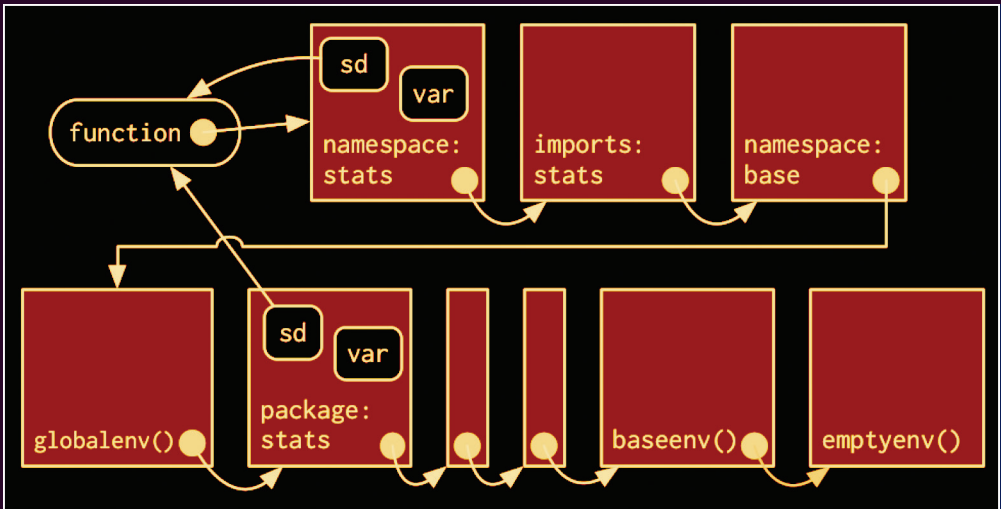


Advanced R



Hadley Wickham

Advanced R

Chapman & Hall/CRC

The R Series

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Aims and Scope

This book series reflects the recent rapid growth in the development and application of R, the programming language and software environment for statistical computing and graphics. R is now widely used in academic research, education, and industry. It is constantly growing, with new versions of the core software released regularly and more than 5,000 packages available. It is difficult for the documentation to keep pace with the expansion of the software, and this vital book series provides a forum for the publication of books covering many aspects of the development and application of R.

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- Using R for the study of topics of statistical methodology, such as linear and mixed modeling, time series, Bayesian methods, and missing data.
- The development of R, including programming, building packages, and graphics.

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CRC Press

Taylor & Francis Group
Boca Raton London New York

CRC Press is an imprint of the
Taylor & Francis Group, an **informa** business
A CHAPMAN & HALL BOOK

CRC Press
Taylor & Francis Group
6000 Broken Sound Parkway NW, Suite 300
Boca Raton, FL 33487-2742

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CRC Press is an imprint of Taylor & Francis Group, an Informa business

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Version Date: 20140813

International Standard Book Number-13: 978-1-4665-8697-0 (eBook - PDF)

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*To Jeff, who makes me happy, and who made
sure I had a life outside this book.*

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1

Introduction

With more than 10 years experience programming in R, I've had the luxury of being able to spend a lot of time trying to figure out and understand how the language works. This book is my attempt to pass on what I've learned so that you can quickly become an effective R programmer. Reading it will help you avoid the mistakes I've made and dead ends I've gone down, and will teach you useful tools, techniques, and idioms that can help you to attack many types of problems. In the process, I hope to show that, despite its frustrating quirks, R is, at its heart, an elegant and beautiful language, well tailored for data analysis and statistics.

If you are new to R, you might wonder what makes learning such a quirky language worthwhile. To me, some of the best features are:

- It's free, open source, and available on every major platform. As a result, if you do your analysis in R, anyone can easily replicate it.
- A massive set of packages for statistical modelling, machine learning, visualisation, and importing and manipulating data. Whatever model or graphic you're trying to do, chances are that someone has already tried to do it. At a minimum, you can learn from their efforts.
- Cutting edge tools. Researchers in statistics and machine learning will often publish an R package to accompany their articles. This means immediate access to the very latest statistical techniques and implementations.
- Deep-seated language support for data analysis. This includes features like missing values, data frames, and subsetting.
- A fantastic community. It is easy to get help from experts on the R-help mailing list (<https://stat.ethz.ch/mailman/listinfo/r-help>), stackoverflow (<http://stackoverflow.com/questions/tagged/r>), or subject-specific mailing lists like R-SIG-mixed-models (<https://stat.ethz.ch/mailman/listinfo/r-sig-mixed-models>).

[//stat.ethz.ch/mailman/listinfo/r-sig-mixed-models](http://stat.ethz.ch/mailman/listinfo/r-sig-mixed-models)) or `ggplot2` (<https://groups.google.com/forum/#!forum/ggplot2>). You can also connect with other R learners via twitter (<https://twitter.com/search?q=%23rstats>), linkedin (<http://www.linkedin.com/groups/R-Project-Statistical-Computing-77616>), and through many local user groups (<http://blog.revolutionanalytics.com/local-r-groups.html>).

- Powerful tools for communicating your results. R packages make it easy to produce html or pdf reports (<http://yihui.name/knitr/>), or create interactive websites (<http://www.rstudio.com/shiny/>).
- A strong foundation in functional programming. The ideas of functional programming are well suited to solving many of the challenges of data analysis. R provides a powerful and flexible toolkit which allows you to write concise yet descriptive code.
- An IDE (<http://www.rstudio.com/ide/>) tailored to the needs of interactive data analysis and statistical programming.
- Powerful metaprogramming facilities. R is not just a programming language, it is also an environment for interactive data analysis. Its metaprogramming capabilities allow you to write magically succinct and concise functions and provides an excellent environment for designing domain-specific languages.
- Designed to connect to high-performance programming languages like C, Fortran, and C++.

Of course, R is not perfect. R's biggest challenge is that most R users are not programmers. This means that:

- Much of the R code you'll see in the wild is written in haste to solve a pressing problem. As a result, code is not very elegant, fast, or easy to understand. Most users do not revise their code to address these shortcomings.
- Compared to other programming languages, the R community tends to be more focussed on results instead of processes. Knowledge of software engineering best practices is patchy: for instance, not enough R programmers use source code control or automated testing.
- Metaprogramming is a double-edged sword. Too many R functions use tricks to reduce the amount of typing at the cost of making code that is hard to understand and that can fail in unexpected ways.

- Inconsistency is rife across contributed packages, even within base R. You are confronted with over 20 years of evolution every time you use R. Learning R can be tough because there are many special cases to remember.
- R is not a particularly fast programming language, and poorly written R code can be terribly slow. R is also a profligate user of memory.

Personally, I think these challenges create a great opportunity for experienced programmers to have a profound positive impact on R and the R community. R users do care about writing high quality code, particularly for reproducible research, but they don't yet have the skills to do so. I hope this book will not only help more R users to become R programmers but also encourage programmers from other languages to contribute to R.

1.1 Who should read this book

This book is aimed at two complementary audiences:

- Intermediate R programmers who want to dive deeper into R and learn new strategies for solving diverse problems.
- Programmers from other languages who are learning R and want to understand why R works the way it does.

To get the most out of this book, you'll need to have written a decent amount of code in R or another programming language. You might not know all the details, but you should be familiar with how functions work in R and although you may currently struggle to use them effectively, you should be familiar with the `apply` family (like `apply()` and `lapply()`).

1.2 What you will get out of this book

This book describes the skills I think an advanced R programmer should have: the ability to produce quality code that can be used in a wide variety of circumstances.

After reading this book, you will:

- Be familiar with the fundamentals of R. You will understand complex data types and the best ways to perform operations on them. You will have a deep understanding of how functions work, and be able to recognise and use the four object systems in R.
- Understand what functional programming means, and why it is a useful tool for data analysis. You'll be able to quickly learn how to use existing tools, and have the knowledge to create your own functional tools when needed.
- Appreciate the double-edged sword of metaprogramming. You'll be able to create functions that use non-standard evaluation in a principled way, saving typing and creating elegant code to express important operations. You'll also understand the dangers of metaprogramming and why you should be careful about its use.
- Have a good intuition for which operations in R are slow or use a lot of memory. You'll know how to use profiling to pinpoint performance bottlenecks, and you'll know enough C++ to convert slow R functions to fast C++ equivalents.
- Be comfortable reading and understanding the majority of R code. You'll recognise common idioms (even if you wouldn't use them yourself) and be able to critique others' code.

1.3 Meta-techniques

There are two meta-techniques that are tremendously helpful for improving your skills as an R programmer: reading source code and adopting a scientific mindset.

Reading source code is important because it will help you write better code. A great place to start developing this skill is to look at the source code of the functions and packages you use most often. You'll find things that are worth emulating in your own code and you'll develop a sense of taste for what makes good R code. You will also see things that you don't like, either because its virtues are not obvious or it offends your sensibilities. Such code is nonetheless valuable, because it helps make concrete your opinions on good and bad code.

A scientific mindset is extremely helpful when learning R. If you don't understand how something works, develop a hypothesis, design some experiments, run them, and record the results. This exercise is extremely useful since if you can't figure something out and need to get help, you can easily show others what you tried. Also, when you learn the right answer, you'll be mentally prepared to update your world view. When I clearly describe a problem to someone else (the art of creating a reproducible example (<http://stackoverflow.com/questions/5963269>)), I often figure out the solution myself.

1.4 Recommended reading

R is still a relatively young language, and the resources to help you understand it are still maturing. In my personal journey to understand R, I've found it particularly helpful to use resources from other programming languages. R has aspects of both functional and object-oriented (OO) programming languages. Learning how these concepts are expressed in R will help you leverage your existing knowledge of other programming languages, and will help you identify areas where you can improve.

To understand why R's object systems work the way they do, I found *The Structure and Interpretation of Computer Programs* (<http://mitpress.mit.edu/sicp/full-text/book/book.html>) (SICP) by Harold Abelson and Gerald Jay Sussman, particularly helpful. It's a concise but deep book. After reading it, I felt for the first time that I could actually design my own object-oriented system. The book was my first introduction to the generic function style of OO common in R. It helped me understand its strengths and weaknesses. SICP also talks a lot about functional programming, and how to create simple functions which become powerful when combined.

To understand the trade-offs that R has made compared to other programming languages, I found *Concepts, Techniques and Models of Computer Programming* (<http://amzn.com/0262220695?tag=devtools-20>) by Peter van Roy and Sef Haridi extremely helpful. It helped me understand that R's copy-on-modify semantics make it substantially easier to reason about code, and that while its current implementation is not particularly efficient, it is a solvable problem.

If you want to learn to be a better programmer, there's no place better

to turn than *The Pragmatic Programmer* (<http://amzn.com/020161622X?tag=devtools-20>) by Andrew Hunt and David Thomas. This book is language agnostic, and provides great advice for how to be a better programmer.

1.5 Getting help

Currently, there are two main venues to get help when you're stuck and can't figure out what's causing the problem: stackoverflow (<http://stackoverflow.com>) and the R-help mailing list. You can get fantastic help in both venues, but they do have their own cultures and expectations. It's usually a good idea to spend a little time lurking, learning about community expectations, before you put up your first post.

Some good general advice:

- Make sure you have the latest version of R and of the package (or packages) you are having problems with. It may be that your problem is the result of a recently fixed bug.
- Spend some time creating a reproducible example (<http://stackoverflow.com/questions/5963269>). This is often a useful process in its own right, because in the course of making the problem reproducible you often figure out what's causing the problem.
- Look for related problems before posting. If someone has already asked your question and it has been answered, it's much faster for everyone if you use the existing answer.

1.6 Acknowledgments

I would like to thank the tireless contributors to R-help and, more recently, stackoverflow (<http://stackoverflow.com/questions/tagged/r>). There are too many to name individually, but I'd particularly like to thank Luke Tierney, John Chambers, Dirk Eddebuettel, JJ Allaire

and Brian Ripley for generously giving their time and correcting my countless misunderstandings.

This book was written in the open (<https://github.com/hadley/adv-r/>), and chapters were advertised on twitter (<https://twitter.com/hadleywickham>) when complete. It is truly a community effort: many people read drafts, fixed typos, suggested improvements, and contributed content. Without those contributors, the book wouldn't be nearly as good as it is, and I'm deeply grateful for their help. Special thanks go to Peter Li, who read the book from cover-to-cover and provided many fixes. Other outstanding contributors were Aaron Schumacher, @crtahlin, Lingbing Feng, @juancentro, and @johnbaums.

Thanks go to all contributors in alphabetical order: Aaron Schumacher, Aaron Wolen, @aaronwolen, @absolutelyNoWarranty, Adam Hunt, @agrabovsky, @ajdm, @alexbbrown, @alko989, @allegretto, @AmeliaMN, @andrewla, Andy Teucher, Anthony Damico, Anton Antonov, @aranlunzer, @arilamstein, @avilella, @baptiste, @blindjesse, @blmoore, @bnjmn, Brandon Hurr, @BrianDiggs, @Bryce, C. Jason Liang, @Carson, @cdrv, Ching Boon, @chiphogg, Christopher Brown, @christophergandrud, Clay Ford, @cornelius1729, @cplouffe, Craig Citro, @crossfitAL, @crowding, Crt Ahlin, @crtahlin, @cscheid, @cs-gillespie, @cusanovich, @cwarden, @cwickham, Daniel Lee, @darrkj, @Dasonk, David Hajage, David LeBauer, @dchudz, dennis feehan, @dfeehan, Dirk Eddelbuettel, @dkahle, @dlebauer, @dlschweizer, @dmontaner, @dougmitarotonda, @dpatschke, @duncandonutz, @EdFineOKL, @EDiLD, @eipi10, @elegrand, @EmilRehnberg, Eric C. Anderson, @etb, @fabian-s, Facundo Muñoz, @flammy0530, @fpepin, Frank Farach, @freezby, @fyears, Garrett Grolemond, @garrettgman, @gavinsimpson, @gggtest, Gökçen Eraslan, Gregg Whitworth, @gregorp, @gsee, @gsk3, @gthb, @hassaad85, @i, Iain Dillingham, @ijlyttle, Ilan Man, @immanuelcostigan, @initdch, Jason Asher, Jason Knight, @jasondavies, @jastingo, @jcborras, Jeff Allen, @jeharmse, @jentjr, @JestonBlu, @JimInNashville, @jinlong25, JJ Allaire, Jochen Van de Velde, Johann Hibschan, John Blischak, John Verzani, @johnbaums, @johnjosephhorton, Joris Muller, Joseph Casillas, @juancentro, @kdauria, @kenahoo, @kent37, Kevin Markham, Kevin Ushey, @kforner, Kirill Müller, Kun Ren, Laurent Gatto, @Lawrence-Liu, @ldfmrails, @lgatto, @liangcj, Lingbing Feng, @lynaghk, Maarten Kruijver, Mamoun Benghezal, @mannyishere, Matt Pettis, @mattbaggott, Matthew Grogan, @mattmalin, Michael Kane, @michaelbach, @mjsduncan, @Mullefa, @myqlarson, Nacho Caballero, Nick Carchedi, @nstjhp, @ogennadi, Oliver Keyes, @otepoti, Parker Abercrombie, @patperu,

Patrick Miller, @pdb61, @pengyu, Peter F Schulam, Peter Lindbrook, Peter Meilstrup, @philchalmers, @picasa, @piccolbo, @pierrerroudier, @pooryorick, R. Mark Sharp, Ramnath Vaidyanathan, @ramnathv, @Rappster, Ricardo Pietrobon, Richard Cotton, @richardreeve, @rmflight, @rmsharp, Robert M Flight, @RobertZK, @robiRagan, Romain François, @rrunner, @rubenfcasal, @sailingwave, @sarunas-merkliopas, @sbgraves237, Scott Ritchie, @scottko, @scottl, Sean Anderson, Sean Carmody, Sean Wilkinson, @sebastian-c, Sebastien Vigneau, @shabbychef, Shannon Rush, Simon O’Hanlon, Simon Potter, @SplashDance, @ste-fan, Stefan Widgren, @stephens999, Steven Pav, @strongh, @stuttgartur, @surmann, @swnydick, @taekyunk, Tal Galili, @talgalili, @tdenes, @Thomas, @thomasherbig, @thomaszumbrunn, Tim Cole, @tjmahr, Tom Buckley, Tom Crockett, @ttriche, @twjacobs, @tyhenkaline, @tylerritchie, @ulrichatz, @varun729, @victorkryukov, @vijaybarve, @vzemlys, @wchi144, @wibeasley, @WilCrofter, William Doane, Winston Chang, @wmc3, @wordnerd, Yoni Ben-Meshulam, @zackham, @zerokarmaleft, Zhongpeng Lin.

1.7 Conventions

Throughout this book I use `f()` to refer to functions, `g` to refer to variables and function parameters, and `h/` to paths.

Larger code blocks intermingle input and output. Output is commented so that if you have an electronic version of the book, e.g., <http://adv-r.had.co.nz>, you can easily copy and paste examples into R. Output comments look like `#>` to distinguish them from regular comments.

1.8 Colophon

This book was written in Rmarkdown (<http://rmarkdown.rstudio.com/>) inside Rstudio (<http://www.rstudio.com/ide/>). knitr (<http://yihui.name/knitr/>) and pandoc (<http://johnmacfarlane.net/pandoc/>) converted the raw Rmarkdown to html and pdf. The website (<http://adv-r.had.co.nz>) was made with jekyll (<http://jekyllrb.com/>), styled with bootstrap (<http://getbootstrap.com/>), and automatically

published to Amazon's S3 (<http://aws.amazon.com/s3/>) by travis-ci (<https://travis-ci.org/>). The complete source is available from github (<https://github.com/hadley/adv-r>).

Code is set in inconsolata (<http://levien.com/type/myfonts/inconsolata.html>).

Part I

Foundations

2

Data structures

This chapter summarises the most important data structures in base R. You've probably used many (if not all) of them before, but you may not have thought deeply about how they are interrelated. In this brief overview, I won't discuss individual types in depth. Instead, I'll show you how they fit together as a whole. If you need more details, you can find them in R's documentation.

R's base data structures can be organised by their dimensionality (1d, 2d, or nd) and whether they're homogeneous (all contents must be of the same type) or heterogeneous (the contents can be of different types). This gives rise to the five data types most often used in data analysis:

| | Homogeneous | Heterogeneous |
|----|---------------|---------------|
| 1d | Atomic vector | List |
| 2d | Matrix | Data frame |
| nd | Array | |

Almost all other objects are built upon these foundations. In Chapter 7 you'll see how more complicated objects are built of these simple pieces. Note that R has no 0-dimensional, or scalar types. Individual numbers or strings, which you might think would be scalars, are actually vectors of length one.

Given an object, the best way to understand what data structures it's composed of is to use `str()`. `str()` is short for structure and it gives a compact, human readable description of any R data structure.

Quiz

Take this short quiz to determine if you need to read this chapter. If the answers quickly come to mind, you can comfortably skip this chapter. You can check your answers in Section 2.5.

1. What are the three properties of a vector, other than its contents?
2. What are the four common types of atomic vectors? What are the two rare types?
3. What are attributes? How do you get them and set them?
4. How is a list different from an atomic vector? How is a matrix different from a data frame?
5. Can you have a list that is a matrix? Can a data frame have a column that is a matrix?

Outline

- Section 2.1 introduces you to atomic vectors and lists, R's 1d data structures.
- Section 2.2 takes a small detour to discuss attributes, R's flexible meta-data specification. Here you'll learn about factors, an important data structure created by setting attributes of an atomic vector.
- Section 2.3 introduces matrices and arrays, data structures for storing 2d and higher dimensional data.
- Section 2.4 teaches you about the data frame, the most important data structure for storing data in R. Data frames combine the behaviour of lists and matrices to make a structure ideally suited for the needs of statistical data.

2.1 Vectors

The basic data structure in R is the vector. Vectors come in two flavours: atomic vectors and lists. They have three common properties:

- Type, `typeof()`, what it is.

- Length, `length()`, how many elements it contains.
- Attributes, `attributes()`, additional arbitrary metadata.

They differ in the types of their elements: all elements of an atomic vector must be the same type, whereas the elements of a list can have different types.

NB: `is.vector()` does not test if an object is a vector. Instead it returns `TRUE` only if the object is a vector with no attributes apart from names. Use `is.atomic(x) || is.list(x)` to test if an object is actually a vector.

2.1.1 Atomic vectors

There are four common types of atomic vectors that I'll discuss in detail: logical, integer, double (often called numeric), and character. There are two rare types that I will not discuss further: complex and raw.

Atomic vectors are usually created with `c()`, short for combine:

```
dbl_var <- c(1, 2.5, 4.5)
# With the L suffix, you get an integer rather than a double
int_var <- c(1L, 6L, 10L)
# Use TRUE and FALSE (or T and F) to create logical vectors
log_var <- c(TRUE, FALSE, T, F)
chr_var <- c("these are", "some strings")
```

Atomic vectors are always flat, even if you nest `c()`'s:

```
c(1, c(2, c(3, 4)))
#> [1] 1 2 3 4
# the same as
c(1, 2, 3, 4)
#> [1] 1 2 3 4
```

Missing values are specified with `NA`, which is a logical vector of length 1. `NA` will always be coerced to the correct type if used inside `c()`, or you can create NAs of a specific type with `NA_real_` (a double vector), `NA_integer_` and `NA_character_`.

2.1.1.1 Types and tests

Given a vector, you can determine its type with `typeof()`, or check if it's a specific type with an “is” function: `is.character()`, `is.double()`, `is.integer()`, `is.logical()`, or, more generally, `is.atomic()`.

```
int_var <- c(1L, 6L, 10L)
typeof(int_var)
#> [1] "integer"
is.integer(int_var)
#> [1] TRUE
is.atomic(int_var)
#> [1] TRUE
```

```
dbl_var <- c(1, 2.5, 4.5)
typeof(dbl_var)
#> [1] "double"
is.double(dbl_var)
#> [1] TRUE
is.atomic(dbl_var)
#> [1] TRUE
```

NB: `is.numeric()` is a general test for the “numberliness” of a vector and returns `TRUE` for both integer and double vectors. It is not a specific test for double vectors, which are often called numeric.

```
is.numeric(int_var)
#> [1] TRUE
is.numeric(dbl_var)
#> [1] TRUE
```

2.1.1.2 Coercion

All elements of an atomic vector must be the same type, so when you attempt to combine different types they will be **coerced** to the most flexible type. Types from least to most flexible are: logical, integer, double, and character.

For example, combining a character and an integer yields a character:

```
str(c("a", 1))
#> chr [1:2] "a" "1"
```


When a logical vector is coerced to an integer or double, TRUE becomes 1 and FALSE becomes 0. This is very useful in conjunction with `sum()` and `mean()`

```
x <- c(FALSE, FALSE, TRUE)
as.numeric(x)
#> [1] 0 0 1

# Total number of TRUEs
sum(x)
#> [1] 1

# Proportion that are TRUE
mean(x)
#> [1] 0.3333
```

Coercion often happens automatically. Most mathematical functions (+, log, abs, etc.) will coerce to a double or integer, and most logical operations (&, |, any, etc) will coerce to a logical. You will usually get a warning message if the coercion might lose information. If confusion is likely, explicitly coerce with `as.character()`, `as.double()`, `as.integer()`, or `as.logical()`.

2.1.2 Lists

Lists are different from atomic vectors because their elements can be of any type, including lists. You construct lists by using `list()` instead of `c()`:

```
x <- list(1:3, "a", c(TRUE, FALSE, TRUE), c(2.3, 5.9))
str(x)
#> List of 4
#> $ : int [1:3] 1 2 3
#> $ : chr "a"
#> $ : logi [1:3] TRUE FALSE TRUE
#> $ : num [1:2] 2.3 5.9
```

Lists are sometimes called **recursive** vectors, because a list can contain other lists. This makes them fundamentally different from atomic vectors.

```
x <- list(list(list(list())))
str(x)
#> List of 1
#> $ :List of 1
#> ..$ :List of 1
#> .. ..$ : list()
is.recursive(x)
#> [1] TRUE
```

`c()` will combine several lists into one. If given a combination of atomic vectors and lists, `c()` will coerce the vectors to list before combining them. Compare the results of `list()` and `c()`:

```
x <- list(list(1, 2), c(3, 4))
y <- c(list(1, 2), c(3, 4))
str(x)
#> List of 2
#> $ :List of 2
#> ..$ : num 1
#> ..$ : num 2
#> $ : num [1:2] 3 4
str(y)
#> List of 4
#> $ : num 1
#> $ : num 2
#> $ : num 3
#> $ : num 4
```

The `typeof()` a list is `list`. You can test for a list with `is.list()` and coerce to a list with `as.list()`. You can turn a list into an atomic vector with `unlist()`. If the elements of a list have different types, `unlist()` uses the same coercion rules as `c()`.

Lists are used to build up many of the more complicated data structures in R. For example, both data frames (described in Section 2.4) and linear models objects (as produced by `lm()`) are lists:

```
is.list(mtcars)
#> [1] TRUE

mod <- lm(mpg ~ wt, data = mtcars)
is.list(mod)
#> [1] TRUE
```

2.1.3 Exercises

1. What are the six types of atomic vector? How does a list differ from an atomic vector?
2. What makes `is.vector()` and `is.numeric()` fundamentally different to `is.list()` and `is.character()`?
3. Test your knowledge of vector coercion rules by predicting the output of the following uses of `c()`:

```
c(1, FALSE)
c("a", 1)
c(list(1), "a")
c(TRUE, 1L)
```

4. Why do you need to use `unlist()` to convert a list to an atomic vector? Why doesn't `as.vector()` work?
5. Why is `1 == "1"` true? Why is `-1 < FALSE` true? Why is `"one" < 2` false?
6. Why is the default missing value, `NA`, a logical vector? What's special about logical vectors? (Hint: think about `c(FALSE, NA_character_)`.)

2.2 Attributes

All objects can have arbitrary additional attributes, used to store meta-data about the object. Attributes can be thought of as a named list (with unique names). Attributes can be accessed individually with `attr()` or all at once (as a list) with `attributes()`.

```
y <- 1:10
attr(y, "my_attribute") <- "This is a vector"
attr(y, "my_attribute")
#> [1] "This is a vector"
str(attributes(y))
#> List of 1
#> $ my_attribute: chr "This is a vector"
```

The `structure()` function returns a new object with modified attributes:

```
structure(1:10, my_attribute = "This is a vector")
#> [1] 1 2 3 4 5 6 7 8 9 10
#> attr("my_attribute")
#> [1] "This is a vector"
```

By default, most attributes are lost when modifying a vector:

```
attributes(y[1])
#> NULL
attributes(sum(y))
#> NULL
```

The only attributes not lost are the three most important:

- Names, a character vector giving each element a name, described in Section 2.2.0.1.
- Dimensions, used to turn vectors into matrices and arrays, described in Section 2.3.
- Class, used to implement the S3 object system, described in Section 7.2.

Each of these attributes has a specific accessor function to get and set values. When working with these attributes, use `names(x)`, `class(x)`, and `dim(x)`, not `attr(x, "names")`, `attr(x, "class")`, and `attr(x, "dim")`.

2.2.0.1 Names

You can name a vector in three ways:

- When creating it: `x <- c(a = 1, b = 2, c = 3)`.
- By modifying an existing vector in place: `x <- 1:3; names(x) <- c("a", "b", "c")`.
- By creating a modified copy of a vector: `x <- setNames(1:3, c("a", "b", "c"))`.

Names don't have to be unique. However, character subsetting, described in Section 3.4.1, is the most important reason to use names and it is most useful when the names are unique.

Not all elements of a vector need to have a name. If some names are missing, `names()` will return an empty string for those elements. If all names are missing, `names()` will return `NULL`.

```
y <- c(a = 1, 2, 3)
names(y)
#> [1] "a" "" ""

z <- c(1, 2, 3)
names(z)
#> NULL
```

You can create a new vector without names using `unname(x)`, or remove names in place with `names(x) <- NULL`.

2.2.1 Factors

One important use of attributes is to define factors. A factor is a vector that can contain only predefined values, and is used to store categorical data. Factors are built on top of integer vectors using two attributes: the `class()`, “factor”, which makes them behave differently from regular integer vectors, and the `levels()`, which defines the set of allowed values.

```
x <- factor(c("a", "b", "b", "a"))
x
#> [1] a b b a
#> Levels: a b
class(x)
#> [1] "factor"
levels(x)
#> [1] "a" "b"

# You can't use values that are not in the levels
x[2] <- "c"
#> Warning: invalid factor level, NA generated
x
#> [1] a <NA> b a
#> Levels: a b

# NB: you can't combine factors
c(factor("a"), factor("b"))
#> [1] 1 1
```

Factors are useful when you know the possible values a variable may take, even if you don't see all values in a given dataset. Using a factor

instead of a character vector makes it obvious when some groups contain no observations:

```
sex_char <- c("m", "m", "m")
sex_factor <- factor(sex_char, levels = c("m", "f"))

table(sex_char)
#> sex_char
#> m
#> 3
table(sex_factor)
#> sex_factor
#> m f
#> 3 0
```

Sometimes when a data frame is read directly from a file, a column you'd thought would produce a numeric vector instead produces a factor. This is caused by a non-numeric value in the column, often a missing value encoded in a special way like . or -. To remedy the situation, coerce the vector from a factor to a character vector, and then from a character to a double vector. (Be sure to check for missing values after this process.) Of course, a much better plan is to discover what caused the problem in the first place and fix that; using the `na.strings` argument to `read.csv()` is often a good place to start.

```
# Reading in "text" instead of from a file here:
z <- read.csv(text = "value\n12\n1\n.\n9")
typeof(z$value)
#> [1] "integer"
as.double(z$value)
#> [1] 3 2 1 4
# Oops, that's not right: 3 2 1 4 are the levels of a factor,
# not the values we read in!
class(z$value)
#> [1] "factor"
# We can fix it now:
as.double(as.character(z$value))
#> Warning: NAs introduced by coercion
#> [1] 12 1 NA 9
# Or change how we read it in:
z <- read.csv(text = "value\n12\n1\n.\n9", na.strings=".")
typeof(z$value)
```

```
#> [1] "integer"
class(z$value)
#> [1] "integer"
z$value
#> [1] 12  1 NA  9
# Perfect! :)
```

Unfortunately, most data loading functions in R automatically convert character vectors to factors. This is suboptimal, because there's no way for those functions to know the set of all possible levels or their optimal order. Instead, use the argument `stringsAsFactors = FALSE` to suppress this behaviour, and then manually convert character vectors to factors using your knowledge of the data. A global option, `options(stringsAsFactors = FALSE)`, is available to control this behaviour, but I don't recommend using it. Changing a global option may have unexpected consequences when combined with other code (either from packages, or code that you're `source()`ing), and global options make code harder to understand because they increase the number of lines you need to read to understand how a single line of code will behave.

While factors look (and often behave) like character vectors, they are actually integers. Be careful when treating them like strings. Some string methods (like `gsub()` and `grep1()`) will coerce factors to strings, while others (like `nchar()`) will throw an error, and still others (like `c()`) will use the underlying integer values. For this reason, it's usually best to explicitly convert factors to character vectors if you need string-like behaviour. In early versions of R, there was a memory advantage to using factors instead of character vectors, but this is no longer the case.

2.2.2 Exercises

1. An early draft used this code to illustrate `structure()`:

```
structure(1:5, comment = "my attribute")
#> [1] 1 2 3 4 5
```

But when you print that object you don't see the comment attribute. Why? Is the attribute missing, or is there something else special about it? (Hint: try using `help()`.)

2. What happens to a factor when you modify its levels?

```
f1 <- factor(letters)
levels(f1) <- rev(levels(f1))
```

3. What does this code do? How do f2 and f3 differ from f1?

```
f2 <- rev(factor(letters))

f3 <- factor(letters, levels = rev(letters))
```

2.3 Matrices and arrays

Adding a `dim()` attribute to an atomic vector allows it to behave like a multi-dimensional **array**. A special case of the array is the **matrix**, which has two dimensions. Matrices are used commonly as part of the mathematical machinery of statistics. Arrays are much rarer, but worth being aware of.

Matrices and arrays are created with `matrix()` and `array()`, or by using the assignment form of `dim()`:

```
# Two scalar arguments to specify rows and columns
a <- matrix(1:6, ncol = 3, nrow = 2)
# One vector argument to describe all dimensions
b <- array(1:12, c(2, 3, 2))

# You can also modify an object in place by setting dim()
c <- 1:6
dim(c) <- c(3, 2)
c
#>      [,1] [,2]
#> [1,]    1    4
#> [2,]    2    5
#> [3,]    3    6
dim(c) <- c(2, 3)
c
#>      [,1] [,2] [,3]
#> [1,]    1    3    5
#> [2,]    2    4    6
```

`length()` and `names()` have high-dimensional generalisations:

- `length()` generalises to `nrow()` and `ncol()` for matrices, and `dim()` for arrays.

- `names()` generalises to `rownames()` and `colnames()` for matrices, and `dimnames()`, a list of character vectors, for arrays.

```
length(a)
#> [1] 6
nrow(a)
#> [1] 2
ncol(a)
#> [1] 3
rownames(a) <- c("A", "B")
colnames(a) <- c("a", "b", "c")
a
#>   a b c
#> A 1 3 5
#> B 2 4 6

length(b)
#> [1] 12
dim(b)
#> [1] 2 3 2
dimnames(b) <- list(c("one", "two"), c("a", "b", "c"), c("A", "B"))
b
#> , , A
#>
#>   a b c
#> one 1 3 5
#> two 2 4 6
#>
#> , , B
#>
#>   a b c
#> one 7 9 11
#> two 8 10 12
```

`c()` generalises to `cbind()` and `rbind()` for matrices, and to `abind()` (provided by the `abind` package) for arrays. You can transpose a matrix with `t()`; the generalised equivalent for arrays is `aperm()`.

You can test if an object is a matrix or array using `is.matrix()` and `is.array()`, or by looking at the length of the `dim()`. `as.matrix()` and `as.array()` make it easy to turn an existing vector into a matrix or array.

Vectors are not the only 1-dimensional data structure. You can have matrices with a single row or single column, or arrays with a single

dimension. They may print similarly, but will behave differently. The differences aren't too important, but it's useful to know they exist in case you get strange output from a function (`tapply()` is a frequent offender). As always, use `str()` to reveal the differences.

```
str(1:3)                # 1d vector
#> int [1:3] 1 2 3
str(matrix(1:3, ncol = 1)) # column vector
#> int [1:3, 1] 1 2 3
str(matrix(1:3, nrow = 1)) # row vector
#> int [1, 1:3] 1 2 3
str(array(1:3, 3))       # "array" vector
#> int [1:3(1d)] 1 2 3
```

While atomic vectors are most commonly turned into matrices, the dimension attribute can also be set on lists to make list-matrices or list-arrays:

```
l <- list(1:3, "a", TRUE, 1.0)
dim(l) <- c(2, 2)
l
#>      [,1]      [,2]
#> [1,] Integer,3 TRUE
#> [2,] "a"      1
```

These are relatively esoteric data structures, but can be useful if you want to arrange objects into a grid-like structure. For example, if you're running models on a spatio-temporal grid, it might be natural to preserve the grid structure by storing the models in a 3d array.

2.3.1 Exercises

1. What does `dim()` return when applied to a vector?
2. If `is.matrix(x)` is `TRUE`, what will `is.array(x)` return?
3. How would you describe the following three objects? What makes them different to `1:5`?

```
x1 <- array(1:5, c(1, 1, 5))
x2 <- array(1:5, c(1, 5, 1))
x3 <- array(1:5, c(5, 1, 1))
```

2.4 Data frames

A data frame is the most common way of storing data in R, and if used systematically (<http://vita.had.co.nz/papers/tidy-data.pdf>) makes data analysis easier. Under the hood, a data frame is a list of equal-length vectors. This makes it a 2-dimensional structure, so it shares properties of both the matrix and the list. This means that a data frame has `names()`, `colnames()`, and `rownames()`, although `names()` and `colnames()` are the same thing. The `length()` of a data frame is the length of the underlying list and so is the same as `ncol()`; `nrow()` gives the number of rows.

As described in Chapter 3, you can subset a data frame like a 1d structure (where it behaves like a list), or a 2d structure (where it behaves like a matrix).

2.4.1 Creation

You create a data frame using `data.frame()`, which takes named vectors as input:

```
df <- data.frame(x = 1:3, y = c("a", "b", "c"))
str(df)
#> 'data.frame':    3 obs. of  2 variables:
#>  $ x: int  1 2 3
#>  $ y: Factor w/ 3 levels "a","b","c": 1 2 3
```

Beware `data.frame()`'s default behaviour which turns strings into factors. Use `stringsAsFactors = FALSE` to suppress this behaviour:

```
df <- data.frame(
  x = 1:3,
  y = c("a", "b", "c"),
  stringsAsFactors = FALSE)
str(df)
#> 'data.frame':    3 obs. of  2 variables:
#>  $ x: int  1 2 3
#>  $ y: chr  "a" "b" "c"
```

2.4.2 Testing and coercion

Because a `data.frame` is an S3 class, its type reflects the underlying vector used to build it: the list. To check if an object is a data frame, use `class()` or test explicitly with `is.data.frame()`:

```
typeof(df)
#> [1] "list"
class(df)
#> [1] "data.frame"
is.data.frame(df)
#> [1] TRUE
```

You can coerce an object to a data frame with `as.data.frame()`:

- A vector will create a one-column data frame.
- A list will create one column for each element; it's an error if they're not all the same length.
- A matrix will create a data frame with the same number of columns and rows.

2.4.3 Combining data frames

You can combine data frames using `cbind()` and `rbind()`:

```
cbind(df, data.frame(z = 3:1))
#>   x y z
#> 1 1 a 3
#> 2 2 b 2
#> 3 3 c 1
rbind(df, data.frame(x = 10, y = "z"))
#>   x y
#> 1  1 a
#> 2  2 b
#> 3  3 c
#> 4 10 z
```

When combining column-wise, the number of rows must match, but row names are ignored. When combining row-wise, both the number

and names of columns must match. Use `plyr::rbind.fill()` to combine data frames that don't have the same columns.

It's a common mistake to try and create a data frame by `cbind()`ing vectors together. This doesn't work because `cbind()` will create a matrix unless one of the arguments is already a data frame. Instead use `data.frame()` directly:

```
bad <- data.frame(cbind(a = 1:2, b = c("a", "b")))
str(bad)
#> 'data.frame':    2 obs. of  2 variables:
#> $ a: Factor w/ 2 levels "1","2": 1 2
#> $ b: Factor w/ 2 levels "a","b": 1 2
good <- data.frame(a = 1:2, b = c("a", "b"),
  stringsAsFactors = FALSE)
str(good)
#> 'data.frame':    2 obs. of  2 variables:
#> $ a: int  1 2
#> $ b: chr  "a" "b"
```

The conversion rules for `cbind()` are complicated and best avoided by ensuring all inputs are of the same type.

2.4.4 Special columns

Since a data frame is a list of vectors, it is possible for a data frame to have a column that is a list:

```
df <- data.frame(x = 1:3)
df$y <- list(1:2, 1:3, 1:4)
df
#>   x      y
#> 1 1      1, 2
#> 2 2      1, 2, 3
#> 3 3 1, 2, 3, 4
```

However, when a list is given to `data.frame()`, it tries to put each item of the list into its own column, so this fails:

```
data.frame(x = 1:3, y = list(1:2, 1:3, 1:4))
#> Error: arguments imply differing number of rows: 2, 3, 4
```

A workaround is to use `I()`, which causes `data.frame()` to treat the list as one unit:

```
df1 <- data.frame(x = 1:3, y = I(list(1:2, 1:3, 1:4)))
str(df1)
#> 'data.frame':    3 obs. of  2 variables:
#>  $ x: int  1 2 3
#>  $ y:List of 3
#>   ..$ : int  1 2
#>   ..$ : int  1 2 3
#>   ..$ : int  1 2 3 4
#>   ..- attr(*, "class")= chr "AsIs"
df1[2, "y"]
#> [[1]]
#> [1] 1 2 3
```

`I()` adds the `AsIs` class to its input, but this can usually be safely ignored.

Similarly, it's also possible to have a column of a data frame that's a matrix or array, as long as the number of rows matches the data frame:

```
dfm <- data.frame(x = 1:3, y = I(matrix(1:9, nrow = 3)))
str(dfm)
#> 'data.frame':    3 obs. of  2 variables:
#>  $ x: int  1 2 3
#>  $ y: 'AsIs' int  [1:3, 1:3] 1 2 3 4 5 6 7 8 9
dfm[2, "y"]
#>      [,1] [,2] [,3]
#> [1,]    2    5    8
```

Use list and array columns with caution: many functions that work with data frames assume that all columns are atomic vectors.

2.4.5 Exercises

1. What attributes does a data frame possess?
2. What does `as.matrix()` do when applied to a data frame with columns of different types?
3. Can you have a data frame with 0 rows? What about 0 columns?

2.5 Answers

1. The three properties of a vector are type, length, and attributes.
2. The four common types of atomic vector are logical, integer, double (sometimes called numeric), and character. The two rarer types are complex and raw.
3. Attributes allow you to associate arbitrary additional meta-data to any object. You can get and set individual attributes with `attr(x, "y")` and `attr(x, "y") <- value`; or get and set all attributes at once with `attributes()`.
4. The elements of a list can be any type (even a list); the elements of an atomic vector are all of the same type. Similarly, every element of a matrix must be the same type; in a data frame, the different columns can have different types.
5. You can make “list-array” by assuming dimensions to a list. You can make a matrix a column of a data frame with `df$x <- matrix()`, or using `I()` when creating a new data frame `data.frame(x = I(matrix()))`.

3

Subsetting

R's subsetting operators are powerful and fast. Mastery of subsetting allows you to succinctly express complex operations in a way that few other languages can match. Subsetting is hard to learn because you need to master a number of interrelated concepts:

- The three subsetting operators.
- The six types of subsetting.
- Important differences in behaviour for different objects (e.g., vectors, lists, factors, matrices, and data frames).
- The use of subsetting in conjunction with assignment.

This chapter helps you master subsetting by starting with the simplest type of subsetting: subsetting an atomic vector with `[]`. It then gradually extends your knowledge, first to more complicated data types (like arrays and lists), and then to the other subsetting operators, `[[` and `$`. You'll then learn how subsetting and assignment can be combined to modify parts of an object, and, finally, you'll see a large number of useful applications.

Subsetting is a natural complement to `str()`. `str()` shows you the structure of any object, and subsetting allows you to pull out the pieces that you're interested in.

Quiz

Take this short quiz to determine if you need to read this chapter. If the answers quickly come to mind, you can comfortably skip this chapter. Check your answers in Section 3.5.

1. What is the result of subsetting a vector with positive integers, negative integers, a logical vector, or a character vector?

2. What's the difference between `[]`, `[[`, and `$` when applied to a list?
3. When should you use `drop = FALSE`?
4. If `x` is a matrix, what does `x[] <- 0` do? How is it different to `x <- 0`?
5. How can you use a named vector to relabel categorical variables?

Outline

- Section 3.1 starts by teaching you about `[]`. You'll start by learning the six types of data that you can use to subset atomic vectors. You'll then learn how those six data types act when used to subset lists, matrices, data frames, and S3 objects.
- Section 3.2 expands your knowledge of subsetting operators to include `[[` and `$`, focussing on the important principles of simplifying vs. preserving.
- In Section 3.3 you'll learn the art of subassignment, combining subsetting and assignment to modify parts of an object.
- Section 3.4 leads you through eight important, but not obvious, applications of subsetting to solve problems that you often encounter in a data analysis.

3.1 Data types

It's easiest to learn how subsetting works for atomic vectors, and then how it generalises to higher dimensions and other more complicated objects. We'll start with `[]`, the most commonly used operator. Section 3.2 will cover `[[` and `$`, the two other main subsetting operators.

3.1.1 Atomic vectors

Let's explore the different types of subsetting with a simple vector, `x`.

```
x <- c(2.1, 4.2, 3.3, 5.4)
```

Note that the number after the decimal point gives the original position in the vector.

There are five things that you can use to subset a vector:

- **Positive integers** return elements at the specified positions:

```
x[c(3, 1)]
#> [1] 3.3 2.1
x[order(x)]
#> [1] 2.1 3.3 4.2 5.4

# Duplicated indices yield duplicated values
x[c(1, 1)]
#> [1] 2.1 2.1

# Real numbers are silently truncated to integers
x[c(2.1, 2.9)]
#> [1] 4.2 4.2
```

- **Negative integers** omit elements at the specified positions:

```
x[-c(3, 1)]
#> [1] 4.2 5.4
```

You can't mix positive and negative integers in a single subset:

```
x[c(-1, 2)]
#> Error: only 0's may be mixed with negative subscripts
```

- **Logical vectors** select elements where the corresponding logical value is TRUE. This is probably the most useful type of subsetting because you write the expression that creates the logical vector:

```
x[c(TRUE, TRUE, FALSE, FALSE)]
#> [1] 2.1 4.2
x[x > 3]
#> [1] 4.2 3.3 5.4
```

If the logical vector is shorter than the vector being subsetted, it will be *recycled* to be the same length.

```
x[c(TRUE, FALSE)]
#> [1] 2.1 3.3
# Equivalent to
x[c(TRUE, FALSE, TRUE, FALSE)]
#> [1] 2.1 3.3
```

A missing value in the index always yields a missing value in the output:

```
x[c(TRUE, TRUE, NA, FALSE)]
#> [1] 2.1 4.2 NA
```

- **Nothing** returns the original vector. This is not useful for vectors but is very useful for matrices, data frames, and arrays. It can also be useful in conjunction with assignment.

```
x[]
#> [1] 2.1 4.2 3.3 5.4
```

- **Zero** returns a zero-length vector. This is not something you usually do on purpose, but it can be helpful for generating test data.

```
x[0]
#> numeric(0)
```

If the vector is named, you can also use:

- **Character vectors** to return elements with matching names.

```
(y <- setNames(x, letters[1:4]))
#>  a  b  c  d
#> 2.1 4.2 3.3 5.4
y[c("d", "c", "a")]
#>  d  c  a
#> 5.4 3.3 2.1
```

```
# Like integer indices, you can repeat indices
y[c("a", "a", "a")]
#>  a  a  a
#> 2.1 2.1 2.1
```

```
# When subsetting with [ names are always matched exactly
z <- c(abc = 1, def = 2)
z[c("a", "d")]
#> <NA> <NA>
#>  NA  NA
```

3.1.2 Lists

Subsetting a list works in the same way as subsetting an atomic vector. Using `[]` will always return a list; `[[` and `$`, as described below, let you pull out the components of the list.

3.1.3 Matrices and arrays

You can subset higher-dimensional structures in three ways:

- With multiple vectors.
- With a single vector.
- With a matrix.

The most common way of subsetting matrices (2d) and arrays (>2d) is a simple generalisation of 1d subsetting: you supply a 1d index for each dimension, separated by a comma. Blank subsetting is now useful because it lets you keep all rows or all columns.

```
a <- matrix(1:9, nrow = 3)
colnames(a) <- c("A", "B", "C")
a[1:2, ]
#>      A B C
#> [1,] 1 4 7
#> [2,] 2 5 8
a[c(T, F, T), c("B", "A")]
#>      B A
#> [1,] 4 1
#> [2,] 6 3
a[0, -2]
#>      A C
```

By default, `[]` will simplify the results to the lowest possible dimensionality. See Section 3.2.1 to learn how to avoid this.

Because matrices and arrays are implemented as vectors with special attributes, you can subset them with a single vector. In that case, they will behave like a vector. Arrays in R are stored in column-major order:

```
(vals <- outer(1:5, 1:5, FUN = "paste", sep = ","))
#>      [,1] [,2] [,3] [,4] [,5]
```

```
#> [1,] "1,1" "1,2" "1,3" "1,4" "1,5"
#> [2,] "2,1" "2,2" "2,3" "2,4" "2,5"
#> [3,] "3,1" "3,2" "3,3" "3,4" "3,5"
#> [4,] "4,1" "4,2" "4,3" "4,4" "4,5"
#> [5,] "5,1" "5,2" "5,3" "5,4" "5,5"
vals[c(4, 15)]
#> [1] "4,1" "5,3"
```

You can also subset higher-dimensional data structures with an integer matrix (or, if named, a character matrix). Each row in the matrix specifies the location of one value, where each column corresponds to a dimension in the array being subsetted. This means that you use a 2 column matrix to subset a matrix, a 3 column matrix to subset a 3d array, and so on. The result is a vector of values:

```
vals <- outer(1:5, 1:5, FUN = "paste", sep = ",")
select <- matrix(ncol = 2, byrow = TRUE, c(
  1, 1,
  3, 1,
  2, 4
))
vals[select]
#> [1] "1,1" "3,1" "2,4"
```

3.1.4 Data frames

Data frames possess the characteristics of both lists and matrices: if you subset with a single vector, they behave like lists; if you subset with two vectors, they behave like matrices.

```
df <- data.frame(x = 1:3, y = 3:1, z = letters[1:3])

df[df$x == 2, ]
#>   x y z
#> 2 2 2 b
df[c(1, 3), ]
#>   x y z
#> 1 1 3 a
#> 3 3 1 c
```

```
# There are two ways to select columns from a data frame
```

```
# Like a list:
df[c("x", "z")]
#>   x z
#> 1 1 a
#> 2 2 b
#> 3 3 c
# Like a matrix
df[, c("x", "z")]
#>   x z
#> 1 1 a
#> 2 2 b
#> 3 3 c

# There's an important difference if you select a single
# column: matrix subsetting simplifies by default, list
# subsetting does not.
str(df["x"])
#> 'data.frame':   3 obs. of  1 variable:
#> $ x: int  1 2 3
str(df[, "x"])
#> int [1:3] 1 2 3
```

3.1.5 S3 objects

S3 objects are made up of atomic vectors, arrays, and lists, so you can always pull apart an S3 object using the techniques described above and the knowledge you gain from `str()`.

