

# Paradoxes of the Material Conditional

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## 1 Indicative Conditional vs Subjunctive Conditional

**Indicative** *If Art does not sell Baja Bar & Grill, then we will meet at Baja Bar & Grill for Phil Club.*

**Subjunctive** *If Art had not put Baja Bar Grill up for sale, then we would not have to consider a different location for Phil Club.*

## 2 Materialism

**Materialism (M)** The material conditional, denoted by " $\supset$ ", is the correct analysis of the English indicative conditional.

$P$	$Q$	$P \supset Q$
$T$	$T$	$T$
$T$	$F$	$F$
$F$	$T$	$T$
$F$	$F$	$T$

## 3 Paradoxes

$\neg P \models P \supset Q$

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**C** If  $2+2=5$ , then  $2+2=3$ .

**Turkey-Paris Paradox<sup>1</sup>**

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**P1** If John is in Paris, then he is in France.

**P2** If John is in Istanbul, then he is in Turkey.

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**C** Therefore, if John is in Paris he is in Turkey, or, if he is in Istanbul he is in France.

**Switches Paradox<sup>2</sup>**

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**P1** If you throw switch S and T, the motor will start.

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**C** Therefore, either if you throw switch S the motor will start, or if you throw switch T the motor will start.

## 4 Resolutions

### 3-Valued Logic<sup>1</sup>

$P$	$Q$	$P \implies Q$
$T$	$T$	$T$
$T$	$F$	$F$
$T$	$G$	$G$
$F$	$T$	$G$
$F$	$F$	$G$
$F$	$G$	$G$
$G$	$T$	$T$
$G$	$F$	$F$
$G$	$G$	$G$

### Conversational Implicature<sup>4</sup>

### Robustness in Assertions<sup>3</sup>

"If  $P$ , then  $Q$ " is assertable just in case it is *robust* with respect to  $P$ . That is, if one

## 5 References

1. *The Propositional Logic of Ordinary Discourse* - William S. Cooper (1967)
2. *The Logic of Conditionals* - Ernst Adams (1965)
3. *On Assertion Conditions and Indicative Conditionals* - Frank Jackson (1979)
4. *Studies in the Way of Words* - H.P. Grice (1989)
5. *Ifs* - Editors: William L. Harper, Robert Stalnaker, Glenn Pearce (1981)