighted and directed graph  $G = (V, E)$ , with  $V = \{1, 2, 3, \dots, 8\}$  and  $E$  determined by the following edges list:

(1,2)	(1,3)	(2,7)	(3,2)	(3,4)	(3,5)	(3,7)	(4,5)	(4,8)	(5,6)	(5,8)	(7,5)	(7,6)	(8,6)
5	2	2	3	4	2	1	3	1	2	1	1	4	2

Draw the graph avoiding edges crossing, and then draw:

- A tree associated to a depth-first traversal starting with vertex **1**.
- A tree associated to a breath-first traversal starting with vertex **1**.
- A minimum spanning tree of the undirected underlying graph, indicating its total weight.
- A tree with the shortest paths from vertex **1** to all other vertices of the graph, indicating for each vertex the minimum distance calculated.
- A modification of the graph where their vertices are aligned and ordered topologically.