3.1.6 S4 objects

There are also two additional subsetting operators that are needed for S4 objects: `@` (equivalent to `$`), and `slot()` (equivalent to `[[`). `@` is more restrictive than `$` in that it will return an error if the slot does not exist. These are described in more detail in Section 7.3.

3.1.7 Exercises

1. Fix each of the following common data frame subsetting errors:

```
mtcars[mtcars$cyl = 4, ]
mtcars[-1:4, ]
mtcars[mtcars$cyl <= 5]
mtcars[mtcars$cyl == 4 | 6, ]
```

2. Why does `x <- 1:5; x[NA]` yield five missing values? (Hint: why is it different from `x[NA_real_]`?)
3. What does `upper.tri()` return? How does subsetting a matrix with it work? Do we need any additional subsetting rules to describe its behaviour?

```
x <- outer(1:5, 1:5, FUN = "*")
x[upper.tri(x)]
```

4. Why does `mtcars[1:20]` return a error? How does it differ from the similar `mtcars[1:20,]`?
5. Implement your own function that extracts the diagonal entries from a matrix (it should behave like `diag(x)` where `x` is a matrix).
6. What does `df[is.na(df)] <- 0` do? How does it work?

3.2 Subsetting operators

There are two other subsetting operators: `[[` and `$`. `[[` is similar to `[`, except it can only return a single value and it allows you to pull pieces out of a list. `$` is a useful shorthand for `[[` combined with character subsetting.

You need `[[` when working with lists. This is because when `[` is applied to a list it always returns a list: it never gives you the contents of the list. To get the contents, you need `[[`:

“If list `x` is a train carrying objects, then `x[[5]]` is the object in car 5; `x[4:6]` is a train of cars 4-6.”

— @RLangTip

Because it can return only a single value, you must use `[[` with either a single positive integer or a string:


```

a <- list(a = 1, b = 2)
a[[1]]
#> [1] 1
a[["a"]]
#> [1] 1

# If you do supply a vector it indexes recursively
b <- list(a = list(b = list(c = list(d = 1))))
b[[c("a", "b", "c", "d")]]
#> [1] 1
# Same as
b[["a"]][["b"]][["c"]][["d"]]
#> [1] 1

```

Because data frames are lists of columns, you can use `[[` to extract a column from data frames: `mtcars[[1]]`, `mtcars[["cyl"]]`.

S3 and S4 objects can override the standard behaviour of `[` and `[[` so they behave differently for different types of objects. The key difference is usually how you select between simplifying or preserving behaviours, and what the default is.

3.2.1 Simplifying vs. preserving subsetting

It's important to understand the distinction between simplifying and preserving subsetting. Simplifying subsets returns the simplest possible data structure that can represent the output, and is useful interactively because it usually gives you what you want. Preserving subsetting keeps the structure of the output the same as the input, and is generally better for programming because the result will always be the same type. Omitting `drop = FALSE` when subsetting matrices and data frames is one of the most common sources of programming errors. (It will work for your test cases, but then someone will pass in a single column data frame and it will fail in an unexpected and unclear way.)

Unfortunately, how you switch between simplifying and preserving differs for different data types, as summarised in the table below.

| | Simplifying | Preserving |
|--------|---------------------|-------------------|
| Vector | <code>x[[1]]</code> | <code>x[1]</code> |
| List | <code>x[[1]]</code> | <code>x[1]</code> |

| | Simplifying | Preserving |
|------------|---|---|
| Factor | <code>x[1:4, drop = T]</code> | <code>x[1:4]</code> |
| Array | <code>x[1,]</code> or <code>x[, 1]</code> | <code>x[1, , drop = F]</code> or <code>x[, 1, drop = F]</code> |
| Data frame | <code>x[, 1]</code> or <code>x[[1]]</code> | <code>x[, 1, drop = F]</code> or <code>x[1]</code> |

Preserving is the same for all data types: you get the same type of output as input. Simplifying behaviour varies slightly between different data types, as described below:

- **Atomic vector:** removes names.

```
x <- c(a = 1, b = 2)
x[1]
#> a
#> 1
x[[1]]
#> [1] 1
```

- **List:** return the object inside the list, not a single element list.

```
y <- list(a = 1, b = 2)
str(y[1])
#> List of 1
#> $ a: num 1
str(y[[1]])
#> num 1
```

- **Factor:** drops any unused levels.

```
z <- factor(c("a", "b"))
z[1]
#> [1] a
#> Levels: a b
z[1, drop = TRUE]
#> [1] a
#> Levels: a
```

- **Matrix** or **array:** if any of the dimensions has length 1, drops that dimension.

```
a <- matrix(1:4, nrow = 2)
a[1, , drop = FALSE]
#>      [,1] [,2]
#> [1,]    1    3
a[1, ]
#> [1] 1 3
```

- **Data frame:** if output is a single column, returns a vector instead of a data frame.

```
df <- data.frame(a = 1:2, b = 1:2)
str(df[1])
#> 'data.frame':    2 obs. of  1 variable:
#> $ a: int  1 2
str(df[[1]])
#> int [1:2] 1 2
str(df[, "a", drop = FALSE])
#> 'data.frame':    2 obs. of  1 variable:
#> $ a: int  1 2
str(df[, "a"])
#> int [1:2] 1 2
```

3.2.2 \$

\$ is a shorthand operator, where `x$y` is equivalent to `x[["y", exact = FALSE]]`. It's often used to access variables in a data frame, as in `mtcars$cyl` or `diamonds$carat`.

One common mistake with \$ is to try and use it when you have the name of a column stored in a variable:

```
var <- "cyl"
# Doesn't work - mtcars$var translated to mtcars[["var"]]
mtcars$var
#> NULL

# Instead use [[
mtcars[[var]]
#> [1] 6 6 4 6 8 6 8 4 4 6 6 8 8 8 8 8 4 4 4 4 8 8 8 8 4 4 4 8
#> [30] 6 8 4
```

There's one important difference between \$ and [/. \$ does partial matching:

```
x <- list(abc = 1)
x$a
#> [1] 1
x[["a"]]
#> NULL
```

If you want to avoid this behaviour you can set the global option `warn-PartialMatchDollar` to `TRUE`. Use with caution: it may affect behaviour in other code you have loaded (e.g., from a package).

3.2.3 Missing/out of bounds indices

`[` and `[[` differ slightly in their behaviour when the index is out of bounds (OOB), for example, when you try to extract the fifth element of a length four vector, or subset a vector with `NA` or `NULL`:

```
x <- 1:4
str(x[5])
#> int NA
str(x[NA_real_])
#> int NA
str(x[NULL])
#> int(0)
```

The following table summarises the results of subsetting atomic vectors and lists with `[` and `[[` and different types of OOB value.

| Operator | Index | Atomic | List |
|-----------------|-----------------------|-------------------|-------------------------|
| <code>[</code> | OOB | NA | <code>list(NULL)</code> |
| <code>[</code> | <code>NA_real_</code> | NA | <code>list(NULL)</code> |
| <code>[</code> | <code>NULL</code> | <code>x[0]</code> | <code>list(NULL)</code> |
| <code>[[</code> | OOB | Error | Error |
| <code>[[</code> | <code>NA_real_</code> | Error | <code>NULL</code> |
| <code>[[</code> | <code>NULL</code> | Error | Error |

If the input vector is named, then the names of OOB, missing, or `NULL` components will be `"<NA>"`.

3.2.4 Exercises

1. Given a linear model, e.g., `mod <- lm(mpg ~ wt, data = mtcars)`, extract the residual degrees of freedom. Extract the R squared from the model summary (`summary(mod)`)

3.3 Subsetting and assignment

All subsetting operators can be combined with assignment to modify selected values of the input vector.

```
x <- 1:5
x[c(1, 2)] <- 2:3
x
#> [1] 2 3 3 4 5

# The length of the LHS needs to match the RHS
x[-1] <- 4:1
x
#> [1] 2 4 3 2 1

# Note that there's no checking for duplicate indices
x[c(1, 1)] <- 2:3
x
#> [1] 3 4 3 2 1

# You can't combine integer indices with NA
x[c(1, NA)] <- c(1, 2)
#> Error: NAs are not allowed in subscripted assignments
# But you can combine logical indices with NA
# (where they're treated as false).
x[c(T, F, NA)] <- 1
x
#> [1] 1 4 3 1 1

# This is mostly useful when conditionally modifying vectors
df <- data.frame(a = c(1, 10, NA))
df$a[df$a < 5] <- 0
df$a
#> [1] 0 10 NA
```

Subsetting with nothing can be useful in conjunction with assignment because it will preserve the original object class and structure. Compare the following two expressions. In the first, `mtcars` will remain as a data frame. In the second, `mtcars` will become a list.

```
mtcars[] <- lapply(mtcars, as.integer)
mtcars <- lapply(mtcars, as.integer)
```

With lists, you can use subsetting + assignment + `NULL` to remove components from a list. To add a literal `NULL` to a list, use `[` and `list(NULL)`:

```
x <- list(a = 1, b = 2)
x[["b"]] <- NULL
str(x)
#> List of 1
#> $ a: num 1
```

```
y <- list(a = 1)
y[["b"]] <- list(NULL)
str(y)
#> List of 2
#> $ a: num 1
#> $ b: NULL
```

3.4 Applications

The basic principles described above give rise to a wide variety of useful applications. Some of the most important are described below. Many of these basic techniques are wrapped up into more concise functions (e.g., `subset()`, `merge()`, `plyr::arrange()`), but it is useful to understand how they are implemented with basic subsetting. This will allow you to adapt to new situations that are not dealt with by existing functions.

3.4.1 Lookup tables (character subsetting)

Character matching provides a powerful way to make lookup tables. Say you want to convert abbreviations:

```
x <- c("m", "f", "u", "f", "f", "m", "m")
lookup <- c(m = "Male", f = "Female", u = NA)
lookup[x]
#>      m      f      u      f      f      m
#>  "Male" "Female" NA "Female" "Female" "Male"
#>      m
#>  "Male"
unname(lookup[x])
#> [1] "Male" "Female" NA      "Female" "Female" "Male"
#> [7] "Male"

# Or with fewer output values
c(m = "Known", f = "Known", u = "Unknown")[x]
#>      m      f      u      f      f      m
#>  "Known" "Known" "Unknown" "Known" "Known" "Known"
#>      m
#>  "Known"
```

If you don't want names in the result, use `unname()` to remove them.

3.4.2 Matching and merging by hand (integer subsetting)

You may have a more complicated lookup table which has multiple columns of information. Suppose we have a vector of integer grades, and a table that describes their properties:

```
grades <- c(1, 2, 2, 3, 1)

info <- data.frame(
  grade = 3:1,
  desc = c("Excellent", "Good", "Poor"),
  fail = c(F, F, T)
)
```

We want to duplicate the `info` table so that we have a row for each value in `grades`. We can do this in two ways, either using `match()` and integer subsetting, or `rownames()` and character subsetting:

```
grades
#> [1] 1 2 2 3 1
```

```
# Using match
id <- match(grades, info$grade)
info[id, ]

#>      grade      desc fail
#> 3         1      Poor  TRUE
#> 2         2      Good FALSE
#> 2.1       2      Good FALSE
#> 1         3 Excellent FALSE
#> 3.1       1      Poor  TRUE

# Using rownames
rownames(info) <- info$grade
info[as.character(grades), ]

#>      grade      desc fail
#> 1         1      Poor  TRUE
#> 2         2      Good FALSE
#> 2.1       2      Good FALSE
#> 3         3 Excellent FALSE
#> 1.1       1      Poor  TRUE
```

If you have multiple columns to match on, you'll need to first collapse them to a single column (with `interaction()`, `paste()`, or `plyr::id()`). You can also use `merge()` or `plyr::join()`, which do the same thing for you — read the source code to see how.

3.4.3 Random samples/bootstrap (integer subsetting)

You can use integer indices to perform random sampling or bootstrapping of a vector or data frame. `sample()` generates a vector of indices, then subsetting to access the values:

```
df <- data.frame(x = rep(1:3, each = 2), y = 6:1, z = letters[1:6])

# Randomly reorder
df[sample(nrow(df)), ]

#>   x y z
#> 5 3 2 e
#> 6 3 1 f
#> 1 1 6 a
#> 2 1 5 b
#> 3 2 4 c
#> 4 2 3 d
```



```
# Select 3 random rows
df[sample(nrow(df), 3), ]
#>   x y z
#> 2 1 5 b
#> 1 1 6 a
#> 5 3 2 e
# Select 6 bootstrap replicates
df[sample(nrow(df), 6, rep = T), ]
#>   x y z
#> 1   1 6 a
#> 2   1 5 b
#> 6   3 1 f
#> 1.1 1 6 a
#> 4   2 3 d
#> 1.2 1 6 a
```

The arguments of `sample()` control the number of samples to extract, and whether sampling is performed with or without replacement.

3.4.4 Ordering (integer subsetting)

`order()` takes a vector as input and returns an integer vector describing how the subsetting vector should be ordered:

```
x <- c("b", "c", "a")
order(x)
#> [1] 3 1 2
x[order(x)]
#> [1] "a" "b" "c"
```

To break ties, you can supply additional variables to `order()`, and you can change from ascending to descending order using `decreasing = TRUE`. By default, any missing values will be put at the end of the vector; however, you can remove them with `na.last = NA` or put at the front with `na.last = FALSE`.

For two or more dimensions, `order()` and integer subsetting makes it easy to order either the rows or columns of an object:

```
# Randomly reorder df
df2 <- df[sample(nrow(df)), 3:1]
df2
```

```
#>   z y x
#> 4 d 3 2
#> 1 a 6 1
#> 3 c 4 2
#> 6 f 1 3
#> 5 e 2 3
#> 2 b 5 1
```

```
df2[order(df2$x), ]
#>   z y x
#> 1 a 6 1
#> 2 b 5 1
#> 4 d 3 2
#> 3 c 4 2
#> 6 f 1 3
#> 5 e 2 3
df2[, order(names(df2))]
#>   x y z
#> 4 2 3 d
#> 1 1 6 a
#> 3 2 4 c
#> 6 3 1 f
#> 5 3 2 e
#> 2 1 5 b
```

More concise, but less flexible, functions are available for sorting vectors, `sort()`, and data frames, `plyr::arrange()`.

3.4.5 Expanding aggregated counts (integer subsetting)

Sometimes you get a data frame where identical rows have been collapsed into one and a count column has been added. `rep()` and integer subsetting make it easy to uncollapse the data by subsetting with a repeated row index:

```
df <- data.frame(x = c(2, 4, 1), y = c(9, 11, 6), n = c(3, 5, 1))
rep(1:nrow(df), df$n)
#> [1] 1 1 1 2 2 2 2 2 3
df[rep(1:nrow(df), df$n), ]
#>   x y n
#> 1  2 9 3
#> 1.1 2 9 3
```

```
#> 1.2 2 9 3
#> 2 4 11 5
#> 2.1 4 11 5
#> 2.2 4 11 5
#> 2.3 4 11 5
#> 2.4 4 11 5
#> 3 1 6 1
```

3.4.6 Removing columns from data frames (character subsetting)

There are two ways to remove columns from a data frame. You can set individual columns to NULL:

```
df <- data.frame(x = 1:3, y = 3:1, z = letters[1:3])
df$z <- NULL
```

Or you can subset to return only the columns you want:

```
df <- data.frame(x = 1:3, y = 3:1, z = letters[1:3])
df[c("x", "y")]
#>   x y
#> 1 1 3
#> 2 2 2
#> 3 3 1
```

If you know the columns you don't want, use set operations to work out which columns to keep:

```
df[setdiff(names(df), "z")]
#>   x y
#> 1 1 3
#> 2 2 2
#> 3 3 1
```

3.4.7 Selecting rows based on a condition (logical subsetting)

Because it allows you to easily combine conditions from multiple columns, logical subsetting is probably the most commonly used technique for extracting rows out of a data frame.

```
mtcars[mtcars$gear == 5, ]
#>      mpg cyl  disp  hp drat    wt  qsec vs am gear carb
#> 27 26.0   4 120.3  91 4.43 2.140 16.7  0  1    5    2
#> 28 30.4   4  95.1 113 3.77 1.513 16.9  1  1    5    2
#> 29 15.8   8 351.0 264 4.22 3.170 14.5  0  1    5    4
#> 30 19.7   6 145.0 175 3.62 2.770 15.5  0  1    5    6
#> 31 15.0   8 301.0 335 3.54 3.570 14.6  0  1    5    8
mtcars[mtcars$gear == 5 & mtcars$cyl == 4, ]
#>      mpg cyl  disp  hp drat    wt  qsec vs am gear carb
#> 27 26.0   4 120.3  91 4.43 2.140 16.7  0  1    5    2
#> 28 30.4   4  95.1 113 3.77 1.513 16.9  1  1    5    2
```

Remember to use the vector boolean operators `&` and `|`, not the short-circuiting scalar operators `&&` and `||` which are more useful inside if statements. Don't forget De Morgan's laws (http://en.wikipedia.org/wiki/De_Morgan's_laws), which can be useful to simplify negations:

- $!(X \ \& \ Y)$ is the same as $!X \ | \ !Y$
- $!(X \ | \ Y)$ is the same as $!X \ \& \ !Y$

For example, $!(X \ \& \ !(Y \ | \ Z))$ simplifies to $!X \ | \ !(Y|Z)$, and then to $!X \ | \ Y \ | \ Z$.

`subset()` is a specialised shorthand function for subsetting data frames, and saves some typing because you don't need to repeat the name of the data frame. You'll learn how it works in Chapter 13.

```
subset(mtcars, gear == 5)
#>      mpg cyl  disp  hp drat    wt  qsec vs am gear carb
#> 27 26.0   4 120.3  91 4.43 2.140 16.7  0  1    5    2
#> 28 30.4   4  95.1 113 3.77 1.513 16.9  1  1    5    2
#> 29 15.8   8 351.0 264 4.22 3.170 14.5  0  1    5    4
#> 30 19.7   6 145.0 175 3.62 2.770 15.5  0  1    5    6
#> 31 15.0   8 301.0 335 3.54 3.570 14.6  0  1    5    8
subset(mtcars, gear == 5 & cyl == 4)
#>      mpg cyl  disp  hp drat    wt  qsec vs am gear carb
#> 27 26.0   4 120.3  91 4.43 2.140 16.7  0  1    5    2
#> 28 30.4   4  95.1 113 3.77 1.513 16.9  1  1    5    2
```

3.4.8 Boolean algebra vs. sets (logical & integer subsetting)

It's useful to be aware of the natural equivalence between set operations (integer subsetting) and boolean algebra (logical subsetting). Using set operations is more effective when:

- You want to find the first (or last) TRUE.
- You have very few TRUEs and very many FALSEs; a set representation may be faster and require less storage.

`which()` allows you to convert a boolean representation to an integer representation. There's no reverse operation in base R but we can easily create one:

```
x <- sample(10) < 4
which(x)
#> [1] 3 8 9

unwhich <- function(x, n) {
  out <- rep_len(FALSE, n)
  out[x] <- TRUE
  out
}
unwhich(which(x), 10)
#> [1] FALSE FALSE TRUE FALSE FALSE FALSE FALSE TRUE TRUE
#> [10] FALSE
```

Let's create two logical vectors and their integer equivalents and then explore the relationship between boolean and set operations.

```
(x1 <- 1:10 %% 2 == 0)
#> [1] FALSE TRUE FALSE TRUE FALSE TRUE FALSE TRUE FALSE
#> [10] TRUE
(x2 <- which(x1))
#> [1] 2 4 6 8 10
(y1 <- 1:10 %% 5 == 0)
#> [1] FALSE FALSE FALSE FALSE TRUE FALSE FALSE FALSE
#> [10] TRUE
(y2 <- which(y1))
#> [1] 5 10
```

```

# X & Y <-> intersect(x, y)
x1 & y1
#> [1] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
#> [10] TRUE
intersect(x2, y2)
#> [1] 10

# X | Y <-> union(x, y)
x1 | y1
#> [1] FALSE TRUE FALSE TRUE TRUE TRUE FALSE TRUE FALSE
#> [10] TRUE
union(x2, y2)
#> [1] 2 4 6 8 10 5

# X & !Y <-> setdiff(x, y)
x1 & !y1
#> [1] FALSE TRUE FALSE TRUE FALSE TRUE FALSE TRUE FALSE
#> [10] FALSE
setdiff(x2, y2)
#> [1] 2 4 6 8

# xor(X, Y) <-> setdiff(union(x, y), intersect(x, y))
xor(x1, y1)
#> [1] FALSE TRUE FALSE TRUE TRUE TRUE FALSE TRUE FALSE
#> [10] FALSE
setdiff(union(x2, y2), intersect(x2, y2))
#> [1] 2 4 6 8 5

```

When first learning subsetting, a common mistake is to use `x[which(y)]` instead of `x[y]`. Here the `which()` achieves nothing: it switches from logical to integer subsetting but the result will be exactly the same. Also beware that `x[-which(y)]` is **not** equivalent to `x[!y]`: if `y` is all `FALSE`, `which(y)` will be `integer(0)` and `-integer(0)` is still `integer(0)`, so you'll get no values, instead of all values. In general, avoid switching from logical to integer subsetting unless you want, for example, the first or last `TRUE` value.

3.4.9 Exercises

1. How would you randomly permute the columns of a data frame? (This is an important technique in random forests.)

Can you simultaneously permute the rows and columns in one step?

2. How would you select a random sample of `m` rows from a data frame? What if the sample had to be contiguous (i.e., with an initial row, a final row, and every row in between)?
3. How could you put the columns in a data frame in alphabetical order?

3.5 Answers

1. Positive integers select elements at specific positions, negative integers drop elements; logical vectors keep elements at positions corresponding to `TRUE`; character vectors select elements with matching names.
2. `[]` selects sub-lists. It always returns a list; if you use it with a single positive integer, it returns a list of length one. `[[` selects an element within a list. `$` is a convenient shorthand: `x$y` is equivalent to `x[["y"]]`.
3. Use `drop = FALSE` if you are subsetting a matrix, array, or data frame and you want to preserve the original dimensions. You should almost always use it when subsetting inside a function.
4. If `x` is a matrix, `x[] <- 0` will replace every element with 0, keeping the same number of rows and columns. `x <- 0` completely replaces the matrix with the value 0.
5. A named character vector can act as a simple lookup table: `c(x = 1, y = 2, z = 3)[c("y", "z", "x")]`

4

Vocabulary

An important part of being fluent in R is having a good working vocabulary. Below, I have listed the functions that I believe constitute such a vocabulary. You don't need to be intimately familiar with the details of every function, but you should at least be aware that they all exist. If there are functions in this list that you've never heard of, I strongly recommend that you read their documentation.

I came up with this list by looking through all the functions in the base, stats, and utils packages, and extracting those that I think are most useful. The list also includes a few pointers to particularly important functions in other packages, and some of the more important `options()`.

4.1 The basics

```
# The first functions to learn
?
str

# Important operators and assignment
%in%, match
=, <-, <<-
$, [, [[, head, tail, subset
with
assign, get

# Comparison
all.equal, identical
!=, ==, >, >=, <, <=
is.na, complete.cases
is.finite
```

```
# Basic math
*, +, -, /, ^, %, %/, %%
abs, sign
acos, asin, atan, atan2
sin, cos, tan
ceiling, floor, round, trunc, signif
exp, log, log10, log2, sqrt

max, min, prod, sum
cummax, cummin, cumprod, cumsum, diff
pmax, pmin
range
mean, median, cor, sd, var
rle

# Functions to do with functions
function
missing
on.exit
return, invisible

# Logical & sets
&, |, !, xor
all, any
intersect, union, setdiff, setequal
which

# Vectors and matrices
c, matrix
# automatic coercion rules character > numeric > logical
length, dim, ncol, nrow
cbind, rbind
names, colnames, rownames
t
diag
sweep
as.matrix, data.matrix

# Making vectors
c
rep, rep_len
seq, seq_len, seq_along
```

```
rev
sample
choose, factorial, combn
(is/as).(character/numeric/logical/...)

# Lists & data.frames
list, unlist
data.frame, as.data.frame
split
expand.grid

# Control flow
if, &&, || (short circuiting)
for, while
next, break
switch
ifelse

# Apply & friends
lapply, sapply, vapply
apply
tapply
replicate
```

4.2 Common data structures

```
# Date time
ISOdate, ISOdatetime, strptime, strftime, date
difftime
julian, months, quarters, weekdays
library(lubridate)

# Character manipulation
grep, agrep
gsub
strsplit
chartr
nchar
tolower, toupper
```

```
substr
paste
library(stringr)

# Factors
factor, levels, nlevels
reorder, relevel
cut, findInterval
interaction
options(stringsAsFactors = FALSE)

# Array manipulation
array
dim
dimnames
aperm
library(abind)
```

4.3 Statistics

```
# Ordering and tabulating
duplicated, unique
merge
order, rank, quantile
sort
table, ftable

# Linear models
fitted, predict, resid, rstandard
lm, glm
hat, influence.measures
logLik, df, deviance
formula, ~, I
anova, coef, confint, vcov
contrasts

# Miscellaneous tests
apropos("\\.test$")
```

```
# Random variables
(q, p, d, r) * (beta, binom, cauchy, chisq, exp, f, gamma, geom,
  hyper, lnorm, logis, multinom, nbinom, norm, pois, signrank, t,
  unif, weibull, wilcox, birthday, tukey)

# Matrix algebra
crossprod, tcrossprod
eigen, qr, svd
%*%, %o%, outer
rcond
solve
```

4.4 Working with R

```
# Workspace
ls, exists, rm
getwd, setwd
q
source
install.packages, library, require

# Help
help, ?
help.search
apropos
RSiteSearch
citation
demo
example
vignette

# Debugging
traceback
browser
recover
options(error = )
stop, warning, message
tryCatch, try
```

4.5 I/O

```
# Output
print, cat
message, warning
dput
format
sink, capture.output

# Reading and writing data
data
count.fields
read.csv, write.csv
read.delim, write.delim
read.fwf
readLines, writeLines
readRDS, saveRDS
load, save
library(foreign)

# Files and directories
dir
basename, dirname, tools::file_ext
file.path
path.expand, normalizePath
file.choose
file.copy, file.create, file.remove, file.rename, dir.create
file.exists, file.info
tempdir, tempfile
download.file, library(downloader)
```

5

Style guide

Good coding style is like using correct punctuation. You can manage without it, but it sure makes things easier to read. As with styles of punctuation, there are many possible variations. The following guide describes the style that I use (in this book and elsewhere). It is based on Google's R style guide (<http://google-styleguide.googlecode.com/svn/trunk/google-r-style.html>), with a few tweaks. You don't have to use my style, but you really should use a consistent style.

Good style is important because while your code only has one author, it'll usually have multiple readers. This is especially true when you're writing code with others. In that case, it's a good idea to agree on a common style up-front. Since no style is strictly better than another, working with others may mean that you'll need to sacrifice some preferred aspects of your style.

The `formatR` package, by Yihui Xie, makes it easier to clean up poorly formatted code. It can't do everything, but it can quickly get your code from terrible to pretty good. Make sure to read the notes on the wiki (<https://github.com/yihui/formatR/wiki>) before using it.

5.1 Notation and naming

5.1.1 File names

File names should be meaningful and end in `.R`.

```
# Good
fit-models.R
utility-functions.R
```

```
# Bad
```

```
foo.r  
stuff.r
```

If files need to be run in sequence, prefix them with numbers:

```
0-download.R  
1-parse.R  
2-explore.R
```

5.1.2 Object names

“There are only two hard things in Computer Science: cache invalidation and naming things.”

— Phil Karlton

Variable and function names should be lowercase. Use an underscore (`_`) to separate words within a name. Generally, variable names should be nouns and function names should be verbs. Strive for names that are concise and meaningful (this is not easy!).

```
# Good  
day_one  
day_1  
  
# Bad  
first_day_of_the_month  
DayOne  
dayone  
djm1
```

Where possible, avoid using names of existing functions and variables. This will cause confusion for the readers of your code.

```
# Bad  
T <- FALSE  
c <- 10  
mean <- function(x) sum(x)
```

5.2 Syntax

5.2.1 Spacing

Place spaces around all infix operators (`=`, `+`, `-`, `<-`, etc.). The same rule applies when using `=` in function calls. Always put a space after a comma, and never before (just like in regular English).

```
# Good
average <- mean(feet / 12 + inches, na.rm = TRUE)
```

```
# Bad
average<-mean(feet/12+inches,na.rm=TRUE)
```

There's a small exception to this rule: `:`, `::` and `:::` don't need spaces around them.

```
# Good
x <- 1:10
base::get
```

```
# Bad
x <- 1 : 10
base :: get
```

Place a space before left parentheses, except in a function call.

```
# Good
if (debug) do(x)
plot(x, y)
```

```
# Bad
if(debug)do(x)
plot (x, y)
```

Extra spacing (i.e., more than one space in a row) is ok if it improves alignment of equal signs or assignments (`<-`).

```
list(
  total = a + b + c,
  mean  = (a + b + c) / n
)
```

Do not place spaces around code in parentheses or square brackets (unless there's a comma, in which case see above).

```
# Good
if (debug) do(x)
diamonds[5, ]

# Bad
if ( debug ) do(x) # No spaces around debug
x[1,] # Needs a space after the comma
x[1 ,] # Space goes after comma not before
```

5.2.2 Curly braces

An opening curly brace should never go on its own line and should always be followed by a new line. A closing curly brace should always go on its own line, unless it's followed by `else`.

Always indent the code inside curly braces.

```
# Good

if (y < 0 && debug) {
  message("Y is negative")
}

if (y == 0) {
  log(x)
} else {
  y ^ x
}

# Bad

if (y < 0 && debug)
message("Y is negative")
```

```
if (y == 0) {  
  log(x)  
}  
else {  
  y ^ x  
}
```

It's ok to leave very short statements on the same line:

```
if (y < 0 && debug) message("Y is negative")
```

5.2.3 Line length

Strive to limit your code to 80 characters per line. This fits comfortably on a printed page with a reasonably sized font. If you find yourself running out of room, this is a good indication that you should encapsulate some of the work in a separate function.

5.2.4 Indentation

When indenting your code, use two spaces. Never use tabs or mix tabs and spaces.

The only exception is if a function definition runs over multiple lines. In that case, indent the second line to where the definition starts:

```
long_function_name <- function(a = "a long argument",  
                                b = "another argument",  
                                c = "another long argument") {  
  # As usual code is indented by two spaces.  
}
```

5.2.5 Assignment

Use `<-`, not `=`, for assignment.

```
# Good  
x <- 5  
# Bad  
x = 5
```

5.3 Organisation

5.3.1 Commenting guidelines

Comment your code. Each line of a comment should begin with the comment symbol and a single space: `#`. Comments should explain the why, not the what.

Use commented lines of `-` and `=` to break up your file into easily readable chunks.

```
# Load data -----
```

```
# Plot data -----
```

6

Functions

Functions are a fundamental building block of R: to master many of the more advanced techniques in this book, you need a solid foundation in how functions work. You've probably already created many R functions, and you're familiar with the basics of how they work. The focus of this chapter is to turn your existing, informal knowledge of functions into a rigorous understanding of what functions are and how they work. You'll see some interesting tricks and techniques in this chapter, but most of what you'll learn will be more important as the building blocks for more advanced techniques.

The most important thing to understand about R is that functions are objects in their own right. You can work with them exactly the same way you work with any other type of object. This theme will be explored in depth in Chapter 10.

Quiz

Answer the following questions to see if you can safely skip this chapter. You can find the answers at the end of the chapter in Section 6.7.

1. What are the three components of a function?
2. What does the following code return?

```
y <- 10
f1 <- function(x) {
  function() {
    x + 10
  }
}
```

f1(1)()

3. How would you more typically write this code?

```
`+`(1, `*`(2, 3))
```

4. How could you make this call easier to read?

```
mean(, TRUE, x = c(1:10, NA))
```

5. Does the following function throw an error when called? Why/why not?

```
f2 <- function(a, b) {  
  a * 10  
}  
f2(10, stop("This is an error!"))
```

6. What is an infix function? How do you write it? What's a replacement function? How do you write it?
7. What function do you use to ensure that a cleanup action occurs regardless of how a function terminates?

Outline

- Section 6.1 describes the three main components of a function.
- Section 6.2 teaches you how R finds values from names, the process of lexical scoping.
- Section 6.3 shows you that everything that happens in R is a result of a function call, even if it doesn't look like it.
- Section 6.4 discusses the three ways of supplying arguments to a function, how to call a function given a list of arguments, and the impact of lazy evaluation.
- Section 6.5 describes two special types of function: infix and replacement functions.
- Section 6.6 discusses how and when functions return values, and how you can ensure that a function does something before it exits.

Prerequisites

The only package you'll need is `pryr`, which is used to explore what happens when modifying vectors in place. Install it with `install.packages("pryr")`.

6.1 Function components

All R functions have three parts:

- the `body()`, the code inside the function.
- the `formals()`, the list of arguments which controls how you can call the function.
- the `environment()`, the “map” of the location of the function’s variables.

When you print a function in R, it shows you these three important components. If the environment isn’t displayed, it means that the function was created in the global environment.

```
f <- function(x) x^2
f
#> function(x) x^2

formals(f)
#> $x
body(f)
#> x^2
environment(f)
#> <environment: R_GlobalEnv>
```

The assignment forms of `body()`, `formals()`, and `environment()` can also be used to modify functions.

Like all objects in R, functions can also possess any number of additional `attributes()`. One attribute used by base R is “`srcref`”, short for source reference, which points to the source code used to create the function. Unlike `body()`, this contains code comments and other formatting. You can also add attributes to a function. For example, you can set the `class()` and add a custom `print()` method.

6.1.1 Primitive functions

There is one exception to the rule that functions have three components. Primitive functions, like `sum()`, call C code directly with `.Primitive()`

and contain no R code. Therefore their `formals()`, `body()`, and `environment()` are all `NULL`:

```
sum
#> function (... , na.rm = FALSE) .Primitive("sum")
formals(sum)
#> NULL
body(sum)
#> NULL
environment(sum)
#> NULL
```

Primitive functions are only found in the `base` package, and since they operate at a low level, they can be more efficient (primitive replacement functions don't have to make copies), and can have different rules for argument matching (e.g., `switch` and `call`). This, however, comes at a cost of behaving differently from all other functions in R. Hence the R core team generally avoids creating them unless there is no other option.

6.1.2 Exercises

1. What function allows you to tell if an object is a function? What function allows you to tell if a function is a primitive function?
2. This code makes a list of all functions in the base package.

```
objs <- mget(ls("package:base"), inherits = TRUE)
funs <- Filter(is.function, objs)
```

Use it to answer the following questions:

- a. Which base function has the most arguments?
 - b. How many base functions have no arguments? What's special about those functions?
 - c. How could you adapt the code to find all primitive functions?
3. What are the three important components of a function?
 4. When does printing a function not show what environment it was created in?

6.2 Lexical scoping

Scoping is the set of rules that govern how R looks up the value of a symbol. In the example below, scoping is the set of rules that R applies to go from the symbol `x` to its value `10`:

```
x <- 10
x
#> [1] 10
```

Understanding scoping allows you to:

- build tools by composing functions, as described in Chapter 10.
- overrule the usual evaluation rules and do non-standard evaluation, as described in Chapter 13.

R has two types of scoping: **lexical scoping**, implemented automatically at the language level, and **dynamic scoping**, used in select functions to save typing during interactive analysis. We discuss lexical scoping here because it is intimately tied to function creation. Dynamic scoping is described in more detail in Section 13.3.

Lexical scoping looks up symbol values based on how functions were nested when they were created, not how they are nested when they are called. With lexical scoping, you don't need to know how the function is called to figure out where the value of a variable will be looked up. You just need to look at the function's definition.

The “lexical” in lexical scoping doesn't correspond to the usual English definition (“of or relating to words or the vocabulary of a language as distinguished from its grammar and construction”) but comes from the computer science term “lexing”, which is part of the process that converts code represented as text to meaningful pieces that the programming language understands.

There are four basic principles behind R's implementation of lexical scoping:

- name masking
- functions vs. variables

- a fresh start
- dynamic lookup

You probably know many of these principles already, although you might not have thought about them explicitly. Test your knowledge by mentally running through the code in each block before looking at the answers.

6.2.1 Name masking

The following example illustrates the most basic principle of lexical scoping, and you should have no problem predicting the output.

```
f <- function() {  
  x <- 1  
  y <- 2  
  c(x, y)  
}  
f()  
rm(f)
```

If a name isn't defined inside a function, R will look one level up.

```
x <- 2  
g <- function() {  
  y <- 1  
  c(x, y)  
}  
g()  
rm(x, g)
```

The same rules apply if a function is defined inside another function: look inside the current function, then where that function was defined, and so on, all the way up to the global environment, and then on to other loaded packages. Run the following code in your head, then confirm the output by running the R code.

```
x <- 1  
h <- function() {  
  y <- 2
```

```

i <- function() {
  z <- 3
  c(x, y, z)
}
i()
}
h()
rm(x, h)

```

The same rules apply to closures, functions created by other functions. Closures will be described in more detail in Chapter 10; here we'll just look at how they interact with scoping. The following function, `j()`, returns a function. What do you think this function will return when we call it?

```

j <- function(x) {
  y <- 2
  function() {
    c(x, y)
  }
}
k <- j(1)
k()
rm(j, k)

```

This seems a little magical (how does R know what the value of `y` is after the function has been called). It works because `k` preserves the environment in which it was defined and because the environment includes the value of `y`. Chapter 8 gives some pointers on how you can dive in and figure out what values are stored in the environment associated with each function.

6.2.2 Functions vs. variables

The same principles apply regardless of the type of associated value — finding functions works exactly the same way as finding variables:

```

l <- function(x) x + 1
m <- function() {
  l <- function(x) x * 2
  l(10)
}

```

```

}
m()
#> [1] 20
rm(1, m)

```

For functions, there is one small tweak to the rule. If you are using a name in a context where it's obvious that you want a function (e.g., `f(3)`), R will ignore objects that are not functions while it is searching. In the following example `n` takes on a different value depending on whether R is looking for a function or a variable.

```

n <- function(x) x / 2
o <- function() {
  n <- 10
  n(n)
}
o()
#> [1] 5
rm(n, o)

```

However, using the same name for functions and other objects will make for confusing code, and is generally best avoided.

6.2.3 A fresh start

What happens to the values in between invocations of a function? What will happen the first time you run this function? What will happen the second time? (If you haven't seen `exists()` before: it returns `TRUE` if there's a variable of that name, otherwise it returns `FALSE`.)

```

j <- function() {
  if (!exists("a")) {
    a <- 1
  } else {
    a <- a + 1
  }
  print(a)
}
j()
rm(j)

```

You might be surprised that it returns the same value, 1, every time. This is because every time a function is called, a new environment is created to host execution. A function has no way to tell what happened the last time it was run; each invocation is completely independent. (We'll see some ways to get around this in Section 10.3.2.)

6.2.4 Dynamic lookup

Lexical scoping determines where to look for values, not when to look for them. R looks for values when the function is run, not when it's created. This means that the output of a function can be different depending on objects outside its environment:

```
f <- function() x
x <- 15
f()
#> [1] 15

x <- 20
f()
#> [1] 20
```

You generally want to avoid this behaviour because it means the function is no longer self-contained. This is a common error — if you make a spelling mistake in your code, you won't get an error when you create the function, and you might not even get one when you run the function, depending on what variables are defined in the global environment.

One way to detect this problem is the `findGlobals()` function from `codetools`. This function lists all the external dependencies of a function:

```
f <- function() x + 1
codetools::findGlobals(f)
#> [1] "+" "x"
```

Another way to try and solve the problem would be to manually change the environment of the function to the `emptyenv()`, an environment which contains absolutely nothing:

```
environment(f) <- emptyenv()
f()
#> Error: could not find function "+"
```



```

      x ^ 2
    }
    f(x) + 1
  }
  f(x) * 2
}
f(10)

```

6.3 Every operation is a function call

“To understand computations in R, two slogans are helpful:

- Everything that exists is an object.
- Everything that happens is a function call.”

— John Chambers

The previous example of redefining `()` works because every operation in R is a function call, whether or not it looks like one. This includes infix operators like `+`, control flow operators like `for`, `if`, and `while`, subsetting operators like `[]` and `$`, and even the curly brace `{`. This means that each pair of statements in the following example is exactly equivalent. Note that ```, the backtick, lets you refer to functions or variables that have otherwise reserved or illegal names:

```

x <- 10; y <- 5
x + y
#> [1] 15
`+`(x, y)
#> [1] 15

for (i in 1:2) print(i)
#> [1] 1
#> [1] 2
`for`(i, 1:2, print(i))
#> [1] 1
#> [1] 2

if (i == 1) print("yes!") else print("no.")

```

```

#> [1] "no."
`if`(i == 1, print("yes!"), print("no."))
#> [1] "no."

x[3]
#> [1] NA
`[`(x, 3)
#> [1] NA

{ print(1); print(2); print(3) }
#> [1] 1
#> [1] 2
#> [1] 3
`{`(print(1), print(2), print(3))
#> [1] 1
#> [1] 2
#> [1] 3

```

It is possible to override the definitions of these special functions, but this is almost certainly a bad idea. However, there are occasions when it might be useful: it allows you to do something that would have otherwise been impossible. For example, this feature makes it possible for the `dplyr` package to translate R expressions into SQL expressions. Chapter 15 uses this idea to create domain specific languages that allow you to concisely express new concepts using existing R constructs.

It's more often useful to treat special functions as ordinary functions. For example, we could use `sapply()` to add 3 to every element of a list by first defining a function `add()`, like this:

```

add <- function(x, y) x + y
sapply(1:10, add, 3)
#> [1] 4 5 6 7 8 9 10 11 12 13

```

But we can also get the same effect using the built-in `+` function.

```

sapply(1:5, `+`, 3)
#> [1] 4 5 6 7 8
sapply(1:5, "+", 3)
#> [1] 4 5 6 7 8

```

Note the difference between ``+`` and `"+"`. The first one is the value of the object called `+`, and the second is a string containing the character `+`. The

second version works because `lapply` can be given the name of a function instead of the function itself: if you read the source of `lapply()`, you'll see the first line uses `match.fun()` to find functions given their names.

A more useful application is to combine `lapply()` or `sapply()` with sub-setting:

```
x <- list(1:3, 4:9, 10:12)
sapply(x, "[", 2)
#> [1] 2 5 11

# equivalent to
sapply(x, function(x) x[2])
#> [1] 2 5 11
```

Remembering that everything that happens in R is a function call will help you in Chapter 14.

6.4 Function arguments

It's useful to distinguish between the formal arguments and the actual arguments of a function. The formal arguments are a property of the function, whereas the actual or calling arguments can vary each time you call the function. This section discusses how calling arguments are mapped to formal arguments, how you can call a function given a list of arguments, how default arguments work, and the impact of lazy evaluation.

6.4.1 Calling functions

When calling a function you can specify arguments by position, by complete name, or by partial name. Arguments are matched first by exact name (perfect matching), then by prefix matching, and finally by position.

```
f <- function(abcdef, bcde1, bcde2) {
  list(a = abcdef, b1 = bcde1, b2 = bcde2)
}
```

```

str(f(1, 2, 3))
#> List of 3
#> $ a : num 1
#> $ b1: num 2
#> $ b2: num 3
str(f(2, 3, abcdef = 1))
#> List of 3
#> $ a : num 1
#> $ b1: num 2
#> $ b2: num 3

# Can abbreviate long argument names:
str(f(2, 3, a = 1))
#> List of 3
#> $ a : num 1
#> $ b1: num 2
#> $ b2: num 3

# But this doesn't work because abbreviation is ambiguous
str(f(1, 3, b = 1))
#> Error: argument 3 matches multiple formal arguments

```

Generally, you only want to use positional matching for the first one or two arguments; they will be the most commonly used, and most readers will know what they are. Avoid using positional matching for less commonly used arguments, and only use readable abbreviations with partial matching. (If you are writing code for a package that you want to publish on CRAN you can not use partial matching, and must use complete names.) Named arguments should always come after unnamed arguments. If a function uses `...` (discussed in more detail below), you can only specify arguments listed after `...` with their full name.

These are good calls:

```

mean(1:10)
mean(1:10, trim = 0.05)

```

This is probably overkill:

```

mean(x = 1:10)

```

And these are just confusing:

```
mean(1:10, n = T)
mean(1:10, , FALSE)
mean(1:10, 0.05)
mean(, TRUE, x = c(1:10, NA))
```

6.4.2 Calling a function given a list of arguments

Suppose you had a list of function arguments:

```
args <- list(1:10, na.rm = TRUE)
```

How could you then send that list to `mean()`? You need `do.call()`:

```
do.call(mean, list(1:10, na.rm = TRUE))
#> [1] 5.5
# Equivalent to
mean(1:10, na.rm = TRUE)
#> [1] 5.5
```

6.4.3 Default and missing arguments

Function arguments in R can have default values.

```
f <- function(a = 1, b = 2) {
  c(a, b)
}
f()
#> [1] 1 2
```

Since arguments in R are evaluated lazily (more on that below), the default value can be defined in terms of other arguments:

```
g <- function(a = 1, b = a * 2) {
  c(a, b)
}
g()
#> [1] 1 2
g(10)
#> [1] 10 20
```

Default arguments can even be defined in terms of variables created within the function. This is used frequently in base R functions, but I think it is bad practice, because you can't understand what the default values will be without reading the complete source code.

```
h <- function(a = 1, b = d) {  
  d <- (a + 1) ^ 2  
  c(a, b)  
}  
h()  
#> [1] 1 4  
h(10)  
#> [1] 10 121
```

You can determine if an argument was supplied or not with the `missing()` function.

```
i <- function(a, b) {  
  c(missing(a), missing(b))  
}  
i()  
#> [1] TRUE TRUE  
i(a = 1)  
#> [1] FALSE TRUE  
i(b = 2)  
#> [1] TRUE FALSE  
i(1, 2)  
#> [1] FALSE FALSE
```

Sometimes you want to add a non-trivial default value, which might take several lines of code to compute. Instead of inserting that code in the function definition, you could use `missing()` to conditionally compute it if needed. However, this makes it hard to know which arguments are required and which are optional without carefully reading the documentation. Instead, I usually set the default value to `NULL` and use `is.null()` to check if the argument was supplied.

6.4.4 Lazy evaluation

By default, R function arguments are lazy — they're only evaluated if they're actually used:

```
f <- function(x) {  
  10  
}  
f(stop("This is an error!"))  
#> [1] 10
```

If you want to ensure that an argument is evaluated you can use `force()`:

```
f <- function(x) {  
  force(x)  
  10  
}  
f(stop("This is an error!"))  
#> Error: This is an error!
```

This is important when creating closures with `lapply()` or a loop:

```
add <- function(x) {  
  function(y) x + y  
}  
adders <- lapply(1:10, add)  
adders[[1]](10)  
#> [1] 20  
adders[[10]](10)  
#> [1] 20
```

`x` is lazily evaluated the first time that you call one of the adder functions. At this point, the loop is complete and the final value of `x` is 10. Therefore all of the adder functions will add 10 on to their input, probably not what you wanted! Manually forcing evaluation fixes the problem:

```
add <- function(x) {  
  force(x)  
  function(y) x + y  
}  
adders2 <- lapply(1:10, add)  
adders2[[1]](10)  
#> [1] 11  
adders2[[10]](10)  
#> [1] 20
```

This code is exactly equivalent to

```
add <- function(x) {
  x
  function(y) x + y
}
```

because the force function is defined as `force <- function(x) x`. However, using this function clearly indicates that you're forcing evaluation, not that you've accidentally typed `x`.

Default arguments are evaluated inside the function. This means that if the expression depends on the current environment the results will differ depending on whether you use the default value or explicitly provide one.

```
f <- function(x = ls()) {
  a <- 1
  x
}
```

`ls()` evaluated inside `f`:

```
f()
#> [1] "a" "x"
```

`ls()` evaluated in global environment:

```
f(ls())
#> [1] "add"      "adders"    "adders2"   "args"      "f"
#> [6] "funs"     "g"         "h"         "i"         "metadata"
#> [11] "objs"     "x"         "y"
```

More technically, an unevaluated argument is called a **promise**, or (less commonly) a thunk. A promise is made up of two parts:

- The expression which gives rise to the delayed computation. (It can be accessed with `substitute()`. See Chapter 13 for more details.)
- The environment where the expression was created and where it should be evaluated.

The first time a promise is accessed the expression is evaluated in the environment where it was created. This value is cached, so that subsequent

access to the evaluated promise does not recompute the value (but the original expression is still associated with the value, so `substitute()` can continue to access it). You can find more information about a promise using `pryr::promise_info()`. This uses some C++ code to extract information about the promise without evaluating it, which is impossible to do in pure R code.

Laziness is useful in if statements — the second statement below will be evaluated only if the first is true. If it wasn't, the statement would return an error because `NULL > 0` is a logical vector of length 0 and not a valid input to `if`.

```
x <- NULL
if (!is.null(x) && x > 0) {

}
```

We could implement “&&” ourselves:

```
`&&` <- function(x, y) {
  if (!x) return(FALSE)
  if (!y) return(FALSE)

  TRUE
}
a <- NULL
!is.null(a) && a > 0
#> [1] FALSE
```

This function would not work without lazy evaluation because both `x` and `y` would always be evaluated, testing `a > 0` even when `a` was `NULL`.

Sometimes you can also use laziness to eliminate an if statement altogether. For example, instead of:

```
if (is.null(a)) stop("a is null")
#> Error: a is null
```

You could write:

```
!is.null(a) || stop("a is null")
#> Error: a is null
```

6.4.5 ...

There is a special argument called `...`. This argument will match any arguments not otherwise matched, and can be easily passed on to other functions. This is useful if you want to collect arguments to call another function, but you don't want to prespecify their possible names. `...` is often used in conjunction with S3 generic functions to allow individual methods to be more flexible.

One relatively sophisticated user of `...` is the base `plot()` function. `plot()` is a generic method with arguments `x`, `y` and `...`. To understand what `...` does for a given function we need to read the help: “Arguments to be passed to methods, such as graphical parameters”. Most simple invocations of `plot()` end up calling `plot.default()` which has many more arguments, but also has `...`. Again, reading the documentation reveals that `...` accepts “other graphical parameters”, which are listed in the help for `par()`. This allows us to write code like:

```
plot(1:5, col = "red")
plot(1:5, cex = 5, pch = 20)
```

This illustrates both the advantages and disadvantages of `...`: it makes `plot()` very flexible, but to understand how to use it, we have to carefully read the documentation. Additionally, if we read the source code for `plot.default`, we can discover undocumented features. It's possible to pass along other arguments to `axis()` and `box()`:

```
plot(1:5, bty = "u")
plot(1:5, labels = FALSE)
```

To capture `...` in a form that is easier to work with, you can use `list(...)`. (See Section 13.5.2 for other ways to capture `...` without evaluating the arguments.)

```
f <- function(...) {
  names(list(...))
}
f(a = 1, b = 2)
#> [1] "a" "b"
```

Using `...` comes at a price — any misspelled arguments will not raise an error, and any arguments after `...` must be fully named. This makes it easy for typos to go unnoticed:


```
sum(1, 2, NA, na.rm = TRUE)
#> [1] NA
```

It's often better to be explicit rather than implicit, so you might instead ask users to supply a list of additional arguments. That's certainly easier if you're trying to use `...` with multiple additional functions.

6.4.6 Exercises

1. Clarify the following list of odd function calls:

```
x <- sample(replace = TRUE, 20, x = c(1:10, NA))
y <- runif(min = 0, max = 1, 20)
cor(m = "k", y = y, u = "p", x = x)
```

2. What does this function return? Why? Which principle does it illustrate?

```
f1 <- function(x = {y <- 1; 2}, y = 0) {
  x + y
}
f1()
```

3. What does this function return? Why? Which principle does it illustrate?

```
f2 <- function(x = z) {
  z <- 100
  x
}
f2()
```

6.5 Special calls

R supports two additional syntaxes for calling special types of functions: infix and replacement functions.

6.5.1 Infix functions

Most functions in R are “prefix” operators: the name of the function comes before the arguments. You can also create infix functions where the function name comes in between its arguments, like `+` or `-`. All user created infix functions must start and end with `%` and R comes with the following infix functions predefined: `%%`, `%*%`, `%/%`, `%in%`, `%o%`, `%x%`. (The complete list of built-in infix operators that don’t need `%` is: `::`, `:::`, `$`, `@`, `^`, `*`, `/`, `+`, `-`, `>`, `>=`, `<`, `<=`, `==`, `!=`, `!`, `&`, `&&`, `|`, `||`, `~`, `<-`, `<<-`)

For example, we could create a new operator that pastes together strings:

```
`%+%` <- function(a, b) paste(a, b, sep = "")
"new" %+% " string"
#> [1] "new string"
```

Note that when creating the function, you have to put the name in backticks because it’s a special name. This is just a syntactic sugar for an ordinary function call; as far as R is concerned there is no difference between these two expressions:

```
"new" %+% " string"
#> [1] "new string"
`%+%`("new", " string")
#> [1] "new string"
```

Or indeed between

```
1 + 5
#> [1] 6
`+`(1, 5)
#> [1] 6
```

The names of infix functions are more flexible than regular R functions: they can contain any sequence of characters (except “%”, of course). You will need to escape any special characters in the string used to define the function, but not when you call it:

```
`% %` <- function(a, b) paste(a, b)
`%'%'` <- function(a, b) paste(a, b)
`%/\\%` <- function(a, b) paste(a, b)
```

```
"a" % % "b"
#> [1] "a b"
"a" %'%' "b"
#> [1] "a b"
"a" %/\% "b"
#> [1] "a b"
```

R's default precedence rules mean that infix operators are composed from left to right:

```
`%-%` <- function(a, b) paste0("(", a, " %-% ", b, ")")
"a" %-% "b" %-% "c"
#> [1] "((a %-% b) %-% c)"
```

There's one infix function that I use very often. It's inspired by Ruby's `||` logical or operator, although it works a little differently in R because Ruby has a more flexible definition of what evaluates to `TRUE` in an if statement. It's useful as a way of providing a default value in case the output of another function is `NULL`:

```
`%||%' <- function(a, b) if (!is.null(a)) a else b
function_that_might_return_null() %||% default value
```

6.5.2 Replacement functions

Replacement functions act like they modify their arguments in place, and have the special name `xxx<-`. They typically have two arguments (`x` and `value`), although they can have more, and they must return the modified object. For example, the following function allows you to modify the second element of a vector:

```
`second<-` <- function(x, value) {
  x[2] <- value
  x
}
x <- 1:10
second(x) <- 5L
x
#> [1] 1 5 3 4 5 6 7 8 9 10
```

When R evaluates the assignment `second(x) <- 5`, it notices that the left hand side of the `<-` is not a simple name, so it looks for a function named `second<-` to do the replacement.

I say they “act” like they modify their arguments in place, because they actually create a modified copy. We can see that by using `pryr::address()` to find the memory address of the underlying object.

```
library(pryr)
x <- 1:10
address(x)
#> [1] "0x7fb3024fad48"
second(x) <- 6L
address(x)
#> [1] "0x7fb3059d9888"
```

Built-in functions that are implemented using `.Primitive()` will modify in place:

```
x <- 1:10
address(x)
#> [1] "0x103945110"

x[2] <- 7L
address(x)
#> [1] "0x103945110"
```

It’s important to be aware of this behaviour since it has important performance implications.

If you want to supply additional arguments, they go in between `x` and `value`:

```
`modify<-` <- function(x, position, value) {
  x[position] <- value
  x
}
modify(x, 1) <- 10
x
#> [1] 10 6 3 4 5 6 7 8 9 10
```

When you call `modify(x, 1) <- 10`, behind the scenes R turns it into:

```
x <- `modify<-`(x, 1, 10)
```

This means you can't do things like:

```
modify(get("x"), 1) <- 10
```

because that gets turned into the invalid code:

```
get("x") <- `modify<-`(get("x"), 1, 10)
```

It's often useful to combine replacement and subsetting:

```
x <- c(a = 1, b = 2, c = 3)
names(x)
#> [1] "a" "b" "c"
names(x)[2] <- "two"
names(x)
#> [1] "a" "two" "c"
```

This works because the expression `names(x)[2] <- "two"` is evaluated as if you had written:

```
`*tmp*` <- names(x)
`*tmp*`[2] <- "two"
names(x) <- `*tmp*`
```

(Yes, it really does create a local variable named `*tmp*`, which is removed afterwards.)

6.5.3 Exercises

1. Create a list of all the replacement functions found in the base package. Which ones are primitive functions?
2. What are valid names for user created infix functions?
3. Create an infix `xor()` operator.
4. Create infix versions of the set functions `intersect()`, `union()`, and `setdiff()`.
5. Create a replacement function that modifies a random location in a vector.

6.6 Return values

The last expression evaluated in a function becomes the return value, the result of invoking the function.

```
f <- function(x) {  
  if (x < 10) {  
    0  
  } else {  
    10  
  }  
}  
f(5)  
#> [1] 0  
f(15)  
#> [1] 10
```

Generally, I think it's good style to reserve the use of an explicit `return()` for when you are returning early, such as for an error, or a simple case of the function. This style of programming can also reduce the level of indentation, and generally make functions easier to understand because you can reason about them locally.

```
f <- function(x, y) {  
  if (!x) return(y)  
  
  # complicated processing here  
}
```

Functions can return only a single object. But this is not a limitation because you can return a list containing any number of objects.

The functions that are the easiest to understand and reason about are pure functions: functions that always map the same input to the same output and have no other impact on the workspace. In other words, pure functions have no **side effects**: they don't affect the state of the world in any way apart from the value they return.

R protects you from one type of side effect: most R objects have copy-on-modify semantics. So modifying a function argument does not change the original value:

```
f <- function(x) {  
  x$a <- 2  
  x  
}  
x <- list(a = 1)  
f(x)  
#> $a  
#> [1] 2  
x$a  
#> [1] 1
```

(There are two important exceptions to the copy-on-modify rule: environments and reference classes. These can be modified in place, so extra care is needed when working with them.)

This is notably different to languages like Java where you can modify the inputs of a function. This copy-on-modify behaviour has important performance consequences which are discussed in depth in Chapter 17. (Note that the performance consequences are a result of R's implementation of copy-on-modify semantics; they are not true in general. Clojure is a new language that makes extensive use of copy-on-modify semantics with limited performance consequences.)

Most base R functions are pure, with a few notable exceptions:

- `library()` which loads a package, and hence modifies the search path.
- `setwd()`, `Sys.setenv()`, `Sys.setlocale()` which change the working directory, environment variables, and the locale, respectively.
- `plot()` and friends which produce graphical output.
- `write()`, `write.csv()`, `saveRDS()`, etc. which save output to disk.
- `options()` and `par()` which modify global settings.
- S4 related functions which modify global tables of classes and methods.
- Random number generators which produce different numbers each time you run them.

It's generally a good idea to minimise the use of side-effects, and where possible, to minimise the footprint of side effects by separating pure from impure functions. Pure functions are easier to test (because all you need to worry about are the input values and the output), and are less likely

to work differently on different versions of R or on different platforms. For example, this is one of the motivating principles of `ggplot2`: most operations work on an object that represents a plot, and only the final `print` or `plot` call has the side effect of actually drawing the plot.

Functions can return `invisible` values, which are not printed out by default when you call the function.

```
f1 <- function() 1
f2 <- function() invisible(1)

f1()
#> [1] 1
f2()
f1() == 1
#> [1] TRUE
f2() == 1
#> [1] TRUE
```

You can force an invisible value to be displayed by wrapping it in parentheses:

```
(f2())
#> [1] 1
```

The most common function that returns invisibly is `<-`:

```
a <- 2
(a <- 2)
#> [1] 2
```

This is what makes it possible to assign one value to multiple variables:

```
a <- b <- c <- d <- 2
```

because this is parsed as:

```
(a <- (b <- (c <- (d <- 2))))
#> [1] 2
```


6.6.1 On exit

As well as returning a value, functions can set up other triggers to occur when the function is finished using `on.exit()`. This is often used as a way to guarantee that changes to the global state are restored when the function exits. The code in `on.exit()` is run regardless of how the function exits, whether with an explicit (early) return, an error, or simply reaching the end of the function body.

```
in_dir <- function(dir, code) {  
  old <- setwd(dir)  
  on.exit(setwd(old))  
  
  force(code)  
}  
getwd()  
#> [1] "/Users/hadley/Documents/adv-r/adv-r"  
in_dir("~", getwd())  
#> [1] "/Users/hadley"
```

The basic pattern is simple:

- We first set the directory to a new location, capturing the current location from the output of `setwd()`.
- We then use `on.exit()` to ensure that the working directory is returned to the previous value regardless of how the function exits.
- Finally, we explicitly force evaluation of the code. (We don't actually need `force()` here, but it makes it clear to readers what we're doing.)

Caution: If you're using multiple `on.exit()` calls within a function, make sure to set `add = TRUE`. Unfortunately, the default in `on.exit()` is `add = FALSE`, so that every time you run it, it overwrites existing exit expressions. Because of the way `on.exit()` is implemented, it's not possible to create a variant with `add = TRUE`, so you must be careful when using it.

6.6.2 Exercises

1. How does the `chdir` parameter of `source()` compare to `in_dir()`? Why might you prefer one approach to the other?

2. What function undoes the action of `library()`? How do you save and restore the values of `options()` and `par()`?
3. Write a function that opens a graphics device, runs the supplied code, and closes the graphics device (always, regardless of whether or not the plotting code worked).
4. We can use `on.exit()` to implement a simple version of `capture.output()`.

```
capture.output2 <- function(code) {
  temp <- tempfile()
  on.exit(file.remove(temp), add = TRUE)

  sink(temp)
  on.exit(sink(), add = TRUE)

  force(code)
  readLines(temp)
}
capture.output2(cat("a", "b", "c", sep = "\n"))
#> [1] "a" "b" "c"
```

Compare `capture.output()` to `capture.output2()`. How do the functions differ? What features have I removed to make the key ideas easier to see? How have I rewritten the key ideas to be easier to understand?

6.7 Quiz answers

1. The three components of a function are its body, arguments, and environment.
2. `f1(1)()` returns 11.
3. You'd normally write it in infix style: `1 + (2 * 3)`.
4. Rewriting the call to `mean(c(1:10, NA), na.rm = TRUE)` is easier to understand.
5. No, it does not throw an error because the second argument is never used so it's never evaluated.
6. See Section 6.5.1 and Section 6.5.2.
7. You use `on.exit()`; see Section 6.6.1 for details.

7

OO field guide

This chapter is a field guide for recognising and working with R's objects in the wild. R has three object oriented systems (plus the base types), so it can be a bit intimidating. The goal of this guide is not to make you an expert in all four systems, but to help you identify which system you're working with and to help you use it effectively.

Central to any object-oriented system are the concepts of class and method. A **class** defines the behaviour of **objects** by describing their attributes and their relationship to other classes. The class is also used when selecting **methods**, functions that behave differently depending on the class of their input. Classes are usually organised in a hierarchy: if a method does not exist for a child, then the parent's method is used instead; the child **inherits** behaviour from the parent.

R's three OO systems differ in how classes and methods are defined:

- **S3** implements a style of OO programming called generic-function OO. This is different from most programming languages, like Java, C++, and C#, which implement message-passing OO. With message-passing, messages (methods) are sent to objects and the object determines which function to call. Typically, this object has a special appearance in the method call, usually appearing before the name of the method/message: e.g., `canvas.drawRect("blue")`. S3 is different. While computations are still carried out via methods, a special type of function called a **generic function** decides which method to call, e.g., `drawRect(canvas, "blue")`. S3 is a very casual system. It has no formal definition of classes.
- **S4** works similarly to S3, but is more formal. There are two major differences to S3. S4 has formal class definitions, which describe the representation and inheritance for each class, and has special helper functions for defining generics and methods. S4 also has multiple dispatch, which means that generic functions can pick methods based on the class of any number of arguments, not just one.

- **Reference classes**, called RC for short, are quite different from S3 and S4. RC implements message-passing OO, so methods belong to classes, not functions. `$` is used to separate objects and methods, so method calls look like `canvas$drawRect("blue")`. RC objects are also mutable: they don't use R's usual copy-on-modify semantics, but are modified in place. This makes them harder to reason about, but allows them to solve problems that are difficult to solve with S3 or S4.

There's also one other system that's not quite OO, but it's important to mention here:

- **base types**, the internal C-level types that underlie the other OO systems. Base types are mostly manipulated using C code, but they're important to know about because they provide the building blocks for the other OO systems.

The following sections describe each system in turn, starting with base types. You'll learn how to recognise the OO system that an object belongs to, how method dispatch works, and how to create new objects, classes, generics, and methods for that system. The chapter concludes with a few remarks on when to use each system.

Prerequisites

You'll need the `pryr` package, `install.packages("pryr")`, to access useful functions for examining OO properties.

Quiz

Think you know this material already? If you can answer the following questions correctly, you can safely skip this chapter. Find the answers at the end of the chapter in Section 7.6.

1. How do you tell what OO system (base, S3, S4, or RC) an object is associated with?
2. How do you determine the base type (like integer or list) of an object?
3. What is a generic function?
4. What are the main differences between S3 and S4? What are the main differences between S4 & RC?

Outline

- Section 7.1 teaches you about R's base object system. Only R-core can add new classes to this system, but it's important to know about because it underpins the three other systems.
- Section 7.2 shows you the basics of the S3 object system. It's the simplest and most commonly used OO system.
- Section 7.3 discusses the more formal and rigorous S4 system.
- Section 7.4 teaches you about R's newest OO system: reference classes, or RC for short.
- Section 7.5 advises on which OO system to use if you're starting a new project.

7.1 Base types

Underlying every R object is a C structure (or struct) that describes how that object is stored in memory. The struct includes the contents of the object, the information needed for memory management, and, most importantly for this section, a **type**. This is the **base type** of an R object. Base types are not really an object system because only the R core team can create new types. As a result, new base types are added very rarely: the most recent change, in 2011, added two exotic types that you never see in R, but are useful for diagnosing memory problems (NEWSXP and FREESXP). Prior to that, the last type added was a special base type for S4 objects (S4SXP) in 2005.

Chapter 2 explains the most common base types (atomic vectors and lists), but base types also encompass functions, environments, and other more exotic objects like names, calls, and promises that you'll learn about later in the book. You can determine an object's base type with `typeof()`. Unfortunately the names of base types are not used consistently throughout R, and `type` and the corresponding "is" function may use different names:

```
# The type of a function is "closure"
f <- function() {}
typeof(f)
```

```
#> [1] "closure"
is.function(f)
#> [1] TRUE

# The type of a primitive function is "builtin"
typeof(sum)
#> [1] "builtin"
is.primitive(sum)
#> [1] TRUE
```

You may have heard of `mode()` and `storage.mode()`. I recommend ignoring these functions because they're just aliases of the names returned by `typeof()`, and exist solely for S compatibility. Read their source code if you want to understand exactly what they do.

Functions that behave differently for different base types are almost always written in C, where dispatch occurs using switch statements (e.g., `switch(TYPEOF(x))`). Even if you never write C code, it's important to understand base types because everything else is built on top of them: S3 objects can be built on top of any base type, S4 objects use a special base type, and RC objects are a combination of S4 and environments (another base type). To see if an object is a pure base type, i.e., it doesn't also have S3, S4, or RC behaviour, check that `is.object(x)` returns `FALSE`.

7.2 S3

S3 is R's first and simplest OO system. It is the only OO system used in the base and stats packages, and it's the most commonly used system in CRAN packages. S3 is informal and ad hoc, but it has a certain elegance in its minimalism: you can't take away any part of it and still have a useful OO system.

7.2.1 Recognising objects, generic functions, and methods

Most objects that you encounter are S3 objects. But unfortunately there's no simple way to test if an object is an S3 object in base R. The closest you can come is `is.object(x) & !isS4(x)`, i.e., it's an object, but not S4. An easier way is to use `pryr::otype()`:

```
library(pryr)

df <- data.frame(x = 1:10, y = letters[1:10])
otype(df)      # A data frame is an S3 class
#> [1] "S3"
otype(df$x)    # A numeric vector isn't
#> [1] "base"
otype(df$y)    # A factor is
#> [1] "S3"
```

In S3, methods belong to functions, called **generic functions**, or generics for short. S3 methods do not belong to objects or classes. This is different from most other programming languages, but is a legitimate OO style.

To determine if a function is an S3 generic, you can inspect its source code for a call to `UseMethod()`: that's the function that figures out the correct method to call, the process of **method dispatch**. Similar to `otype()`, `pryr` also provides `ftype()` which describes the object system, if any, associated with a function:

```
mean
#> function (x, ...)
#> UseMethod("mean")
#> <bytecode: 0x7f96ac563c68>
#> <environment: namespace:base>
ftype(mean)
#> [1] "s3"      "generic"
```

Some S3 generics, like `[]`, `sum()`, and `cbind()`, don't call `UseMethod()` because they are implemented in C. Instead, they call the C functions `DispatchGroup()` or `DispatchOrEval()`. Functions that do method dispatch in C code are called **internal generics** and are documented in `"internal generic"`. `ftype()` knows about these special cases too.

Given a class, the job of an S3 generic is to call the right S3 method. You can recognise S3 methods by their names, which look like `generic.class()`. For example, the Date method for the `mean()` generic is called `mean.Date()`, and the factor method for `print()` is called `print.factor()`.

This is the reason that most modern style guides discourage the use of `.` in function names: it makes them look like S3 methods. For example, is `t.test()` the `test` method for `t` objects? Similarly, the use of `.` in class

names can also be confusing: is `print.data.frame()` the `print()` method for `data.frames`, or the `print.data()` method for `frames`? `pryr::ftype()` knows about these exceptions, so you can use it to figure out if a function is an S3 method or generic:

```
ftype(t.data.frame) # data frame method for t()
#> [1] "s3"          "method"
ftype(t.test)       # generic function for t tests
#> [1] "s3"          "generic"
```

You can see all the methods that belong to a generic with `methods()`:

```
methods("mean")
#> [1] mean.Date      mean.default    mean.difftime  mean.POSIXct
#> [5] mean.POSIXlt
methods("t.test")
#> [1] t.test.default* t.test.formula*
#>
#> Non-visible functions are asterisked
```

(Apart from methods defined in the base package, most S3 methods will not be visible: use `getS3method()` to read their source code.)

You can also list all generics that have a method for a given class:

```
methods(class = "ts")
#> [1] [.ts*          [<-.ts*         aggregate.ts
#> [4] as.data.frame.ts cbind.ts*       cycle.ts*
#> [7] diff.ts*        diffinv.ts*     kernapply.ts*
#> [10] lines.ts*       monthplot.ts*   na.omit.ts*
#> [13] Ops.ts*         plot.ts         print.ts*
#> [16] t.ts*          time.ts*        window.ts*
#> [19] window<-ts*
#>
#> Non-visible functions are asterisked
```

There's no way to list all S3 classes, as you'll learn in the following section.

7.2.2 Defining classes and creating objects

S3 is a simple and ad hoc system; it has no formal definition of a class. To make an object an instance of a class, you just take an existing base object and set the class attribute. You can do that during creation with `structure()`, or after the fact with `class<-()`:

```
# Create and assign class in one step
foo <- structure(list(), class = "foo")

# Create, then set class
foo <- list()
class(foo) <- "foo"
```

S3 objects are usually built on top of lists, or atomic vectors with attributes. (You can refresh your memory of attributes with Section 2.2.) You can also turn functions into S3 objects. Other base types are either rarely seen in R, or have unusual semantics that don't work well with attributes.

You can determine the class of any object using `class(x)`, and see if an object inherits from a specific class using `inherits(x, "classname")`.

```
class(foo)
#> [1] "foo"
inherits(foo, "foo")
#> [1] TRUE
```

The class of an S3 object can be a vector, which describes behaviour from most to least specific. For example, the class of the `glm()` object is `c("glm", "lm")` indicating that generalised linear models inherit behaviour from linear models. Class names are usually lower case, and you should avoid `..`. Otherwise, opinion is mixed whether to use underscores (`my_class`) or CamelCase (`MyClass`) for multi-word class names.

Most S3 classes provide a constructor function:

```
foo <- function(x) {
  if (!is.numeric(x)) stop("X must be numeric")
  structure(list(x), class = "foo")
}
```

You should use it if it's available (like for `factor()` and `data.frame()`). This ensures that you're creating the class with the correct components. Constructor functions usually have the same name as the class.

Apart from developer supplied constructor functions, S3 has no checks for correctness. This means you can change the class of existing objects:

```
# Create a linear model
mod <- lm(log(mpg) ~ log(displ), data = mtcars)
class(mod)
#> [1] "lm"
print(mod)
#>
#> Call:
#> lm(formula = log(mpg) ~ log(displ), data = mtcars)
#>
#> Coefficients:
#> (Intercept)      log(displ)
#>      5.381      -0.459

# Turn it into a data frame (!)
class(mod) <- "data.frame"
# But unsurprisingly this doesn't work very well
print(mod)
#> [1] coefficients residuals      effects      rank
#> [5] fitted.values assign      qr          df.residual
#> [9] xlevels      call      terms      model
#> <0 rows> (or 0-length row.names)
# However, the data is still there
mod$coefficients
#> (Intercept)      log(displ)
#>      5.3810      -0.4586
```

If you've used other OO languages, this might make you feel uneasy. But surprisingly, this flexibility causes few problems: while you *can* change the type of an object, you never should. R doesn't protect you from yourself: you can easily shoot yourself in the foot. As long as you don't aim the gun at your foot and pull the trigger, you won't have a problem.

7.2.3 Creating new methods and generics

To add a new generic, create a function that calls `UseMethod()`. `UseMethod()` takes two arguments: the name of the generic function,

and the argument to use for method dispatch. If you omit the second argument it will dispatch on the first argument to the function. There's no need to pass any of the arguments of the generic to `UseMethod()` and you shouldn't do so. `UseMethod()` uses black magic to find them out for itself.

```
f <- function(x) UseMethod("f")
```

A generic isn't useful without some methods. To add a method, you just create a regular function with the correct (`generic.class`) name:

```
f.a <- function(x) "Class a"

a <- structure(list(), class = "a")
class(a)
#> [1] "a"
f(a)
#> [1] "Class a"
```

Adding a method to an existing generic works in the same way:

```
mean.a <- function(x) "a"
mean(a)
#> [1] "a"
```

As you can see, there's no check to make sure that the method returns the class compatible with the generic. It's up to you to make sure that your method doesn't violate the expectations of existing code.

7.2.4 Method dispatch

S3 method dispatch is relatively simple. `UseMethod()` creates a vector of function names, like `paste0("generic", ".", c(class(x), "default"))` and looks for each in turn. The "default" class makes it possible to set up a fall back method for otherwise unknown classes.

```
f <- function(x) UseMethod("f")
f.a <- function(x) "Class a"
f.default <- function(x) "Unknown class"
```

```
f(structure(list(), class = "a"))
#> [1] "Class a"
# No method for b class, so uses method for a class
f(structure(list(), class = c("b", "a")))
#> [1] "Class a"
# No method for c class, so falls back to default
f(structure(list(), class = "c"))
#> [1] "Unknown class"
```

Group generic methods add a little more complexity. Group generics make it possible to implement methods for multiple generics with one function. The four group generics and the functions they include are:

- Math: `abs`, `sign`, `sqrt`, `floor`, `cos`, `sin`, `log`, `exp`, ...
- Ops: `+`, `-`, `*`, `/`, `^`, `%%`, `%/%`, `&`, `|`, `!`, `==`, `!=`, `<`, `<=`, `>=`, `>`
- Summary: `all`, `any`, `sum`, `prod`, `min`, `max`, `range`
- Complex: `Arg`, `Conj`, `Im`, `Mod`, `Re`

Group generics are a relatively advanced technique and are beyond the scope of this chapter but you can find out more about them in `?groupGeneric`. The most important thing to take away from this is to recognise that Math, Ops, Summary, and Complex aren't real functions, but instead represent groups of functions. Note that inside a group generic function a special variable `.Generic` provides the actual generic function called.

If you have complex class hierarchies it's sometimes useful to call the "parent" method. It's a little bit tricky to define exactly what that means, but it's basically the method that would have been called if the current method did not exist. Again, this is an advanced technique: you can read about it in `?NextMethod`.

Because methods are normal R functions, you can call them directly:

```
c <- structure(list(), class = "c")
# Call the correct method:
f.default(c)
#> [1] "Unknown class"
# Force R to call the wrong method:
f.a(c)
#> [1] "Class a"
```

However, this is just as dangerous as changing the class of an object, so you shouldn't do it. Please don't point the loaded gun at your foot! The

only reason to call the method directly is that sometimes you can get considerable performance improvements by skipping method dispatch. See Section 17.5 for details.

You can also call an S3 generic with a non-S3 object. Non-internal S3 generics will dispatch on the **implicit class** of base types. (Internal generics don't do that for performance reasons.) The rules to determine the implicit class of a base type are somewhat complex, but are shown in the function below:

```
iclass <- function(x) {
  if (is.object(x)) {
    stop("x is not a primitive type", call. = FALSE)
  }

  c(
    if (is.matrix(x)) "matrix",
    if (is.array(x) && !is.matrix(x)) "array",
    if (is.double(x)) "double",
    if (is.integer(x)) "integer",
    mode(x)
  )
}
iclass(matrix(1:5))
#> [1] "matrix" "integer" "numeric"
iclass(array(1:5))
#> [1] "array" "double" "numeric"
```

7.2.5 Exercises

1. Read the source code for `t()` and `t.test()` and confirm that `t.test()` is an S3 generic and not an S3 method. What happens if you create an object with class `test` and call `t()` with it?
2. What classes have a method for the `Math` group generic in base R? Read the source code. How do the methods work?
3. R has two classes for representing date time data, `POSIXct` and `POSIXlt`, which both inherit from `POSIXt`. Which generics have different behaviours for the two classes? Which generics share the same behaviour?
4. Which base generic has the greatest number of defined methods?

5. `UseMethod()` calls methods in a special way. Predict what the following code will return, then run it and read the help for `UseMethod()` to figure out what's going on. Write down the rules in the simplest form possible.

```
y <- 1
g <- function(x) {
  y <- 2
  UseMethod("g")
}
g.numeric <- function(x) y
g(10)

h <- function(x) {
  x <- 10
  UseMethod("h")
}
h.character <- function(x) paste("char", x)
h.numeric <- function(x) paste("num", x)

h("a")
```

6. Internal generics don't dispatch on the implicit class of base types. Carefully read `?internal_generic` to determine why the length of `f` and `g` is different in the example below. What function helps distinguish between the behaviour of `f` and `g`?

```
f <- function() 1
g <- function() 2
class(g) <- "function"

class(f)
class(g)

length.function <- function(x) "function"
length(f)
length(g)
```

7.3 S4

S4 works in a similar way to S3, but it adds formality and rigour. Methods still belong to functions, not classes, but:

- Classes have formal definitions which describe their fields and inheritance structures (parent classes).
- Method dispatch can be based on multiple arguments to a generic function, not just one.
- There is a special operator, @, for extracting slots (aka fields) from an S4 object.

All S4 related code is stored in the `methods` package. This package is always available when you're running R interactively, but may not be available when running R in batch mode. For this reason, it's a good idea to include an explicit `library(methods)` whenever you're using S4.

S4 is a rich and complex system. There's no way to explain it fully in a few pages. Here I'll focus on the key ideas underlying S4 so you can use existing S4 objects effectively. To learn more, some good references are:

- S4 system development in Bioconductor (<http://www.bioconductor.org/help/course-materials/2010/AdvancedR/S4InBioconductor.pdf>)
- John Chambers' *Software for Data Analysis* (<http://amzn.com/0387759352?tag=devtools-20>)
- Martin Morgan's answers to S4 questions on stackoverflow (<http://stackoverflow.com/search?tab=votes&q=user%3a547331%20%5bs4%5d%20is%3aanswe>)

7.3.1 Recognising objects, generic functions, and methods

Recognising S4 objects, generics, and methods is easy. You can identify an S4 object because `str()` describes it as a "formal" class, `isS4()` returns `TRUE`, and `pryr::otype()` returns "S4". S4 generics and methods are also easy to identify because they are S4 objects with well defined classes.

There aren't any S4 classes in the commonly used base packages (stats, graphics, utils, datasets, and base), so we'll start by creating an S4 object from the built-in stats4 package, which provides some S4 classes and methods associated with maximum likelihood estimation:

```
library(stats4)

# From example(mle)
y <- c(26, 17, 13, 12, 20, 5, 9, 8, 5, 4, 8)
nLL <- function(lambda) - sum(dpois(y, lambda, log = TRUE))
fit <- mle(nLL, start = list(lambda = 5), nobs = length(y))

# An S4 object
isS4(fit)
#> [1] TRUE
otype(fit)
#> [1] "S4"

# An S4 generic
isS4(nobs)
#> [1] TRUE
ftype(nobs)
#> [1] "s4"      "generic"

# Retrieve an S4 method, described later
mle_nobs <- method_from_call(nobs(fit))
isS4(mle_nobs)
#> [1] TRUE
ftype(mle_nobs)
#> [1] "s4"      "method"
```

Use `is()` with one argument to list all classes that an object inherits from. Use `is()` with two arguments to test if an object inherits from a specific class.

```
is(fit)
#> [1] "mle"
is(fit, "mle")
#> [1] TRUE
```

You can get a list of all S4 generics with `getGenerics()`, and a list of all S4 classes with `getClasses()`. This list includes shim classes for S3

classes and base types. You can list all S4 methods with `showMethods()`, optionally restricting selection either by `generic` or by `class` (or both). It's also a good idea to supply `where = search()` to restrict the search to methods available in the global environment.

7.3.2 Defining classes and creating objects

In S3, you can turn any object into an object of a particular class just by setting the class attribute. S4 is much stricter: you must define the representation of a class with `setClass()`, and create a new object with `new()`. You can find the documentation for a class with a special syntax: `class?className`, e.g., `class?mle`.

An S4 class has three key properties:

- A **name**: an alpha-numeric class identifier. By convention, S4 class names use UpperCamelCase.
- A named list of **slots** (fields), which defines slot names and permitted classes. For example, a person class might be represented by a character name and a numeric age: `list(name = "character", age = "numeric")`.
- A string giving the class it inherits from, or, in S4 terminology, that it **contains**. You can provide multiple classes for multiple inheritance, but this is an advanced technique which adds much complexity.

In slots and contains you can use S4 classes, S3 classes registered with `setOldClass()`, or the implicit class of a base type. In slots you can also use the special class `ANY` which does not restrict the input.

S4 classes have other optional properties like a `validity` method that tests if an object is valid, and a `prototype` object that defines default slot values. See `?setClass` for more details.

The following example creates a `Person` class with fields `name` and `age`, and an `Employee` class that inherits from `Person`. The `Employee` class inherits the slots and methods from the `Person`, and adds an additional slot, `boss`. To create objects we call `new()` with the name of the class, and name-value pairs of slot values.

```
setClass("Person",  
  slots = list(name = "character", age = "numeric"))  
setClass("Employee",
```

```

  slots = list(boss = "Person"),
  contains = "Person")

alice <- new("Person", name = "Alice", age = 40)
john <- new("Employee", name = "John", age = 20, boss = alice)

```

Most S4 classes also come with a constructor function with the same name as the class: if that exists, use it instead of calling `new()` directly.

To access slots of an S4 object use `@` or `slot()`:

```

alice@age
#> [1] 40
slot(john, "boss")
#> An object of class "Person"
#> Slot "name":
#> [1] "Alice"
#>
#> Slot "age":
#> [1] 40

```

(`@` is equivalent to `$`, and `slot()` to `[[`.)

If an S4 object contains (inherits) from an S3 class or a base type, it will have a special `.Data` slot which contains the underlying base type or S3 object:

```

setClass("RangedNumeric",
  contains = "numeric",
  slots = list(min = "numeric", max = "numeric"))
rn <- new("RangedNumeric", 1:10, min = 1, max = 10)
rn@min
#> [1] 1
rn@.Data
#> [1] 1 2 3 4 5 6 7 8 9 10

```

Since R is an interactive programming language, it's possible to create new classes or redefine existing classes at any time. This can be a problem when you're interactively experimenting with S4. If you modify a class, make sure you also recreate any objects of that class, otherwise you'll end up with invalid objects.

7.3.3 Creating new methods and generics

S4 provides special functions for creating new generics and methods. `setGeneric()` creates a new generic or converts an existing function into a generic. `setMethod()` takes the name of the generic, the classes the method should be associated with, and a function that implements the method. For example, we could take `union()`, which usually just works on vectors, and make it work with data frames:

```
setGeneric("union")
#> [1] "union"
setMethod("union",
  c(x = "data.frame", y = "data.frame"),
  function(x, y) {
    unique(rbind(x, y))
  }
)
#> [1] "union"
```

If you create a new generic from scratch, you need to supply a function that calls `standardGeneric()`:

```
setGeneric("myGeneric", function(x) {
  standardGeneric("myGeneric")
})
#> [1] "myGeneric"
```

`standardGeneric()` is the S4 equivalent to `UseMethod()`.

7.3.4 Method dispatch

If an S4 generic dispatches on a single class with a single parent, then S4 method dispatch is the same as S3 dispatch. The main difference is how you set up default values: S4 uses the special class `ANY` to match any class and “missing” to match a missing argument. Like S3, S4 also has group generics, documented in `?S4groupGeneric`, and a way to call the “parent” method, `callNextMethod()`.

Method dispatch becomes considerably more complicated if you dispatch on multiple arguments, or if your classes use multiple inheritance. The rules are described in `?Methods`, but they are complicated and it’s difficult to predict which method will be called. For this reason, I strongly

recommend avoiding multiple inheritance and multiple dispatch unless absolutely necessary.

Finally, there are two methods that find which method gets called given the specification of a generic call:

```
# From methods: takes generic name and class names
selectMethod("nobs", list("mle"))

# From pryr: takes an unevaluated function call
method_from_call(nobs(fit))
```

7.3.5 Exercises

1. Which S4 generic has the most methods defined for it? Which S4 class has the most methods associated with it?
2. What happens if you define a new S4 class that doesn't "contain" an existing class? (Hint: read about virtual classes in `?Classes`.)
3. What happens if you pass an S4 object to an S3 generic? What happens if you pass an S3 object to an S4 generic? (Hint: read `?setOldClass` for the second case.)

7.4 RC

Reference classes (or RC for short) are the newest OO system in R. They were introduced in version 2.12. They are fundamentally different to S3 and S4 because:

- RC methods belong to objects, not functions
- RC objects are mutable: the usual R copy-on-modify semantics do not apply

These properties make RC objects behave more like objects do in most other programming languages, e.g., Python, Ruby, Java, and C#. Reference classes are implemented using R code: they are a special S4 class that wraps around an environment.

7.4.1 Defining classes and creating objects

Since there aren't any reference classes provided by the base R packages, we'll start by creating one. RC classes are best used for describing stateful objects, objects that change over time, so we'll create a simple class to model a bank account.

Creating a new RC class is similar to creating a new S4 class, but you use `setRefClass()` instead of `setClass()`. The first, and only required argument, is an alphanumeric **name**. While you can use `new()` to create new RC objects, it's good style to use the object returned by `setRefClass()` to generate new objects. (You can also do that with S4 classes, but it's less common.)

```
Account <- setRefClass("Account")
Account$new()
#> Reference class object of class "Account"
```

`setRefClass()` also accepts a list of name-class pairs that define class **fields** (equivalent to S4 slots). Additional named arguments passed to `new()` will set initial values of the fields. You can get and set field values with `$`:

```
Account <- setRefClass("Account",
  fields = list(balance = "numeric"))

a <- Account$new(balance = 100)
a$balance
#> [1] 100
a$balance <- 200
a$balance
#> [1] 200
```

Instead of supplying a class name for the field, you can provide a single argument function which will act as an accessor method. This allows you to add custom behaviour when getting or setting a field. See `?setRefClass` for more details.

Note that RC objects are **mutable**, i.e., they have reference semantics, and are not copied-on-modify:

```
b <- a
b$balance
```

```
#> [1] 200
a$balance <- 0
b$balance
#> [1] 0
```

For this reason, RC objects come with a `copy()` method that allow you to make a copy of the object:

```
c <- a$copy()
c$balance
#> [1] 0
a$balance <- 100
c$balance
#> [1] 0
```

An object is not very useful without some behaviour defined by **methods**. RC methods are associated with a class and can modify its fields in place. In the following example, note that you access the value of fields with their name, and modify them with `<<-`. You'll learn more about `<<-` in Section 8.4.

```
Account <- setRefClass("Account",
  fields = list(balance = "numeric"),
  methods = list(
    withdraw = function(x) {
      balance <<- balance - x
    },
    deposit = function(x) {
      balance <<- balance + x
    }
  )
)
```

You call an RC method in the same way as you access a field:

```
a <- Account$new(balance = 100)
a$deposit(100)
a$balance
#> [1] 200
```

The final important argument to `setRefClass()` is `contains`. This is the

name of the parent RC class to inherit behaviour from. The following example creates a new type of bank account that returns an error preventing the balance from going below 0.

```
NoOverdraft <- setRefClass("NoOverdraft",
  contains = "Account",
  methods = list(
    withdraw = function(x) {
      if (balance < x) stop("Not enough money")
      balance <- balance - x
    }
  )
)
accountJohn <- NoOverdraft$new(balance = 100)
accountJohn$deposit(50)
accountJohn$balance
#> [1] 150
accountJohn$withdraw(200)
#> Error: Not enough money
```

All reference classes eventually inherit from `envRefClass`. It provides useful methods like `copy()` (shown above), `callSuper()` (to call the parent field), `field()` (to get the value of a field given its name), `export()` (equivalent to `as()`), and `show()` (overridden to control printing). See the inheritance section in `setRefClass()` for more details.

7.4.2 Recognising objects and methods

You can recognise RC objects because they are S4 objects (`isS4(x)`) that inherit from “refClass” (`is(x, "refClass")`). `pryr::otype()` will return “RC”. RC methods are also S4 objects, with class `refMethodDef`.

7.4.3 Method dispatch

Method dispatch is very simple in RC because methods are associated with classes, not functions. When you call `x$f()`, R will look for a method `f` in the class of `x`, then in its parent, then its parent’s parent, and so on. From within a method, you can call the parent method directly with `callSuper(...)`.

7.4.4 Exercises

1. Use a field function to prevent the account balance from being directly manipulated. (Hint: create a “hidden” `.balance` field, and read the help for the `fields` argument in `setRefClass()`.)
2. I claimed that there aren’t any RC classes in base R, but that was a bit of a simplification. Use `getClasses()` and find which classes `extend()` from `envRefClass`. What are the classes used for? (Hint: recall how to look up the documentation for a class.)

7.5 Picking a system

Three OO systems is a lot for one language, but for most R programming, S3 suffices. In R you usually create fairly simple objects and methods for pre-existing generic functions like `print()`, `summary()`, and `plot()`. S3 is well suited to this task, and the majority of OO code that I have written in R is S3. S3 is a little quirky, but it gets the job done with a minimum of code.

If you are creating more complicated systems of interrelated objects, S4 may be more appropriate. A good example is the `Matrix` package by Douglas Bates and Martin Maechler. It is designed to efficiently store and compute with many different types of sparse matrices. As of version 1.1.3, it defines 102 classes and 20 generic functions. The package is well written and well commented, and the accompanying vignette (`vignette("Intro2Matrix", package = "Matrix")`) gives a good overview of the structure of the package. S4 is also used extensively by Bioconductor packages, which need to model complicated interrelationships between biological objects. Bioconductor provides many good resources (<https://www.google.com/search?q=bioconductor+s4>) for learning S4. If you’ve mastered S3, S4 is relatively easy to pick up; the ideas are all the same, it is just more formal, more strict, and more verbose.

If you’ve programmed in a mainstream OO language, RC will seem very natural. But because they can introduce side effects through mutable state, they are harder to understand. For example, when you usually call `f(a, b)` in R you can assume that `a` and `b` will not be modified. But if `a` and `b` are RC objects, they might be modified in the place. Generally, when using RC objects you want to minimise side effects as

much as possible, and use them only where mutable states are absolutely required. The majority of functions should still be “functional”, and free of side effects. This makes code easier to reason about and easier for other R programmers to understand.

7.6 Quiz answers

1. To determine the OO system of an object, you use a process of elimination. If `!is.object(x)`, it's a base object. If `!isS4(x)`, it's S3. If `!is(x, "refClass")`, it's S4; otherwise it's RC.
2. Use `typeof()` to determine the base class of an object.
3. A generic function calls specific methods depending on the class of its inputs. In S3 and S4 object systems, methods belong to generic functions, not classes like in other programming languages.
4. S4 is more formal than S3, and supports multiple inheritance and multiple dispatch. RC objects have reference semantics, and methods belong to classes, not functions.

8

Environments

The environment is the data structure that powers scoping. This chapter dives deep into environments, describing their structure in depth, and using them to improve your understanding of the four scoping rules described in Section 6.2.

Environments can also be useful data structures in their own right because they have reference semantics. When you modify a binding in an environment, the environment is not copied; it's modified in place. Reference semantics are not often needed, but can be extremely useful.

Quiz

If you can answer the following questions correctly, you already know the most important topics in this chapter. You can find the answers at the end of the chapter in Section 8.6.

1. List at least three ways that an environment is different to a list.
2. What is the parent of the global environment? What is the only environment that doesn't have a parent?
3. What is the enclosing environment of a function? Why is it important?
4. How do you determine the environment from which a function was called?
5. How are `<-` and `<<-` different?

Outline

- Section 8.1 introduces you to the basic properties of an environment and shows you how to create your own.
- Section 8.2 provides a function template for computing with environments, illustrating the idea with a useful function.

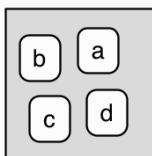
- Section 8.3 revises R’s scoping rules in more depth, showing how they correspond to four types of environment associated with each function.
- Section 8.4 describes the rules that names must follow (and how to bend them), and shows some variations on binding a name to a value.
- Section 8.5 discusses three problems where environments are useful data structures in their own right, independent of the role they place in scoping.

Prerequisites

This chapter uses many functions from the `pryr` package to pry open R and look inside at the messy details. You can install `pryr` by running `install.packages("pryr")`

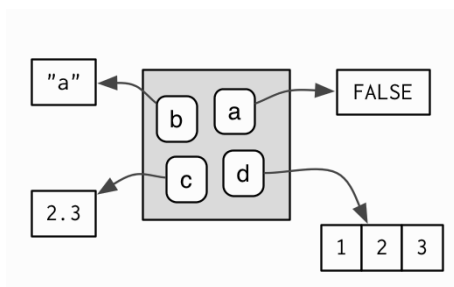
8.1 Environment basics

The job of an environment is to associate, or **bind**, a set of names to a set of values. You can think of an environment as a bag of names:



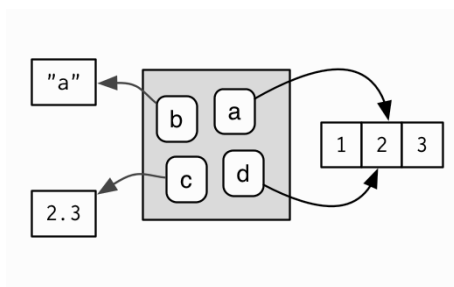
Each name points to an object stored elsewhere in memory:

```
e <- new.env()
e$a <- FALSE
e$b <- "a"
e$c <- 2.3
e$d <- 1:3
```



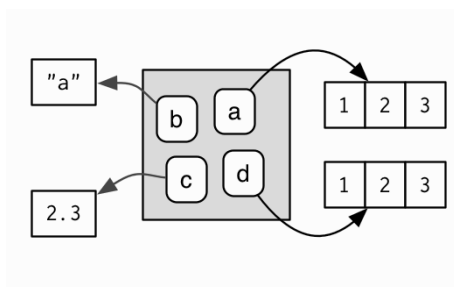
The objects don't live in the environment so multiple names can point to the same object:

```
e$a <- e$d
```



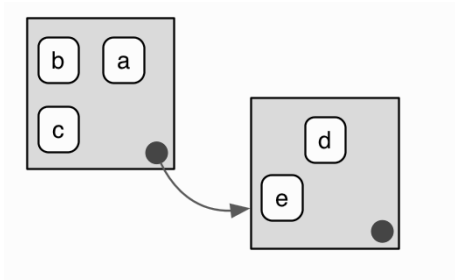
Confusingly they can also point to different objects that have the same value:

```
e$a <- 1:3
```



If an object has no names pointing to it, it gets automatically deleted by the garbage collector. This process is described in more detail in Section 18.2.

Every environment has a parent, another environment. In diagrams, I'll represent the pointer to parent with a small black circle. The parent is used to implement lexical scoping: if a name is not found in an environment, then R will look in its parent (and so on). Only one environment doesn't have a parent: the **empty** environment.



We use the metaphor of a family to refer to environments. The grandparent of an environment is the parent's parent, and the ancestors include all parent environments up to the empty environment. It's rare to talk about the children of an environment because there are no back links: given an environment we have no way to find its children.

Generally, an environment is similar to a list, with four important exceptions:

- Every object in an environment has a unique name.
- The objects in an environment are not ordered (i.e., it doesn't make sense to ask what the first object in an environment is).
- An environment has a parent.
- Environments have reference semantics.

More technically, an environment is made up of two components, the **frame**, which contains the name-object bindings (and behaves much like a named list), and the parent environment. Unfortunately "frame" is used inconsistently in R. For example, `parent.frame()` doesn't give you the parent frame of an environment. Instead, it gives you the *calling* environment. This is discussed in more detail in Section 8.3.4.

There are four special environments:

- The `globalenv()`, or global environment, is the interactive workspace. This is the environment in which you normally work. The parent of the global environment is the last package that you attached with `library()` or `require()`.

- The `baseenv()`, or base environment, is the environment of the base package. Its parent is the empty environment.
- The `emptyenv()`, or empty environment, is the ultimate ancestor of all environments, and the only environment without a parent.
- The `environment()` is the current environment.

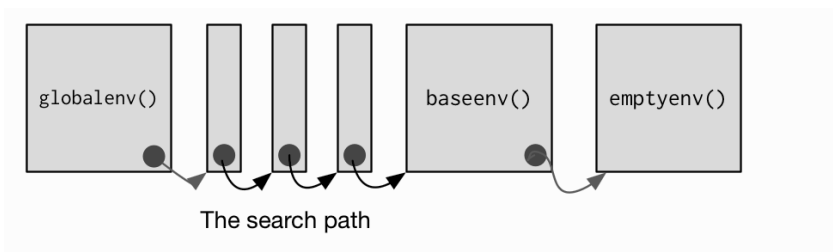
`search()` lists all parents of the global environment. This is called the search path because objects in these environments can be found from the top-level interactive workspace. It contains one environment for each attached package and any other objects that you've `attach()`ed. It also contains a special environment called `Autoloads` which is used to save memory by only loading package objects (like big datasets) when needed.

You can access any environment on the search list using `as.environment()`.

```
search()
#> [1] ".GlobalEnv"          "package:stats"       "package:graphics"
#> [4] "package:grDevices"   "package:utils"       "package:datasets"
#> [7] "package:methods"     "Autoloads"           "package:base"

as.environment("package:stats")
#> <environment: package:stats>
```

`globalenv()`, `baseenv()`, the environments on the search path, and `emptyenv()` are connected as shown below. Each time you load a new package with `library()` it is inserted between the global environment and the package that was previously at the top of the search path.



To create an environment manually, use `new.env()`. You can list the bindings in the environment's frame with `ls()` and see its parent with `parent.env()`.

```
e <- new.env()
# the default parent provided by new.env() is environment from
# which it is called - in this case that's the global environment.
parent.env(e)
#> <environment: R_GlobalEnv>
ls(e)
#> character(0)
```

The easiest way to modify the bindings in an environment is to treat it like a list:

```
e$a <- 1
e$b <- 2
ls(e)
#> [1] "a" "b"
e$a
#> [1] 1
```

By default, `ls()` only shows names that don't begin with `..`. Use `all.names = TRUE` to show all bindings in an environment:

```
e$.a <- 2
ls(e)
#> [1] "a" "b"
ls(e, all.names = TRUE)
#> [1] ".a" "a" "b"
```

Another useful way to view an environment is `ls.str()`. It is more useful than `str()` because it shows each object in the environment. Like `ls()`, it also has an `all.names` argument.

```
str(e)
#> <environment: 0x7fdd1d4cff10>
ls.str(e)
#> a : num 1
#> b : num 2
```

Given a name, you can extract the value to which it is bound with `$`, `[[`, or `get()`:

- `$` and `[[` look only in one environment and return `NULL` if there is no binding associated with the name.

- `get()` uses the regular scoping rules and throws an error if the binding is not found.

```
e$c <- 3
e$c
#> [1] 3
e[["c"]]
#> [1] 3
get("c", envir = e)
#> [1] 3
```

Deleting objects from environments works a little differently from lists. With a list you can remove an entry by setting it to `NULL`. In environments, that will create a new binding to `NULL`. Instead, use `rm()` to remove the binding.

```
e <- new.env()

e$a <- 1
e$a <- NULL
ls(e)
#> [1] "a"

rm("a", envir = e)
ls(e)
#> character(0)
```

You can determine if a binding exists in an environment with `exists()`. Like `get()`, its default behaviour is to follow the regular scoping rules and look in parent environments. If you don't want this behavior, use `inherits = FALSE`:

```
x <- 10
exists("x", envir = e)
#> [1] TRUE
exists("x", envir = e, inherits = FALSE)
#> [1] FALSE
```

To compare environments, you must use `identical()` not `==`:

```
identical(globalenv(), environment())
```

```
#> [1] TRUE
globalenv() == environment()
#> Error: comparison (1) is possible only for atomic and list
#> types
```

8.1.1 Exercises

1. List three ways in which an environment differs from a list.
2. If you don't supply an explicit environment, where do `ls()` and `rm()` look? Where does `<-` make bindings?
3. Using `parent.env()` and a loop (or a recursive function), verify that the ancestors of `globalenv()` include `baseenv()` and `emptyenv()`. Use the same basic idea to implement your own version of `search()`.

8.2 Recursing over environments

Environments form a tree, so it's often convenient to write a recursive function. This section shows you how by applying your new knowledge of environments to understand the helpful `pryr::where()`. Given a name, `where()` finds the environment *where* that name is defined, using R's regular scoping rules:

```
library(pryr)
x <- 5
where("x")
#> <environment: R_GlobalEnv>
where("mean")
#> <environment: base>
```

The definition of `where()` is straightforward. It has two arguments: the name to look for (as a string), and the environment in which to start the search. (We'll learn later why `parent.frame()` is a good default in Section 8.3.4.)

```
where <- function(name, env = parent.frame()) {
  if (identical(env, emptyenv())) {
```

```

# Base case
stop("Can't find ", name, call. = FALSE)

} else if (exists(name, envir = env, inherits = FALSE)) {
  # Success case
  env

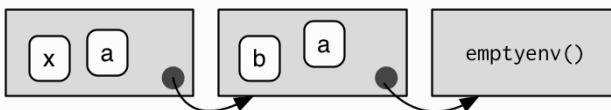
} else {
  # Recursive case
  where(name, parent.env(env))
}
}

```

There are three cases:

- The base case: we've reached the empty environment and haven't found the binding. We can't go any further, so we throw an error.
- The successful case: the name exists in this environment, so we return the environment.
- The recursive case: the name was not found in this environment, so try the parent.

It's easier to see what's going on with an example. Imagine you have two environments as in the following diagram:



- If you're looking for `a`, `where()` will find it in the first environment.
- If you're looking for `b`, it's not in the first environment, so `where()` will look in its parent and find it there.
- If you're looking for `c`, it's not in the first environment, or the second environment, so `where()` reaches the empty environment and throws an error.

It's natural to work with environments recursively, so `where()` provides a useful template. Removing the specifics of `where()` shows the structure more clearly:

```
f <- function(..., env = parent.frame()) {
  if (identical(env, emptyenv())) {
    # base case
  } else if (success) {
    # success case
  } else {
    # recursive case
    f(..., env = parent.env(env))
  }
}
```

Iteration vs. recursion

It's possible to use a loop instead of recursion. This might run slightly faster (because we eliminate some function calls), but I think it's harder to understand. I include it because you might find it easier to see what's happening if you're less familiar with recursive functions.

```
is_empty <- function(x) identical(x, emptyenv())

f2 <- function(..., env = parent.frame()) {
  while(!is_empty(env)) {
    if (success) {
      # success case
      return()
    }
    # inspect parent
    env <- parent.env(env)
  }

  # base case
}
```

8.2.1 Exercises

1. Modify `where()` to find all environments that contain a binding for `name`.
2. Write your own version of `get()` using a function written in the style of `where()`.

3. Write a function called `fget()` that finds only function objects. It should have two arguments, `name` and `env`, and should obey the regular scoping rules for functions: if there's an object with a matching name that's not a function, look in the parent. For an added challenge, also add an `inherits` argument which controls whether the function recurses up the parents or only looks in one environment.
4. Write your own version of `exists(inherits = FALSE)` (Hint: use `ls().`) Write a recursive version that behaves like `exists(inherits = TRUE)`.

8.3 Function environments

Most environments are not created by you with `new.env()` but are created as a consequence of using functions. This section discusses the four types of environments associated with a function: enclosing, binding, execution, and calling.

The **enclosing** environment is the environment where the function was created. Every function has one and only one enclosing environment. For the three other types of environment, there may be 0, 1, or many environments associated with each function:

- Binding a function to a name with `<-` defines a **binding** environment.
- Calling a function creates an ephemeral **execution** environment that stores variables created during execution.
- Every execution environment is associated with a **calling** environment, which tells you where the function was called.

The following sections will explain why each of these environments is important, how to access them, and how you might use them.

8.3.1 The enclosing environment

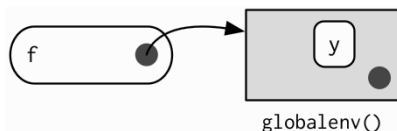
When a function is created, it gains a reference to the environment where it was made. This is the **enclosing environment** and is used for lexical scoping. You can determine the enclosing environment of a function by calling `environment()` with a function as its first argument:

```

y <- 1
f <- function(x) x + y
environment(f)
#> <environment: R_GlobalEnv>

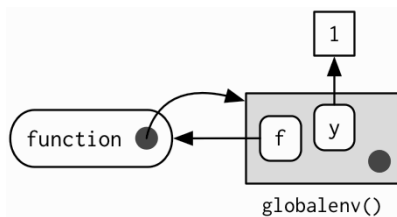
```

In diagrams, I'll depict functions as rounded rectangles. The enclosing environment of a function is given by a small black circle:



8.3.2 Binding environments

The previous diagram is too simple because functions don't have names. Instead, the name of a function is defined by a binding. The binding environments of a function are all the environments which have a binding to it. The following diagram better reflects this relationship because the enclosing environment contains a binding from `f` to the function:

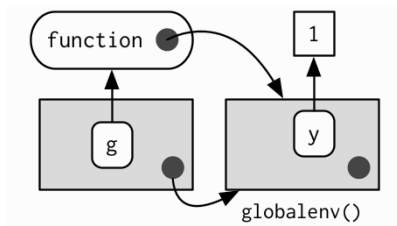


In this case the enclosing and binding environments are the same. They will be different if you assign a function into a different environment:

```

e <- new.env()
e$g <- function() 1

```



The enclosing environment belongs to the function, and never changes, even if the function is moved to a different environment. The enclosing environment determines how the function finds values; the binding environments determine how we find the function.

The distinction between the binding environment and the enclosing environment is important for package namespaces. Package namespaces keep packages independent. For example, if package A uses the base `mean()` function, what happens if package B creates its own `mean()` function? Namespaces ensure that package A continues to use the base `mean()` function, and that package A is not affected by package B (unless explicitly asked for).

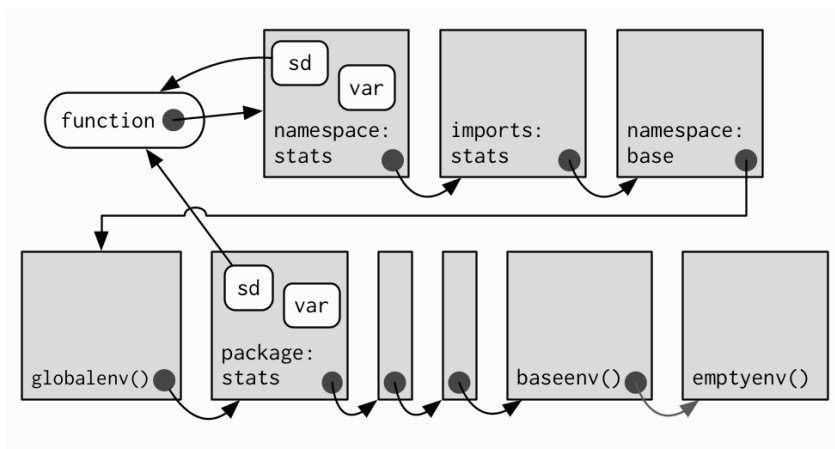
Namespaces are implemented using environments, taking advantage of the fact that functions don't have to live in their enclosing environments. For example, take the base function `sd()`. It's binding and enclosing environments are different:

```
environment(sd)
#> <environment: namespace:stats>
where("sd")
# <environment: package:stats>
```

The definition of `sd()` uses `var()`, but if we make our own version of `var()` it doesn't affect `sd()`:

```
x <- 1:10
sd(x)
#> [1] 3.028
var <- function(x, na.rm = TRUE) 100
sd(x)
#> [1] 3.028
```

This works because every package has two environments associated with it: the *package* environment and the *namespace* environment. The package environment contains every publicly accessible function, and is placed on the search path. The namespace environment contains all functions (including internal functions), and its parent environment is a special imports environment that contains bindings to all the functions that the package needs. Every exported function in a package is bound into the *package* environment, but enclosed by the *namespace* environment. This complicated relationship is illustrated by the following diagram:



When we type `var` into the console, it's found first in the global environment. When `sd()` looks for `var()` it finds it first in its namespace environment so never looks in the `globalenv()`.

8.3.3 Execution environments

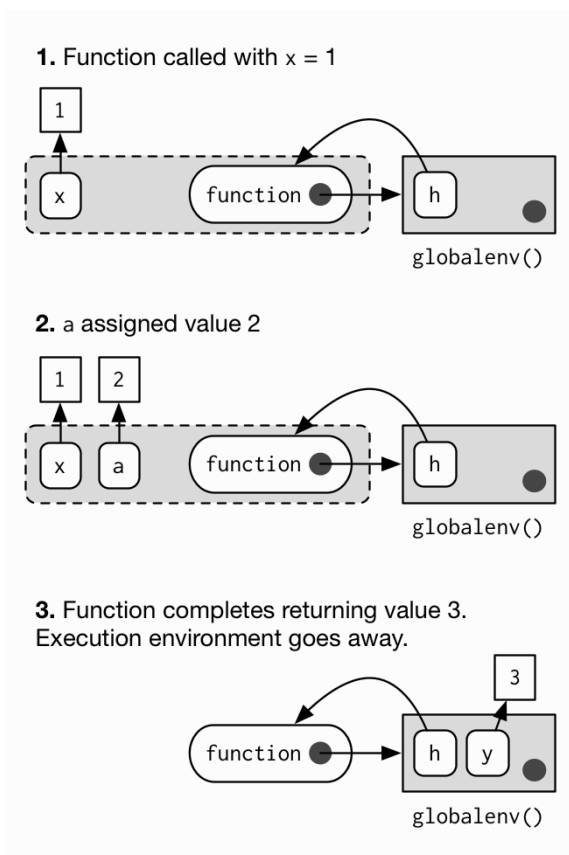
What will the following function return the first time its run? What about the second?

```
g <- function(x) {
  if (!exists("a", inherits = FALSE)) {
    message("Defining a")
    a <- 1
  } else {
    a <- a + 1
  }
  a
}
g(10)
g(10)
```

This function returns the same value every time it is called because of the fresh start principle, described in Section 6.2.3. Each time a function is called, a new environment is created to host execution. The parent of the execution environment is the enclosing environment of the function. Once the function has completed, this environment is thrown away.

Let's depict that graphically with a simpler function. I draw execution environments around the function they belong to with a dotted border.

```
h <- function(x) {
  a <- 2
  x + a
}
y <- h(1)
```

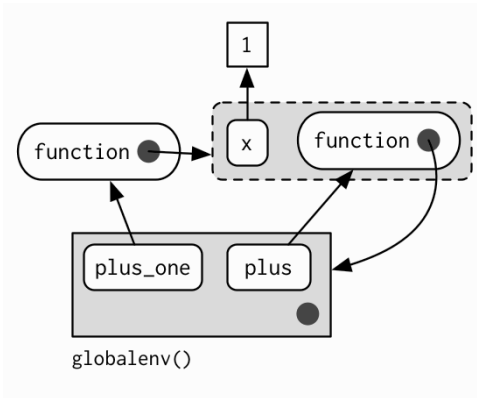


When you create a function inside another function, the enclosing environment of the child function is the execution environment of the parent, and the execution environment is no longer ephemeral. The following example illustrates that idea with a function factory, `plus()`. We use that factory to create a function called `plus_one()`. The enclosing environment of `plus_one()` is the execution environment of `plus()` where `x` is bound to the value 1.

```

plus <- function(x) {
  function(y) x + y
}
plus_one <- plus(1)
identical(parent.env(environment(plus_one)), environment(plus))
#> [1] TRUE

```



You'll learn more about function factories in Chapter 10.

8.3.4 Calling environments

Look at the following code. What do you expect `i()` to return when the code is run?

```

h <- function() {
  x <- 10
  function() {
    x
  }
}
i <- h()
x <- 20
i()

```

The top-level `x` (bound to 20) is a red herring: using the regular scoping rules, `h()` looks first where it is defined and finds that the value associated with `x` is 10. However, it's still meaningful to ask what value `x` is associated with in the environment where `i()` is called: `x` is 10 in the

environment where `h()` is defined, but it is 20 in the environment where `h()` is called.

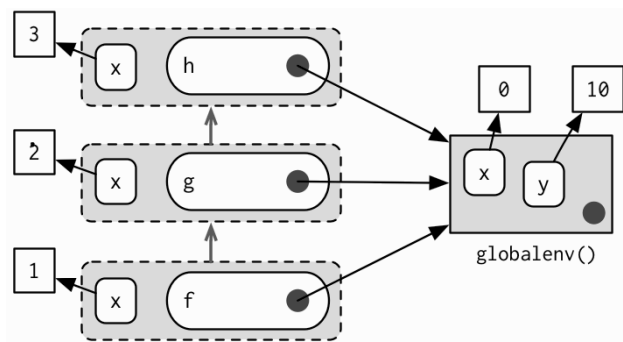
We can access this environment using the unfortunately named `parent.frame()`. This function returns the **environment** where the function was called. We can also use this function to look up the value of names in that environment:

```
f2 <- function() {
  x <- 10
  function() {
    def <- get("x", environment())
    cll <- get("x", parent.frame())
    list(defined = def, called = cll)
  }
}
g2 <- f2()
x <- 20
str(g2())
#> List of 2
#> $ defined: num 10
#> $ called : num 20
```

In more complicated scenarios, there's not just one parent call, but a sequence of calls which lead all the way back to the initiating function, called from the top-level. The following code generates a call stack three levels deep. The open-ended arrows represent the calling environment of each execution environment.

```
x <- 0
y <- 10
f <- function() {
  x <- 1
  g()
}
g <- function() {
  x <- 2
  h()
}
h <- function() {
  x <- 3
  x + y
}
```

```
f()
#> [1] 13
```



Note that each execution environment has two parents: a calling environment and an enclosing environment. R's regular scoping rules only use the enclosing parent; `parent.frame()` allows you to access the calling parent.

Looking up variables in the calling environment rather than in the enclosing environment is called **dynamic scoping**. Few languages implement dynamic scoping (Emacs Lisp is a notable exception (<http://www.gnu.org/software/emacs/emacs-paper.html#SEC15>)). This is because dynamic scoping makes it much harder to reason about how a function operates: not only do you need to know how it was defined, you also need to know in what context it was called. Dynamic scoping is primarily useful for developing functions that aid interactive data analysis. It is one of the topics discussed in Chapter 13.

8.3.5 Exercises

1. List the four environments associated with a function. What does each one do? Why is the distinction between enclosing and binding environments particularly important?
2. Draw a diagram that shows the enclosing environments of this function:

```
f1 <- function(x1) {
  f2 <- function(x2) {
    f3 <- function(x3) {
      x1 + x2 + x3
    }
  }
}
```

```
      f3(3)
    }
  f2(2)
}
f1(1)
```

3. Expand your previous diagram to show function bindings.
4. Expand it again to show the execution and calling environments.
5. Write an enhanced version of `str()` that provides more information about functions. Show where the function was found and what environment it was defined in.

8.4 Binding names to values

Assignment is the act of binding (or rebinding) a name to a value in an environment. It is the counterpart to scoping, the set of rules that determines how to find the value associated with a name. Compared to most languages, R has extremely flexible tools for binding names to values. In fact, you can not only bind values to names, but you can also bind expressions (promises) or even functions, so that every time you access the value associated with a name, you get something different!

You've probably used regular assignment in R thousands of times. Regular assignment creates a binding between a name and an object in the current environment. Names usually consist of letters, digits, `.` and `_`, and can't begin with `_`. If you try to use a name that doesn't follow these rules, you get an error:

```
_abc <- 1
# Error: unexpected input in "_"
```

Reserved words (like `TRUE`, `NULL`, `if`, and `function`) follow the rules but are reserved by R for other purposes:

```
if <- 10
#> Error: unexpected assignment in "if <-"
```

A complete list of reserved words can be found in `?Reserved`.

It's possible to override the usual rules and use a name with any sequence of characters by surrounding the name with backticks:

```
`a + b` <- 3
`:)` <- "smile"
` ` <- "spaces"
ls()
# [1] "      " "   ")" "a + b"
`:)`
# [1] "smile"
```

Quotes

You can also create non-syntactic bindings using single and double quotes instead of backticks, but I don't recommend it. The ability to use strings on the left hand side of the assignment arrow is a historical artefact, used before R supported backticks.

The regular assignment arrow, `<-`, always creates a variable in the current environment. The deep assignment arrow, `<<-`, never creates a variable in the current environment, but instead modifies an existing variable found by walking up the parent environments. You can also do deep binding with `assign(): name <<- value` is equivalent to `assign("name", value, inherits = TRUE)`.

```
x <- 0
f <- function() {
  x <<- 1
}
f()
x
#> [1] 1
```

If `<<-` doesn't find an existing variable, it will create one in the global environment. This is usually undesirable, because global variables introduce non-obvious dependencies between functions. `<<-` is most often used in conjunction with a closure, as described in Section 10.3.

There are two other special types of binding, delayed and active:

- Rather than assigning the result of an expression immediately, a **delayed binding** creates and stores a promise to evaluate the expression when needed. We can create delayed bindings with the special assignment operator `%<d-%`, provided by the `pryr` package.

```
library(pryr)
system.time(b %<d-% {Sys.sleep(1); 1})
#>    user  system elapsed
#> 0.000    0.000    0.001
system.time(b)
#>    user  system elapsed
#> 0.000    0.000    1.001
```

`%<d-%` is a wrapper around the base `delayedAssign()` function, which you may need to use directly if you need more control. Delayed bindings are used to implement `autoload()`, which makes R behave as if the package data is in memory, even though it's only loaded from disk when you ask for it.

- **Active** are not bound to a constant object. Instead, they're re-computed every time they're accessed:

```
x %<a-% runif(1)
x
#> [1] 0.4424
x
#> [1] 0.8112
rm(x)
```

`%<a-%` is a wrapper for the base function `makeActiveBinding()`. You may want to use this function directly if you want more control. Active bindings are used to implement reference class fields.

8.4.1 Exercises

1. What does this function do? How does it differ from `<<-` and why might you prefer it?

```
rebind <- function(name, value, env = parent.frame()) {
  if (identical(env, emptyenv())) {
    stop("Can't find ", name, call. = FALSE)
  } else if (exists(name, envir = env, inherits = FALSE)) {
    assign(name, value, envir = env)
  } else {
```

```

      rebind(name, value, parent.env(env))
    }
  }
  rebind("a", 10)
  #> Error: Can't find a
  a <- 5
  rebind("a", 10)
  a
  #> [1] 10

```

2. Create a version of `assign()` that will only bind new names, never re-bind old names. Some programming languages only do this, and are known as single assignment languages ([http://en.wikipedia.org/wiki/Assignment_\(computer_science\)#Single_assignment](http://en.wikipedia.org/wiki/Assignment_(computer_science)#Single_assignment)).
3. Write an assignment function that can do active, delayed, and locked bindings. What might you call it? What arguments should it take? Can you guess which sort of assignment it should do based on the input?

8.5 Explicit environments

As well as powering scoping, environments are also useful data structures in their own right because they have **reference semantics**. Unlike most objects in R, when you modify an environment, it does not make a copy. For example, look at this `modify()` function.

```

modify <- function(x) {
  x$a <- 2
  invisible()
}

```

If you apply it to a list, the original list is not changed because modifying a list actually creates and modifies a copy.

```

x_l <- list()
x_l$a <- 1
modify(x_l)

```



```
x_l$a  
#> [1] 1
```

However, if you apply it to an environment, the original environment *is* modified:

```
x_e <- new.env()  
x_e$a <- 1  
modify(x_e)  
x_e$a  
#> [1] 2
```

Just as you can use a list to pass data between functions, you can also use an environment. When creating your own environment, note that you should set its parent environment to be the empty environment. This ensures you don't accidentally inherit objects from somewhere else:

```
x <- 1  
e1 <- new.env()  
get("x", envir = e1)  
#> [1] 1  
  
e2 <- new.env(parent = emptyenv())  
get("x", envir = e2)  
#> Error: object 'x' not found
```

Environments are data structures useful for solving three common problems:

- Avoiding copies of large data.
- Managing state within a package.
- Efficiently looking up values from names.

These are described in turn below.

8.5.1 Avoiding copies

Since environments have reference semantics, you'll never accidentally create a copy. This makes it a useful vessel for large objects. It's a common technique for bioconductor packages which often have to manage

large genomic objects. Changes to R 3.1.0 have made this use substantially less important because modifying a list no longer makes a deep copy. Previously, modifying a single element of a list would cause every element to be copied, an expensive operation if some elements are large. Now, modifying a list efficiently reuses existing vectors, saving much time.

8.5.2 Package state

Explicit environments are useful in packages because they allow you to maintain state across function calls. Normally, objects in a package are locked, so you can't modify them directly. Instead, you can do something like this:

```
my_env <- new.env(parent = emptyenv())
my_env$a <- 1

get_a <- function() {
  my_env$a
}
set_a <- function(value) {
  old <- my_env$a
  my_env$a <- value
  invisible(old)
}
```

Returning the old value from setter functions is a good pattern because it makes it easier to reset the previous value in conjunction with `on.exit()` (see more in Section 6.6.1).

8.5.3 As a hashmap

A hashmap is a data structure that takes constant, $O(1)$, time to find an object based on its name. Environments provide this behaviour by default, so can be used to simulate a hashmap. See the CRAN package `hash` for a complete development of this idea.

8.6 Quiz answers

1. There are four ways: every object in an environment must have a name; order doesn't matter; environments have parents; environments have reference semantics.
2. The parent of the global environment is the last package that you loaded. The only environment that doesn't have a parent is the empty environment.
3. The enclosing environment of a function is the environment where it was created. It determines where a function looks for variables.
4. Use `parent.frame()`.
5. `<-` always creates a binding in the current environment; `<<-` rebinds an existing name in a parent of the current environment.

9

Debugging, condition handling, and defensive programming

What happens when something goes wrong with your R code? What do you do? What tools do you have to address the problem? This chapter will teach you how to fix unanticipated problems (debugging), show you how functions can communicate problems and how you can take action based on those communications (condition handling), and teach you how to avoid common problems before they occur (defensive programming).

Debugging is the art and science of fixing unexpected problems in your code. In this section you'll learn the tools and techniques that help you get to the root cause of an error. You'll learn general strategies for debugging, useful R functions like `traceback()` and `browser()`, and interactive tools in RStudio.

Not all problems are unexpected. When writing a function, you can often anticipate potential problems (like a non-existent file or the wrong type of input). Communicating these problems to the user is the job of **conditions**: errors, warnings, and messages.

- Fatal errors are raised by `stop()` and force all execution to terminate. Errors are used when there is no way for a function to continue.
- Warnings are generated by `warning()` and are used to display potential problems, such as when some elements of a vectorised input are invalid, like `log(-1:2)`.
- Messages are generated by `message()` and are used to give informative output in a way that can easily be suppressed by the user (`?suppressMessages()`). I often use messages to let the user know what value the function has chosen for an important missing argument.

Conditions are usually displayed prominently, in a bold font or coloured red depending on your R interface. You can tell them apart because errors always start with “Error” and warnings with “Warning message”.

Function authors can also communicate with their users with `print()` or `cat()`, but I think that's a bad idea because it's hard to capture and selectively ignore this sort of output. Printed output is not a condition, so you can't use any of the useful condition handling tools you'll learn about below.

Condition handling tools, like `withCallingHandlers()`, `tryCatch()`, and `try()` allow you to take specific actions when a condition occurs. For example, if you're fitting many models, you might want to continue fitting the others even if one fails to converge. R offers an exceptionally powerful condition handling system based on ideas from Common Lisp, but it's currently not very well documented or often used. This chapter will introduce you to the most important basics, but if you want to learn more, I recommend the following two sources:

- *A prototype of a condition system for R* (<http://homepage.stat.uiowa.edu/~luke/R/exceptions/simpcond.html>) by Robert Gentleman and Luke Tierney. This describes an early version of R's condition system. While the implementation has changed somewhat since this document was written, it provides a good overview of how the pieces fit together, and some motivation for its design.
- *Beyond Exception Handling: Conditions and Restarts* (<http://www.gigamonkeys.com/book/beyond-exception-handling-conditions-and-restarts.html>) by Peter Seibel. This describes exception handling in Lisp, which happens to be very similar to R's approach. It provides useful motivation and more sophisticated examples. I have provided an R translation of the chapter at <http://adv-r.had.co.nz/beyond-exception-handling.html>.

The chapter concludes with a discussion of “defensive” programming: ways to avoid common errors before they occur. In the short run you'll spend more time writing code, but in the long run you'll save time because error messages will be more informative and will let you narrow in on the root cause more quickly. The basic principle of defensive programming is to “fail fast”, to raise an error as soon as something goes wrong. In R, this takes three particular forms: checking that inputs are correct, avoiding non-standard evaluation, and avoiding functions that can return different types of output.

Quiz

Want to skip this chapter? Go for it, if you can answer the questions below. Find the answers at the end of the chapter in Section 9.5.

1. How can you find out where an error occurred?
2. What does `browser()` do? List the five useful single-key commands that you can use inside of a `browser()` environment.
3. What function do you use to ignore errors in block of code?
4. Why might you want to create an error with a custom S3 class?

Outline

1. Section 9.1 outlines a general approach for finding and resolving bugs.
2. Section 9.2 introduces you to the R functions and Rstudio features that help you locate exactly where an error occurred.
3. Section 9.3 shows you how you can catch conditions (errors, warnings, and messages) in your own code. This allows you to create code that's both more robust and more informative in the presence of errors.
4. Section 9.4 introduces you to some important techniques for defensive programming, techniques that help prevent bugs from occurring in the first place.

9.1 Debugging techniques

“Finding your bug is a process of confirming the many things that you believe are true — until you find one which is not true.”

—Norm Matloff

Debugging code is challenging. Many bugs are subtle and hard to find. Indeed, if a bug was obvious, you probably would've been able to avoid it in the first place. While it's true that with a good technique, you can productively debug a problem with just `print()`, there are times when additional help would be welcome. In this section, we'll discuss some useful tools, which R and RStudio provide, and outline a general procedure for debugging.

While the procedure below is by no means foolproof, it will hopefully help you to organise your thoughts when debugging. There are four steps:

1. Realise that you have a bug

If you're reading this chapter, you've probably already completed this step. It is a surprisingly important one: you can't fix a bug until you know it exists. This is one reason why automated test suites are important when producing high-quality code. Unfortunately, automated testing is outside the scope of this book, but you can read more about it at <http://r-pkgs.had.co.nz/tests.html>.

2. Make it repeatable

Once you've determined you have a bug, you need to be able to reproduce it on command. Without this, it becomes extremely difficult to isolate its cause and to confirm that you've successfully fixed it.

Generally, you will start with a big block of code that you know causes the error and then slowly whittle it down to get to the smallest possible snippet that still causes the error. Binary search is particularly useful for this. To do a binary search, you repeatedly remove half of the code until you find the bug. This is fast because, with each step, you reduce the amount of code to look through by half.

If it takes a long time to generate the bug, it's also worthwhile to figure out how to generate it faster. The quicker you can do this, the quicker you can figure out the cause.

As you work on creating a minimal example, you'll also discover similar inputs that don't trigger the bug. Make note of them: they will be helpful when diagnosing the cause of the bug.

If you're using automated testing, this is also a good time to create an automated test case. If your existing test coverage is low, take the opportunity to add some nearby tests to ensure that existing good behaviour is preserved. This reduces the chances of creating a new bug.

3. Figure out where it is

If you're lucky, one of the tools in the following section will help you to quickly identify the line of code that's causing the bug. Usually, however, you'll have to think a bit more about the problem. It's a great idea to adopt the scientific method. Generate hypotheses, design experiments to test them, and record your results. This may seem like a lot of work, but a systematic approach will end up saving you time. I often

waste a lot of time relying on my intuition to solve a bug (“oh, it must be an off-by-one error, so I’ll just subtract 1 here”), when I would have been better off taking a systematic approach.

4. Fix it and test it

Once you’ve found the bug, you need to figure out how to fix it and to check that the fix actually worked. Again, it’s very useful to have automated tests in place. Not only does this help to ensure that you’ve actually fixed the bug, it also helps to ensure you haven’t introduced any new bugs in the process. In the absence of automated tests, make sure to carefully record the correct output, and check against the inputs that previously failed.

9.2 Debugging tools

To implement a strategy of debugging, you’ll need tools. In this section, you’ll learn about the tools provided by R and the RStudio IDE. RStudio’s integrated debugging support makes life easier by exposing existing R tools in a user friendly way. I’ll show you both the R and RStudio ways so that you can work with whatever environment you use. You may also want to refer to the official RStudio debugging documentation (<http://www.rstudio.com/ide/docs/debugging/overview>) which always reflects the tools in the latest version of RStudio.

There are three key debugging tools:

- RStudio’s error inspector and `traceback()` which list the sequence of calls that lead to the error.
- RStudio’s “Rerun with Debug” tool and `options(error = browser)` which open an interactive session where the error occurred.
- RStudio’s breakpoints and `browser()` which open an interactive session at an arbitrary location in the code.

I’ll explain each tool in more detail below.

You shouldn’t need to use these tools when writing new functions. If you find yourself using them frequently with new code, you may want

to reconsider your approach. Instead of trying to write one big function all at once, work interactively on small pieces. If you start small, you can quickly identify why something doesn't work. But if you start large, you may end up struggling to identify the source of the problem.

9.2.1 Determining the sequence of calls

The first tool is the **call stack**, the sequence of calls that lead up to an error. Here's a simple example: you can see that `f()` calls `g()` calls `h()` calls `i()` which adds together a number and a string creating a error:

```
f <- function(a) g(a)
g <- function(b) h(b)
h <- function(c) i(c)
i <- function(d) "a" + d
f(10)
```

When we run this code in Rstudio we see:

```
> f(10)
```

Error in "a" + d : non-numeric argument to binary operator

[Show Traceback](#)
[Rerun with Debug](#)

Two options appear to the right of the error message: “Show Traceback” and “Rerun with Debug”. If you click “Show traceback” you see:

```
> f(10)
```

Error in "a" + d : non-numeric argument to binary operator

[Hide Traceback](#)
[Rerun with Debug](#)

```

4 i(c) at exceptions-example.R#3
3 h(b) at exceptions-example.R#2
2 g(a) at exceptions-example.R#1
1 f(10)
```

If you're not using Rstudio, you can use `traceback()` to get the same information:


```
traceback()
# 4: i(c) at exceptions-example.R#3
# 3: h(b) at exceptions-example.R#2
# 2: g(a) at exceptions-example.R#1
# 1: f(10)
```



Read the call stack from bottom to top: the initial call is `f()`, which calls `g()`, then `h()`, then `i()`, which triggers the error. If you're calling code that you `source()`d into R, the traceback will also display the location of the function, in the form `filename.r#linenumber`. These are clickable in Rstudio, and will take you to the corresponding line of code in the editor.

Sometimes this is enough information to let you track down the error and fix it. However, it's usually not. `traceback()` shows you where the error occurred, but not why. The next useful tool is the interactive debugger, which allows you to pause execution of a function and interactively explore its state.

9.2.2 Browsing on error

The easiest way to enter the interactive debugger is through RStudio's "Rerun with Debug" tool. This reruns the command that created the error, pausing execution where the error occurred. You're now in an interactive state inside the function, and you can interact with any object defined there. You'll see the corresponding code in the editor (with the statement that will be run next highlighted), objects in the current environment in the "Environment" pane, the call stack in a "Traceback" pane, and you can run arbitrary R code in the console.

As well as any regular R function, there are a few special commands you can use in debug mode. You can access them either with the Rstudio toolbar () or with the keyboard:

- Next, `n`: executes the next step in the function. Be careful if you have a variable named `n`; to print it you'll need to do `print(n)`.
- Step into,  or `s`: works like next, but if the next step is a function, it will step into that function so you can work through each line.
- Finish,  or `f`: finishes execution of the current loop or function.
- Continue, `c`: leaves interactive debugging and continues regular execution of the function. This is useful if you've fixed the bad state and want to check that the function proceeds correctly.
- Stop, `Q`: stops debugging, terminates the function, and returns to the global workspace. Use this once you've figured out where the problem is, and you're ready to fix it and reload the code.

There are two other slightly less useful commands that aren't available in the toolbar:

- `Enter`: repeats the previous command. I find this too easy to activate accidentally, so I turn it off using `options(browserNLdisabled = TRUE)`.
- `where`: prints stack trace of active calls (the interactive equivalent of `traceback`).

To enter this style of debugging outside of RStudio, you can use the `error` option which specifies a function to run when an error occurs. The function most similar to Rstudio's debug is `browser()`: this will start an interactive console in the environment where the error occurred. Use `options(error = browser)` to turn it on, re-run the previous command, then use `options(error = NULL)` to return to the default error behaviour. You could automate this with the `browseOnce()` function as defined below:

```
browseOnce <- function() {
  old <- getOption("error")
  function() {
    options(error = old)
    browser()
  }
}
options(error = browseOnce())

f <- function() stop("!")
# Enters browser
f()
# Runs normally
f()
```

(You'll learn more about functions that return functions in Chapter 10.)

There are two other useful functions that you can use with the `error` option:

- `recover` is a step up from `browser`, as it allows you to enter the environment of any of the calls in the call stack. This is useful because often the root cause of the error is a number of calls back.

- `dump.frames` is an equivalent to `recover` for non-interactive code. It creates a `last.dump.rda` file in the current working directory. Then, in a later interactive R session, you load that file, and use `debugger()` to enter an interactive debugger with the same interface as `recover()`. This allows interactive debugging of batch code.

```
# In batch R process ----
dump_and_quit <- function() {
  # Save debugging info to file last.dump.rda
  dump.frames(to.file = TRUE)
  # Quit R with error status
  q(status = 1)
}
options(error = dump_and_quit)

# In a later interactive session ----
load("last.dump.rda")
debugger()
```

To reset error behaviour to the default, use `options(error = NULL)`. Then errors will print a message and abort function execution.

9.2.3 Browsing arbitrary code

As well as entering an interactive console on error, you can enter it at an arbitrary code location by using either an Rstudio breakpoint or `browser()`. You can set a breakpoint in Rstudio by clicking to the left of the line number, or pressing `Shift + F9`. Equivalently, add `browser()` where you want execution to pause. Breakpoints behave similarly to `browser()` but they are easier to set (one click instead of nine key presses), and you don't run the risk of accidentally including a `browser()` statement in your source code. There are two small downsides to breakpoints:

- There are a few unusual situations in which breakpoints will not work: read breakpoint troubleshooting (<http://www.rstudio.com/ide/docs/debugging/breakpoint-troubleshooting>) for more details.
- RStudio currently does not support conditional breakpoints, whereas you can always put `browser()` inside an `if` statement.

As well as adding `browser()` yourself, there are two other functions that will add it to code:

- `debug()` inserts a browser statement in the first line of the specified function. `undebug()` removes it. Alternatively, you can use `debugonce()` to browse only on the next run.
- `utils::setBreakpoint()` works similarly, but instead of taking a function name, it takes a file name and line number and finds the appropriate function for you.

These two functions are both special cases of `trace()`, which inserts arbitrary code at any position in an existing function. `trace()` is occasionally useful when you're debugging code that you don't have the source for. To remove tracing from a function, use `untrace()`. You can only perform one trace per function, but that one trace can call multiple functions.

9.2.4 The call stack: `traceback()`, `where`, and `recover()`

Unfortunately the call stacks printed by `traceback()`, `browser() + where`, and `recover()` are not consistent. The following table shows how the call stacks from a simple nested set of calls are displayed by the three tools.

| <code>traceback()</code> | <code>where</code> | <code>recover()</code> |
|-------------------------------|-------------------------------------|------------------------|
| 4: <code>stop("Error")</code> | where 1: <code>stop("Error")</code> | 1: <code>f()</code> |
| 3: <code>h(x)</code> | where 2: <code>h(x)</code> | 2: <code>g(x)</code> |
| 2: <code>g(x)</code> | where 3: <code>g(x)</code> | 3: <code>h(x)</code> |
| 1: <code>f()</code> | where 4: <code>f()</code> | |

Note that numbering is different between `traceback()` and `where`, and that `recover()` displays calls in the opposite order, and omits the call to `stop()`. RStudio displays calls in the same order as `traceback()` but omits the numbers.

9.2.5 Other types of failure

There are other ways for a function to fail apart from throwing an error or returning an incorrect result.

- A function may generate an unexpected warning. The easiest way to

track down warnings is to convert them into errors with `options(warn = 2)` and use the regular debugging tools. When you do this you'll see some extra calls in the call stack, like `doWithOneRestart()`, `withOneRestart()`, `withRestarts()`, and `.signalSimpleWarning()`. Ignore these: they are internal functions used to turn warnings into errors.

- A function may generate an unexpected message. There's no built-in tool to help solve this problem, but it's possible to create one:

```
message2error <- function(code) {
  withCallingHandlers(code, message = function(e) stop(e))
}

f <- function() g()
g <- function() message("Hi!")
g()
# Error in message("Hi!"): Hi!
message2error(g())
traceback()
# 10: stop(e) at #2
# 9: (function (e) stop(e))(list(message = "Hi!\n",
#      call = message("Hi!")))
# 8: signalCondition(cond)
# 7: doWithOneRestart(return(expr), restart)
# 6: withOneRestart(expr, restarts[[1L]])
# 5: withRestarts()
# 4: message("Hi!") at #1
# 3: g()
# 2: withCallingHandlers(code, message = function(e) stop(e))
#      at #2
# 1: message2error(g())
```

As with warnings, you'll need to ignore some of the calls on the traceback (i.e., the first two and the last seven).

- A function might never return. This is particularly hard to debug automatically, but sometimes terminating the function and looking at the call stack is informative. Otherwise, use the basic debugging strategies described above.
- The worst scenario is that your code might crash R completely, leaving you with no way to interactively debug your code. This indicates a bug in underlying C code. This is hard to debug. Sometimes an interactive

debugger, like `gdb`, can be useful, but describing how to use it is beyond the scope of this book.

If the crash is caused by base R code, post a reproducible example to R-help. If it's in a package, contact the package maintainer. If it's your own C or C++ code, you'll need to use numerous `print()` statements to narrow down the location of the bug, and then you'll need to use many more print statements to figure out which data structure doesn't have the properties that you expect.

9.3 Condition handling

Unexpected errors require interactive debugging to figure out what went wrong. Some errors, however, are expected, and you want to handle them automatically. In R, expected errors crop up most frequently when you're fitting many models to different datasets, such as bootstrap replicates. Sometimes the model might fail to fit and throw an error, but you don't want to stop everything. Instead, you want to fit as many models as possible and then perform diagnostics after the fact.

In R, there are three tools for handling conditions (including errors) programmatically:

- `try()` gives you the ability to continue execution even when an error occurs.
- `tryCatch()` lets you specify **handler** functions that control what happens when a condition is signalled.
- `withCallingHandlers()` is a variant of `tryCatch()` that runs its handlers in a different context. It's rarely needed, but is useful to be aware of.

The following sections describe these tools in more detail.

9.3.1 Ignore errors with `try`

`try()` allows execution to continue even after an error has occurred. For example, normally if you run a function that throws an error, it terminates immediately and doesn't return a value:


```
f1 <- function(x) {  
  log(x)  
  10  
}  
f1("x")  
#> Error: non-numeric argument to mathematical function
```

However, if you wrap the statement that creates the error in `try()`, the error message will be printed but execution will continue:

```
f2 <- function(x) {  
  try(log(x))  
  10  
}  
f2("a")  
#> Error in log(x) : non-numeric argument to mathematical function  
#> [1] 10
```

You can suppress the message with `try(..., silent = TRUE)`.

To pass larger blocks of code to `try()`, wrap them in `{}`:

```
try({  
  a <- 1  
  b <- "x"  
  a + b  
})
```

You can also capture the output of the `try()` function. If successful, it will be the last result evaluated in the block (just like a function). If unsuccessful it will be an (invisible) object of class “try-error”:

```
success <- try(1 + 2)  
failure <- try("a" + "b")  
class(success)  
#> [1] "numeric"  
class(failure)  
#> [1] "try-error"
```

`try()` is particularly useful when you’re applying a function to multiple elements in a list:

```
elements <- list(1:10, c(-1, 10), c(T, F), letters)
results <- lapply(elements, log)
#> Warning: NaNs produced
#> Error: non-numeric argument to mathematical function
results <- lapply(elements, function(x) try(log(x)))
#> Warning: NaNs produced
```

There isn't a built-in function to test for the `try-error` class, so we'll define one. Then you can easily find the locations of errors with `sapply()` (as discussed in Chapter 11), and extract the successes or look at the inputs that lead to failures.

```
is.error <- function(x) inherits(x, "try-error")
succeeded <- !sapply(results, is.error)

# look at successful results
str(results[succeeded])
#> List of 3
#> $ : num [1:10] 0 0.693 1.099 1.386 1.609 ...
#> $ : num [1:2] NaN 2.3
#> $ : num [1:2] 0 -Inf

# look at inputs that failed
str(elements[!succeeded])
#> List of 1
#> $ : chr [1:26] "a" "b" "c" "d" ...
```

Another useful `try()` idiom is using a default value if an expression fails. Simply assign the default value outside the `try` block, and then run the risky code:

```
default <- NULL
try(default <- read.csv("possibly-bad-input.csv"), silent = TRUE)
```

There is also `plyr::failwith()`, which makes this strategy even easier to implement. See Section 12.2 for more details.

9.3.2 Handle conditions with `tryCatch()`

`tryCatch()` is a general tool for handling conditions: in addition to errors, you can take different actions for warnings, messages, and interrupts.

You've seen errors (made by `stop()`), warnings (`warning()`) and messages (`message()`) before, but interrupts are new. They can't be generated directly by the programmer, but are raised when the user attempts to terminate execution by pressing Ctrl + Break, Escape, or Ctrl + C (depending on the platform).

With `tryCatch()` you map conditions to **handlers**, named functions that are called with the condition as an input. If a condition is signalled, `tryCatch()` will call the first handler whose name matches one of the classes of the condition. The only useful built-in names are `error`, `warning`, `message`, `interrupt`, and the catch-all condition. A handler function can do anything, but typically it will either return a value or create a more informative error message. For example, the `show_condition()` function below sets up handlers that return the type of condition signalled:

```
show_condition <- function(code) {
  tryCatch(code,
    error = function(c) "error",
    warning = function(c) "warning",
    message = function(c) "message"
  )
}
show_condition(stop("!"))
#> [1] "error"
show_condition(warning("?!"))
#> [1] "warning"
show_condition(message("?"))
#> [1] "message"

# If no condition is captured, tryCatch returns the
# value of the input
show_condition(10)
#> [1] 10
```

You can use `tryCatch()` to implement `try()`. A simple implementation is shown below. `base::try()` is more complicated in order to make the error message look more like what you'd see if `tryCatch()` wasn't used. Note the use of `conditionMessage()` to extract the message associated with the original error.

```
try2 <- function(code, silent = FALSE) {
  tryCatch(code, error = function(c) {
```

```

    msg <- conditionMessage(c)
    if (!silent) message(c)
    invisible(structure(msg, class = "try-error"))
  })
}

try2(1)
#> [1] 1
try2(stop("Hi"))
try2(stop("Hi"), silent = TRUE)

```

As well as returning default values when a condition is signalled, handlers can be used to make more informative error messages. For example, by modifying the message stored in the error condition object, the following function wraps `read.csv()` to add the file name to any errors:

```

read.csv2 <- function(file, ...) {
  tryCatch(read.csv(file, ...), error = function(c) {
    c$message <- paste0(c$message, " (in ", file, ")")
    stop(c)
  })
}
read.csv("code/dummy.csv")
#> Error: cannot open the connection
read.csv2("code/dummy.csv")
#> Error: cannot open the connection (in code/dummy.csv)

```

Catching interrupts can be useful if you want to take special action when the user tries to abort running code. But be careful, it's easy to create a loop that you can never escape (unless you kill R)!

```

# Don't let the user interrupt the code
i <- 1
while(i < 3) {
  tryCatch({
    Sys.sleep(0.5)
    message("Try to escape")
  }, interrupt = function(x) {
    message("Try again!")
    i <- i + 1
  })
}

```

`tryCatch()` has one other argument: `finally`. It specifies a block of code (not a function) to run regardless of whether the initial expression succeeds or fails. This can be useful for clean up (e.g., deleting files, closing connections). This is functionally equivalent to using `on.exit()` but it can wrap smaller chunks of code than an entire function.

9.3.3 `withCallingHandlers()`

An alternative to `tryCatch()` is `withCallingHandlers()`. There are two main differences between these functions:

- The return value of `tryCatch()` handlers is returned by `tryCatch()`, whereas the return value of `withCallingHandlers()` handlers is ignored:

```
f <- function() stop("!")
tryCatch(f(), error = function(e) 1)
#> [1] 1
withCallingHandlers(f(), error = function(e) 1)
#> Error: !
```

- The handlers in `withCallingHandlers()` are called in the context of the call that generated the condition whereas the handlers in `tryCatch()` are called in the context of `tryCatch()`. This is shown here with `sys.calls()`, which is the run-time equivalent of `traceback()` — it lists all calls leading to the current function.

```
f <- function() g()
g <- function() h()
h <- function() stop("!")

tryCatch(f(), error = function(e) print(sys.calls()))
# [[1]] tryCatch(f(), error = function(e) print(sys.calls()))
# [[2]] tryCatchList(expr, classes, parentenv, handlers)
# [[3]] tryCatchOne(expr, names, parentenv, handlers[[1L]])
# [[4]] value[[3L]](cond)

withCallingHandlers(f(), error = function(e) print(sys.calls()))
# [[1]] withCallingHandlers(f(),
#   error = function(e) print(sys.calls()))
# [[2]] f()
# [[3]] g()
# [[4]] h()
```

```
# [[5]] stop("!")
# [[6]] .handleSimpleError(
#   function (e) print(sys.calls()), "!", quote(h()))
# [[7]] h(simpleError(msg, call))
```

This also affects the order in which `on.exit()` is called.

These subtle differences are rarely useful, except when you're trying to capture exactly what went wrong and pass it on to another function. For most purposes, you should never need to use `withCallingHandlers()`.

9.3.4 Custom signal classes

One of the challenges of error handling in R is that most functions just call `stop()` with a string. That means if you want to figure out if a particular error occurred, you have to look at the text of the error message. This is error prone, not only because the text of the error might change over time, but also because many error messages are translated, so the message might be completely different to what you expect.

R has a little known and little used feature to solve this problem. Conditions are S3 classes, so you can define your own classes if you want to distinguish different types of error. Each condition signalling function, `stop()`, `warning()`, and `message()`, can be given either a list of strings, or a custom S3 condition object. Custom condition objects are not used very often, but are very useful because they make it possible for the user to respond to different errors in different ways. For example, “expected” errors (like a model failing to converge for some input datasets) can be silently ignored, while unexpected errors (like no disk space available) can be propagated to the user.

R doesn't come with a built-in constructor function for conditions, but we can easily add one. Conditions must contain `message` and `call` components, and may contain other useful components. When creating a new condition, it should always inherit from `condition` and one of `error`, `warning`, or `message`.

```
condition <- function(subclass, message, call = sys.call(-1), ...) {
  structure(
    class = c(subclass, "condition"),
    list(message = message, call = call),
    ...
  )
}
```

```

}
is.condition <- function(x) inherits(x, "condition")

```

You can signal an arbitrary condition with `signalCondition()`, but nothing will happen unless you've instantiated a custom signal handler (with `tryCatch()` or `withCallingHandlers()`). Instead, use `stop()`, `warning()`, or `message()` as appropriate to trigger the usual handling. R won't complain if the class of your condition doesn't match the function, but you should avoid this in real code.

```

c <- condition(c("my_error", "error"), "This is an error")
signalCondition(c)
# NULL
stop(c)
# Error: This is an error
warning(c)
# Warning message: This is an error
message(c)
# This is an error

```

You can then use `tryCatch()` to take different actions for different types of errors. In this example we make a convenient `custom_stop()` function that allows us to signal error conditions with arbitrary classes. In a real application, it would be better to have individual S3 constructor functions that you could document, describing the error classes in more detail.

```

custom_stop <- function(subclass, message, call = sys.call(-1),
                        ...) {
  c <- condition(c(subclass, "error"), message, call = call, ...)
  stop(c)
}

my_log <- function(x) {
  if (!is.numeric(x))
    custom_stop("invalid_class", "my_log() needs numeric input")
  if (any(x < 0))
    custom_stop("invalid_value", "my_log() needs positive inputs")

  log(x)
}
tryCatch(

```

```

my_log("a"),
invalid_class = function(c) "class",
invalid_value = function(c) "value"
)
#> [1] "class"

```

Note that when using `tryCatch()` with multiple handlers and custom classes, the first handler to match any class in the signal's class hierarchy is called, not the best match. For this reason, you need to make sure to put the most specific handlers first:

```

tryCatch(customStop("my_error", "!"),
  error = function(c) "error",
  my_error = function(c) "my_error"
)
#> [1] "error"
tryCatch(custom_stop("my_error", "!"),
  my_error = function(c) "my_error",
  error = function(c) "error"
)
#> [1] "my_error"

```

9.3.5 Exercises

- Compare the following two implementations of `message2error()`. What is the main advantage of `withCallingHandlers()` in this scenario? (Hint: look carefully at the traceback.)

```

message2error <- function(code) {
  withCallingHandlers(code, message = function(e) stop(e))
}
message2error <- function(code) {
  tryCatch(code, message = function(e) stop(e))
}

```

9.4 Defensive programming

Defensive programming is the art of making code fail in a well-defined manner even when something unexpected occurs. A key principle of

defensive programming is to “fail fast”: as soon as something wrong is discovered, signal an error. This is more work for author of the function (you!), but it makes debugging easier for users because they get errors early rather than later, after unexpected input has passed through several functions.

In R, the “fail fast” principle is implemented in three ways:

- Be strict about what you accept. For example, if your function is not vectorised in its inputs, but uses functions that are, make sure to check that the inputs are scalars. You can use `stopifnot()`, the `assertthat` (<https://github.com/hadley/assertthat>) package, or simple `if` statements and `stop()`.
- Avoid functions that use non-standard evaluation, like `subset`, `transform`, and `with`. These functions save time when used interactively, but because they make assumptions to reduce typing, when they fail, they often fail with uninformative error messages. You can learn more about non-standard evaluation in Chapter 13.
- Avoid functions that return different types of output depending on their input. The two biggest offenders are `[]` and `sapply()`. Whenever subsetting a data frame in a function, you should always use `drop = FALSE`, otherwise you will accidentally convert 1-column data frames into vectors. Similarly, never use `sapply()` inside a function: always use the stricter `vapply()` which will throw an error if the inputs are incorrect types and return the correct type of output even for zero-length inputs.

There is a tension between interactive analysis and programming. When you’re working interactively, you want R to do what you mean. If it guesses wrong, you want to discover that right away so you can fix it. When you’re programming, you want functions that signal errors if anything is even slightly wrong or underspecified. Keep this tension in mind when writing functions. If you’re writing functions to facilitate interactive data analysis, feel free to guess what the analyst wants and recover from minor misspecifications automatically. If you’re writing functions for programming, be strict. Never try to guess what the caller wants.

9.4.1 Exercises

- The goal of the `col_means()` function defined below is to compute the means of all numeric columns in a data frame.

```
col_means <- function(df) {
  numeric <- sapply(df, is.numeric)
  numeric_cols <- df[, numeric]

  data.frame(lapply(numeric_cols, mean))
}
```

However, the function is not robust to unusual inputs. Look at the following results, decide which ones are incorrect, and modify `col_means()` to be more robust. (Hint: there are two function calls in `col_means()` that are particularly prone to problems.)

```
col_means(mtcars)
col_means(mtcars[, 0])
col_means(mtcars[0, ])
col_means(mtcars[, "mpg", drop = F])
col_means(1:10)
col_means(as.matrix(mtcars))
col_means(as.list(mtcars))

mtcars2 <- mtcars
mtcars2[-1] <- lapply(mtcars2[-1], as.character)
col_means(mtcars2)
```

- The following function “lags” a vector, returning a version of `x` that is `n` values behind the original. Improve the function so that it (1) returns a useful error message if `n` is not a vector, and (2) has reasonable behaviour when `n` is 0 or longer than `x`.

```
lag <- function(x, n = 1L) {
  xlen <- length(x)
  c(rep(NA, n), x[seq_len(xlen - n)])
}
```

9.5 Quiz answers

1. The most useful tool to determine where an error occurred is `traceback()`. Or use Rstudio, which displays it automatically where an error occurs.

2. `browser()` pauses execution at the specified line and allows you to enter an interactive environment. In that environment, there are five useful commands: `n`, execute the next command; `s`, step into the next function; `f`, finish the current loop or function; `c`, continue execution normally; `Q`, stop the function and return to the console.
3. You could use `try()` or `tryCatch()`.
4. Because you can then capture specific types of error with `tryCatch()`, rather than relying on the comparison of error strings, which is risky, especially when messages are translated.

Part II

Functional programming

10

Functional programming

R, at its heart, is a functional programming (FP) language. This means that it provides many tools for the creation and manipulation of functions. In particular, R has what's known as first class functions. You can do anything with functions that you can do with vectors: you can assign them to variables, store them in lists, pass them as arguments to other functions, create them inside functions, and even return them as the result of a function.

The chapter starts by showing a motivating example, removing redundancy and duplication in code used to clean and summarise data. Then you'll learn about the three building blocks of functional programming: anonymous functions, closures (functions written by functions), and lists of functions. These pieces are twined together in the conclusion which shows how to build a suite of tools for numerical integration, starting from very simple primitives. This is a recurring theme in FP: start with small, easy-to-understand building blocks, combine them into more complex structures, and apply them with confidence.

The discussion of functional programming continues in the following two chapters: Chapter 11 explores functions that take functions as arguments and return vectors as output, and Chapter 12 explores functions that take functions as input and return them as output.

Outline

- Section 10.1 motivates functional programming using a common problem: cleaning and summarising data before serious analysis.
- Section 10.2 shows you a side of functions that you might not have known about: you can use functions without giving them a name.
- Section 10.3 introduces the closure, a function written by another function. A closure can access its own arguments, and variables defined in its parent.

- Section 10.4 shows how to put functions in a list, and explains why you might care.
- Section 10.5 concludes the chapter with a case study that uses anonymous functions, closures and lists of functions to build a flexible toolkit for numerical integration.

Prerequisites

You should be familiar with the basic rules of lexical scoping, as described in Section 6.2. Make sure you’ve installed the `pryr` package with `install.packages("pryr")`

10.1 Motivation

Imagine you’ve loaded a data file, like the one below, that uses `-99` to represent missing values. You want to replace all the `-99`s with `NA`s.

```
# Generate a sample dataset
set.seed(1014)
df <- data.frame(replicate(6, sample(c(1:10, -99), 6, rep = TRUE)))
names(df) <- letters[1:6]
df
#>   a  b c  d  e f
#> 1  1  6 1  5 -99 1
#> 2 10  4 4 -99  9 3
#> 3  7  9 5  4  1 4
#> 4  2  9 3  8  6 8
#> 5  1 10 5  9  8 6
#> 6  6  2 1  3  8 5
```

When you first started writing R code, you might have solved the problem with copy-and-paste:

```
df$a[df$a == -99] <- NA
df$b[df$b == -99] <- NA
df$c[df$c == -98] <- NA
df$d[df$d == -99] <- NA
```



```
df$e[df$e == -99] <- NA
df$f[df$g == -99] <- NA
```

One problem with copy-and-paste is that it's easy to make mistakes. Can you spot the two in the block above? These mistakes are inconsistencies that arose because we didn't have an authoritative description of the desired action (replace `-99` with `NA`). Duplicating an action makes bugs more likely and makes it harder to change code. For example, if the code for a missing value changes from `-99` to `9999`, you'd need to make the change in multiple places.

To prevent bugs and to make more flexible code, adopt the “do not repeat yourself”, or DRY, principle. Popularised by the “pragmatic programmers” (<http://pragprog.com/about>), Dave Thomas and Andy Hunt, this principle states: “every piece of knowledge must have a single, unambiguous, authoritative representation within a system”. FP tools are valuable because they provide tools to reduce duplication.

We can start applying FP ideas by writing a function that fixes the missing values in a single vector:

```
fix_missing <- function(x) {
  x[x == -99] <- NA
  x
}
df$a <- fix_missing(df$a)
df$b <- fix_missing(df$b)
df$c <- fix_missing(df$c)
df$d <- fix_missing(df$d)
df$e <- fix_missing(df$e)
df$f <- fix_missing(df$e)
```

This reduces the scope of possible mistakes, but it doesn't eliminate them: you can no longer accidentally type `-98` instead of `-99`, but you can still mess up the name of variable. The next step is to remove this possible source of error by combining two functions. One function, `fix_missing()`, knows how to fix a single vector; the other, `lapply()`, knows how to do something to each column in a data frame.

`lapply()` takes three inputs: `x`, a list; `f`, a function; and `...`, other arguments to pass to `f()`. It applies the function to each element of the list and returns a new list. `lapply(x, f, ...)` is equivalent to the following for loop:

```
out <- vector("list", length(x))
for (i in seq_along(x)) {
  out[[i]] <- f(x[[i]], ...)
}
```

The real `lapply()` is rather more complicated since it's implemented in C for efficiency, but the essence of the algorithm is the same. `lapply()` is called a **functional**, because it takes a function as an argument. Functionals are an important part of functional programming. You'll learn more about them in Chapter 11.

We can apply `lapply()` to this problem because data frames are lists. We just need a neat little trick to make sure we get back a data frame, not a list. Instead of assigning the results of `lapply()` to `df`, we'll assign them to `df[]`. R's usual rules ensure that we get a data frame, not a list. (If this comes as a surprise, you might want to read Section 3.3.) Putting these pieces together gives us:

```
fix_missing <- function(x) {
  x[x == -99] <- NA
  x
}
df[] <- lapply(df, fix_missing)
```

This code has five advantages over copy and paste:

- It's more compact.
- If the code for a missing value changes, it only needs to be updated in one place.
- It works for any number of columns. There is no way to accidentally miss a column.
- There is no way to accidentally treat one column differently than another.
- It is easy to generalise this technique to a subset of columns:

```
df[1:5] <- lapply(df[1:5], fix_missing)
```

The key idea is function composition. Take two simple functions, one which does something to every column and one which fixes missing values, and combine them to fix missing values in every column. Writing

simple functions that can be understood in isolation and then composed is a powerful technique.

What if different columns used different codes for missing values? You might be tempted to copy-and-paste:

```
fix_missing_99 <- function(x) {  
  x[x == -99] <- NA  
  x  
}  
fix_missing_999 <- function(x) {  
  x[x == -999] <- NA  
  x  
}  
fix_missing_9999 <- function(x) {  
  x[x == -999] <- NA  
  x  
}
```

As before, it's easy to create bugs. Instead we could use closures, functions that make and return functions. Closures allow us to make functions based on a template:

```
missing_fixer <- function(na_value) {  
  function(x) {  
    x[x == na_value] <- NA  
    x  
  }  
}  
fix_missing_99 <- missing_fixer(-99)  
fix_missing_999 <- missing_fixer(-999)  
  
fix_missing_99(c(-99, -999))  
#> [1] NA -999  
fix_missing_999(c(-99, -999))  
#> [1] -99 NA
```

Extra argument

In this case, you could argue that we should just add another argument:

```
fix_missing <- function(x, na.value) {  
  x[x == na.value] <- NA  
  x  
}
```

That's a reasonable solution here, but it doesn't always work well in every situation. We'll see more compelling uses for closures in Section 11.5.

Now consider a related problem. Once you've cleaned up your data, you might want to compute the same set of numerical summaries for each variable. You could write code like this:

```
mean(df$a)  
median(df$a)  
sd(df$a)  
mad(df$a)  
IQR(df$a)  
  
mean(df$b)  
median(df$b)  
sd(df$b)  
mad(df$b)  
IQR(df$b)
```

But again, you'd be better off identifying and removing duplicate items. Take a minute or two to think about how you might tackle this problem before reading on.

One approach would be to write a summary function and then apply it to each column:

```
summary <- function(x) {  
  c(mean(x), median(x), sd(x), mad(x), IQR(x))  
}  
lapply(df, summary)
```

That's a great start, but there's still some duplication. It's easier to see if we make the summary function more realistic:

```
summary <- function(x) {  
  c(mean(x, na.rm = TRUE),  
    median(x, na.rm = TRUE),  
    sd(x, na.rm = TRUE),  
    mad(x, na.rm = TRUE),  
    IQR(x, na.rm = TRUE))  
}
```

All five functions are called with the same arguments (`x` and `na.rm`) repeated five times. As always, duplication makes our code fragile: it's easier to introduce bugs and harder to adapt to changing requirements.

To remove this source of duplication, you can take advantage of another functional programming technique: storing functions in lists.

```
summary <- function(x) {  
  funs <- c(mean, median, sd, mad, IQR)  
  lapply(funs, function(f) f(x, na.rm = TRUE))  
}
```

This chapter discusses these techniques in more detail. But before you can start learning them, you need to learn the simplest FP tool, the anonymous function.

10.2 Anonymous functions

In R, functions are objects in their own right. They aren't automatically bound to a name. Unlike many languages (e.g., C, C++, Python, and Ruby), R doesn't have a special syntax for creating a named function: when you create a function, you use the regular assignment operator to give it a name. If you choose not to give the function a name, you get an **anonymous function**.

You use an anonymous function when it's not worth the effort to give it a name:

```
lapply(mtcars, function(x) length(unique(x)))
Filter(function(x) !is.numeric(x), mtcars)
integrate(function(x) sin(x) ^ 2, 0, pi)
```

Like all functions in R, anonymous functions have `formals()`, a `body()`, and a `parent environment()`:

```
formals(function(x = 4) g(x) + h(x))
#> $x
#> [1] 4
body(function(x = 4) g(x) + h(x))
#> g(x) + h(x)
environment(function(x = 4) g(x) + h(x))
#> <environment: R_GlobalEnv>
```

You can call an anonymous function without giving it a name, but the code is a little tricky to read because you must use parentheses in two different ways: first, to call a function, and second to make it clear that you want to call the anonymous function itself, as opposed to calling a (possibly invalid) function *inside* the anonymous function:

```
# This does not call the anonymous function.
# (Note that "3" is not a valid function.)
function(x) 3()
#> function(x) 3()

# With appropriate parenthesis, the function is called:
(function(x) 3)()
#> [1] 3

# So this anonymous function syntax
(function(x) x + 3)(10)
#> [1] 13

# behaves exactly the same as
f <- function(x) x + 3
f(10)
#> [1] 13
```

You can call anonymous functions with named arguments, but doing so is a good sign that your function needs a name.

One of the most common uses for anonymous functions is to create

closures, functions made by other functions. Closures are described in the next section.

10.2.1 Exercises

1. Given a function, like "mean", `match.fun()` lets you find a function. Given a function, can you find its name? Why doesn't that make sense in R?
2. Use `lapply()` and an anonymous function to find the coefficient of variation (the standard deviation divided by the mean) for all columns in the `mtcars` dataset.
3. Use `integrate()` and an anonymous function to find the area under the curve for the following functions. Use Wolfram Alpha (<http://www.wolframalpha.com/>) to check your answers.
 1. $y = x^2 - x$, x in $[0, 10]$
 2. $y = \sin(x) + \cos(x)$, x in $[-\pi, \pi]$
 3. $y = \exp(x) / x$, x in $[10, 20]$
4. A good rule of thumb is that an anonymous function should fit on one line and shouldn't need to use `{}`. Review your code. Where could you have used an anonymous function instead of a named function? Where should you have used a named function instead of an anonymous function?

10.3 Closures

"An object is data with functions. A closure is a function with data."
— John D. Cook

One use of anonymous functions is to create small functions that are not worth naming. Another important use is to create closures, functions written by functions. Closures get their name because they **enclose** the environment of the parent function and can access all its variables. This is useful because it allows us to have two levels of parameters: a parent level that controls operation and a child level that does the work.

The following example uses this idea to generate a family of power functions in which a parent function (`power()`) creates two child functions (`square()` and `cube()`).

```
power <- function(exponent) {  
  function(x) {  
    x ^ exponent  
  }  
}
```

```
square <- power(2)  
square(2)  
#> [1] 4  
square(4)  
#> [1] 16
```

```
cube <- power(3)  
cube(2)  
#> [1] 8  
cube(4)  
#> [1] 64
```

When you print a closure, you don't see anything terribly useful:

```
square  
#> function(x) {  
#>   x ^ exponent  
#> }  
#> <environment: 0x7fa58d810940>  
cube  
#> function(x) {  
#>   x ^ exponent  
#> }  
#> <environment: 0x7fa58d98f098>
```

That's because the function itself doesn't change. The difference is the enclosing environment, `environment(square)`. One way to see the contents of the environment is to convert it to a list:

```
as.list(environment(square))  
#> $exponent  
#> [1] 2  
as.list(environment(cube))  
#> $exponent  
#> [1] 3
```


Another way to see what's going on is to use `pryr::unenclose()`. This function replaces variables defined in the enclosing environment with their values:

```
library(pryr)
unenclose(square)
#> function (x)
#> {
#>     x^2
#> }
unenclose(cube)
#> function (x)
#> {
#>     x^3
#> }
```

The parent environment of a closure is the execution environment of the function that created it, as shown by this code:

```
power <- function(exponent) {
  print(environment())
  function(x) x ^ exponent
}
zero <- power(0)
#> <environment: 0x7fa58ad7e7f0>
environment(zero)
#> <environment: 0x7fa58ad7e7f0>
```

The execution environment normally disappears after the function returns a value. However, functions capture their enclosing environments. This means when function a returns function b, function b captures and stores the execution environment of function a, and it doesn't disappear. (This has important consequences for memory use, see Section 18.2 for details.)

In R, almost every function is a closure. All functions remember the environment in which they were created, typically either the global environment, if it's a function that you've written, or a package environment, if it's a function that someone else has written. The only exception is primitive functions, which call C code directly and don't have an associated environment.

Closures are useful for making function factories, and are one way to manage mutable state in R.

10.3.1 Function factories

A function factory is a factor for making new functions. We've already seen two examples of function factories, `missing_fixer()` and `power()`. You call it with arguments that describe the desired actions, and it returns a function that will do the work for you. For `missing_fixer()` and `power()`, there's not much benefit in using a function factory instead of a single function with multiple arguments. Function factories are most useful when:

- The different levels are more complex, with multiple arguments and complicated bodies.
- Some work only needs to be done once, when the function is generated.

Function factories are particularly well suited to maximum likelihood problems, and you'll see a more compelling use of them in Section 11.5.

10.3.2 Mutable state

Having variables at two levels allows you to maintain state across function invocations. This is possible because while the execution environment is refreshed every time, the enclosing environment is constant. The key to managing variables at different levels is the double arrow assignment operator (`<<-`). Unlike the usual single arrow assignment (`<-`) that always assigns in the current environment, the double arrow operator will keep looking up the chain of parent environments until it finds a matching name. (Section 8.4 has more details on how it works.)

Together, a static parent environment and `<<-` make it possible to maintain state across function calls. The following example shows a counter that records how many times a function has been called. Each time `new_counter` is run, it creates an environment, initialises the counter `i` in this environment, and then creates a new function.

```
new_counter <- function() {  
  i <- 0  
  function() {  
    i <<- i + 1  
    i  
  }  
}
```

The new function is a closure, and its enclosing environment is the environment created when `new_counter()` is run. Ordinarily, function execution environments are temporary, but a closure maintains access to the environment in which it was created. In the example below, closures `counter_one()` and `counter_two()` each get their own enclosing environments when run, so they can maintain different counts.

```
counter_one <- new_counter()
counter_two <- new_counter()

counter_one()
#> [1] 1
counter_one()
#> [1] 2
counter_two()
#> [1] 1
```

The counters get around the “fresh start” limitation by not modifying variables in their local environment. Since the changes are made in the unchanging parent (or enclosing) environment, they are preserved across function calls.

What happens if you don’t use a closure? What happens if you use `<-` instead of `<<-`? Make predictions about what will happen if you replace `new_counter()` with the variants below, then run the code and check your predictions.

```
i <- 0
new_counter2 <- function() {
  i <<- i + 1
  i
}
new_counter3 <- function() {
  i <- 0
  function() {
    i <- i + 1
    i
  }
}
```

Modifying values in a parent environment is an important technique because it is one way to generate “mutable state” in R. Mutable state is normally hard because every time it looks like you’re modifying an

object, you're actually creating and then modifying a copy. However, if you do need mutable objects and your code is not very simple, it's usually better to use reference classes, as described in Section 7.4.

The power of closures is tightly coupled with the more advanced ideas in Chapter 11 and Chapter 12. You'll see many more closures in those two chapters. The following section discusses the third technique of functional programming in R: the ability to store functions in a list.

10.3.3 Exercises

1. Why are functions created by other functions called closures?
2. What does the following statistical function do? What would be a better name for it? (The existing name is a bit of a hint.)

```
bc <- function(lambda) {
  if (lambda == 0) {
    function(x) log(x)
  } else {
    function(x) (x ^ lambda - 1) / lambda
  }
}
```

3. What does `approxfun()` do? What does it return?
4. What does `ecdf()` do? What does it return?
5. Create a function that creates functions that compute the *i*th central moment (http://en.wikipedia.org/wiki/Central_moment) of a numeric vector. You can test it by running the following code:

```
m1 <- moment(1)
m2 <- moment(2)

x <- runif(100)
stopifnot(all.equal(m1(x), 0))
stopifnot(all.equal(m2(x), var(x) * 99 / 100))
```

6. Create a function `pick()` that takes an index, *i*, as an argument and returns a function with an argument *x* that subsets *x* with *i*.

```
lapply(mtcars, pick(5))
# should do the same as this
lapply(mtcars, function(x) x[[5]])
```

10.4 Lists of functions

In R, functions can be stored in lists. This makes it easier to work with groups of related functions, in the same way a data frame makes it easier to work with groups of related vectors.

We'll start with a simple benchmarking example. Imagine you are comparing the performance of multiple ways of computing the arithmetic mean. You could do this by storing each approach (function) in a list:

```
compute_mean <- list(
  base = function(x) mean(x),
  sum = function(x) sum(x) / length(x),
  manual = function(x) {
    total <- 0
    n <- length(x)
    for (i in seq_along(x)) {
      total <- total + x[i] / n
    }
    total
  }
)
```

Calling a function from a list is straightforward. You extract it then call it:

```
x <- runif(1e5)
system.time(compute_mean$base(x))
#>   user  system elapsed
#> 0.001   0.000   0.001
system.time(compute_mean[[2]](x))
#>   user  system elapsed
#>    0      0         0
system.time(compute_mean[["manual"]](x))
#>   user  system elapsed
#> 0.053   0.003   0.055
```

To call each function (e.g., to check that they all return the same results), use `lapply()`. We'll need either an anonymous function or a new named function, since there isn't a built-in function to handle this situation.

```
lapply(compute_mean, function(f) f(x))
#> $base
#> [1] 0.4995
#>
#> $sum
#> [1] 0.4995
#>
#> $manual
#> [1] 0.4995
```

```
call_fun <- function(f, ...) f(...)
lapply(compute_mean, call_fun, x)
#> $base
#> [1] 0.4995
#>
#> $sum
#> [1] 0.4995
#>
#> $manual
#> [1] 0.4995
```

To time each function, we can combine `lapply()` and `system.time()`:

```
lapply(compute_mean, function(f) system.time(f(x)))
#> $base
#>   user  system elapsed
#> 0.000   0.000   0.001
#>
#> $sum
#>   user  system elapsed
#>    0      0         0
#>
#> $manual
#>   user  system elapsed
#> 0.051   0.003   0.054
```

Another use for a list of functions is to summarise an object in multiple ways. To do that, we could store each summary function in a list, and then run them all with `lapply()`:

```
x <- 1:10
funs <- list(
```

```
    sum = sum,
    mean = mean,
    median = median
  )
  lapply(funs, function(f) f(x))
#> $sum
#> [1] 55
#>
#> $mean
#> [1] 5.5
#>
#> $median
#> [1] 5.5
```

What if we wanted our summary functions to automatically remove missing values? One approach would be make a list of anonymous functions that call our summary functions with the appropriate arguments:

```
funs2 <- list(
  sum = function(x, ...) sum(x, ..., na.rm = TRUE),
  mean = function(x, ...) mean(x, ..., na.rm = TRUE),
  median = function(x, ...) median(x, ..., na.rm = TRUE)
)
lapply(funs2, function(f) f(x))
#> $sum
#> [1] 55
#>
#> $mean
#> [1] 5.5
#>
#> $median
#> [1] 5.5
```

This, however, leads to a lot of duplication. Apart from a different function name, each function is almost identical. A better approach would be to modify our `lapply()` call to include the extra argument:

```
lapply(funs, function(f) f(x, na.rm = TRUE))
```

10.4.1 Moving lists of functions to the global environment

From time to time you may create a list of functions that you want to be available without having to use a special syntax. For example, imagine

you want to create HTML code by mapping each tag to an R function. The following example uses a function factory to create functions for the tags `<p>` (paragraph), `` (bold), and `<i>` (italics).

```
simple_tag <- function(tag) {
  force(tag)
  function(...) {
    paste0("<", tag, ">", paste0(...), "</", tag, ">")
  }
}
tags <- c("p", "b", "i")
html <- lapply(setNames(tags, tags), simple_tag)
```

I've put the functions in a list because I don't want them to be available all the time. The risk of a conflict between an existing R function and an HTML tag is high. But keeping them in a list makes code more verbose:

```
html$p("This is ", html$b("bold"), " text.")
#> [1] "<p>This is <b>bold</b> text.</p>"
```

Depending on how long we want the effect to last, you have three options to eliminate the use of `html$`:

- For a very temporary effect, you can use `with()`:

```
with(html, p("This is ", b("bold"), " text."))
#> [1] "<p>This is <b>bold</b> text.</p>"
```
- For a longer effect, you can `attach()` the functions to the search path, then `detach()` when you're done:

```
attach(html)
p("This is ", b("bold"), " text.")
#> [1] "<p>This is <b>bold</b> text.</p>"
detach(html)
```

- Finally, you could copy the functions to the global environment with `list2env()`. You can undo this by deleting the functions after you're done.

```
list2env(html, environment())
#> <environment: R_GlobalEnv>
p("This is ", b("bold"), " text.")
#> [1] "<p>This is <b>bold</b> text.</p>"
rm(list = names(html), envir = environment())
```


I recommend the first option, using `with()`, because it makes it very clear when code is being executed in a special context and what that context is.

10.4.2 Exercises

1. Implement a summary function that works like `base::summary()`, but uses a list of functions. Modify the function so it returns a closure, making it possible to use it as a function factory.
2. Which of the following commands is equivalent to `with(x, f(z))`?
 - (a) `x$f(x$z)`.
 - (b) `f(x$z)`.
 - (c) `x$f(z)`.
 - (d) `f(z)`.
 - (e) It depends.

10.5 Case study: numerical integration

To conclude this chapter, I'll develop a simple numerical integration tool using first-class functions. Each step in the development of the tool is driven by a desire to reduce duplication and to make the approach more general.

The idea behind numerical integration is simple: find the area under a curve by approximating the curve with simpler components. The two simplest approaches are the **midpoint** and **trapezoid** rules. The midpoint rule approximates a curve with a rectangle. The trapezoid rule uses a trapezoid. Each takes the function we want to integrate, `f`, and a range of values, from `a` to `b`, to integrate over. For this example, I'll try to integrate $\sin x$ from 0 to π . This is a good choice for testing because it has a simple answer: 2.

```
midpoint <- function(f, a, b) {  
  (b - a) * f((a + b) / 2)  
}
```

```
trapezoid <- function(f, a, b) {
  (b - a) / 2 * (f(a) + f(b))
}
```

```
midpoint(sin, 0, pi)
#> [1] 3.142
trapezoid(sin, 0, pi)
#> [1] 1.924e-16
```

Neither of these functions gives a very good approximation. To make them more accurate using the idea that underlies calculus: we'll break up the range into smaller pieces and integrate each piece using one of the simple rules. This is called **composite integration**. I'll implement it using two new functions:

```
midpoint_composite <- function(f, a, b, n = 10) {
  points <- seq(a, b, length = n + 1)
  h <- (b - a) / n

  area <- 0
  for (i in seq_len(n)) {
    area <- area + h * f((points[i] + points[i + 1]) / 2)
  }
  area
}

trapezoid_composite <- function(f, a, b, n = 10) {
  points <- seq(a, b, length = n + 1)
  h <- (b - a) / n

  area <- 0
  for (i in seq_len(n)) {
    area <- area + h / 2 * (f(points[i]) + f(points[i + 1]))
  }
  area
}

midpoint_composite(sin, 0, pi, n = 10)
#> [1] 2.008
midpoint_composite(sin, 0, pi, n = 100)
#> [1] 2
trapezoid_composite(sin, 0, pi, n = 10)
#> [1] 1.984
```

```
trapezoid_composite(sin, 0, pi, n = 100)
#> [1] 2
```

You'll notice that there's a lot of duplication between `midpoint_composite()` and `trapezoid_composite()`. Apart from the internal rule used to integrate over a range, they are basically the same. From these specific functions you can extract a more general composite integration function:

```
composite <- function(f, a, b, n = 10, rule) {
  points <- seq(a, b, length = n + 1)

  area <- 0
  for (i in seq_len(n)) {
    area <- area + rule(f, points[i], points[i + 1])
  }

  area
}

composite(sin, 0, pi, n = 10, rule = midpoint)
#> [1] 2.008
composite(sin, 0, pi, n = 10, rule = trapezoid)
#> [1] 1.984
```

This function takes two functions as arguments: the function to integrate and the integration rule. We can now add even better rules for integrating over smaller ranges:

```
simpson <- function(f, a, b) {
  (b - a) / 6 * (f(a) + 4 * f((a + b) / 2) + f(b))
}

boole <- function(f, a, b) {
  pos <- function(i) a + i * (b - a) / 4
  fi <- function(i) f(pos(i))

  (b - a) / 90 *
    (7 * fi(0) + 32 * fi(1) + 12 * fi(2) + 32 * fi(3) + 7 * fi(4))
}

composite(sin, 0, pi, n = 10, rule = simpson)
#> [1] 2
```

```
composite(sin, 0, pi, n = 10, rule = boole)
#> [1] 2
```

It turns out that the midpoint, trapezoid, Simpson, and Boole rules are all examples of a more general family called Newton-Cotes rules (http://en.wikipedia.org/wiki/Newton%E2%80%93Cotes_formulas). (They are polynomials of increasing complexity.) We can use this common structure to write a function that can generate any general Newton-Cotes rule:

```
newton_cotes <- function(coef, open = FALSE) {
  n <- length(coef) + open

  function(f, a, b) {
    pos <- function(i) a + i * (b - a) / n
    points <- pos(seq.int(0, length(coef) - 1))

    (b - a) / sum(coef) * sum(f(points) * coef)
  }
}

boole <- newton_cotes(c(7, 32, 12, 32, 7))
milne <- newton_cotes(c(2, -1, 2), open = TRUE)
composite(sin, 0, pi, n = 10, rule = milne)
#> [1] 1.994
```

Mathematically, the next step in improving numerical integration is to move from a grid of evenly spaced points to a grid where the points are closer together near the end of the range, such as Gaussian quadrature. That's beyond the scope of this case study, but you could implement it with similar techniques.

10.5.1 Exercises

1. Instead of creating individual functions (e.g., `midpoint()`, `trapezoid()`, `simpson()`, etc.), we could store them in a list. If we did that, how would that change the code? Can you create the list of functions from a list of coefficients for the Newton-Cotes formulae?
2. The trade-off between integration rules is that more complex rules are slower to compute, but need fewer pieces. For `sin()`

in the range $[0, \pi]$, determine the number of pieces needed so that each rule will be equally accurate. Illustrate your results with a graph. How do they change for different functions? $\sin(1 / x^2)$ is particularly challenging.

11

Functionals

“To become significantly more reliable, code must become more transparent. In particular, nested conditions and loops must be viewed with great suspicion. Complicated control flows confuse programmers. Messy code often hides bugs.”

— Bjarne Stroustrup

A higher-order function is a function that takes a function as an input or returns a function as output. We’ve already seen one type of higher order function: closures, functions returned by another function. The complement to a closure is a **functional**, a function that takes a function as an input and returns a vector as output. Here’s a simple functional: it calls the function provided as input with 1000 random uniform numbers.

```
randomise <- function(f) f(runif(1e3))
randomise(mean)
#> [1] 0.4897
randomise(mean)
#> [1] 0.4858
randomise(sum)
#> [1] 497.5
```

The chances are that you’ve already used a functional: the three most frequently used are `lapply()`, `apply()`, and `tapply()`. All three take a function as input (among other things) and return a vector as output.

A common use of functionals is as an alternative to `for` loops. For loops have a bad rap in R. They have a reputation for being slow (although that reputation is only partly true, see Section 18.4 for more details). But the real downside of `for` loops is that they’re not very expressive. A `for` loop conveys that it’s iterating over something, but doesn’t clearly convey a high level goal. Instead of using a `for` loop, it’s better to use a functional. Each functional is tailored for a specific task, so when

you recognise the functional you know immediately why it's being used. Functionals play other roles as well as replacements for for-loops. They are useful for encapsulating common data manipulation tasks like split-apply-combine, for thinking “functionally”, and for working with mathematical functions.

Functionals reduce bugs in your code by better communicating intent. Functionals implemented in base R are well tested (i.e., bug-free) and efficient, because they're used by so many people. Many are written in C, and use special tricks to enhance performance. That said, using functionals will not always produce the fastest code. Instead, it helps you clearly communicate and build tools that solve a wide range of problems. It's a mistake to focus on speed until you know it'll be a problem. Once you have clear, correct code you can make it fast using the techniques you'll learn in Chapter 17.

Outline

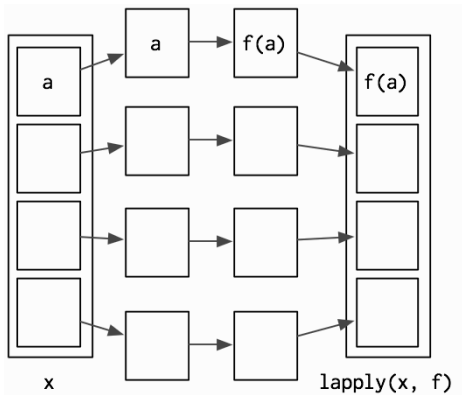
- Section 11.1 introduces your first functional: `lapply()`.
- Section 11.2 shows you variants of `lapply()` that produce different outputs, take different inputs, and distribute computation in different ways.
- Section 11.3 discusses functionals that work with more complex data structures like matrices and arrays.
- Section 11.4 teaches you about the powerful `Reduce()` and `Filter()` functions which are useful for working with lists.
- Section 11.5 discusses functionals that you might be familiar with from mathematics, like root finding, integration, and optimisation.
- Section 11.6 provides some important caveats about when you shouldn't attempt to convert a loop into a functional.
- Section 11.7 finishes off the chapter by showing you how functionals can take a simple building block and use it to create a set of powerful and consistent tools.

Prerequisites

You'll use closures frequently used in conjunction with functionals. If you need a refresher, review Section 10.3.

11.1 My first functional: `lapply()`

The simplest functional is `lapply()`, which you may already be familiar with. `lapply()` takes a function, applies it to each element in a list, and returns the results in the form of a list. `lapply()` is the building block for many other functionals, so it's important to understand how it works. Here's a pictorial representation:



`lapply()` is written in C for performance, but we can create a simple R implementation that does the same thing:

```
lapply2 <- function(x, f, ...) {  
  out <- vector("list", length(x))  
  for (i in seq_along(x)) {  
    out[[i]] <- f(x[[i]], ...)  
  }  
  out  
}
```

From this code, you can see that `lapply()` is a wrapper for a common for loop pattern: create a container for output, apply `f()` to each component of a list, and fill the container with the results. All other for loop functionals are variations on this theme: they simply use different types of input or output.

`lapply()` makes it easier to work with lists by eliminating much of the boilerplate associated with looping. This allows you to focus on the function that you're applying:

```
# Create some random data
l <- replicate(20, runif(sample(1:10, 1)), simplify = FALSE)

# With a for loop
out <- vector("list", length(l))
for (i in seq_along(l)) {
  out[[i]] <- length(l[[i]])
}
unlist(out)
#> [1] 8 8 1 4 6 6 9 8 9 10 2 6 4 3 2 7 3 10 6
#> [20] 9

# With lapply
unlist(lapply(l, length))
#> [1] 8 8 1 4 6 6 9 8 9 10 2 6 4 3 2 7 3 10 6
#> [20] 9
```

(I'm using `unlist()` to convert the output from a list to a vector to make it more compact. We'll see other ways of making the output a vector shortly.)

Since data frames are also lists, `lapply()` is also useful when you want to do something to each column of a data frame:

```
# What class is each column?
unlist(lapply(mtcars, class))
#>      mpg      cyl      disp      hp      drat      wt
#> "numeric" "numeric" "numeric" "numeric" "numeric" "numeric"
#>      qsec      vs      am      gear      carb
#> "numeric" "numeric" "numeric" "numeric" "numeric"

# Divide each column by the mean
mtcars[] <- lapply(mtcars, function(x) x / mean(x))
```

The pieces of `x` are always supplied as the first argument to `f`. If you want to vary a different argument, you can use an anonymous function. The following example varies the amount of trimming applied when computing the mean of a fixed `x`.

```
trims <- c(0, 0.1, 0.2, 0.5)
x <- rcauchy(1000)
unlist(lapply(trims, function(trim) mean(x, trim = trim)))
#> [1] 1.48503 -0.07759 -0.04445 -0.03894
```

11.1.1 Looping patterns

It's useful to remember that there are three basic ways to loop over a vector:

1. loop over the elements: `for (x in xs)`
2. loop over the numeric indices: `for (i in seq_along(xs))`
3. loop over the names: `for (nm in names(xs))`

The first form is usually not a good choice for a for loop because it leads to inefficient ways of saving output. With this form it's very natural to save the output by extending a datastructure, like in this example:

```
xs <- runif(1e3)
res <- c()
for (x in xs) {
  # This is slow!
  res <- c(res, sqrt(x))
}
```

This is slow because each time you extend the vector, R has to copy all of the existing elements. Section 17.7 discusses this problem in more depth. Instead, it's much better to create the space you'll need for the output and then fill it in. This is easiest with the second form:

```
res <- numeric(length(xs))
for (i in seq_along(xs)) {
  res[i] <- sqrt(xs[i])
}
```

Just as there are three basic ways to use a for loop, there are three basic ways to use `lapply()`:

```
lapply(xs, function(x) {})
lapply(seq_along(xs), function(i) {})
lapply(names(xs), function(nm) {})
```

Typically you'd use the first form because `lapply()` takes care of saving the output for you. However, if you need to know the position or name of the element you're working with, you should use the second or third form. Both give you an element's position (`i`, `nm`) and value (`xs[[i]]`, `xs[[nm]]`). If you're struggling to solve a problem using one form, you might find it easier with another.

11.1.2 Exercises

1. Why are the following two invocations of `lapply()` equivalent?

```
trims <- c(0, 0.1, 0.2, 0.5)
x <- rcauchy(100)

lapply(trims, function(trim) mean(x, trim = trim))
lapply(trims, mean, x = x)
```

2. The function below scales a vector so it falls in the range $[0, 1]$. How would you apply it to every column of a data frame? How would you apply it to every numeric column in a data frame?

```
scale01 <- function(x) {
  rng <- range(x, na.rm = TRUE)
  (x - rng[1]) / (rng[2] - rng[1])
}
```

3. Use both for loops and `lapply()` to fit linear models to the `mtcars` using the formulas stored in this list:

```
formulas <- list(
  mpg ~ disp,
  mpg ~ I(1 / disp),
  mpg ~ disp + wt,
  mpg ~ I(1 / disp) + wt
)
```

4. Fit the model `mpg ~ disp` to each of the bootstrap replicates of `mtcars` in the list below by using a for loop and `lapply()`. Can you do it without an anonymous function?

```
bootstraps <- lapply(1:10, function(i) {
  rows <- sample(1:nrow(mtcars), rep = TRUE)
  mtcars[rows, ]
})
```

5. For each model in the previous two exercises, extract R^2 using the function below.

```
rsq <- function(mod) summary(mod)$r.squared
```

11.2 For loop functionals: friends of `lapply()`

The key to using functionals in place of for loops is recognising that common looping patterns are already implemented in existing base functionals. Once you've mastered these existing functionals, the next step is to start writing your own: if you discover you're duplicating the same looping pattern in many places, you should extract it out into its own function.

The following sections build on `lapply()` and discuss:

- `sapply()` and `vapply()`, variants of `lapply()` that produce vectors, matrices, and arrays as **output**, instead of lists.
- `Map()` and `mapply()` which iterate over multiple **input** data structures in parallel.
- `mclapply()` and `mcMap()`, parallel versions of `lapply()` and `Map()`.
- Writing a new function, `rollapply()`, to solve a new problem.

11.2.1 Vector output: `sapply` and `vapply`

`sapply()` and `vapply()` are very similar to `lapply()` except they simplify their output to produce an atomic vector. While `sapply()` guesses, `vapply()` takes an additional argument specifying the output type. `sapply()` is great for interactive use because it saves typing, but if you use it inside your functions you'll get weird errors if you supply the wrong type of input. `vapply()` is more verbose, but gives more informative error messages and never fails silently. It is better suited for use inside other functions.

The following example illustrates these differences. When given a data frame, `sapply()` and `vapply()` return the same results. When given an empty list, `sapply()` returns another empty list instead of the more correct zero-length logical vector.

```
sapply(mtcars, is.numeric)
#> mpg cyl disp hp drat wt qsec vs am gear carb
#> TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
vapply(mtcars, is.numeric, logical(1))
```

```
#> mpg cyl disp hp drat wt qsec vs am gear carb
#> TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE TRUE
sapply(list(), is.numeric)
#> list()
vapply(list(), is.numeric, logical(1))
#> logical(0)
```

If the function returns results of different types or lengths, `sapply()` will silently return a list, while `vapply()` will throw an error. `sapply()` is fine for interactive use because you'll normally notice if something goes wrong, but it's dangerous when writing functions.

The following example illustrates a possible problem when extracting the class of columns in data frame: if you falsely assume that class only has one value and use `sapply()`, you won't find out about the problem until some future function is given a list instead of a character vector.

```
df <- data.frame(x = 1:10, y = letters[1:10])
sapply(df, class)
#>      x      y
#> "integer" "factor"
vapply(df, class, character(1))
#>      x      y
#> "integer" "factor"

df2 <- data.frame(x = 1:10, y = Sys.time() + 1:10)
sapply(df2, class)
#> $x
#> [1] "integer"
#>
#> $y
#> [1] "POSIXct" "POSIXt"
vapply(df2, class, character(1))
#> Error: values must be length 1,
#> but FUN(X[[2]]) result is length 2
```

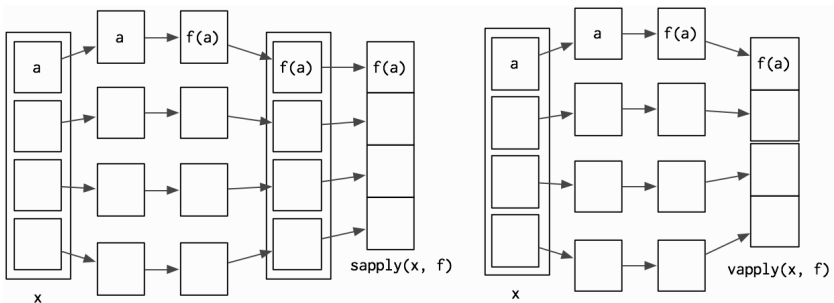
`sapply()` is a thin wrapper around `lapply()` that transforms a list into a vector in the final step. `vapply()` is an implementation of `lapply()` that assigns results to a vector (or matrix) of appropriate type instead of as a list. The following code shows a pure R implementation of the essence of `sapply()` and `vapply()` (the real functions have better error handling and preserve names, among other things).

```

sapply2 <- function(x, f, ...) {
  res <- lapply2(x, f, ...)
  simplify2array(res)
}

vapply2 <- function(x, f, f.value, ...) {
  out <- matrix(rep(f.value, length(x)), nrow = length(x))
  for (i in seq_along(x)) {
    res <- f(x[i], ...)
    stopifnot(
      length(res) == length(f.value),
      typeof(res) == typeof(f.value)
    )
    out[i, ] <- res
  }
  out
}

```



`vapply()` and `sapply()` have different outputs from `lapply()`. The following section discusses `Map()`, which has different inputs.

11.2.2 Multiple inputs: Map (and mapply)

With `lapply()`, only one argument to the function varies; the others are fixed. This makes it poorly suited for some problems. For example, how would you find a weighted mean when you have two lists, one of observations and the other of weights?

```

# Generate some sample data
xs <- replicate(5, runif(10), simplify = FALSE)
ws <- replicate(5, rpois(10, 5) + 1, simplify = FALSE)

```

It's easy to use `lapply()` to compute the unweighted means:

```
unlist(lapply(xs, mean))
#> [1] 0.4696 0.4793 0.4474 0.5755 0.4490
```

But how could we supply the weights to `weighted.mean()`? `lapply(x, means, w)` won't work because the additional arguments to `lapply()` are passed to every call. We could change looping forms:

```
unlist(lapply(seq_along(xs), function(i) {
  weighted.mean(xs[[i]], ws[[i]])
}))
#> [1] 0.4554 0.5370 0.4301 0.6391 0.4411
```

This works, but it's a little clumsy. A cleaner alternative is to use `Map`, a variant of `lapply()`, where all arguments can vary. This lets us write:

```
unlist(Map(weighted.mean, xs, ws))
#> [1] 0.4554 0.5370 0.4301 0.6391 0.4411
```

Note that the order of arguments is a little different: `function` is the first argument for `Map()` and the second for `lapply()`.

This is equivalent to:

```
stopifnot(length(xs) == length(ws))
out <- vector("list", length(xs))
for (i in seq_along(xs)) {
  out[[i]] <- weighted.mean(xs[[i]], ws[[i]])
}
```

There's a natural equivalence between `Map()` and `lapply()` because you can always convert a `Map()` to an `lapply()` that iterates over indices. But using `Map()` is more concise, and more clearly indicates what you're trying to do.

`Map` is useful whenever you have two (or more) lists (or data frames) that you need to process in parallel. For example, another way of standardising columns is to first compute the means and then divide by them. We could do this with `lapply()`, but if we do it in two steps, we can more easily check the results at each step, which is particularly important if the first step is more complicated.


```
mtmeans <- lapply(mtcars, mean)
mtmeans[] <- Map(`\'`, mtcars, mtmeans)

# In this case, equivalent to
mtcars[] <- lapply(mtcars, function(x) x / mean(x))
```

If some of the arguments should be fixed and constant, use an anonymous function:

```
Map(function(x, w) weighted.mean(x, w, na.rm = TRUE), xs, ws)
```

We'll see a more compact way to express the same idea in the next chapter.

mapply

You may be more familiar with `mapply()` than `Map()`. I prefer `Map()` because:

- It's equivalent to `mapply` with `simplify = FALSE`, which is almost always what you want.
- Instead of using an anonymous function to provide constant inputs, `mapply` has the `MoreArgs` argument that takes a list of extra arguments that will be supplied, as is, to each call. This breaks R's usual lazy evaluation semantics, and is inconsistent with other functions.

In brief, `mapply()` adds more complication for little gain.

11.2.3 Rolling computations

What if you need a for loop replacement that doesn't exist in base R? You can often create your own by recognising common looping structures and implementing your own wrapper. For example, you might be interested in smoothing your data using a rolling (or running) mean function:

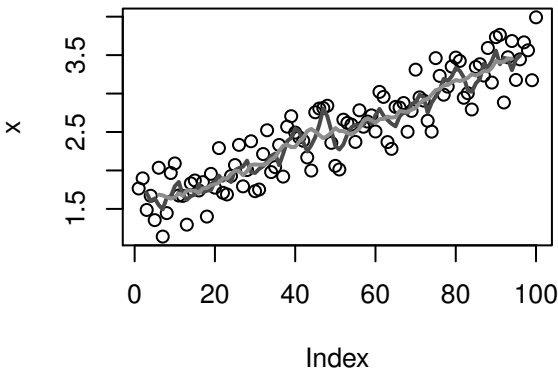
```
rollmean <- function(x, n) {
  out <- rep(NA, length(x))

  offset <- trunc(n / 2)
  for (i in (offset + 1):(length(x) - n + offset - 1)) {
```

```

    out[i] <- mean(x[(i - offset):(i + offset - 1)])
  }
  out
}
x <- seq(1, 3, length = 1e2) + runif(1e2)
plot(x)
lines(rollmean(x, 5), col = "blue", lwd = 2)
lines(rollmean(x, 10), col = "red", lwd = 2)

```

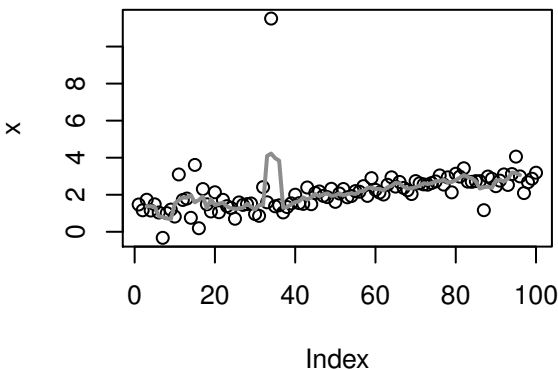


But if the noise was more variable (i.e., it has a longer tail), you might worry that your rolling mean was too sensitive to outliers. Instead, you might want to compute a rolling median.

```

x <- seq(1, 3, length = 1e2) + rt(1e2, df = 2) / 3
plot(x)
lines(rollmean(x, 5), col = "red", lwd = 2)

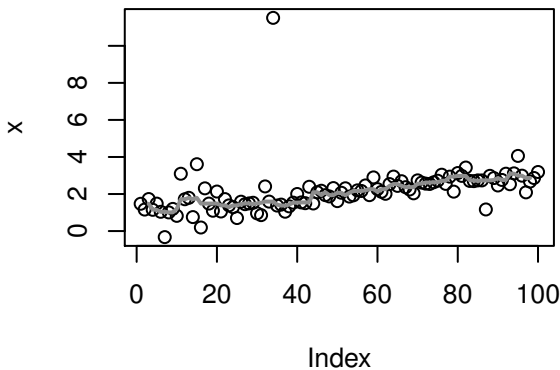
```



To change `rollmean()` to `rollmedian()`, all you need to do is replace `mean` with `median` inside the loop. But instead of copying and pasting to create a new function, we could extract the idea of computing a rolling summary into its own function:

```
rollapply <- function(x, n, f, ...) {
  out <- rep(NA, length(x))

  offset <- trunc(n / 2)
  for (i in (offset + 1):(length(x) - n + offset + 1)) {
    out[i] <- f(x[(i - offset):(i + offset)], ...)
  }
  out
}
plot(x)
lines(rollapply(x, 5, median), col = "red", lwd = 2)
```



You might notice that the internal loop looks pretty similar to a `vapply()` loop, so we could rewrite the function as:

```
rollapply <- function(x, n, f, ...) {
  offset <- trunc(n / 2)
  locs <- (offset + 1):(length(x) - n + offset + 1)
  num <- vapply(
    locs,
    function(i) f(x[(i - offset):(i + offset)], ...),
    numeric(1)
  )
  c(rep(NA, offset), num)
}
```

This is effectively the same as the implementation in `zoo::rollapply()`, which provides many more features and much more error checking.

11.2.4 Parallelisation

One interesting thing about the implementation of `lapply()` is that because each iteration is isolated from all others, the order in which they are computed doesn't matter. For example, `lapply3()` scrambles the order of computation, but the results are always the same:

```
lapply3 <- function(x, f, ...) {
  out <- vector("list", length(x))
  for (i in sample(seq_along(x))) {
    out[[i]] <- f(x[[i]], ...)
  }
  out
}
unlist(lapply(1:10, sqrt))
#> [1] 1.000 1.414 1.732 2.000 2.236 2.449 2.646 2.828 3.000
#> [10] 3.162
unlist(lapply3(1:10, sqrt))
#> [1] 1.000 1.414 1.732 2.000 2.236 2.449 2.646 2.828 3.000
#> [10] 3.162
```

This has a very important consequence: since we can compute each element in any order, it's easy to dispatch the tasks to different cores, and compute them in parallel. This is what `parallel::mclapply()` (and `parallel::mcMap()`) does. (These functions are not available in Windows, but you can use the similar `parLapply()` with a bit more work. See Section 17.10 for more details.)

```
library(parallel)
unlist(mclapply(1:10, sqrt, mc.cores = 4))
#> [1] 1.000 1.414 1.732 2.000 2.236 2.449 2.646 2.828 3.000
#> [10] 3.162
```

In this case, `mclapply()` is actually slower than `lapply()`. This is because the cost of the individual computations is low, and additional work is needed to send the computation to the different cores and to collect the results.

If we take a more realistic example, generating bootstrap replicates of a linear model for example, the advantages are clearer:

```
boot_df <- function(x) x[sample(nrow(x), rep = T), ]
rsquared <- function(mod) summary(mod)$r.square
boot_lm <- function(i) {
  rsquared(lm(mpg ~ wt + disp, data = boot_df(mtcars)))
}

system.time(lapply(1:500, boot_lm))
#>   user  system elapsed
#> 0.776   0.003   0.779
system.time(mclapply(1:500, boot_lm, mc.cores = 2))
#>   user  system elapsed
#> 0.001   0.002   0.427
```

While increasing the number of cores will not always lead to linear improvement, switching from `lapply()` or `Map()` to its parallelised forms can dramatically improve computational performance.

11.2.5 Exercises

1. Use `vapply()` to:
 - a) Compute the standard deviation of every column in a numeric data frame.
 - b) Compute the standard deviation of every numeric column in a mixed data frame. (Hint: you'll need to use `vapply()` twice.)
2. Why is using `sapply()` to get the `class()` of each element in a data frame dangerous?
3. The following code simulates the performance of a t-test for non-normal data. Use `sapply()` and an anonymous function to extract the p-value from every trial.

```
trials <- replicate(
  100,
  t.test(rpois(10, 10), rpois(7, 10)),
  simplify = FALSE
)
```

Extra challenge: get rid of the anonymous function by using `[[` directly.

4. What does `replicate()` do? What sort of for loop does it eliminate? Why do its arguments differ from `lapply()` and friends?

5. Implement a version of `lapply()` that supplies FUN with both the name and the value of each component.
 6. Implement a combination of `Map()` and `vapply()` to create an `lapply()` variant that iterates in parallel over all of its inputs and stores its outputs in a vector (or a matrix). What arguments should the function take?
 7. Implement `mcsapply()`, a multicore version of `sapply()`. Can you implement `mcvapply()`, a parallel version of `vapply()`? Why or why not?
-

11.3 Manipulating matrices and data frames

Functionals can also be used to eliminate loops in common data manipulation tasks. In this section, we'll give a brief overview of the available options, hint at how they can help you, and point you in the right direction to learn more. We'll cover three categories of data structure functionals:

- `apply()`, `sweep()`, and `outer()` with work with matrices.
- `tapply()` summarises a vector by groups defined by another vector.
- the `plyr` package, which generalises `tapply()` to make it easy to work with data frames, lists, or arrays as inputs, and data frames, lists, or arrays as outputs.

11.3.1 Matrix and array operations

So far, all the functionals we've seen work with 1d input structures. The three functionals in this section provide useful tools for working with higher-dimensional data structures. `apply()` is a variant of `sapply()` that works with matrices and arrays. You can think of it as an operation that summarises a matrix or array by collapsing each row or column to a single number. It has four arguments:

- `X`, the matrix or array to summarise
- `MARGIN`, an integer vector giving the dimensions to summarise over, 1 = rows, 2 = columns, etc.

- FUN, a summary function
- ... other arguments passed on to FUN

A typical example of `apply()` looks like this

```
a <- matrix(1:20, nrow = 5)
apply(a, 1, mean)
#> [1]  8.5  9.5 10.5 11.5 12.5
apply(a, 2, mean)
#> [1]  3  8 13 18
```

There are a few caveats to using `apply()`. It doesn't have a `simplify` argument, so you can never be completely sure what type of output you'll get. This means that `apply()` is not safe to use inside a function unless you carefully check the inputs. `apply()` is also not idempotent in the sense that if the summary function is the identity operator, the output is not always the same as the input:

```
a1 <- apply(a, 1, identity)
identical(a, a1)
#> [1] FALSE
identical(a, t(a1))
#> [1] TRUE
a2 <- apply(a, 2, identity)
identical(a, a2)
#> [1] TRUE
```

(You can put high-dimensional arrays back in the right order using `aperm()`, or use `plyr::aapply()`, which is idempotent.)

`sweep()` allows you to “sweep” out the values of a summary statistic. It is often used with `apply()` to standardise arrays. The following example scales the rows of a matrix so that all values lie between 0 and 1.

```
x <- matrix(rnorm(20, 0, 10), nrow = 4)
x1 <- sweep(x, 1, apply(x, 1, min), `-'`)
x2 <- sweep(x1, 1, apply(x1, 1, max), `/'`)
```

The final matrix functional is `outer()`. It's a little different in that it takes multiple vector inputs and creates a matrix or array output where the input function is run over every combination of the inputs:

```
# Create a times table
outer(1:3, 1:10, "*")
#>      [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
#> [1,]    1    2    3    4    5    6    7    8    9   10
#> [2,]    2    4    6    8   10   12   14   16   18   20
#> [3,]    3    6    9   12   15   18   21   24   27   30
```

Good places to learn more about `apply()` and friends are:

- “Using `apply`, `sapply`, `lapply` in R” (<http://petewerner.blogspot.com/2012/12/using-apply-sapply-lapply-in-r.html>) by Peter Werner.
- “The infamous `apply` function” (<http://rforpublichealth.blogspot.no/2012/09/the-infamous-apply-function.html>) by Slawa Rokicki.
- “The R `apply` function - a tutorial with examples” (<http://forgetfulfunctor.blogspot.com/2011/07/r-apply-function-tutorial-with-examples.html>) by axiomOfChoice.
- The stackoverflow question “R Grouping functions: `sapply` vs. `lapply` vs. `apply` vs. `tapply` vs. `by` vs. `aggregate`” (<http://stackoverflow.com/questions/3505701>).

11.3.2 Group `apply`

You can think about `tapply()` as a generalisation to `apply()` that allows for “ragged” arrays, arrays where each row can have a different number of columns. This is often needed when you’re trying to summarise a data set. For example, imagine you’ve collected pulse rate data from a medical trial, and you want to compare the two groups:

```
pulse <- round(rnorm(22, 70, 10 / 3)) + rep(c(0, 5), c(10, 12))
group <- rep(c("A", "B"), c(10, 12))

tapply(pulse, group, length)
#>  A  B
#> 10 12
tapply(pulse, group, mean)
#>  A  B
#> 71.6 74.5
```

`tapply()` works by creating a “ragged” data structure from a set of inputs, and then applying a function to the individual elements of that

structure. The first task is actually what the `split()` function does. It takes two inputs and returns a list which groups elements together from the first vector according to elements, or categories, from the second vector:

```
split(pulse, group)
#> $A
#> [1] 74 75 73 74 72 63 74 75 71 65
#>
#> $B
#> [1] 72 72 73 77 73 78 68 78 75 77 71 80
```

Then `tapply()` is just the combination of `split()` and `sapply()`:

```
tapply2 <- function(x, group, f, ..., simplify = TRUE) {
  pieces <- split(x, group)
  sapply(pieces, f, simplify = simplify)
}
tapply2(pulse, group, length)
#>   A   B
#> 10 12
tapply2(pulse, group, mean)
#>    A    B
#> 71.6 74.5
```

Being able to rewrite `tapply()` as a combination of `split()` and `sapply()` is a good indication that we've identified some useful building blocks.

11.3.3 The plyr package

One challenge with using the base functionals is that they have grown organically over time, and have been written by multiple authors. This means that they are not very consistent:

- With `tapply()` and `sapply()`, the `simplify` argument is called `simplify`. With `mapply()`, it's called `SIMPLIFY`. With `apply()`, the argument is absent.
- `vapply()` is a variant of `sapply()` that allows you to describe what the output should be, but there are no corresponding variants for `tapply()`, `apply()`, or `Map()`.

- The first argument of most base functionals is a vector, but the first argument in `Map()` is a function.

This makes learning these operators challenging, as you have to memorise all of the variations. Additionally, if you think about the possible combinations of input and output types, base R only covers a partial set of cases:

| | list | data frame | array |
|------------|-----------------------|------------|-----------------------|
| list | <code>lapply()</code> | | <code>sapply()</code> |
| data frame | <code>by()</code> | | |
| array | | | <code>apply()</code> |

This was one of the driving motivations behind the creation of the `plyr` package. It provides consistently named functions with consistently named arguments and covers all combinations of input and output data structures:

| | list | data frame | array |
|------------|----------------------|----------------------|----------------------|
| list | <code>llply()</code> | <code>ldply()</code> | <code>laply()</code> |
| data frame | <code>dlply()</code> | <code>ddply()</code> | <code>daply()</code> |
| array | <code>alply()</code> | <code>adply()</code> | <code>aaply()</code> |

Each of these functions splits up the input, applies a function to each piece, and then combines the results. Overall, this process is called “split-apply-combine”. You can read more about it and `plyr` in “The Split-Apply-Combine Strategy for Data Analysis” (<http://www.jstatsoft.org/v40/i01/>), an open-access article published in the *Journal of Statistical Software*.

11.3.4 Exercises

1. How does `apply()` arrange the output? Read the documentation and perform some experiments.
2. There’s no equivalent to `split() + vapply()`. Should there be? When would it be useful? Implement one yourself.

3. Implement a pure R version of `split()`. (Hint: use `unique()` and subsetting.) Can you do it without a for loop?
 4. What other types of input and output are missing? Brainstorm before you look up some answers in the `plyr` paper (<http://www.jstatsoft.org/v40/i01/>).
-

11.4 Manipulating lists

Another way of thinking about functionals is as a set of general tools for altering, subsetting, and collapsing lists. Every functional programming language has three tools for this: `Map()`, `Reduce()`, and `Filter()`. We've seen `Map()` already, and the following sections describe `Reduce()`, a powerful tool for extending two-argument functions, and `Filter()`, a member of an important class of functionals that work with predicates, functions that return a single `TRUE` or `FALSE`.

11.4.1 `Reduce()`

`Reduce()` reduces a vector, `x`, to a single value by recursively calling a function, `f`, two arguments at a time. It combines the first two elements with `f`, then combines the result of that call with the third element, and so on. Calling `Reduce(f, 1:3)` is equivalent to `f(f(1, 2), 3)`. `Reduce` is also known as `fold`, because it folds together adjacent elements in the list.

The following two examples show what `Reduce` does with an infix and prefix function:

```
Reduce(`+`, 1:3) # -> ((1 + 2) + 3)
Reduce(sum, 1:3) # -> sum(sum(1, 2), 3)
```

The essence of `Reduce()` can be described by a simple for loop:

```
Reduce2 <- function(f, x) {
  out <- x[[1]]
  for(i in seq(2, length(x))) {
    out <- f(out, x[[i]])
  }
}
```

```
  out
}
```

The real `Reduce()` is more complicated because it includes arguments to control whether the values are reduced from the left or from the right (`right`), an optional initial value (`init`), and an option to output intermediate results (`accumulate`).

`Reduce()` is an elegant way of extending a function that works with two inputs into a function that can deal with any number of inputs. It's useful for implementing many types of recursive operations, like merges and intersections. (We'll see another use in the final case study.) Imagine you have a list of numeric vectors, and you want to find the values that occur in every element:

```
l <- replicate(5, sample(1:10, 15, replace = T), simplify = FALSE)
str(l)
#> List of 5
#> $ : int [1:15] 4 10 7 9 3 10 8 7 2 2 ...
#> $ : int [1:15] 10 3 10 2 2 6 9 6 4 4 ...
#> $ : int [1:15] 1 5 9 9 1 8 5 7 5 7 ...
#> $ : int [1:15] 6 2 10 5 6 3 1 6 1 2 ...
#> $ : int [1:15] 10 5 10 7 7 1 9 9 9 7 ...
```

You could do that by intersecting each element in turn:

```
intersect(intersect(intersect(intersect(l[[1]], l[[2]]),
  l[[3]]), l[[4]]), l[[5]])
#> [1] 10 3
```

That's hard to read. With `Reduce()`, the equivalent is:

```
Reduce(intersect, l)
#> [1] 10 3
```

11.4.2 Predicate functionals

A **predicate** is a function that returns a single TRUE or FALSE, like `is.character`, `all`, or `is.NULL`. A predicate functional applies a predicate to each element of a list or data frame. There are three useful predicate functionals in base R: `Filter()`, `Find()`, and `Position()`.

- `Filter()` selects only those elements which match the predicate.
- `Find()` returns the first element which matches the predicate (or the last element if `right = TRUE`).
- `Position()` returns the position of the first element that matches the predicate (or the last element if `right = TRUE`).

Another useful predicate functional is `where()`, a custom functional generates a logical vector from a list (or a data frame) and a predicate:

```
where <- function(f, x) {
  vapply(x, f, logical(1))
}
```

The following example shows how you might use these functionals with a data frame:

```
df <- data.frame(x = 1:3, y = c("a", "b", "c"))
where(is.factor, df)
#>      x      y
#> FALSE  TRUE
str(Filter(is.factor, df))
#> 'data.frame':   3 obs. of  1 variable:
#> $ y: Factor w/ 3 levels "a","b","c": 1 2 3
str(Find(is.factor, df))
#> Factor w/ 3 levels "a","b","c": 1 2 3
Position(is.factor, df)
#> [1] 2
```

11.4.3 Exercises

1. Why isn't `is.na()` a predicate function? What base R function is closest to being a predicate version of `is.na()`?
2. Use `Filter()` and `vapply()` to create a function that applies a summary statistic to every numeric column in a data frame.
3. What's the relationship between `which()` and `Position()`? What's the relationship between `where()` and `Filter()`?
4. Implement `Any()`, a function that takes a list and a predicate function, and returns `TRUE` if the predicate function returns `TRUE` for any of the inputs. Implement `All()` similarly.

5. Implement the `span()` function from Haskell: given a list `x` and a predicate function `f`, `span` returns the location of the longest sequential run of elements where the predicate is true. (Hint: you might find `rle()` helpful.)

11.5 Mathematical functionals

Functionals are very common in mathematics. The limit, the maximum, the roots (the set of points where $f(x) = 0$), and the definite integral are all functionals: given a function, they return a single number (or vector of numbers). At first glance, these functions don't seem to fit in with the theme of eliminating loops, but if you dig deeper you'll find out that they are all implemented using an algorithm that involves iteration.

In this section we'll use some of R's built-in mathematical functionals. There are three functionals that work with functions to return single numeric values:

- `integrate()` finds the area under the curve defined by `f()`
- `uniroot()` finds where `f()` hits zero
- `optimise()` finds the location of lowest (or highest) value of `f()`

Let's explore how these are used with a simple function, `sin()`:

```
integrate(sin, 0, pi)
#> 2 with absolute error < 2.2e-14
str(uniroot(sin, pi * c(1 / 2, 3 / 2)))
#> List of 5
#> $ root      : num 3.14
#> $ f.root    : num 1.22e-16
#> $ iter      : int 2
#> $ init.it   : int NA
#> $ estim.prec: num 6.1e-05
str(optimise(sin, c(0, 2 * pi)))
#> List of 2
#> $ minimum   : num 4.71
#> $ objective: num -1
str(optimise(sin, c(0, pi), maximum = TRUE))
#> List of 2
```

```
#> $ maximum : num 1.57
#> $ objective: num 1
```

In statistics, optimisation is often used for maximum likelihood estimation (MLE). In MLE, we have two sets of parameters: the data, which is fixed for a given problem, and the parameters, which vary as we try to find the maximum. These two sets of parameters make the problem well suited for closures. Combining closures with optimisation gives rise to the following approach to solving MLE problems.

The following example shows how we might find the maximum likelihood estimate for λ , if our data come from a Poisson distribution. First, we create a function factory that, given a dataset, returns a function that computes the negative log likelihood (NLL) for parameter `lambda`. In R, it's common to work with the negative since `optimise()` defaults to finding the minimum.

```
poisson_nll <- function(x) {
  n <- length(x)
  sum_x <- sum(x)
  function(lambda) {
    n * lambda - sum_x * log(lambda) # + terms not involving lambda
  }
}
```

Note how the closure allows us to precompute values that are constant with respect to the data.

We can use this function factory to generate specific NLL functions for input data. Then `optimise()` allows us to find the best values (the maximum likelihood estimates), given a generous starting range.

```
x1 <- c(41, 30, 31, 38, 29, 24, 30, 29, 31, 38)
x2 <- c(6, 4, 7, 3, 3, 7, 5, 2, 7, 5, 4, 12, 6, 9)
nll1 <- poisson_nll(x1)
nll2 <- poisson_nll(x2)

optimise(nll1, c(0, 100))$minimum
#> [1] 32.1
optimise(nll2, c(0, 100))$minimum
#> [1] 5.467
```

We can check that these values are correct by comparing them to the

analytic solution: in this case, it's just the mean of the data, 32.1 and 5.4667.

Another important mathematical functional is `optim()`. It is a generalisation of `optimise()` that works with more than one dimension. If you're interested in how it works, you might want to explore the `Rvmmmin` package, which provides a pure-R implementation of `optim()`. Interestingly `Rvmmmin` is no slower than `optim()`, even though it is written in R, not C. For this problem, the bottleneck lies not in controlling the optimisation but with having to evaluate the function multiple times.

11.5.1 Exercises

1. Implement `arg_max()`. It should take a function and a vector of inputs, and return the elements of the input where the function returns the highest value. For example, `arg_max(-10:5, function(x) x ^ 2)` should return -10. `arg_max(-5:5, function(x) x ^ 2)` should return `c(-5, 5)`. Also implement the matching `arg_min()` function.
2. Challenge: read about the fixed point algorithm (http://mitpress.mit.edu/sicp/full-text/book/book-Z-H-12.html#%_sec_1.3). Complete the exercises using R.

11.6 Loops that should be left as is

Some loops have no natural functional equivalent. In this section you'll learn about three common cases:

- modifying in place
- recursive functions
- while loops

It's possible to torture these problems to use a functional, but it's not a good idea. You'll create code that is harder to understand, eliminating the main reason for using functionals in the first case.

11.6.1 Modifying in place

If you need to modify part of an existing data frame, it's often better to use a for loop. For example, the following code performs a variable-by-variable transformation by matching the names of a list of functions to the names of variables in a data frame.

```
trans <- list(
  disp = function(x) x * 0.0163871,
  am = function(x) factor(x, levels = c("auto", "manual"))
)
for(var in names(trans)) {
  mtcars[[var]] <- trans[[var]](mtcars[[var]])
}
```

We wouldn't normally use `lapply()` to replace this loop directly, but it is *possible*. Just replace the loop with `lapply()` by using `<-`:

```
lapply(names(trans), function(var) {
  mtcars[[var]] <- trans[[var]](mtcars[[var]])
})
```

The for loop is gone, but the code is longer and much harder to understand. The reader needs to understand `<-` and how `x[[y]] <- z` works (it's not simple!). In short, we've taken a simple, easily understood for loop, and turned it into something few people will understand: not a good idea!

11.6.2 Recursive relationships

It's hard to convert a for loop into a functional when the relationship between elements is not independent, or is defined recursively. For example, exponential smoothing works by taking a weighted average of the current and previous data points. The `exps()` function below implements exponential smoothing with a for loop.

```
exps <- function(x, alpha) {
  s <- numeric(length(x) + 1)
  for (i in seq_along(s)) {
    if (i == 1) {
      s[i] <- x[i]
```

```

    } else {
      s[i] <- alpha * x[i - 1] + (1 - alpha) * s[i - 1]
    }
  }
  s
}
x <- runif(6)
exps(x, 0.5)
#> [1] 0.3607 0.3607 0.2030 0.1066 0.1931 0.2594 0.4287

```

We can't eliminate the for loop because none of the functionals we've seen allow the output at position i to depend on both the input and output at position $i - 1$.

One way to eliminate the for loop in this case is to solve the recurrence relation (http://en.wikipedia.org/wiki/Recurrence_relation#Solving) by removing the recursion and replacing it with explicit references. This requires a new set of mathematical tools, and is challenging, but it can pay off by producing a simpler function.

11.6.3 While loops

Another type of looping construct in R is the while loop. It keeps running until some condition is met. while loops are more general than for loops: you can rewrite every for loop as a while loop, but you can't do the reverse. For example, we could turn this for loop:

```
for (i in 1:10) print(i)
```

into this while loop:

```

i <- 1
while(i <= 10) {
  print(i)
  i <- i + 1
}

```

Not every while loop can be turned into a for loop because many while loops don't know in advance how many times they will be run:

```

i <- 0
while(TRUE) {

```

```
  if (runif(1) > 0.9) break
  i <- i + 1
}
```

This is a common problem when you're writing simulations.

In this case we can remove the loop by recognising a special feature of the problem. Here we're counting the number of successes before Bernoulli trial with $p = 0.1$ fails. This is a geometric random variable, so you could replace the code with `i <- rgeom(1, 0.1)`. Reformulating the problem in this way is hard to do in general, but you'll benefit greatly if you can do it for your problem.

11.7 A family of functions

To finish off the chapter, this case study shows how you can use functionals to take a simple building block and make it powerful and general. I'll start with a simple idea, adding two numbers together, and use functionals to extend it to summing multiple numbers, computing parallel and cumulative sums, and summing across array dimensions.

We'll start by defining a very simple addition function, one which takes two scalar arguments:

```
add <- function(x, y) {
  stopifnot(length(x) == 1, length(y) == 1,
    is.numeric(x), is.numeric(y))
  x + y
}
```

(We're using R's existing addition operator here, which does much more, but the focus here is on how we can take very simple building blocks and extend them to do more.)

I'll also add an `na.rm` argument. A helper function will make this a bit easier: if `x` is missing it should return `y`, if `y` is missing it should return `x`, and if both `x` and `y` are missing then it should return another argument to the function: `identity`. This function is probably a bit more general than what we need now, but it's useful if we implement other binary operators.

```
rm_na <- function(x, y, identity) {
  if (is.na(x) && is.na(y)) {
    identity
  } else if (is.na(x)) {
    y
  } else {
    x
  }
}
rm_na(NA, 10, 0)
#> [1] 10
rm_na(10, NA, 0)
#> [1] 10
rm_na(NA, NA, 0)
#> [1] 0
```

This allows us to write a version of `add()` that can deal with missing values if needed:

```
add <- function(x, y, na.rm = FALSE) {
  if (na.rm && (is.na(x) || is.na(y))) rm_na(x, y, 0) else x + y
}
add(10, NA)
#> [1] NA
add(10, NA, na.rm = TRUE)
#> [1] 10
add(NA, NA)
#> [1] NA
add(NA, NA, na.rm = TRUE)
#> [1] 0
```

Why did we pick an identity of 0? Why should `add(NA, NA, na.rm = TRUE)` return 0? Well, for every other input it returns a number, so even if both arguments are NA, it should still do that. What number should it return? We can figure it out because additional is associative, which means that the order of additional doesn't matter. That means that the following two function calls should return the same value:

```
add(add(3, NA, na.rm = TRUE), NA, na.rm = TRUE)
#> [1] 3
add(3, add(NA, NA, na.rm = TRUE), na.rm = TRUE)
#> [1] 3
```

This implies that `add(NA, NA, na.rm = TRUE)` must be 0, and hence `identity = 0` is the correct default.

Now that we have the basics working, we can extend the function to deal with more complicated inputs. One obvious generalisation is to add more than two numbers. We can do this by iteratively adding two numbers: if the input is `c(1, 2, 3)` we compute `add(add(1, 2), 3)`. This is a simple application of `Reduce()`:

```
r_add <- function(xs, na.rm = TRUE) {  
  Reduce(function(x, y) add(x, y, na.rm = na.rm), xs)  
}  
r_add(c(1, 4, 10))  
#> [1] 15
```

This looks good, but we need to test a few special cases:

```
r_add(NA, na.rm = TRUE)  
#> [1] NA  
r_add(numeric())  
#> NULL
```

These are incorrect. In the first case, we get a missing value even though we've explicitly asked to ignore them. In the second case, we get `NULL` instead of a length one numeric vector (as we do for every other set of inputs).

The two problems are related. If we give `Reduce()` a length one vector, it doesn't have anything to reduce, so it just returns the input. If we give it an input of length zero, it always returns `NULL`. The easiest way to fix this problem is to use the `init` argument of `Reduce()`. This is added to the start of every input vector:

```
r_add <- function(xs, na.rm = TRUE) {  
  Reduce(function(x, y) add(x, y, na.rm = na.rm), xs, init = 0)  
}  
r_add(c(1, 4, 10))  
#> [1] 15  
r_add(NA, na.rm = TRUE)  
#> [1] 0  
r_add(numeric())  
#> [1] 0
```

`r_add()` is equivalent to `sum()`.

It would be nice to have a vectorised version of `add()` so that we can perform the addition of two vectors of numbers in element-wise fashion. We could use `Map()` or `vapply()` to implement this, but neither is perfect. `Map()` returns a list, instead of a numeric vector, so we need to use `simplify2array()`. `vapply()` returns a vector but it requires us to loop over a set of indices.

```
v_add1 <- function(x, y, na.rm = FALSE) {
  stopifnot(length(x) == length(y), is.numeric(x), is.numeric(y))
  if (length(x) == 0) return(numeric())
  simplify2array(
    Map(function(x, y) add(x, y, na.rm = na.rm), x, y)
  )
}

v_add2 <- function(x, y, na.rm = FALSE) {
  stopifnot(length(x) == length(y), is.numeric(x), is.numeric(y))
  vapply(seq_along(x), function(i) add(x[i], y[i], na.rm = na.rm),
    numeric(1))
}
```

A few test cases help to ensure that it behaves as we expect. We're a bit stricter than base R here because we don't do recycling. (You could add that if you wanted, but I find that recycling is a frequent source of silent bugs.)

```
# Both versions give the same results
v_add1(1:10, 1:10)
#> [1]  2  4  6  8 10 12 14 16 18 20
v_add1(numeric(), numeric())
#> numeric(0)
v_add1(c(1, NA), c(1, NA))
#> [1]  2 NA
v_add1(c(1, NA), c(1, NA), na.rm = TRUE)
#> [1] 2 0
```

Another variant of `add()` is the cumulative sum. We can implement it with `Reduce()` by setting the `accumulate` argument to `TRUE`:

```
c_add <- function(xs, na.rm = FALSE) {
```

```

  Reduce(function(x, y) add(x, y, na.rm = na.rm), xs,
         accumulate = TRUE)
}
c_add(1:10)
#> [1]  1  3  6 10 15 21 28 36 45 55
c_add(10:1)
#> [1] 10 19 27 34 40 45 49 52 54 55

```

This is equivalent to `cumsum()`.

Finally, we might want to define addition for more complicated data structures like matrices. We could create `row` and `col` variants that sum across rows and columns, respectively, or we could go the whole hog and define an array version that could sum across any arbitrary set of dimensions. These are easily implemented as combinations of `add()` and `apply()`.

```

row_sum <- function(x, na.rm = FALSE) {
  apply(x, 1, add, na.rm = na.rm)
}
col_sum <- function(x, na.rm = FALSE) {
  apply(x, 2, add, na.rm = na.rm)
}
arr_sum <- function(x, dim, na.rm = FALSE) {
  apply(x, dim, add, na.rm = na.rm)
}

```

The first two are equivalent to `rowSums()` and `colSums()`.

If every function we have created has an existing equivalent in base R, why did we bother? There are two main reasons:

- Since all variants were implemented by combining a simple binary operator (`add()`) and a well-tested functional (`Reduce()`, `Map()`, `apply()`), we know that our variants will behave consistently.
- We can apply the same infrastructure to other operators, especially those that might not have the full suite of variants in base R.

The downside of this approach is that these implementations are not that efficient. (For example, `colSums(x)` is much faster than `apply(x, 2, sum)`.) However, even if they aren't that fast, simple implementations are still a good starting point because they're less likely to have bugs.

When you create faster versions, you can compare the results to make sure your fast versions are still correct.

If you enjoyed this section, you might also enjoy “List out of lambda” (<http://stevelosh.com/blog/2013/03/list-out-of-lambda/>), a blog article by Steve Losh that shows how you can produce high level language structures (like lists) out of more primitive language features (like closures, aka lambdas).

11.7.1 Exercises

1. Implement `smaller` and `larger` functions that, given two inputs, return either the smaller or the larger value. Implement `na.rm = TRUE`: what should the identity be? (Hint: `smaller(x, smaller(NA, NA, na.rm = TRUE), na.rm = TRUE)` must be `x`, so `smaller(NA, NA, na.rm = TRUE)` must be bigger than any other value of `x`.) Use `smaller` and `larger` to implement equivalents of `min()`, `max()`, `pmin()`, `pmax()`, and new functions `row_min()` and `row_max()`.
2. Create a table that has *and*, *or*, *add*, *multiply*, *smaller*, and *larger* in the columns and *binary operator*, *reducing variant*, *vectorised variant*, and *array variants* in the rows.
 - a) Fill in the cells with the names of base R functions that perform each of the roles.
 - b) Compare the names and arguments of the existing R functions. How consistent are they? How could you improve them?
 - c) Complete the matrix by implementing any missing functions.
3. How does `paste()` fit into this structure? What is the scalar binary function that underlies `paste()`? What are the `sep` and `collapse` arguments to `paste()` equivalent to? Are there any `paste` variants that don't have existing R implementations?

12

Function operators

In this chapter, you'll learn about function operators (FOs). A function operator is a function that takes one (or more) functions as input and returns a function as output. In some ways, function operators are similar to functionals: there's nothing you can't do without them, but they can make your code more readable and expressive, and they can help you write code faster. The main difference is that functionals extract common patterns of loop use, where function operators extract common patterns of anonymous function use.

The following code shows a simple function operator, `chatty()`. It wraps a function, making a new function that prints out its first argument. It's useful because it gives you a window to see how functionals, like `vapply()`, work.

```
chatty <- function(f) {  
  function(x, ...) {  
    res <- f(x, ...)  
    cat("Processing ", x, "\n", sep = "  
  }  
}  
f <- function(x) x ^ 2  
s <- c(3, 2, 1)  
chatty(f)(1)  
#> Processing 1  
#> [1] 1  
  
vapply(s, chatty(f), numeric(1))  
#> Processing 3  
#> Processing 2  
#> Processing 1  
#> [1] 9 4 1
```

In the last chapter, we saw that many built-in functionals, like `Reduce()`,

`Filter()`, and `Map()`, have very few arguments, so we had to use anonymous functions to modify how they worked. In this chapter, we'll build specialised substitutes for common anonymous functions that allow us to communicate our intent more clearly. For example, in Section 11.2.2 we used an anonymous function with `Map()` to supply fixed arguments:

```
Map(function(x, y) f(x, y, zs), xs, ys)
```

Later in this chapter, we'll learn about partial application using the `partial()` function. Partial application encapsulates the use of an anonymous function to supply default arguments, and allows us to write succinct code:

```
Map(partial(f, zs = zs), xs, yz)
```

This is an important use of FOs: by transforming the input function, you eliminate parameters from a functional. In fact, as long as the inputs and outputs of the function remain the same, this approach allows your functionals to be more extensible, often in ways you haven't thought of.

The chapter covers four important types of FO: behaviour, input, output, and combining. For each type, I'll show you some useful FOs, and how you can use as another to decompose problems: as combinations of multiple functions instead of combinations of arguments. The goal is not to exhaustively list every possible FO, but to show a selection that demonstrate how they work together with other FP techniques. For your own work, you'll need to think about and experiment with how function operators can help you solve recurring problems.

Outline

- Section 12.1 introduces you to FOs that change the behaviour of a function like automatically logging usage to disk or ensuring that a function is run only once.
- Section 12.2 shows you how to write FOs that manipulate the output of a function. These can do simple things like capturing errors, or fundamentally change what the function does.
- Section 12.3 describes how to modify the inputs to a function using a FO like `Vectorize()` or `partial()`.
- Section 12.4 shows the power of FOs that combine multiple functions with function composition and logical operations.

Prerequisites

As well as writing FOs from scratch, this chapter uses function operators from the `memoise`, `plyr`, and `pryr` packages. Install them by running `install.packages(c("memoise", "plyr", "pryr"))`.

12.1 Behavioural FOs

Behavioural FOs leave the inputs and outputs of a function unchanged, but add some extra behaviour. In this section, we'll look at functions which implement three useful behaviours:

- Add a delay to avoid swamping a server with requests.
- Print to console every *n* invocations to check on a long running process.
- Cache previous computations to improve performance.

To motivate these behaviours, imagine we want to download a long vector of URLs. That's pretty simple with `lapply()` and `download_file()`:

```
download_file <- function(url, ...) {  
  download.file(url, basename(url), ...)  
}  
lapply(urls, download_file)
```

(`download_file()` is a simple wrapper around `utils::download.file()` which provides a reasonable default for the file name.)

There are a number of useful behaviours we might want to add to this function. If the list was long, we might want to print a . every ten URLs so we know that the function's still working. If we're downloading files over the internet, we might want to add a small delay between each request to avoid hammering the server. Implementing these behaviours in a `for` loop is rather complicated. We can no longer use `lapply()` because we need an external counter:

```
i <- 1  
for(url in urls) {  
  i <- i + 1
```

```

    if (i %% 10 == 0) cat(".")
    Sys.delay(1)
    download_file(url)
}

```

Understanding this code is hard because different concerns (iteration, printing, and downloading) are interleaved. In the remainder of this section we'll create FOs that encapsulate each behaviour and allow us to write code like this:

```
lapply(urls, dot_every(10, delay_by(1, download_file)))
```

Implementing `delay_by()` is straightforward, and follows the same basic template that we'll see for the majority of FOs in this chapter:

```

delay_by <- function(delay, f) {
  function(...) {
    Sys.sleep(delay)
    f(...)
  }
}

system.time(runif(100))
#>   user  system elapsed
#> 0.000   0.000   0.001
system.time(delay_by(0.1, runif)(100))
#>   user  system elapsed
#>  0.0    0.0    0.1

```

`dot_every()` is a little bit more complicated because it needs to manage a counter. Fortunately, we saw how to do that in Section 10.3.2.

```

dot_every <- function(n, f) {
  i <- 1
  function(...) {
    if (i %% n == 0) cat(".")
    i <- i + 1
    f(...)
  }
}

x <- lapply(1:100, runif)
x <- lapply(1:100, dot_every(10, runif))
#> .....

```

Notice that I've made the function the last argument in each FO. This makes it easier to read when we compose multiple function operators. If the function were the first argument, then instead of:

```
download <- dot_every(10, delay_by(1, download_file))
```

we'd have

```
download <- dot_every(delay_by(download_file, 1), 10)
```

That's harder to follow because (e.g.) the argument of `dot_every()` is far away from its call. This is sometimes called the Dagwood sandwich (http://en.wikipedia.org/wiki/Dagwood_sandwich) problem: you have too much filling (too many long arguments) between your slices of bread (parentheses).

I've also tried to give the FOs descriptive names: `delay by 1 (second)`, `(print a) dot every 10 (invocations)`. The more clearly the function names used in your code express your intent, the easier it will be for others (including future you) to read and understand the code.

12.1.1 Memoisation

Another thing you might worry about when downloading multiple files is accidentally downloading the same file multiple times. You could avoid this by calling `unique()` on the list of input URLs, or manually managing a data structure that mapped the URL to the result. An alternative approach is to use memoisation: modify a function to automatically cache its results.

```
library(memoise)
```

```
slow_function <- function(x) {
  Sys.sleep(1)
  10
}
system.time(slow_function())
#>    user  system elapsed
#>  0.000   0.000   1.001
system.time(slow_function())
#>    user  system elapsed
```

```
#> 0.000 0.000 1.001
fast_function <- memoise(slow_function)
system.time(fast_function())
#> user system elapsed
#> 0.000 0.001 1.002
system.time(fast_function())
#> user system elapsed
#> 0 0 0
```

Memoisation is an example of the classic computer science tradeoff of memory versus speed. A memoised function can run much faster because it stores all of the previous inputs and outputs, using more memory.

A realistic use of memoisation is computing the Fibonacci series. The Fibonacci series is defined recursively: the first two values are 1 and 1, then $f(n) = f(n - 1) + f(n - 2)$. A naive version implemented in R would be very slow because, for example, `fib(10)` computes `fib(9)` and `fib(8)`, and `fib(9)` computes `fib(8)` and `fib(7)`, and so on. As a result, the value for each value in the series gets computed many, many times. Memoising `fib()` makes the implementation much faster because each value is computed only once.

```
fib <- function(n) {
  if (n < 2) return(1)
  fib(n - 2) + fib(n - 1)
}
system.time(fib(23))
#> user system elapsed
#> 0.071 0.003 0.074
system.time(fib(24))
#> user system elapsed
#> 0.108 0.000 0.108

fib2 <- memoise(function(n) {
  if (n < 2) return(1)
  fib2(n - 2) + fib2(n - 1)
})
system.time(fib2(23))
#> user system elapsed
#> 0.003 0.000 0.003
system.time(fib2(24))
#> user system elapsed
#> 0 0 0
```

It doesn't make sense to memoise all functions. For example, a memoised random number generator is no longer random:

```
runifm <- memoise(runif)
runifm(5)
#> [1] 0.5916 0.2663 0.9651 0.4808 0.4759
runifm(5)
#> [1] 0.5916 0.2663 0.9651 0.4808 0.4759
```

Once we understand `memoise()`, it's straightforward to apply to our problem:

```
download <- dot_every(10, memoise(delay_by(1, download_file)))
```

This gives a function that we can easily use with `lapply()`. However, if something goes wrong with the loop inside `lapply()`, it can be difficult to tell what's going on. The next section will show how we can use FOs to pull back the curtain and look inside.

12.1.2 Capturing function invocations

One challenge with functionals is that it can be hard to see what's going on inside of them. It's not easy to pry open their internals like it is with a for loop. Fortunately we can use FOs to peer behind the curtain with `tee()`.

`tee()`, defined below, has three arguments, all functions: `f`, the function to modify; `on_input`, a function that's called with the inputs to `f`; and `on_output`, a function that's called with the output from `f`.

```
ignore <- function(...) NULL
tee <- function(f, on_input = ignore, on_output = ignore) {
  function(...) {
    on_input(...)
    output <- f(...)
    on_output(output)
    output
  }
}
```

(The function is inspired by the unix shell command `tee`, which is used

to split up streams of file operations so that you can both display what's happening and save intermediate results to a file.)

We can use `tee()` to look inside the `uniroot()` functional, and see how it iterates its way to a solution. The following example finds where `x` and `cos(x)` intersect:

```
g <- function(x) cos(x) - x
zero <- uniroot(g, c(-5, 5))
show_x <- function(x, ...) cat(sprintf("%.08f", x), "\n")

# The location where the function is evaluated:
zero <- uniroot(tee(g, on_input = show_x), c(-5, 5))
#> -5.00000000
#> +5.00000000
#> +0.28366219
#> +0.87520341
#> +0.72298040
#> +0.73863091
#> +0.73908529
#> +0.73902425
#> +0.73908529
# The value of the function:
zero <- uniroot(tee(g, on_output = show_x), c(-5, 5))
#> +5.28366219
#> -4.71633781
#> +0.67637474
#> -0.23436269
#> +0.02685676
#> +0.00076012
#> -0.00000026
#> +0.00010189
#> -0.00000026
```

`cat()` allows us to see what's happening as the function runs, but it doesn't give us a way to work with the values after the function as completed. To do that, we could capture the sequence of calls by creating a function, `remember()`, that records every argument called and retrieves them when coerced into a list. The small amount of S3 code needed is explained in Section 7.2.

```
remember <- function() {
  memory <- list()
```



```

f <- function(...) {
  # This is inefficient!
  memory <- append(memory, list(...))
  invisible()
}

structure(f, class = "remember")
}
as.list.remember <- function(x, ...) {
  environment(x)$memory
}
print.remember <- function(x, ...) {
  cat("Remembering...\n")
  str(as.list(x))
}

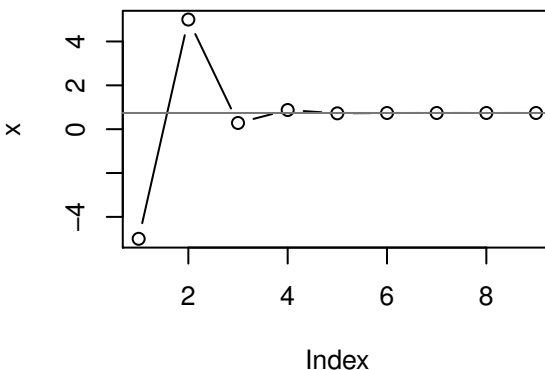
```

Now we can draw a picture showing how uniroot zeroes in on the final answer:

```

locs <- remember()
vals <- remember()
zero <- uniroot(tee(g, locs, vals), c(-5, 5))
x <- unlist(as.list(locs))
error <- unlist(as.list(vals))
plot(x, type = "b"); abline(h = 0.739, col = "grey50")

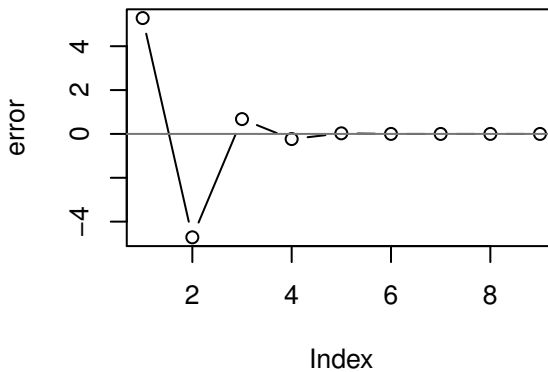
```



```

plot(error, type = "b"); abline(h = 0, col = "grey50")

```



12.1.3 Laziness

The function operators we've seen so far follow a common pattern:

```
funop <- function(f, otherargs) {
  function(...) {
    # maybe do something
    res <- f(...)
    # maybe do something else
    res
  }
}
```

Unfortunately there's a problem with this implementation because function arguments are lazily evaluated: `f()` may have changed between applying the FO and evaluating the function. This is a particular problem if you're using a for loop or `lapply()` to apply multiple function operators. In the following example, we take a list of functions and delay each one. But when we try to evaluate the mean, we get the sum instead.

```
funs <- list(mean = mean, sum = sum)
funs_m <- lapply(funs, delay_by, delay = 0.1)

funs_m$mean(1:10)
#> [1] 55
```

We can avoid that problem by explicitly forcing the evaluation of `f()`:

```

delay_by <- function(delay, f) {
  force(f)
  function(...) {
    Sys.sleep(delay)
    f(...)
  }
}

funs_m <- lapply(funs, delay_by, delay = 0.1)
funs_m$mean(1:10)
#> [1] 5.5

```

It's good practice to do that whenever you create a new FO.

12.1.4 Exercises

1. Write a FO that logs a time stamp and message to a file every time a function is run.
2. What does the following function do? What would be a good name for it?

```

f <- function(g) {
  force(g)
  result <- NULL
  function(...) {
    if (is.null(result)) {
      result <- g(...)
    }
    result
  }
}

runif2 <- f(runif)
runif2(5)
#> [1] 0.01581 0.33986 0.55830 0.45425 0.05724
runif2(10)
#> [1] 0.01581 0.33986 0.55830 0.45425 0.05724

```

3. Modify `delay_by()` so that instead of delaying by a fixed amount of time, it ensures that a certain amount of time has elapsed since the function was last called. That is, if you called `g <- delay_by(1, f); g(); Sys.sleep(2); g()` there shouldn't be an extra delay.

4. Write `wait_until()` which delays execution until a specific time.
5. There are three places we could have added a `memoise` call: why did we choose the one we did?

```
download <- memoise(dot_every(10, delay_by(1, download_file)))
download <- dot_every(10, memoise(delay_by(1, download_file)))
download <- dot_every(10, delay_by(1, memoise(download_file)))
```

6. Why is the `remember()` function inefficient? How could you implement it in more efficient way?
7. Why does the following code, from stackoverflow (<http://stackoverflow.com/questions/8440675>), not do what you expect?

```
# return a linear function with slope a and intercept b.
f <- function(a, b) function(x) a * x + b

# create a list of functions with different parameters.
fs <- Map(f, a = c(0, 1), b = c(0, 1))

fs[[1]](3)
#> [1] 4
# should return 0 * 3 + 0 = 0
```

How can you modify `f` so that it works correctly?

12.2 Output FOs

The next step up in complexity is to modify the output of a function. This could be quite simple, or it could fundamentally change the operation of the function by returning something completely different to its usual output. In this section you'll learn about two simple modifications, `Negate()` and `failwith()`, and two fundamental modifications, `capture_it()` and `time_it()`.

12.2.1 Minor modifications

`base::Negate()` and `plyr::failwith()` offer two minor, but useful, modifications of a function that are particularly handy in conjunction with functionals.

`Negate()` takes a function that returns a logical vector (a predicate function), and returns the negation of that function. This can be a useful shortcut when a function returns the opposite of what you need. The essence of `Negate()` is very simple:

```
Negate <- function(f) {  
  force(f)  
  function(...) !f(...)  
}  
(Negate(is.null))(NULL)  
#> [1] FALSE
```

I often use this idea to make a function, `compact()`, that removes all null elements from a list:

```
compact <- function(x) Filter(Negate(is.null), x)
```

`plyr::failwith()` turns a function that throws an error into a function that returns a default value when there's an error. Again, the essence of `failwith()` is simple; it's just a wrapper around `try()`, the function that captures errors and allows execution to continue.

```
failwith <- function(default = NULL, f, quiet = FALSE) {  
  force(f)  
  function(...) {  
    out <- default  
    try(out <- f(...), silent = quiet)  
    out  
  }  
}  
log("a")  
#> Error: non-numeric argument to mathematical function  
failwith(NA, log)("a")  
#> [1] NA  
failwith(NA, log, quiet = TRUE)("a")  
#> [1] NA
```

(If you haven't seen `try()` before, it's discussed in more detail in Section 9.3.1.)

`failwith()` is very useful in conjunction with functionals: instead of the failure propagating and terminating the higher-level loop, you can complete the iteration and then find out what went wrong. For example, imagine you're fitting a set of generalised linear models (GLMs) to a list of data frames. While GLMs can sometimes fail because of optimisation problems, you'd still want to be able to try to fit all the models, and later look back at those that failed:

```
# If any model fails, all models fail to fit:
models <- lapply(datasets, glm, formula = y ~ x1 + x2 * x3)
# If a model fails, it will get a NULL value
models <- lapply(datasets, failwith(NULL, glm),
  formula = y ~ x1 + x2 * x3)

# remove failed models (NULLs) with compact
ok_models <- compact(models)
# extract the datasets corresponding to failed models
failed_data <- datasets[vapply(models, is.null, logical(1))]
```

I think this is a great example of the power of combining functionals and function operators: it lets you succinctly express what you need to solve a common data analysis problem.

12.2.2 Changing what a function does

Other output function operators can have a more profound effect on the operation of the function. Instead of returning the original return value, we can return some other effect of the function evaluation. Here are two examples:

- Return text that the function `print()`ed:

```
capture_it <- function(f) {
  force(f)
  function(...) {
    capture.output(f(...))
  }
}
str_out <- capture_it(str)
```

```
str(1:10)
#> int [1:10] 1 2 3 4 5 6 7 8 9 10
str_out(1:10)
#> [1] " int [1:10] 1 2 3 4 5 6 7 8 9 10"
```

- Return how long a function took to run:

```
time_it <- function(f) {
  force(f)
  function(...) {
    system.time(f(...))
  }
}
```

`time_it()` allows us to rewrite some of the code from the functionals chapter:

```
compute_mean <- list(
  base = function(x) mean(x),
  sum = function(x) sum(x) / length(x)
)
x <- runif(1e6)
```

```
# Previously we used an anonymous function to time execution:
# lapply(compute_mean, function(f) system.time(f(x)))
```

```
# Now we can compose function operators:
call_fun <- function(f, ...) f(...)
lapply(compute_mean, time_it(call_fun), x)
#> $base
#>   user  system elapsed
#> 0.002   0.000   0.002
#>
#> $sum
#>   user  system elapsed
#> 0.001   0.000   0.001
```

In this example, there's not a huge benefit to using function operators, because the composition is simple and we're applying the same operator to each function. Generally, using function operators is most effective when you are using multiple operators or if the gap between creating them and using them is large.

12.2.3 Exercises

1. Create a `negative()` FO that flips the sign of the output of the function to which it is applied.
2. The `evaluate` package makes it easy to capture all the outputs (results, text, messages, warnings, errors, and plots) from an expression. Create a function like `capture_it()` that also captures the warnings and errors generated by a function.
3. Create a FO that tracks files created or deleted in the working directory (Hint: use `dir()` and `setdiff()`.) What other global effects of functions might you want to track?

12.3 Input FOs

The next step up in complexity is to modify the inputs of a function. Again, you can modify how a function works in a minor way (e.g., setting default argument values), or in a major way (e.g., converting inputs from scalars to vectors, or vectors to matrices).

12.3.1 Prefilling function arguments: partial function application

A common use of anonymous functions is to make a variant of a function that has certain arguments “filled in” already. This is called “partial function application”, and is implemented by `pryr::partial()`. Once you have read Chapter 14, I encourage you to read the source code for `partial()` and figure out how it works — it’s only 5 lines of code!

`partial()` allows us to replace code like

```
f <- function(a) g(a, b = 1)
compact <- function(x) Filter(Negate(is.null), x)
Map(function(x, y) f(x, y, zs), xs, ys)
```

with

```
f <- partial(g, b = 1)
compact <- partial(Filter, Negate(is.null))
Map(partial(f, zs = zs), xs, ys)
```


We can use this idea to simplify the code used when working with lists of functions. Instead of:

```
funs2 <- list(
  sum = function(...) sum(..., na.rm = TRUE),
  mean = function(...) mean(..., na.rm = TRUE),
  median = function(...) median(..., na.rm = TRUE)
)
```

we can write:

```
library(pryr)
funs2 <- list(
  sum = partial(sum, na.rm = TRUE),
  mean = partial(mean, na.rm = TRUE),
  median = partial(median, na.rm = TRUE)
)
```

Using partial function application is a straightforward task in many functional programming languages, but it's not entirely clear how it should interact with R's lazy evaluation rules. The approach `plyr::partial()` takes is to create a function that is as similar as possible to the anonymous function that you'd create by hand. Peter Meilstrup takes a different approach in his `ptools` package (<https://github.com/crowding/ptools/>). If you're interested in the topic, you might want to read about the binary operators he created: `%()`, `%>%`, and `%<=`.

12.3.2 Changing input types

It's also possible to make a major change to a function's input, making a function work with fundamentally different types of data. There are a few existing functions that work along these lines:

- `base::Vectorize()` converts a scalar function to a vector function. It takes a non-vectorised function and vectorises it with respect to the arguments specified in the `vectorize.args` argument. This doesn't give you any magical performance improvements, but it's useful if you want a quick and dirty way of making a vectorised function.

A mildly useful extension to `sample()` would be to vectorize it with respect to size. Doing so would allow you to generate multiple samples in one call.

```

sample2 <- Vectorize(sample, "size", SIMPLIFY = FALSE)
str(sample2(1:5, c(1, 1, 3)))
#> List of 3
#> $ : int 3
#> $ : int 2
#> $ : int [1:3] 1 4 3
str(sample2(1:5, 5:3))
#> List of 3
#> $ : int [1:5] 4 3 5 2 1
#> $ : int [1:4] 5 4 2 1
#> $ : int [1:3] 1 4 2

```

In this example we have used `SIMPLIFY = FALSE` to ensure that our newly vectorised function always returns a list. This is usually what you want.

- `splat()` converts a function that takes multiple arguments to a function that takes a single list of arguments.

```

splat <- function (f) {
  force(f)
  function(args) {
    do.call(f, args)
  }
}

```

This is useful if you want to invoke a function with varying arguments:

```

x <- c(NA, runif(100), 1000)
args <- list(
  list(x),
  list(x, na.rm = TRUE),
  list(x, na.rm = TRUE, trim = 0.1)
)
lapply(args, splat(mean))
#> [[1]]
#> [1] NA
#>
#> [[2]]
#> [1] 10.37
#>
#> [[3]]
#> [1] 0.4757

```

- `plyr::colwise()` converts a vector function to one that works with data frames:

```
median(mtcars)
#> Error: need numeric data
median(mtcars$mpg)
#> [1] 19.2
plyr::colwise(median)(mtcars)
#>   mpg cyl  disp  hp  drat    wt  qsec vs am gear carb
#> 1 19.2   6 196.3 123 3.695 3.325 17.71  0  0   4     2
```

12.3.3 Exercises

1. Our previous `download()` function only downloads a single file. How can you use `partial()` and `lapply()` to create a function that downloads multiple files at once? What are the pros and cons of using `partial()` vs. writing a function by hand?
2. Read the source code for `plyr::colwise()`. How does the code work? What are `colwise()`'s three main tasks? How could you make `colwise()` simpler by implementing each task as a function operator? (Hint: think about `partial()`.)
3. Write FOs that convert a function to return a matrix instead of a data frame, or a data frame instead of a matrix. If you understand S3, call them `as.data.frame.function()` and `as.matrix.function()`.
4. You've seen five functions that modify a function to change its output from one form to another. What are they? Draw a table of the various combinations of types of outputs: what should go in the rows and what should go in the columns? What function operators might you want to write to fill in the missing cells? Come up with example use cases.
5. Look at all the examples of using an anonymous function to partially apply a function in this and the previous chapter. Replace the anonymous function with `partial()`. What do you think of the result? Is it easier or harder to read?

12.4 Combining FOs

Besides just operating on single functions, function operators can take multiple functions as input. One simple example of this is `plyr::each()`. It takes a list of vectorised functions and combines them into a single function.

```
summaries <- plyr::each(mean, sd, median)
summaries(1:10)
#>   mean      sd median
#> 5.500  3.028  5.500
```

Two more complicated examples are combining functions through composition, or through boolean algebra. These capabilities are the glue that allow us to join multiple functions together.

12.4.1 Function composition

An important way of combining functions is through composition: `f(g(x))`. Composition takes a list of functions and applies them sequentially to the input. It's a replacement for the common pattern of anonymous function that chains multiple functions together to get the result you want:

```
sapply(mtcars, function(x) length(unique(x)))
#>   mpg  cyl disp  hp drat   wt  qsec    vs  am gear carb
#>   25    3  27   22  22   29   30     2   2    3    6
```

A simple version of compose looks like this:

```
compose <- function(f, g) {
  function(...) f(g(...))
}
```

(`pryr::compose()` provides a more full-featured alternative that can accept multiple functions and is used for the rest of the examples.)

This allows us to write:

```
sapply(mtcars, compose(length, unique))
#>   mpg   cyl  disp    hp  drat    wt  qsec    vs    am gear carb
#>   25     3   27    22   22    29   30     2     2    3    6
```

Mathematically, function composition is often denoted with the infix operator, \circ , $(f \circ g)(x)$. Haskell, a popular functional programming language, uses `.` to the same end. In R, we can create our own infix composition function:

```
"%o%" <- compose
sapply(mtcars, length %o% unique)
#>   mpg   cyl  disp    hp  drat    wt  qsec    vs    am gear carb
#>   25     3   27    22   22    29   30     2     2    3    6

sqrt(1 + 8)
#> [1] 3
compose(sqrt, `+`)(1, 8)
#> [1] 3
(sqrt %o% `+`)(1, 8)
#> [1] 3
```

Compose also allows for a very succinct implementation of `Negate`, which is just a partially evaluated version of `compose()`.

```
Negate <- partial(compose, `!`)
```

We could implement the population standard deviation with function composition:

```
square <- function(x) x^2
deviation <- function(x) x - mean(x)

sd2 <- sqrt %o% mean %o% square %o% deviation
sd2(1:10)
#> [1] 2.872
```

This type of programming is called *tacit* or *point-free* programming. (The term *point-free* comes from the use of “point” to refer to values in topology; this style is also derogatorily known as *pointless*). In this style of programming, you don’t explicitly refer to variables. Instead, you focus on the high-level composition of functions rather than the

low-level flow of data. The focus is on what's being done, not on objects it's being done to. Since we're using only functions and not parameters, we use verbs and not nouns. This style is common in Haskell, and is the typical style in stack based programming languages like Forth and Factor. It's not a terribly natural or elegant style in R, but it is fun to play with.

`compose()` is particularly useful in conjunction with `partial()`, because `partial()` allows you to supply additional arguments to the functions being composed. One nice side effect of this style of programming is that it keeps a function's arguments near its name. This is important because as the size of the chunk of code you have to hold in your head grows code becomes harder to understand.

Below I take the example from the first section of the chapter and modify it to use the two styles of function composition described above. Both results are longer than the original code, but they may be easier to understand because the function and its arguments are closer together. Note that we still have to read them from right to left (bottom to top): the first function called is the last one written. We could define `compose()` to work in the opposite direction, but in the long run, this is likely to lead to confusion since we'd create a small part of the language that reads differently from every other part.

```
download <- dot_every(10, memoise(delay_by(1, download_file)))
```

```
download <- pryr::compose(
  partial(dot_every, 10),
  memoise,
  partial(delay_by, 1),
  download_file
)
```

```
download <- partial(dot_every, 10) %o%
  memoise %o%
  partial(delay_by, 1) %o%
  download_file
```

12.4.2 Logical predicates and boolean algebra

When I use `Filter()` and other functionals that work with logical predicates, I often find myself using anonymous functions to combine multiple conditions:

```
Filter(function(x) is.character(x) || is.factor(x), iris)
```

As an alternative, we could define function operators that combine logical predicates:

```
and <- function(f1, f2) {  
  force(f1); force(f2)  
  function(...) {  
    f1(...) && f2(...)  
  }  
}
```

```
or <- function(f1, f2) {  
  force(f1); force(f2)  
  function(...) {  
    f1(...) || f2(...)  
  }  
}
```

```
not <- function(f) {  
  force(f)  
  function(...) {  
    !f(...)  
  }  
}
```

This would allow us to write:

```
Filter(or(is.character, is.factor), iris)  
Filter(not(is.numeric), iris)
```

And we now have a boolean algebra on functions, not on the results of functions.

12.4.3 Exercises

1. Implement your own version of `compose()` using `Reduce` and `%o%`. For bonus points, do it without calling `function`.
2. Extend `and()` and `or()` to deal with any number of input functions. Can you do it with `Reduce()`? Can you keep them lazy (e.g., for `and()`, the function returns once it sees the first `FALSE`)?

3. Implement the `xor()` binary operator. Implement it using the existing `xor()` function. Implement it as a combination of `and()` and `or()`. What are the advantages and disadvantages of each approach? Also think about what you'll call the resulting function to avoid a clash with the existing `xor()` function, and how you might change the names of `and()`, `not()`, and `or()` to keep them consistent.
4. Above, we implemented boolean algebra for functions that return a logical function. Implement elementary algebra (`plus()`, `minus()`, `multiply()`, `divide()`, `exponentiate()`, `log()`) for functions that return numeric vectors.

Part III

Computing on the language

13

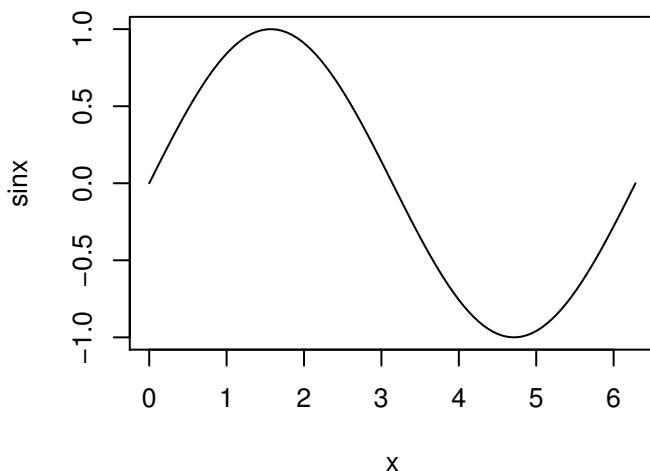
Non-standard evaluation

“Flexibility in syntax, if it does not lead to ambiguity, would seem a reasonable thing to ask of an interactive programming language.”

— Kent Pitman

R has powerful tools for computing not only on values, but also on the actions that lead to those values. If you’re coming from another programming language, they are one of the most surprising features of R. Consider the following simple snippet of code that plots a sine curve:

```
x <- seq(0, 2 * pi, length = 100)
sinx <- sin(x)
plot(x, sinx, type = "l")
```



Look at the labels on the axes. How did R know that the variable on the x axis is called `x` and the variable on the y axis is called `sinx`? In most programming languages, you can only access the values of a function’s arguments. In R, you can also access the code used to compute them.

This makes it possible to evaluate code in non-standard ways: to use what is known as **non-standard evaluation**, or NSE for short. NSE is particularly useful for functions when doing interactive data analysis because it can dramatically reduce the amount of typing.

Outline

- Section 13.1 teaches you how to capture unevaluated expressions using `substitute()`.
- Section 13.2 shows you `subset()` works with combining `substitute()` with `eval()` to allow you to succinctly select rows from a data frame.
- Section 13.3 discusses scoping issues specific to NSE, and will show you how to resolve them.
- Section 13.4 shows why every function that uses NSE should have an escape hatch, a version that uses regular evaluation.
- Section 13.5 teaches you how to use `substitute()` to work with functions that don't have an escape hatch.
- Section 13.6 finishes off the chapter with a discussion of the downsides of NSE.

Prerequisites

Before reading this chapter, make sure you're familiar with environments (Chapter 8) and lexical scoping (Section 6.2). You'll also need to install the `pryr` package with `install.packages("pryr")`. Some exercises require the `plyr` package, which you can install from CRAN with `install.packages("plyr")`.

13.1 Capturing expressions

`substitute()` makes non-standard evaluation possible. It looks at a function argument and instead of seeing the value, it sees the code used to compute the value:

```
f <- function(x) {  
  substitute(x)  
}  
f(1:10)  
#> 1:10  
  
x <- 10  
f(x)  
#> x  
  
y <- 13  
f(x + y^2)  
#> x + y^2
```

For now, we won't worry about exactly what `substitute()` returns (that's the topic of Chapter 14), but we'll call it an expression.

`substitute()` works because function arguments are represented by a special type of object called a **promise**. A promise captures the expression needed to compute the value and the environment in which to compute it. You're not normally aware of promises because the first time you access a promise its code is evaluated in its environment, yielding a value.

`substitute()` is often paired with `deparse()`. That function takes the result of `substitute()`, an expression, and turns it into a character vector.

```
g <- function(x) deparse(substitute(x))  
g(1:10)  
#> [1] "1:10"  
g(x)  
#> [1] "x"  
g(x + y^2)  
#> [1] "x + y^2"
```

There are a lot of functions in Base R that use these ideas. Some use them to avoid quotes:

```
library(ggplot2)  
# the same as  
library("ggplot2")
```

Other functions, like `plot.default()`, use them to provide default labels. `data.frame()` labels variables with the expression used to compute them:

```
x <- 1:4
y <- letters[1:4]
names(data.frame(x, y))
#> [1] "x" "y"
```

We'll learn about the ideas that underlie all these examples by looking at one particularly useful application of NSE: `subset()`.

13.1.1 Exercises

1. One important feature of `deparse()` to be aware of when programming is that it can return multiple strings if the input is too long. For example, the following call produces a vector of length two:

```
g(a + b + c + d + e + f + g + h + i + j + k + l + m +
  n + o + p + q + r + s + t + u + v + w + x + y + z)
```

Why does this happen? Carefully read the documentation. Can you write a wrapper around `deparse()` so that it always returns a single string?

2. Why does `as.Date.default()` use `substitute()` and `deparse()`? Why does `pairwise.t.test()` use them? Read the source code.
3. `pairwise.t.test()` assumes that `deparse()` always returns a length one character vector. Can you construct an input that violates this expectation? What happens?
4. `f()`, defined above, just calls `substitute()`. Why can't we use it to define `g()`? In other words, what will the following code return? First make a prediction. Then run the code and think about the results.

```
f <- function(x) substitute(x)
g <- function(x) deparse(f(x))
g(1:10)
g(x)
g(x + y ^ 2 / z + exp(a * sin(b)))
```

13.2 Non-standard evaluation in subset

While printing out the code supplied to an argument value can be useful, we can actually do more with the unevaluated code. Take `subset()`, for example. It's a useful interactive shortcut for subsetting data frames: instead of repeating the name of data frame many times, you can save some typing:

```
sample_df <- data.frame(a = 1:5, b = 5:1, c = c(5, 3, 1, 4, 1))
```

```
subset(sample_df, a >= 4)
#>   a b c
#> 4 4 2 4
#> 5 5 1 1
# equivalent to:
# sample_df[sample_df$a >= 4, ]
```

```
subset(sample_df, b == c)
#>   a b c
#> 1 1 5 5
#> 5 5 1 1
# equivalent to:
# sample_df[sample_df$b == sample_df$c, ]
```

`subset()` is special because it implements different scoping rules: the expressions `a >= 4` or `b == c` are evaluated in the specified data frame rather than in the current or global environments. This is the essence of non-standard evaluation.

How does `subset()` work? We've already seen how to capture an argument's expression rather than its result, so we just need to figure out how to evaluate that expression in the right context. Specifically, we want `x` to be interpreted as `sample_df$x`, not `globalenv()$x`. To do this, we need `eval()`. This function takes an expression and evaluates it in the specified environment.

Before we can explore `eval()`, we need one more useful function: `quote()`. It captures an unevaluated expression like `substitute()`, but doesn't do any of the advanced transformations that can make `substitute()` confusing. `quote()` always returns its input as is:

```
quote(1:10)
#> 1:10
quote(x)
#> x
quote(x + y^2)
#> x + y^2
```

We need `quote()` to experiment with `eval()` because `eval()`'s first argument is an expression. So if you only provide one argument, it will evaluate the expression in the current environment. This makes `eval(quote(x))` exactly equivalent to `x`, regardless of what `x` is:

```
eval(quote(x <- 1))
eval(quote(x))
#> [1] 1

eval(quote(y))
#> Error: object 'y' not found
```

`quote()` and `eval()` are opposites. In the example below, each `eval()` peels off one layer of `quote()`'s.

```
quote(2 + 2)
#> 2 + 2
eval(quote(2 + 2))
#> [1] 4

quote(quote(2 + 2))
#> quote(2 + 2)
eval(quote(quote(2 + 2)))
#> 2 + 2
eval(eval(quote(quote(2 + 2))))
#> [1] 4
```

`eval()`'s second argument specifies the environment in which the code is executed:

```
x <- 10
eval(quote(x))
#> [1] 10
```



```
e <- new.env()
e$x <- 20
eval(quote(x), e)
#> [1] 20
```

Because lists and data frames bind names to values in a similar way to environments, `eval()`'s second argument need not be limited to an environment: it can also be a list or a data frame.

```
eval(quote(x), list(x = 30))
#> [1] 30
eval(quote(x), data.frame(x = 40))
#> [1] 40
```

This gives us one part of `subset()`:

```
eval(quote(a >= 4), sample_df)
#> [1] FALSE FALSE FALSE TRUE TRUE
eval(quote(b == c), sample_df)
#> [1] TRUE FALSE FALSE FALSE TRUE
```

A common mistake when using `eval()` is to forget to quote the first argument. Compare the results below:

```
a <- 10
eval(quote(a), sample_df)
#> [1] 1 2 3 4 5
eval(a, sample_df)
#> [1] 10

eval(quote(b), sample_df)
#> [1] 5 4 3 2 1
eval(b, sample_df)
#> Error: object 'b' not found
```

We can use `eval()` and `substitute()` to write `subset()`. We first capture the call representing the condition, then we evaluate it in the context of the data frame and, finally, we use the result for subsetting:

```
subset2 <- function(x, condition) {
  condition_call <- substitute(condition)
```

```

  r <- eval(condition_call, x)
  x[r, ]
}
subset2(sample_df, a >= 4)
#>   a b c
#>  4 4 2 4
#>  5 5 1 1

```

13.2.1 Exercises

1. Predict the results of the following lines of code:

```

eval(quote(eval(quote(eval(quote(2 + 2))))))
eval(eval(quote(eval(quote(eval(quote(2 + 2)))))))
quote(eval(quote(eval(quote(eval(quote(2 + 2)))))))

```

2. `subset2()` has a bug if you use it with a single column data frame. What should the following code return? How can you modify `subset2()` so it returns the correct type of object?

```

sample_df2 <- data.frame(x = 1:10)
subset2(sample_df2, x > 8)
#> [1] 9 10

```

3. The real subset function (`subset.data.frame()`) removes missing values in the condition. Modify `subset2()` to do the same: drop the offending rows.
4. What happens if you use `quote()` instead of `substitute()` inside of `subset2()`?
5. The second argument in `subset()` allows you to select variables. It treats variable names as if they were positions. This allows you to do things like `subset(mtcars, , -cyl)` to drop the cylinder variable, or `subset(mtcars, , disp:drat)` to select all the variables between `disp` and `drat`. How does this work? I've made this easier to understand by extracting it out into its own function.

```

select <- function(df, vars) {
  vars <- substitute(vars)
  var_pos <- setNames(as.list(seq_along(df)), names(df))
  pos <- eval(vars, var_pos)
  df[, pos, drop = FALSE]
}

```

```

}
select(mtcars, -cyl)

```

6. What does `evalq()` do? Use it to reduce the amount of typing for the examples above that use both `eval()` and `quote()`.

13.3 Scoping issues

It certainly looks like our `subset2()` function works. But since we're working with expressions instead of values, we need to test things more extensively. For example, the following applications of `subset2()` should all return the same value because the only difference between them is the name of a variable:

```

y <- 4
x <- 4
condition <- 4
condition_call <- 4

subset2(sample_df, a == 4)
#>   a b c
#> 4 4 2 4
subset2(sample_df, a == y)
#>   a b c
#> 4 4 2 4
subset2(sample_df, a == x)
#>      a b c
#> 1     1 5 5
#> 2     2 4 3
#> 3     3 3 1
#> 4     4 2 4
#> 5     5 1 1
#> NA    NA NA NA
#> NA.1  NA NA NA
subset2(sample_df, a == condition)
#> Error: object 'a' not found
subset2(sample_df, a == condition_call)
#> Warning: longer object length is not a multiple of shorter
#> object length

```

```
#> [1] a b c
#> <0 rows> (or 0-length row.names)
```

What went wrong? You can get a hint from the variable names I've chosen: they are all names of variables defined inside `subset2()`. If `eval()` can't find the variable inside the data frame (its second argument), it looks in the environment of `subset2()`. That's obviously not what we want, so we need some way to tell `eval()` where to look if it can't find the variables in the data frame.

The key is the third argument to `eval()`: `enclos`. This allows us to specify a parent (or enclosing) environment for objects that don't have one (like lists and data frames). If the binding is not found in `env`, `eval()` will next look in `enclos`, and then in the parents of `enclos`. `enclos` is ignored if `env` is a real environment. We want to look for `x` in the environment from which `subset2()` was called. In R terminology this is called the **parent frame** and is accessed with `parent.frame()`. This is an example of dynamic scope (http://en.wikipedia.org/wiki/Scope_%28programming%29#Dynamic_scoping): the values come from the location where the function was called, not where it was defined.

With this modification our function now works:

```
subset2 <- function(x, condition) {
  condition_call <- substitute(condition)
  r <- eval(condition_call, x, parent.frame())
  x[r, ]
}

x <- 4
subset2(sample_df, a == x)
#>   a b c
#> 4 4 2 4
```

Using `enclos` is just a shortcut for converting a list or data frame to an environment. We can get the same behaviour by using `list2env()`. It turns a list into an environment with an explicit parent:

```
subset2a <- function(x, condition) {
  condition_call <- substitute(condition)
  env <- list2env(x, parent = parent.frame())
  r <- eval(condition_call, env)
  x[r, ]
}
```

```
}

x <- 5
subset2a(sample_df, a == x)
#>   a b c
#>  5 5 1 1
```

13.3.1 Exercises

1. `plyr::arrange()` works similarly to `subset()`, but instead of selecting rows, it reorders them. How does it work? What does `substitute(order(...))` do? Create a function that does only that and experiment with it.
2. What does `transform()` do? Read the documentation. How does it work? Read the source code for `transform.data.frame()`. What does `substitute(list(...))` do?
3. `plyr::mutate()` is similar to `transform()` but it applies the transformations sequentially so that transformation can refer to columns that were just created:

```
df <- data.frame(x = 1:5)
transform(df, x2 = x * x, x3 = x2 * x)
plyr::mutate(df, x2 = x * x, x3 = x2 * x)
```

How does `mutate` work? What's the key difference between `mutate()` and `transform()`?

4. What does `with()` do? How does it work? Read the source code for `with.default()`. What does `within()` do? How does it work? Read the source code for `within.data.frame()`. Why is the code so much more complex than `with()`?

13.4 Calling from another function

Typically, computing on the language is most useful when functions are called directly by users and less useful when they are called by other functions. While `subset()` saves typing, it's actually difficult to use non-interactively. For example, imagine we want to create a function that

randomly reorders a subset of rows of data. A nice way to do that would be to compose a function that reorders with another that selects. Let's try that:

```
subset2 <- function(x, condition) {
  condition_call <- substitute(condition)
  r <- eval(condition_call, x, parent.frame())
  x[r, ]
}

scramble <- function(x) x[sample(nrow(x)), ]

subscramble <- function(x, condition) {
  scramble(subset2(x, condition))
}
```

But it doesn't work:

```
subscramble(sample_df, a >= 4)
# Error in eval(expr, envir, enclos) : object 'a' not found
traceback()
#> 5: eval(expr, envir, enclos)
#> 4: eval(condition_call, x, parent.frame()) at #3
#> 3: subset2(x, condition) at #1
#> 2: scramble(subset2(x, condition)) at #2
#> 1: subscramble(sample_df, a >= 4)
```

What's gone wrong? To figure it out, let us `debug()` `subset2()` and work through the code line-by-line:

```
debugonce(subset2)
subscramble(sample_df, a >= 4)
#> debugging in: subset2(x, condition)
#> debug at #1: {
#>   condition_call <- substitute(condition)
#>   r <- eval(condition_call, x, parent.frame())
#>   x[r, ]
#> }
n
#> debug at #2: condition_call <- substitute(condition)
n
#> debug at #3: r <- eval(condition_call, x, parent.frame())
```

```

r <- eval(condition_call, x, parent.frame())
#> Error in eval(expr, envir, enclos) : object 'a' not found
condition_call
#> condition
eval(condition_call, x)
#> Error in eval(expr, envir, enclos) : object 'a' not found
Q

```

Can you see what the problem is? `condition_call` contains the expression `condition`. So when we evaluate `condition_call` it also evaluates `condition`, which has the value `a >= 4`. However, this can't be computed because there's no object called `a` in the parent environment. But, if `a` were set in the global environment, even more confusing things can happen:

```

a <- 4
subscramble(sample_df, a == 4)
#>   a b c
#>  4 4 2 4
#>  3 3 3 1
#>  1 1 5 5
#>  5 5 1 1
#>  2 2 4 3

a <- c(1, 1, 4, 4, 4, 4)
subscramble(sample_df, a >= 4)
#>     a b c
#>  5   5 1 1
#> NA NA NA NA
#>  4   4 2 4
#>  3   3 3 1

```

This is an example of the general tension between functions that are designed for interactive use and functions that are safe to program with. A function that uses `substitute()` might reduce typing, but it can be difficult to call from another function.

As a developer, you should always provide an escape hatch: an alternative version of the function that uses standard evaluation. In this case, we could write a version of `subset2()` that takes an already quoted expression:

```

subset2_q <- function(x, condition) {
  r <- eval(condition, x, parent.frame())

```

```

  x[r, ]
}

```

Here I use the suffix `_q` to indicate that it takes a quoted expression. Most users won't need this function so the name can be a little longer.

We can then rewrite both `subset2()` and `subscramble()` to use `subset2_q()`:

```

subset2 <- function(x, condition) {
  subset2_q(x, substitute(condition))
}

subscramble <- function(x, condition) {
  condition <- substitute(condition)
  scramble(subset2_q(x, condition))
}

```

```

subscramble(sample_df, a >= 3)
#>   a b c
#> 5 5 1 1
#> 4 4 2 4
#> 3 3 3 1
subscramble(sample_df, a >= 3)
#>   a b c
#> 3 3 3 1
#> 5 5 1 1
#> 4 4 2 4

```

Base R functions tend to use a different sort of escape hatch. They often have an argument that turns off NSE. For example, `require()` has `character.only = TRUE`. I don't think it's a good idea to use an argument to change the behaviour of another argument because it makes function calls harder to understand.

13.4.1 Exercises

1. The following R functions all use NSE. For each, describe how it uses NSE, and read the documentation to determine its escape hatch.

- `rm()`

- `library()` and `require()`
 - `substitute()`
 - `data()`
 - `data.frame()`
2. Base functions `match.fun()`, `page()`, and `ls()` all try to automatically determine whether you want standard or non-standard evaluation. Each uses a different approach. Figure out the essence of each approach then compare and contrast.
 3. Add an escape hatch to `plyr::mutate()` by splitting it into two functions. One function should capture the unevaluated inputs. The other should take a data frame and list of expressions and perform the computation.
 4. What's the escape hatch for `ggplot2::aes()`? What about `plyr::()`? What do they have in common? What are the advantages and disadvantages of their differences?
 5. The version of `subset2_q()` I presented is a simplification of real code. Why is the following version better?

```
subset2_q <- function(x, cond, env = parent.frame()) {
  r <- eval(cond, x, env)
  x[r, ]
}
```

Rewrite `subset2()` and `subscramble()` to use this improved version.

13.5 Substitute

Most functions that use non-standard evaluation provide an escape hatch. But what happens if you want to call a function that doesn't have one? For example, imagine you want to create a lattice graphic given the names of two variables:

```
library(lattice)
xyplot(mpg ~ disp, data = mtcars)

x <- quote(mpg)
```

```
y <- quote(displ)
xyplot(x ~ y, data = mtcars)
#> Error: object of type 'symbol' is not subsettable
```

We might turn to `substitute()` and use it for another purpose: to modify an expression. Unfortunately `substitute()` has a feature that makes modifying calls interactively a bit of a pain. When run from the global environment, it never does substitutions: in fact, in this situation it behaves just like `quote()`:

```
a <- 1
b <- 2
substitute(a + b + z)
#> a + b + z
```

However, if you run it inside a function, `substitute()` does substitute and leaves everything else as is:

```
f <- function() {
  a <- 1
  b <- 2
  substitute(a + b + z)
}
f()
#> 1 + 2 + z
```

To make it easier to experiment with `substitute()`, `pryr` provides the `subs()` function. It works exactly the same way as `substitute()` except it has a shorter name and it works in the global environment. These two features make experimentation easier:

```
a <- 1
b <- 2
subs(a + b + z)
#> 1 + 2 + z
```

The second argument (of both `subs()` and `substitute()`) can override the use of the current environment, and provide an alternative via a list of name-value pairs. The following example uses this technique to show some variations on substituting a string, variable name, or function call:

```
subs(a + b, list(a = "y"))
#> "y" + b
subs(a + b, list(a = quote(y)))
#> y + b
subs(a + b, list(a = quote(y())))
#> y() + b
```

Remember that every action in R is a function call, so we can also replace `+` with another function:

```
subs(a + b, list("+" = quote(f)))
#> f(a, b)
subs(a + b, list("+" = quote(`*`)))
#> a * b
```

You can also make nonsense code:

```
subs(y <- y + 1, list(y = 1))
#> 1 <- 1 + 1
```

Formally, substitution takes place by examining all the names in the expression. If the name refers to:

1. an ordinary variable, it's replaced by the value of the variable.
2. a promise (a function argument), it's replaced by the expression associated with the promise.
3. ..., it's replaced by the contents of ...

Otherwise it's left as is.

We can use this to create the right call to `xyplot()`:

```
x <- quote(mpg)
y <- quote(displ)
subs(xyplot(x ~ y, data = mtcars))
#> xyplot(mpg ~ displ, data = mtcars)
```

It's even simpler inside a function, because we don't need to explicitly quote the `x` and `y` variables (rule 2 above):

```
xyplot2 <- function(x, y, data = data) {  
  substitute(xyplot(x ~ y, data = data))  
}  
xyplot2(mpg, disp, data = mtcars)  
#> xyplot(mpg ~ disp, data = mtcars)
```

If we include `...` in the call to `substitute`, we can add additional arguments to the call:

```
xyplot3 <- function(x, y, ...) {  
  substitute(xyplot(x ~ y, ...))  
}  
xyplot3(mpg, disp, data = mtcars, col = "red", aspect = "xy")  
#> xyplot(mpg ~ disp, data = mtcars, col = "red", aspect = "xy")
```

To create the plot, we'd then `eval()` this call.

13.5.1 Adding an escape hatch to `substitute`

`substitute()` is itself a function that uses non-standard evaluation and doesn't have an escape hatch. This means we can't use `substitute()` if we already have an expression saved in a variable:

```
x <- quote(a + b)  
substitute(x, list(a = 1, b = 2))  
#> x
```

Although `substitute()` doesn't have a built-in escape hatch, we can use the function itself to create one:

```
substitute_q <- function(x, env) {  
  call <- substitute(substitute(y, env), list(y = x))  
  eval(call)  
}  
  
x <- quote(a + b)  
substitute_q(x, list(a = 1, b = 2))  
#> 1 + 2
```

The implementation of `substitute_q()` is short, but deep. Let's work through the example above: `substitute_q(x, list(a = 1, b = 2))`. It's

a little tricky because `substitute()` uses NSE so we can't use the usual technique of working through the parentheses inside-out.

1. First `substitute(substitute(y, env), list(y = x))` is evaluated. The expression `substitute(y, env)` is captured and `y` is replaced by the value of `x`. Because we've put `x` inside a list, it will be evaluated and the rules of `substitute` will replace `y` with its value. This yields the expression `substitute(a + b, env)`
2. Next we evaluate that expression inside the current function. `substitute()` evaluates its first argument, and looks for name value pairs in `env`. Here, it evaluates as `list(a = 1, b = 2)`. Since these are both values (not promises), the result will be `1 + 2`

A slightly more rigorous version of `substitute_q()` is provided by the `pryr` package.

13.5.2 Capturing unevaluated ...

Another useful technique is to capture all of the unevaluated expressions in Base R functions do this in many ways, but there's one technique that works well across a wide variety of situations:

```
dots <- function(...) {
  eval(substitute(alist(...)))
}
```

This uses the `alist()` function which simply captures all its arguments. This function is the same as `pryr::dots()`. `Pryr` also provides `pryr::named_dots()`, which, by using deparsed expressions as default names, ensures that all arguments are named (just like `data.frame()`).

13.5.3 Exercises

1. Use `subs()` to convert the LHS to the RHS for each of the following pairs:
 - `a + b + c -> a * b * c`
 - `f(g(a, b), c) -> (a + b) * c`
 - `f(a < b, c, d) -> if (a < b) c else d`

2. For each of the following pairs of expressions, describe why you can't use `subs()` to convert one to the other.
 - $a + b + c \rightarrow a + b * c$
 - $f(a, b) \rightarrow f(a, b, c)$
 - $f(a, b, c) \rightarrow f(a, b)$
3. How does `pryr::named_dots()` work? Read the source.

13.6 The downsides of non-standard evaluation

The biggest downside of NSE is that functions that use it are no longer referentially transparent ([http://en.wikipedia.org/wiki/Referential_transparency_\(computer_science\)](http://en.wikipedia.org/wiki/Referential_transparency_(computer_science))). A function is **referentially transparent** if you can replace its arguments with their values and its behaviour doesn't change. For example, if a function, `f()`, is referentially transparent and both `x` and `y` are 10, then `f(x)`, `f(y)`, and `f(10)` will all return the same result. Referentially transparent code is easier to reason about because the names of objects don't matter, and because you can always work from the innermost parentheses outwards.

There are many important functions that by their very nature are not referentially transparent. Take the assignment operator. You can't take `a <- 1` and replace `a` by its value and get the same behaviour. This is one reason that people usually write assignments at the top-level of functions. It's hard to reason about code like this:

```
a <- 1
b <- 2
if ((b <- a + 1) > (a <- b - 1)) {
  b <- b + 2
}
```

Using NSE prevents a function from being referentially transparent. This makes the mental model needed to correctly predict the output much more complicated. So, it's only worthwhile to use NSE if there is significant gain. For example, `library()` and `require()` can be called either with or without quotes, because internally they use `deparse(substitute(x))` plus some other tricks. This means that these two lines do exactly the same thing:

```
library(ggplot2)
library("ggplot2")
```

Things start to get complicated if the variable is associated with a value. What package will this load?

```
ggplot2 <- "plyr"
library(ggplot2)
```

There are a number of other R functions that work in this way, like `ls()`, `rm()`, `data()`, `demo()`, `example()`, and `vignette()`. To me, eliminating two keystrokes is not worth the loss of referential transparency, and I don't recommend you use NSE for this purpose.

One situation where non-standard evaluation is worthwhile is `data.frame()`. If not explicitly supplied, it uses the input to automatically name the output variables:

```
x <- 10
y <- "a"
df <- data.frame(x, y)
names(df)
#> [1] "x" "y"
```

I think it's worthwhile because it eliminates a lot of redundancy in the common scenario when you're creating a data frame from existing variables. More importantly, if needed, it's easy to override this behaviour by supplying names for each variable.

Non-standard evaluation allows you to write functions that are extremely powerful. However, they are harder to understand and to program with. As well as always providing an escape hatch, carefully consider both the costs and benefits of NSE before using it in a new domain.

13.6.1 Exercises

1. What does the following function do? What's the escape hatch? Do you think that this is an appropriate use of NSE?

```
nl <- function(...) {
  dots <- named_dots(...)
  lapply(dots, eval, parent.frame())
}
```

2. Instead of relying on promises, you can use formulas created with `~` to explicitly capture an expression and its environment. What are the advantages and disadvantages of making quoting explicit? How does it impact referential transparency?
3. Read the standard non-standard evaluation rules found at <http://developer.r-project.org/nonstandard-eval.pdf>.

14

Expressions

In Chapter 13, you learned the basics of accessing and evaluating the expressions underlying computation in R. In this chapter, you'll learn how to manipulate these expressions with code. You're going to learn how to metaprogram: how to create programs with other programs!

Outline

- Section 14.1 begins with a deep dive into the structure of expressions. You'll learn about the four components of an expression: constants, names, calls, and pairlists.
- Section 14.2 goes into further details about names.
- Section 14.3 gives more details about calls.
- Section 14.4 takes a minor detour to discuss some common uses of calls in base R.
- Section 14.5 completes the discussion of the four major components of an expression, and shows how you can create functions from their component pieces.
- Section 14.6 discusses how to convert back and forth between expressions and text.
- Section 14.7 concludes the chapter, combining everything you've learned about writing functions that can compute on and modify arbitrary R code.

Prerequisites

Thoroughout this chapter we're going to use tools from the `pryr` package to help see what's going on. If you don't already have it, install it by running `install.packages("pryr")`.

14.1 Structure of expressions

To compute on the language, we first need to understand the structure of the language. That will require some new vocabulary, some new tools, and some new ways of thinking about R code. The first thing you'll need to understand is the distinction between an operation and a result:

```
x <- 4
y <- x * 10
y
#> [1] 40
```

We want to distinguish the action of multiplying `x` by 10 and assigning that result to `y` from the actual result (40). As we've seen in the previous chapter, we can capture the action with `quote()`:

```
z <- quote(y <- x * 10)
z
#> y <- x * 10
```

`quote()` returns an **expression**: an object that represents an action that can be performed by R. (Unfortunately `expression()` does not return an expression in this sense. Instead, it returns something more like a list of expressions. See Section 14.6 for more details.)

An expression is also called an abstract syntax tree (AST) because it represents the hierarchical tree structure of the code. We'll use `pryr::ast()` to see this more clearly:

```
ast(y <- x * 10)
#> \- ()
#>   \- '<-'
#>     \- 'y
#>       \- ()
#>         \- '*'
#>           \- 'x
#>             \- 10
```

There are four possible components of an expression: constants, names, calls, and pairlists.

- **constants** are length one atomic vectors, like "a" or 10. `ast()` displays them as is.

```
ast("a")
#> \-  "a"
ast(1)
#> \-  1
ast(1L)
#> \-  1L
ast(TRUE)
#> \-  TRUE
```

Quoting a constant returns it unchanged:

```
identical(1, quote(1))
#> [1] TRUE
identical("test", quote("test"))
#> [1] TRUE
```

- **names**, or symbols, represent the name of an object rather than its value. `ast()` prefixes names with a backtick.

```
ast(x)
#> \-  `x`
ast(mean)
#> \-  `mean`
ast(`an unusual name`)
#> \-  `an unusual name`
```

- **calls** represent the action of calling a function. Like lists, calls are recursive: they can contain constants, names, pairlists, and other calls. `ast()` prints `()` and then lists the children. The first child is the function that is called, and the remaining children are the function's arguments.

```
ast(f())
#> \-  ()
#> \-  `f`
ast(f(1, 2))
#> \-  ()
#> \-  `f`
#> \-  1
#> \-  2
ast(f(a, b))
#> \-  ()
```

```
#> \- `f`
#> \- `a`
#> \- `b`
ast(f(g(), h(1, a)))
#> \- ()
#> \- `f`
#> \- ()
#> \- `g`
#> \- ()
#> \- `h`
#> \- 1
#> \- `a`
```

As mentioned in Section 6.3, even things that don't look like function calls still have this hierarchical structure:

```
ast(a + b)
#> \- ()
#> \- `+`
#> \- `a`
#> \- `b`
ast(if (x > 1) x else 1/x)
#> \- ()
#> \- `if`
#> \- ()
#> \- `>`
#> \- `x`
#> \- 1
#> \- `x`
#> \- ()
#> \- `/`
#> \- 1
#> \- `x`
```

- **pairlists**, short for dotted pair lists, are a legacy of R's past. They are only used in one place: the formal arguments of a function. `ast()` prints `[]` at the top-level of a pairlist. Like calls, pairlists are also recursive and can contain constants, names, and calls.

```
ast(function(x = 1, y) x)
#> \- ()
#> \- `function`
#> \- []
#> \ x = 1
```

```

#>      \ y ='MISSING
#>      \- 'x
#>      \- <srcref>
ast(function(x = 1, y = x * 2) {x / y})
#> \- ()
#>      \- 'function
#>      \- []
#>          \ x = 1
#>          \ y =( )
#>              \- '*'
#>                  \- 'x
#>                      \- 2
#>      \- ()
#>          \- '{
#>              \- ()
#>                  \- '/'
#>                      \- 'x
#>                          \- 'y
#>      \- <srcref>

```

Note that `str()` does not follow these naming conventions when describing objects. Instead, it describes names as symbols and calls as language objects:

```

str(quote(a))
#> symbol a
str(quote(a + b))
#> language a + b

```

Using low-level functions, it is possible to create call trees that contain objects other than constants, names, calls, and pairlists. The following example uses `substitute()` to insert a data frame into a call tree. This is a bad idea, however, because the object does not print correctly: the printed call looks like it should return “list” but when evaluated, it returns “data.frame”.

```

class_df <- substitute(class(df), list(df = data.frame(x = 10)))
class_df
#> class(list(x = 10))
eval(class_df)
#> [1] "data.frame"

```

Together these four components define the structure of all R code. They are explained in more detail in the following sections.

14.1.1 Exercises

1. There's no existing base function that checks if an element is a valid component of an expression (i.e., it's a constant, name, call, or pairlist). Implement one by guessing the names of the "is" functions for calls, names, and pairlists.
2. `pryr::ast()` uses non-standard evaluation. What's its escape hatch to standard evaluation?
3. What does the call tree of an if statement with multiple else conditions look like?
4. Compare `ast(x + y %+% z)` to `ast(x ^ y %+% z)`. What do they tell you about the precedence of custom infix functions?
5. Why can't an expression contain an atomic vector of length greater than one? Which one of the six types of atomic vector can't appear in an expression? Why?

14.2 Names

Typically, we use `quote()` to capture names. You can also convert a string to a name with `as.name()`. However, this is most useful only when your function receives strings as input. Otherwise it involves more typing than using `quote()`. (You can use `is.name()` to test if an object is a name.)

```
as.name("name")
#> name
identical(quote(name), as.name("name"))
#> [1] TRUE
```

```
is.name("name")
#> [1] FALSE
is.name(quote(name))
#> [1] TRUE
is.name(quote(f(name)))
#> [1] FALSE
```

(Names are also called symbols. `as.symbol()` and `is.symbol()` are identical to `as.name()` and `is.name()`.)

Names that would otherwise be invalid are automatically surrounded by backticks:

```
as.name("a b")
#> `a b`
as.name("if")
#> `if`
```

There's one special name that needs a little extra discussion: the empty name. It is used to represent missing arguments. This object behaves strangely. You can't bind it to a variable. If you do, it triggers an error about missing arguments. It's only useful if you want to programmatically create a function with missing arguments.

```
f <- function(x) 10
formals(f)$x
is.name(formals(f)$x)
#> [1] TRUE
as.character(formals(f)$x)
#> [1] ""
```

```
missing_arg <- formals(f)$x
# Doesn't work!
is.name(missing_arg)
#> Error: argument "missing_arg" is missing, with no default
```

To explicitly create it when needed, call `quote()` with a named argument:

```
quote(expr =)
```

14.2.1 Exercises

1. You can use `formals()` to both get and set the arguments of a function. Use `formals()` to modify the following function so that the default value of `x` is missing and `y` is 10.

```
g <- function(x = 20, y) {
  x + y
}
```

2. Write an equivalent to `get()` using `as.name()` and `eval()`. Write an equivalent to `assign()` using `as.name()`, `substitute()`, and `eval()`. (Don't worry about the multiple ways of choosing an environment; assume that the user supplies it explicitly.)

14.3 Calls

A call is very similar to a list. It has `length`, `[[` and `[` methods, and is recursive because calls can contain other calls. The first element of the call is the function that gets called. It's usually the *name* of a function:

```
x <- quote(read.csv("important.csv", row.names = FALSE))
x[[1]]
#> read.csv
is.name(x[[1]])
#> [1] TRUE
```

But it can also be another call:

```
y <- quote(add(10)(20))
y[[1]]
#> add(10)
is.call(y[[1]])
#> [1] TRUE
```

The remaining elements are the arguments. They can be extracted by name or by position.

```
x <- quote(read.csv("important.csv", row.names = FALSE))
x[[2]]
#> [1] "important.csv"
x$row.names
#> [1] FALSE
names(x)
#> [1] "" "" "row.names"
```


The length of a call minus 1 gives the number of arguments:

```
length(x) - 1
#> [1] 2
```

14.3.1 Modifying a call

You can add, modify, and delete elements of the call with the standard replacement operators, `$<-` and `[[<-`:

```
y <- quote(read.csv("important.csv", row.names = FALSE))
y$row.names <- TRUE
y$col.names <- FALSE
y
#> read.csv("important.csv", row.names = TRUE, col.names = FALSE)

y[[2]] <- quote(paste0(filename, ".csv"))
y[[4]] <- NULL
y
#> read.csv(paste0(filename, ".csv"), row.names = TRUE)

y$sep <- ","
y
#> read.csv(paste0(filename, ".csv"), row.names = TRUE, sep = ",")
```

Calls also support the `[]` method. But use it with care. Removing the first element is unlikely to create a useful call.

```
x[-3] # remove the second argument
#> read.csv("important.csv")
x[-1] # remove the function name - but it's still a call!
#> "important.csv"(row.names = FALSE)
x
#> read.csv("important.csv", row.names = FALSE)
```

If you want a list of the unevaluated arguments (expressions), use explicit coercion:

```
# A list of the unevaluated arguments
as.list(x[-1])
```

```
#> [[1]]
#> [1] "important.csv"
#>
#> $row.names
#> [1] FALSE
```

Generally speaking, because R's function calling semantics are so flexible, getting or setting arguments by position is dangerous. For example, even though the values at each position are different, the following three calls all have the same effect:

```
m1 <- quote(read.delim("data.txt", sep = "|"))
m2 <- quote(read.delim(s = "|", "data.txt"))
m3 <- quote(read.delim(file = "data.txt", , "|"))
```

To work around this problem, `pryr` provides `standardise_call()`. It uses the base `match.call()` function to convert all positional arguments to named arguments:

```
standardise_call(m1)
#> read.delim(file = "data.txt", sep = "|")
standardise_call(m2)
#> read.delim(file = "data.txt", sep = "|")
standardise_call(m3)
#> read.delim(file = "data.txt", sep = "|")
```

14.3.2 Creating a call from its components

To create a new call from its components, you can use `call()` or `as.call()`. The first argument to `call()` is a string which gives a function name. The other arguments are expressions that represent the arguments of the call.

```
call(":", 1, 10)
#> 1:10
call("mean", quote(1:10), na.rm = TRUE)
#> mean(1:10, na.rm = TRUE)
```

`as.call()` is a minor variant of `call()` that takes a single list as input. The first element is a name or call. The subsequent elements are the arguments.

```
as.call(list(quote(mean), quote(1:10)))
#> mean(1:10)
as.call(list(quote(adder(10)), 20))
#> adder(10)(20)
```

14.3.3 Exercises

1. The following two calls look the same, but are actually different:

```
(a <- call("mean", 1:10))
#> mean(1:10)
(b <- call("mean", quote(1:10)))
#> mean(1:10)
identical(a, b)
#> [1] FALSE
```

What's the difference? Which one should you prefer?

2. Implement a pure R version of `do.call()`.
3. Concatenating a call and an expression with `c()` creates a list. Implement `concat()` so that the following code works to combine a call and an additional argument.

```
concat(quote(f), a = 1, b = quote(mean(a)))
#> f(a = 1, b = mean(a))
```

4. Since `list()`s don't belong in expressions, we could create a more convenient call constructor that automatically combines lists into the arguments. Implement `make_call()` so that the following code works.

```
make_call(quote(mean), list(quote(x), na.rm = TRUE))
#> mean(x, na.rm = TRUE)
make_call(quote(mean), quote(x), na.rm = TRUE)
#> mean(x, na.rm = TRUE)
```

5. How does `mode<-` work? How does it use `call()`?
6. Read the source for `pryr::standardise_call()`. How does it work? Why is `is.primitive()` needed?
7. `standardise_call()` doesn't work so well for the following calls. Why?

```

standardise_call(quote(mean(1:10, na.rm = TRUE)))
#> mean(x = 1:10, na.rm = TRUE)
standardise_call(quote(mean(n = T, 1:10)))
#> mean(x = 1:10, n = T)
standardise_call(quote(mean(x = 1:10, , TRUE)))
#> mean(x = 1:10, , TRUE)

```

8. Read the documentation for `pryr::modify_call()`. How do you think it works? Read the source code.
9. Use `ast()` and experimentation to figure out the three arguments in an `if()` call. Which components are required? What are the arguments to the `for()` and `while()` calls?

14.4 Capturing the current call

Many base R functions use the current call: the expression that caused the current function to be run. There are two ways to capture a current call:

- `sys.call()` captures exactly what the user typed.
- `match.call()` makes a call that only uses named arguments. It's like automatically calling `pryr::standardise_call()` on the result of `sys.call()`

The following example illustrates the difference between the two:

```

f <- function(abc = 1, def = 2, ghi = 3) {
  list(sys = sys.call(), match = match.call())
}
f(d = 2, 2)
#> $sys
#> f(d = 2, 2)
#>
#> $match
#> f(abc = 2, def = 2)

```

Modelling functions often use `match.call()` to capture the call used to create the model. This makes it possible to `update()` a model, re-fitting

the model after modifying some of original arguments. Here's an example of `update()` in action:

```
mod <- lm(mpg ~ wt, data = mtcars)
update(mod, formula = . ~ . + cyl)
#>
#> Call:
#> lm(formula = mpg ~ wt + cyl, data = mtcars)
#>
#> Coefficients:
#> (Intercept)          wt          cyl
#>      39.69      -3.19      -1.51
```

How does `update()` work? We can rewrite it using some tools from `pryr` to focus on the essence of the algorithm.

```
update_call <- function (object, formula., ...) {
  call <- object$call

  # Use update.formula to deal with formulas like . ~ .
  if (!missing(formula.)) {
    call$formula <- update.formula(formula(object), formula.)
  }

  modify_call(call, dots(...))
}
update_model <- function(object, formula., ...) {
  call <- update_call(object, formula., ...)
  eval(call, parent.frame())
}
update_model(mod, formula = . ~ . + cyl)
#>
#> Call:
#> lm(formula = mpg ~ wt + cyl, data = mtcars)
#>
#> Coefficients:
#> (Intercept)          wt          cyl
#>      39.69      -3.19      -1.51
```

The original `update()` has an `evaluate` argument that controls whether the function returns the call or the result. But I think it's better, on principle, that a function returns only one type of object, rather than different types depending on the function's arguments.

This rewrite also allows us to fix a small bug in `update()`: it re-evaluates the call in the global environment, when what we really want is to re-evaluate it in the environment where the model was originally fit — in the formula.

```
f <- function() {
  n <- 3
  lm(mpg ~ poly(wt, n), data = mtcars)
}
mod <- f()
update(mod, data = mtcars)
#> Error: object 'n' not found

update_model <- function(object, formula., ...) {
  call <- update_call(object, formula., ...)
  eval(call, environment(formula(object)))
}
update_model(mod, data = mtcars)
#>
#> Call:
#> lm(formula = mpg ~ poly(wt, n), data = mtcars)
#>
#> Coefficients:
#> (Intercept) poly(wt, n)1 poly(wt, n)2 poly(wt, n)3
#>          20.091      -29.116          8.636          0.275
```

This is an important principle to remember: if you want to re-run code captured with `match.call()`, you also need to capture the environment in which it was evaluated, usually the `parent.frame()`. The downside to this is that capturing the environment also means capturing any large objects which happen to be in that environment, which prevents their memory from being released. This topic is explored in more detail in Section 18.2.

Some base R functions use `match.call()` where it's not necessary. For example, `write.csv()` captures the call to `write.csv()` and mangles it to call `write.table()` instead:

```
write.csv <- function(...) {
  Call <- match.call(expand.dots = TRUE)
  for (arg in c("append", "col.names", "sep", "dec", "qmethod")) {
    if (!is.null(Call[[arg]])) {
      warning(gettextf("attempt to set '%s' ignored", arg))
    }
  }
}
```

```

    }
  }
  rn <- eval.parent(Call$row.names)
  Call$append <- NULL
  Call$col.names <- if (is.logical(rn) && !rn) TRUE else NA
  Call$sep <- ", "
  Call$dec <- "."
  Call$qmethod <- "double"
  Call[[1L]] <- as.name("write.table")
  eval.parent(Call)
}

```

To fix this, we could implement `write.csv()` using regular function call semantics:

```

write.csv <- function(x, file = "", sep = ",", qmethod = "double",
  ...) {
  write.table(x = x, file = file, sep = sep, qmethod = qmethod,
    ...)
}

```

This is much easier to understand: it's just calling `write.table()` with different defaults. This also fixes a subtle bug in the original `write.csv()`: `write.csv(mtcars, row = FALSE)` raises an error, but `write.csv(mtcars, row.names = FALSE)` does not. The lesson here is that it's always better to solve a problem with the simplest tool possible.

14.4.1 Exercises

1. Compare and contrast `update_model()` with `update.default()`.
2. Why doesn't `write.csv(mtcars, "mtcars.csv", row = FALSE)` work? What property of argument matching has the original author forgotten?
3. Rewrite `update.formula()` to use R code instead of C code.
4. Sometimes it's necessary to uncover the function that called the function that called the current function (i.e., the grand-parent, not the parent). How can you use `sys.call()` or `match.call()` to find this function?

14.5 Pairlists

Pairlists are a holdover from R's past. They behave identically to lists, but have a different internal representation (as a linked list rather than a vector). Pairlists have been replaced by lists everywhere except in function arguments.

The only place you need to care about the difference between a list and a pairlist is if you're going to construct functions by hand. For example, the following function allows you to construct a function from its component pieces: a list of formal arguments, a body, and an environment. The function uses `as.pairlist()` to ensure that the `function()` has the pairlist of `args` it needs.

```
make_function <- function(args, body, env = parent.frame()) {
  args <- as.pairlist(args)

  eval(call("function", args, body), env)
}
```

This function is also available in `pryr`, where it does a little extra checking of arguments. `make_function()` is best used in conjunction with `alist()`, the argument list function. `alist()` doesn't evaluate its arguments so that `alist(x = a)` is shorthand for `list(x = quote(a))`.

```
add <- make_function(alist(a = 1, b = 2), quote(a + b))
add(1)
#> [1] 3
add(1, 2)
#> [1] 3

# To have an argument with no default, you need an explicit =
make_function(alist(a = , b = a), quote(a + b))
#> function (a, b = a)
#> a + b
# To take `...` as an argument put it on the LHS of =
make_function(alist(a = , b = , ... =), quote(a + b))
#> function (a, b, ...)
#> a + b
```

`make_function()` has one advantage over using closures to construct functions: with it, you can easily read the source code. For example:

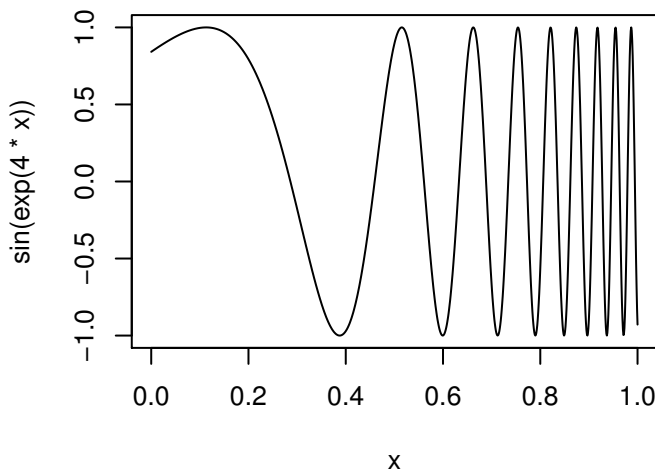

```

adder <- function(x) {
  make_function(alist(y =), substitute({x + y}), parent.frame())
}
adder(10)
#> function (y)
#> {
#>     10 + y
#> }

```

One useful application of `make_function()` is in functions like `curve()`. `curve()` allows you to plot a mathematical function without creating an explicit R function:

```
curve(sin(exp(4 * x)), n = 1000)
```



Here `x` is a pronoun. `x` doesn't represent a single concrete value, but is instead a placeholder that varies over the range of the plot. One way to implement `curve()` would be with `make_function()`:

```

curve2 <- function(expr, xlim = c(0, 1), n = 100,
  env = parent.frame()) {
  f <- make_function(alist(x = ), substitute(expr), env)

  x <- seq(xlim[1], xlim[2], length = n)
  y <- f(x)

```

```
  plot(x, y, type = "l", ylab = deparse(substitute(expr)))
}
```

Functions that use a pronoun are called anaphoric ([http://en.wikipedia.org/wiki/Anaphora_\(linguistics\)](http://en.wikipedia.org/wiki/Anaphora_(linguistics))) functions. They are used in Arc (<http://www.arcfn.com/doc/anaphoric.html>) (a lisp like language), Perl (http://www.perlmonks.org/index.pl?node_id=666047), and Clojure (<http://amalloy.hubpages.com/hub/Unhygenic-anaphoric-Clojure-macros-for-fun-and-profit>).

14.5.1 Exercises

1. How are `alist(a)` and `alist(a =)` different? Think about both the input and the output.
2. Read the documentation and source code for `pryr::partial()`. What does it do? How does it work? Read the documentation and source code for `pryr::unenclose()`. What does it do and how does it work?
3. The actual implementation of `curve()` looks more like

```
curve3 <- function(expr, xlim = c(0, 1), n = 100,
                  env = parent.frame()) {
  env2 <- new.env(parent = env)
  env2$x <- seq(xlim[1], xlim[2], length = n)

  y <- eval(substitute(expr), env2)
  plot(env2$x, y, type = "l",
       ylab = deparse(substitute(expr)))
}
```

How does this approach differ from `curve2()` defined above?

14.6 Parsing and deparsing

Sometimes code is represented as a string, rather than as an expression. You can convert a string to an expression with `parse()`. `parse()` is the opposite of `deparse()`: it takes a character vector and returns an expression object. The primary use of `parse()` is parsing files of code to

disk, so the first argument is a file path. Note that if you have code in a character vector, you need to use the `text` argument:

```
z <- quote(y <- x * 10)
deparse(z)
#> [1] "y <- x * 10"

parse(text = deparse(z))
#> expression(y <- x * 10)
```

Because there might be many top-level calls in a file, `parse()` doesn't return just a single expression. Instead, it returns an expression object, which is essentially a list of expressions:

```
exp <- parse(text = c("
  x <- 4
  x
  5
"))
length(exp)
#> [1] 3
typeof(exp)
#> [1] "expression"

exp[[1]]
#> x <- 4
exp[[2]]
#> x
```

You can create expression objects by hand with `expression()`, but I wouldn't recommend it. There's no need to learn about this esoteric data structure if you already know how to use expressions.

With `parse()` and `eval()`, it's possible to write a simple version of `source()`. We read in the file from disk, `parse()` it and then `eval()` each component in a specified environment. This version defaults to a new environment, so it doesn't affect existing objects. `source()` invisibly returns the result of the last expression in the file, so `simple_source()` does the same.

```
simple_source <- function(file, envir = new.env()) {
  stopifnot(file.exists(file))
```

```

stopifnot(is.environment(envir))

lines <- readLines(file, warn = FALSE)
exprs <- parse(text = lines)

n <- length(exprs)
if (n == 0L) return(invisible())

for (i in seq_len(n - 1)) {
  eval(exprs[i], envir)
}
invisible(eval(exprs[n], envir))
}

```

The real `source()` is considerably more complicated because it can echo input and output, and also has many additional settings to control behaviour.

14.6.1 Exercises

1. What are the differences between `quote()` and `expression()`?
2. Read the help for `deparse()` and construct a call that `deparse()` and `parse()` do not operate symmetrically on.
3. Compare and contrast `source()` and `sys.source()`.
4. Modify `simple_source()` so it returns the result of *every* expression, not just the last one.
5. The code generated by `simple_source()` lacks source references. Read the source code for `sys.source()` and the help for `srcfilecopy()`, then modify `simple_source()` to preserve source references. You can test your code by sourcing a function that contains a comment. If successful, when you look at the function, you'll see the comment and not just the source code.

14.7 Walking the AST with recursive functions

It's easy to modify a single call with `substitute()` or `pryr::modify_call()`. For more complicated tasks we need to work directly with the AST.

The base `codetools` package provides some useful motivating examples of how we can do this:

- `findGlobals()` locates all global variables used by a function. This can be useful if you want to check that your function doesn't inadvertently rely on variables defined in their parent environment.
- `checkUsage()` checks for a range of common problems including unused local variables, unused parameters, and the use of partial argument matching.

To write functions like `findGlobals()` and `checkUsage()`, we'll need a new tool. Because expressions have a tree structure, using a recursive function would be the natural choice. The key to doing that is getting the recursion right. This means making sure that you know what the base case is and figuring out how to combine the results from the recursive case. For calls, there are two base cases (atomic vectors and names) and two recursive cases (calls and pairlists). This means that a function for working with expressions will look like:

```
recurse_call <- function(x) {  
  if (is.atomic(x)) {  
    # Return a value  
  } else if (is.name(x)) {  
    # Return a value  
  } else if (is.call(x)) {  
    # Call recurse_call recursively  
  } else if (is.pairlist(x)) {  
    # Call recurse_call recursively  
  } else {  
    # User supplied incorrect input  
    stop("Don't know how to handle type ", typeof(x),  
         call. = FALSE)  
  }  
}
```

14.7.1 Finding F and T

We'll start simple with a function that determines whether a function uses the logical abbreviations T and F. Using T and F is generally considered to be poor coding practice, and is something that R CMD check will warn about. Let's first compare the AST for T vs. TRUE:

```
ast(TRUE)
#> \- TRUE
ast(T)
#> \- `T`
```

TRUE is parsed as a logical vector of length one, while T is parsed as a name. This tells us how to write our base cases for the recursive function: while an atomic vector will never be a logical abbreviation, a name might, so we'll need to test for both T and F. The recursive cases can be combined because they do the same thing in both cases: they recursively call `logical_abbr()` on each element of the object.

```
logical_abbr <- function(x) {
  if (is.atomic(x)) {
    FALSE
  } else if (is.name(x)) {
    identical(x, quote(T)) || identical(x, quote(F))
  } else if (is.call(x) || is.pairlist(x)) {
    for (i in seq_along(x)) {
      if (logical_abbr(x[[i]])) return(TRUE)
    }
    FALSE
  } else {
    stop("Don't know how to handle type ", typeof(x),
        call. = FALSE)
  }
}
```

```
logical_abbr(quote(TRUE))
#> [1] FALSE
logical_abbr(quote(T))
#> [1] TRUE
logical_abbr(quote(mean(x, na.rm = T)))
#> [1] TRUE
logical_abbr(quote(function(x, na.rm = T) FALSE))
#> [1] TRUE
```

14.7.2 Finding all variables created by assignment

`logical_abbr()` is very simple: it only returns a single TRUE or FALSE. The next task, listing all variables created by assignment, is a little more com-

plicated. We'll start simply, and then make the function progressively more rigorous.

Again, we start by looking at the AST for assignment:

```
ast(x <- 10)
#> \- ()
#>   \- `<-
#>     \- `x
#>       \- 10
```

Assignment is a call where the first element is the name `<-`, the second is the object the name is assigned to, and the third is the value to be assigned. This makes the base cases simple: constants and names don't create assignments, so they return `NULL`. The recursive cases aren't too hard either. We `lapply()` over pairlists and over calls to functions other than `<-`.

```
find_assign <- function(x) {
  if (is.atomic(x) || is.name(x)) {
    NULL
  } else if (is.call(x)) {
    if (identical(x[[1]], quote('<-'))) {
      x[[2]]
    } else {
      lapply(x, find_assign)
    }
  } else if (is.pairlist(x)) {
    lapply(x, find_assign)
  } else {
    stop("Don't know how to handle type ", typeof(x),
         call. = FALSE)
  }
}

find_assign(quote(a <- 1))
#> a
find_assign(quote({
  a <- 1
  b <- 2
}))
#> [[1]]
#> NULL
#>
```

```
#> [[2]]
#> a
#>
#> [[3]]
#> b
```

This function works for these simple cases, but the output is rather verbose and includes some extraneous NULLs. Instead of returning a list, let's keep it simple and use a character vector. We'll also test it with two slightly more complicated examples:

```
find_assign2 <- function(x) {
  if (is.atomic(x) || is.name(x)) {
    character()
  } else if (is.call(x)) {
    if (identical(x[[1]], quote('<-`'))) {
      as.character(x[[2]])
    } else {
      unlist(lapply(x, find_assign2))
    }
  } else if (is.pairlist(x)) {
    unlist(lapply(x, find_assign2))
  } else {
    stop("Don't know how to handle type ", typeof(x),
        call. = FALSE)
  }
}

find_assign2(quote({
  a <- 1
  b <- 2
  a <- 3
}))
#> [1] "a" "b" "a"

find_assign2(quote({
  system.time(x <- print(y <- 5))
}))
#> [1] "x"
```

This is better, but we have two problems: dealing with repeated names and neglecting assignments inside other assignments. The fix for the

first problem is easy. We need to wrap `unique()` around the recursive case to remove duplicate assignments. The fix for the second problem is a bit more tricky. We also need to recurse when the call is to `<-`. `find_assign3()` implements both strategies:

```
find_assign3 <- function(x) {
  if (is.atomic(x) || is.name(x)) {
    character()
  } else if (is.call(x)) {
    if (identical(x[[1]], quote('<-'))) {
      lhs <- as.character(x[[2]])
    } else {
      lhs <- character()
    }

    unique(c(lhs, unlist(lapply(x, find_assign3))))
  } else if (is.pairlist(x)) {
    unique(unlist(lapply(x, find_assign3)))
  } else {
    stop("Don't know how to handle type ", typeof(x),
         call. = FALSE)
  }
}
```

```
find_assign3(quote({
  a <- 1
  b <- 2
  a <- 3
}))
#> [1] "a" "b"
```

```
find_assign3(quote({
  system.time(x <- print(y <- 5))
}))
#> [1] "x" "y"
```

We also need to test subassignment:

```
find_assign3(quote({
  l <- list()
  l$a <- 5
  names(l) <- "b"
```

```

}))
#> [1] "1"      "$"      "a"      "names"

```

We only want assignment of the object itself, not assignment that modifies a property of the object. Drawing the tree for the quoted object will help us see what condition to test for. The second element of the call to `<-` should be a name, not another call.

```

ast(1$a <- 5)
#> \- ()
#> \- '<-
#> \- ()
#> \- '$
#> \- '1
#> \- 'a
#> \- 5
ast(names(1) <- "b")
#> \- ()
#> \- '<-
#> \- ()
#> \- 'names
#> \- '1
#> \- "b"

```

Now we have a complete version:

```

find_assign4 <- function(x) {
  if (is.atomic(x) || is.name(x)) {
    character()
  } else if (is.call(x)) {
    if (identical(x[[1]], quote('<-')) && is.name(x[[2]])) {
      lhs <- as.character(x[[2]])
    } else {
      lhs <- character()
    }
  }

  unique(c(lhs, unlist(lapply(x, find_assign4))))
} else if (is.pairlist(x)) {
  unique(unlist(lapply(x, find_assign4)))
} else {
  stop("Don't know how to handle type ", typeof(x),
    call. = FALSE)
}

```

```

    }
  }

find_assign4(quote({
  l <- list()
  l$a <- 5
  names(l) <- "b"
}))
#> [1] "1"
```

While the complete version of this function is quite complicated, it's important to remember we wrote it by working our way up by writing simple component parts.

14.7.3 Modifying the call tree

The next step up in complexity is returning a modified call tree, like what you get with `bquote()`. `bquote()` is a slightly more flexible form of `quote()`: it allows you to optionally quote and unquote some parts of an expression (it's similar to the backtick operator in Lisp). Everything is quoted, *unless* it's encapsulated in `.()` in which case it's evaluated and the result is inserted:

```

a <- 1
b <- 3
bquote(a + b)
#> a + b
bquote(a + .(b))
#> a + 3
bquote(.(a) + .(b))
#> 1 + 3
bquote(.(a + b))
#> [1] 4
```

This provides a fairly easy way to control what gets evaluated and when. How does `bquote()` work? Below, I've rewritten `bquote()` to use the same style as our other functions: it expects input to be quoted already, and makes the base and recursive cases more explicit:

```

bquote2 <- function (x, where = parent.frame()) {
  if (is.atomic(x) || is.name(x)) {
```

```

    # Leave unchanged
    x
  } else if (is.call(x)) {
    if (identical(x[[1]], quote(.))) {
      # Call to .(), so evaluate
      eval(x[[2]], where)
    } else {
      # Otherwise apply recursively, turning result back into call
      as.call(lapply(x, bquote2, where = where))
    }
  } else if (is.pairlist(x)) {
    as.pairlist(lapply(x, bquote2, where = where))
  } else {
    # User supplied incorrect input
    stop("Don't know how to handle type ", typeof(x),
        call. = FALSE)
  }
}

x <- 1
y <- 2
bquote2(quote(x == .(x)))
#> x == 1
bquote2(quote(function(x = .(x)) {
  x + .(y)
})))
#> function(x = 1) {
#>   x + 2
#> }
```

The main difference between this and the previous recursive functions is that after we process each element of calls and pairlists, we need to coerce them back to their original types.

Note that functions that modify the source tree are most useful for creating expressions that are used at run-time, rather than those that are saved back to the original source file. This is because all non-code information is lost:

```

bquote2(quote(function(x = .(x)) {
  # This is a comment
  x + # funky spacing
  .(y)
}))
```

```

}))
#> function(x = 1) {
#>     x + 2
#> }

```

These tools are somewhat similar to Lisp macros, as discussed in Programmer’s Niche: Macros in R (http://www.r-project.org/doc/Rnews/Rnews_2001-3.pdf#page=10) by Thomas Lumley. However, macros are run at compile-time, which doesn’t have any meaning in R, and always return expressions. They’re also somewhat like Lisp fexprs (<http://en.wikipedia.org/wiki/Fexpr>). A fexpr is a function where the arguments are not evaluated by default. The terms macro and fexpr are useful to know when looking for useful techniques from other languages.

14.7.4 Exercises

1. Why does `logical_abbr()` use a for loop instead of a functional like `lapply()`?
2. `logical_abbr()` works when given quoted objects, but doesn’t work when given an existing function, as in the example below. Why not? How could you modify `logical_abbr()` to work with functions? Think about what components make up a function.

```

f <- function(x = TRUE) {
  g(x + T)
}
logical_abbr(f)

```

3. Write a function called `ast_type()` that returns either “constant”, “name”, “call”, or “pairlist”. Rewrite `logical_abbr()`, `find_assign()`, and `bquote2()` to use this function with `switch()` instead of nested if statements.
4. Write a function that extracts all calls to a function. Compare your function to `pryr::fun_calls()`.
5. Write a wrapper around `bquote2()` that does non-standard evaluation so that you don’t need to explicitly `quote()` the input.
6. Compare `bquote2()` to `bquote()`. There is a subtle bug in `bquote()`: it won’t replace calls to functions with no arguments. Why?

```
bquote.(x)(), list(x = quote(f)))  
#> .(x)()  
bquote.(x)(1), list(x = quote(f)))  
#> f(1)
```

7. Improve the base `recurse_call()` template to also work with lists of functions and expressions (e.g., as from `parse(path_to_file)`).

15

Domain specific languages

The combination of first class environments, lexical scoping, non-standard evaluation, and metaprogramming gives us a powerful toolkit for creating embedded domain specific languages (DSLs) in R. Embedded DSLs take advantage of a host language's parsing and execution framework, but adjust the semantics to make them more suitable for a specific task. DSLs are a very large topic, and this chapter will only scratch the surface, focussing on important implementation techniques rather than on how you might come up with the language in the first place. If you're interested in learning more, I highly recommend *Domain Specific Languages* (<http://amzn.com/0321712943?tag=devtools-20>) by Martin Fowler. It discusses many options for creating a DSL and provides many examples of different languages.

R's most popular DSL is the formula specification, which provides a succinct way of describing the relationship between predictors and the response in a model. Other examples include `ggplot2` (for visualisation) and `plyr` (for data manipulation). Another package that makes extensive use of these ideas is `dplyr`, which provides `translate_sql()` to convert R expressions into SQL:

```
library(dplyr)
translate_sql(sin(x) + tan(y))
#> <SQL> SIN("x") + TAN("y")
translate_sql(x < 5 & !(y >= 5))
#> <SQL> "x" < 5.0 AND NOT(("y" >= 5.0))
translate_sql(first %like% "Had*")
#> <SQL> "first" LIKE 'Had*'
translate_sql(first %in% c("John", "Roger", "Robert"))
#> <SQL> "first" IN ('John', 'Roger', 'Robert')
translate_sql(like == 7)
#> <SQL> "like" = 7.0
```

This chapter will develop two simple, but useful DSLs: one to generate

HTML, and the other to turn mathematical expressions expressed in R code into LaTeX.

Prerequisites

This chapter together pulls together many techniques discussed elsewhere in the book. In particular, you'll need to understand environments, functionals, non-standard evaluation, and metaprogramming.

15.1 HTML

HTML (hypertext markup language) is the language that underlies the majority of the web. It's a special case of SGML (standard generalised markup language), and it's similar but not identical to XML (extensible markup language). HTML looks like this:

```
<body>
  <h1 id='first'>A heading</h1>
  <p>Some text &amp; <b>some bold text.</b></p>
  <img src='myimg.png' width='100' height='100' />
</body>
```

Even if you've never looked at HTML before, you can still see that the key component of its coding structure is tags, `<tag></tag>`. Tags can be contained inside other tags and intermingled with text. Generally, HTML ignores whitespaces (a sequence of whitespace is equivalent to a single space) so you could put the previous example on a single line and it would still display the same in a browser:

```
<body><h1 id='first'>A heading</h1><p>Some text &amp; <b>some bold
text.</b></p><img src='myimg.png' width='100' height='100' />
</body>
```

However, like R code, you usually want to indent HTML to make the structure more obvious.

There are over 100 HTML tags. But to illustrate HTML, we're going to focus on just a few:

- `<body>`: the top-level tag that all content is enclosed within
- `<h1>`: creates a heading-1, the top level heading
- `<p>`: creates a paragraph
- ``: emboldens text
- ``: embeds an image

(You probably guessed what these did already!)

Tags can also have named attributes. They look like `<tag a="a" b="b"></tag>`. Tag values should always be enclosed in either single or double quotes. Two important attributes used with just about every tag are `id` and `class`. These are used in conjunction with CSS (cascading style sheets) in order to control the style of the document.

Some tags, like ``, can't have any content. These are called **void tags** and have a slightly different syntax. Instead of writing ``, you write ``. Since they have no content, attributes are more important. In fact, `img` has three that are used for almost every image: `src` (where the image lives), `width`, and `height`.

Because `<` and `>` have special meanings in HTML, you can't write them directly. Instead you have to use the HTML escapes: `>` and `<`. And, since those escapes use `&`, if you want a literal ampersand you have to escape with `&`.

15.1.1 Goal

Our goal is to make it easy to generate HTML from R. To give a concrete example, we want to generate the following HTML with code that looks as similar to the HTML as possible.

```
<body>
  <h1 id='first'>A heading</h1>
  <p>Some text &amp; <b>some bold text.</b></p>
  <img src='myimg.png' width='100' height='100' />
</body>
```

To do so, we will work our way up to the following DSL:

```
with_html(body(
  h1("A heading", id = "first"),
  p("Some text &", b("some bold text.")),
  img(src = "myimg.png", width = 100, height = 100)
))
```

Note that the nesting of function calls is the same as the nesting of tags: unnamed arguments become the content of the tag, and named arguments become their attributes. Because tags and text are clearly distinct in this API, we can automatically escape `&` and other special characters.

15.1.2 Escaping

Escaping is so fundamental to DSLs that it'll be our first topic. To create a way of escaping characters, we need to give “`&`” a special meaning without ending up double-escaping. The easiest way to do this is to create an S3 class that distinguishes between regular text (that needs escaping) and HTML (that doesn't).

```
html <- function(x) structure(x, class = "html")
print.html <- function(x, ...) {
  out <- paste0("<HTML> ", x)
  cat(paste(strwrap(out), collapse = "\n"), "\n", sep = "")
}
```

We then write an escape method that leaves HTML unchanged and escapes the special characters (`&`, `<`, `>`) for ordinary text. We also add a list method for convenience.

```
escape <- function(x) UseMethod("escape")
escape.html <- function(x) x
escape.character <- function(x) {
  x <- gsub("&", "&amp;", x)
  x <- gsub("<", "&lt;", x)
  x <- gsub(">", "&gt;", x)

  html(x)
}
escape.list <- function(x) {
  lapply(x, escape)
}

# Now we check that it works
escape("This is some text.")
#> <HTML> This is some text.
escape("x > 1 & y < 2")
```

```
#> <HTML> x &gt; 1 &amp; y &lt; 2

# Double escaping is not a problem
escape(escape("This is some text. 1 > 2"))
#> <HTML> This is some text. 1 &gt; 2

# And text we know is HTML doesn't get escaped.
escape(html("<hr />"))
#> <HTML> <hr />
```

Escaping is an important component for many DSLs.

15.1.3 Basic tag functions

Next, we'll write a few simple tag functions and then figure out how to generalise this function to cover all possible HTML tags. Let's start with `<p>`. HTML tags can have both attributes (e.g., `id` or `class`) and children (like `` or `<i>`). We need some way of separating these in the function call. Given that attributes are named values and children don't have names, it seems natural to separate using named arguments from unnamed ones. For example, a call to `p()` might look like:

```
p("Some text.", b("some bold text"), class = "mypara")
```

We could list all the possible attributes of the `<p>` tag in the function definition. However, that's hard not only because there are many attributes, but also because it's possible to use custom attributes (<http://html5doctor.com/html5-custom-data-attributes/>). Instead, we'll just use `...` and separate the components based on whether or not they are named. To do this correctly, we need to be aware of an inconsistency in `names()`:

```
names(c(a = 1, b = 2))
#> [1] "a" "b"
names(c(a = 1, 2))
#> [1] "a" ""
names(c(1, 2))
#> NULL
```

With this in mind, we create two helper functions to extract the named and unnamed components of a vector:

```

named <- function(x) {
  if (is.null(names(x))) return(NULL)
  x[names(x) != ""]
}
unnamed <- function(x) {
  if (is.null(names(x))) return(x)
  x[names(x) == ""]
}

```

We can now create our `p()` function. Notice that there's one new function here: `html_attributes()`. It uses a list of name-value pairs to create the correct specification of HTML attributes. It's a little complicated (in part, because it deals with some idiosyncracies of HTML that I haven't mentioned.). However, because it's not that important and doesn't introduce any new ideas, I won't discuss it here (you can find the source online).

```

source("dsl-html-attributes.r", local = TRUE)
p <- function(...) {
  args <- list(...)
  attribs <- html_attributes(named(args))
  children <- unlist(escape(unnamed(args)))

  html(paste0(
    "<p", attribs, ">",
    paste(children, collapse = ""),
    "</p>"
  ))
}

p("Some text")
#> <HTML> <p>Some text</p>
p("Some text", id = "myid")
#> <HTML> <p id = 'myid'>Some text</p>
p("Some text", image = NULL)
#> <HTML> <p image>Some text</p>
p("Some text", class = "important", "data-value" = 10)
#> <HTML> <p class = 'important' data-value = '10'>Some
#> text</p>

```

15.1.4 Tag functions

With this definition of `p()`, it's pretty easy to see how we can apply this approach to different tags: we just need to replace "p" with a variable. We'll use a closure to make it easy to generate a tag function given a tag name:

```
tag <- function(tag) {
  force(tag)
  function(...) {
    args <- list(...)
    attribs <- html_attributes(named(args))
    children <- unlist(escape(unnamed(args)))

    html(paste0(
      "<", tag, attribs, ">",
      paste(children, collapse = ""),
      "</", tag, ">"
    ))
  }
}
```

(We're forcing the evaluation of `tag` with the expectation that we'll be calling this function from a loop. This will help to avoid potential bugs caused by lazy evaluation.)

Now we can run our earlier example:

```
p <- tag("p")
b <- tag("b")
i <- tag("i")
p("Some text.", b("Some bold text"), i("Some italic text"),
  class = "mypara")
#> <HTML> <p class = 'mypara'>Some text.<b>Some bold
#> text</b><i>Some italic text</i></p>
```

Before we continue writing functions for every possible HTML tag, we need to create a variant of `tag()` for void tags. It can be very similar to `tag()`, but if there are any unnamed tags, it needs to throw an error. Also note that the tag itself will look slightly different:

```
void_tag <- function(tag) {
  force(tag)
```

```

function(...) {
  args <- list(...)
  if (length(unnamed(args)) > 0) {
    stop("Tag ", tag, " can not have children", call. = FALSE)
  }
  attribs <- html_attributes(named(args))

  html(paste0("<", tag, attribs, " />"))
}
}

img <- void_tag("img")
img(src = "myimage.png", width = 100, height = 100)
#> <HTML> <img src = 'myimage.png' width = '100' height =
#> '100' />

```

15.1.5 Processing all tags

Next we need a list of all the HTML tags:

```

tags <- c("a", "abbr", "address", "article", "aside", "audio",
  "b", "bdi", "bdo", "blockquote", "body", "button", "canvas",
  "caption", "cite", "code", "colgroup", "data", "datalist",
  "dd", "del", "details", "dfn", "div", "dl", "dt", "em",
  "eventsource", "fieldset", "figcaption", "figure", "footer",
  "form", "h1", "h2", "h3", "h4", "h5", "h6", "head", "header",
  "hgroup", "html", "i", "iframe", "ins", "kbd", "label",
  "legend", "li", "mark", "map", "menu", "meter", "nav",
  "noscript", "object", "ol", "optgroup", "option", "output",
  "p", "pre", "progress", "q", "ruby", "rp", "rt", "s", "samp",
  "script", "section", "select", "small", "span", "strong",
  "style", "sub", "summary", "sup", "table", "tbody", "td",
  "textarea", "tfoot", "th", "thead", "time", "title", "tr",
  "u", "ul", "var", "video")

void_tags <- c("area", "base", "br", "col", "command", "embed",
  "hr", "img", "input", "keygen", "link", "meta", "param",
  "source", "track", "wbr")

```

If you look at this list carefully, you'll see there are quite a few tags that have the same name as base R functions (`body`, `col`, `q`, `source`, `sub`, `summary`, `table`), and others that have the same name as popular packages

(e.g., `map`). This means we don't want to make all the functions available by default, in either the global environment or the package environment. Instead, we'll put them in a list and add some additional code to make it easy to use them when desired. First, we make a named list:

```
tag_fs <- c(
  setNames(lapply(tags, tag), tags),
  setNames(lapply(void_tags, void_tag), void_tags)
)
```

This gives us an explicit (but verbose) way to call tag functions:

```
tag_fs$p("Some text.", tag_fs$b("Some bold text"),
  tag_fs$i("Some italic text"))
#> <HTML> <p>Some text.<b>Some bold text</b><i>Some
#> italic text</i></p>
```

We can then finish off our HTML DSL with a function that allows us to evaluate code in the context of that list:

```
with_html <- function(code) {
  eval(substitute(code), tag_fs)
}
```

This gives us a succinct API which allows us to write HTML when we need it but doesn't clutter up the namespace when we don't.

```
with_html(body(
  h1("A heading", id = "first"),
  p("Some text &", b("some bold text.")),
  img(src = "myimg.png", width = 100, height = 100)
))
#> <HTML> <body><h1 id = 'first'>A heading</h1><p>Some
#> text &#38;#38;<b>some bold text.</b></p><img src =
#> 'myimg.png' width = '100' height = '100' /></body>
```

If you want to access the R function overridden by an HTML tag with the same name inside `with_html()`, you can use the full `package::function` specification.

15.1.6 Exercises

1. The escaping rules for `<script>` and `<style>` tags are different: you don't want to escape angle brackets or ampersands, but you do want to escape `</script>` or `</style>`. Adapt the code above to follow these rules.
2. The use of `...` for all functions has some big downsides. There's no input validation and there will be little information in the documentation or autocomplete about how they are used in the function. Create a new function that, when given a named list of tags and their attribute names (like below), creates functions which address this problem.

```
list(  
  a = c("href"),  
  img = c("src", "width", "height")  
)
```

All tags should get `class` and `id` attributes.

3. Currently the HTML doesn't look terribly pretty, and it's hard to see the structure. How could you adapt `tag()` to do indenting and formatting?

15.2 LaTeX

The next DSL will convert R expressions into their LaTeX math equivalents. (This is a bit like `?plotmath`, but for text instead of plots.) LaTeX is the lingua franca of mathematicians and statisticians: whenever you want to describe an equation in text (e.g., in an email), you write it as a LaTeX equation. Since many reports are produced using both R and LaTeX, it might be useful to be able to automatically convert mathematical expressions from one language to the other.

Because we need to convert both functions and names, this mathematical DSL will be more complicated than the HTML DSL. We'll also need to create a "default" conversion, so that functions we don't know about get a standard conversion. Like the HTML DSL, we'll also write functionals to make it easier to generate the translators.

Before we begin, let's quickly cover how formulas are expressed in LaTeX.

15.2.1 LaTeX mathematics

LaTeX mathematics are complex. Fortunately, they are well documented (<http://en.wikibooks.org/wiki/LaTeX/Mathematics>). That said, they have a fairly simple structure:

- Most simple mathematical equations are written in the same way you'd type them in R: $x * y, z ^ 5$. Subscripts are written using `_` (e.g., x_1).
- Special characters start with a `\`: $\pi =$, \pm , and so on. There are a huge number of symbols available in LaTeX. Googling for `latex math symbols` will return many lists (<http://www.sunilpatel.co.uk/latex-type/latex-math-symbols/>). There's even a service (<http://detexify.kirelabs.org/classify.html>) that will look up the symbol you sketch in the browser.
- More complicated functions look like `\name{arg1}{arg2}`. For example, to write a fraction you'd use `\frac{a}{b}`. To write a square root, you'd use `\sqrt{a}`.
- To group elements together use `{}`: i.e., $x ^ a + b$ vs. $x ^ {a + b}$.
- In good math typesetting, a distinction is made between variables and functions. But without extra information, LaTeX doesn't know whether $f(a * b)$ represents calling the function f with input $a * b$, or is shorthand for $f * (a * b)$. If f is a function, you can tell LaTeX to typeset it using an upright font with `\textrm{f}(a * b)`.

15.2.2 Goal

Our goal is to use these rules to automatically convert an R expression to its appropriate LaTeX representation. We'll tackle this in four stages:

- Convert known symbols: `pi -> \pi`
- Leave other symbols unchanged: `x -> x, y -> y`
- Convert known functions to their special forms: `sqrt(frac(a, b)) -> \sqrt{\frac{a, b}}`
- Wrap unknown functions with `\textrm`: `f(a) -> \textrm{f}(a)`

We'll code this translation in the opposite direction of what we did with the HTML DSL. We'll start with infrastructure, because that makes it easy to experiment with our DSL, and then work our way back down to generate the desired output.

15.2.3 to_math

To begin, we need a wrapper function that will convert R expressions into LaTeX math expressions. This will work the same way as `to_html()`: capture the unevaluated expression and evaluate it in a special environment. However, the special environment is no longer fixed. It will vary depending on the expression. We do this in order to be able to deal with symbols and functions that we haven't yet seen.

```
to_math <- function(x) {
  expr <- substitute(x)
  eval(expr, latex_env(expr))
}
```

15.2.4 Known symbols

Our first step is to create an environment that will convert the special LaTeX symbols used for Greek, e.g., `pi` to `\pi`. This is the same basic trick used in `subset` that makes it possible to select column ranges by name (`subset(mtcars, , cyl:wt)`): bind a name to a string in a special environment.

We create that environment by naming a vector, converting the vector into a list, and converting the list into an environment.

```
greek <- c(
  "alpha", "theta", "tau", "beta", "vartheta", "pi", "upsilon",
  "gamma", "gamma", "varpi", "phi", "delta", "kappa", "rho",
  "varphi", "epsilon", "lambda", "varrho", "chi", "varepsilon",
  "mu", "sigma", "psi", "zeta", "nu", "varsigma", "omega", "eta",
  "xi", "Gamma", "Lambda", "Sigma", "Psi", "Delta", "Xi",
  "Upsilon", "Omega", "Theta", "Pi", "Phi")
greek_list <- setNames(paste0("\\", greek), greek)
greek_env <- list2env(as.list(greek_list), parent = emptyenv())
```

We can then check it:

```
latex_env <- function(expr) {
  greek_env
}

to_math(pi)
```

```
#> [1] "\\pi"
to_math(beta)
#> [1] "\\beta"
```

15.2.5 Unknown symbols

If a symbol isn't Greek, we want to leave it as is. This is tricky because we don't know in advance what symbols will be used, and we can't possibly generate them all. So we'll use a little bit of metaprogramming to find out what symbols are present in an expression. The `all_names` function takes an expression and does the following: if it's a name, it converts it to a string; if it's a call, it recurses down through its arguments.

```
all_names <- function(x) {
  if (is.atomic(x)) {
    character()
  } else if (is.name(x)) {
    as.character(x)
  } else if (is.call(x) || is.pairlist(x)) {
    children <- lapply(x[-1], all_names)
    unique(unlist(children))
  } else {
    stop("Don't know how to handle type ", typeof(x),
         call. = FALSE)
  }
}

all_names(quote(x + y + f(a, b, c, 10)))
#> [1] "x" "y" "a" "b" "c"
```

We now want to take that list of symbols, and convert it to an environment so that each symbol is mapped to its corresponding string representation (e.g., so `eval(quote(x), env)` yields `"x"`). We again use the pattern of converting a named character vector to a list, then converting the list to an environment.

```
latex_env <- function(expr) {
  names <- all_names(expr)
  symbol_list <- setNames(as.list(names), names)
  symbol_env <- list2env(symbol_list)
```

```

    symbol_env
  }

to_math(x)
#> [1] "x"
to_math(longvariablename)
#> [1] "longvariablename"
to_math(pi)
#> [1] "pi"

```

This works, but we need to combine it with the Greek symbols environment. Since we want to give preference to Greek over defaults (e.g., `to_math(pi)` should give `"\\pi"`, not `"pi"`), `symbol_env` needs to be the parent of `greek_env`. To do that, we need to make a copy of `greek_env` with a new parent. While R doesn't come with a function for cloning environments, we can easily create one by combining two existing functions:

```

clone_env <- function(env, parent = parent.env(env)) {
  list2env(as.list(env), parent = parent)
}

```

This gives us a function that can convert both known (Greek) and unknown symbols.

```

latex_env <- function(expr) {
  # Unknown symbols
  names <- all_names(expr)
  symbol_list <- setNames(as.list(names), names)
  symbol_env <- list2env(symbol_list)

  # Known symbols
  clone_env(greek_env, symbol_env)
}

to_math(x)
#> [1] "x"
to_math(longvariablename)
#> [1] "longvariablename"
to_math(pi)
#> [1] "\\pi"

```

15.2.6 Known functions

Next we'll add functions to our DSL. We'll start with a couple of helper closures that make it easy to add new unary and binary operators. These functions are very simple: they only assemble strings. (Again we use `force()` to make sure the arguments are evaluated at the right time.)

```
unary_op <- function(left, right) {
  force(left)
  force(right)
  function(e1) {
    paste0(left, e1, right)
  }
}
```

```
binary_op <- function(sep) {
  force(sep)
  function(e1, e2) {
    paste0(e1, sep, e2)
  }
}
```

Using these helpers, we can map a few illustrative examples of converting R to LaTeX. Note that with R's lexical scoping rules helping us, we can easily provide new meanings for standard functions like `+`, `-`, and `*`, and even `(` and `{`.

```
# Binary operators
f_env <- new.env(parent = emptyenv())
f_env$"+" <- binary_op(" + ")
f_env$"- " <- binary_op(" - ")
f_env$"*" <- binary_op(" * ")
f_env$"/" <- binary_op(" / ")
f_env$"^" <- binary_op("^")
f_env$"[" <- binary_op(" _ ")

# Grouping
f_env$"{" <- unary_op("\\left{ ", " \\right}")
f_env$"(" <- unary_op("\\left( ", " \\right)")
f_env$paste <- paste

# Other math functions
```

```

f_env$sqrt <- unary_op("\\sqrt{", "}")
f_env$sin <- unary_op("\\sin(", ")")
f_env$log <- unary_op("\\log(", ")")
f_env$abs <- unary_op("\\left| ", "\\right| ")
f_env$frac <- function(a, b) {
  paste0("\\frac{", a, "}{", b, "}")
}

# Labelling
f_env$hat <- unary_op("\\hat{", "}")
f_env$tilde <- unary_op("\\tilde{", "}")

```

We again modify `latex_env()` to include this environment. It should be the last environment R looks for names in: in other words, `sin(sin)` should work.

```

latex_env <- function(expr) {
  # Known functions
  f_env

  # Default symbols
  names <- all_names(expr)
  symbol_list <- setNames(as.list(names), names)
  symbol_env <- list2env(symbol_list, parent = f_env)

  # Known symbols
  greek_env <- clone_env(greek_env, parent = symbol_env)
}

to_math(sin(x + pi))
#> [1] "\\sin(x + \\pi)"
to_math(log(x_i ^ 2))
#> [1] "\\log(x_i^2)"
to_math(sin(sin))
#> [1] "\\sin(sin)"

```

15.2.7 Unknown functions

Finally, we'll add a default for functions that we don't yet know about. Like the unknown names, we can't know in advance what these will be, so we again use a little metaprogramming to figure them out:

```

all_calls <- function(x) {
  if (is.atomic(x) || is.name(x)) {
    character()
  } else if (is.call(x)) {
    fname <- as.character(x[[1]])
    children <- lapply(x[-1], all_calls)
    unique(c(fname, unlist(children)))
  } else if (is.pairlist(x)) {
    unique(unlist(lapply(x[-1], all_calls), use.names = FALSE))
  } else {
    stop("Don't know how to handle type ", typeof(x), call. = FALSE)
  }
}

all_calls(quote(f(g + b, c, d(a))))
#> [1] "f" "+" "d"

```

And we need a closure that will generate the functions for each unknown call.

```

unknown_op <- function(op) {
  force(op)
  function(...) {
    contents <- paste(..., collapse = ", ")
    paste0("\mathrm{", op, "}", contents, ")")
  }
}

```

And again we update `latex_env()`:

```

latex_env <- function(expr) {
  calls <- all_calls(expr)
  call_list <- setNames(lapply(calls, unknown_op), calls)
  call_env <- list2env(call_list)

  # Known functions
  f_env <- clone_env(f_env, call_env)

  # Default symbols
  symbols <- all_names(expr)
  symbol_list <- setNames(as.list(symbols), symbols)
  symbol_env <- list2env(symbol_list, parent = f_env)
}

```

```
# Known symbols
greek_env <- clone_env(greek_env, parent = symbol_env)
}

to_math(f(a * b))
#> [1] "\\mathrm{f}(a * b)"
```

15.2.8 Exercises

1. Add escaping. The special symbols that should be escaped by adding a backslash in front of them are `\`, `$`, and `%`. Just as with HTML, you'll need to make sure you don't end up double-escaping. So you'll need to create a small S3 class and then use that in function operators. That will also allow you to embed arbitrary LaTeX if needed.
2. Complete the DSL to support all the functions that `plotmath` supports.
3. There's a repeating pattern in `latex_env()`: we take a character vector, do something to each piece, convert it to a list, and then convert the list to an environment. Write a function that automates this task, and then rewrite `latex_env()`.
4. Study the source code for `dplyr`. An important part of its structure is `partial_eval()` which helps manage expressions when some of the components refer to variables in the database while others refer to local R objects. Note that you could use very similar ideas if you needed to translate small R expressions into other languages, like JavaScript or Python.

Part IV

Performance

16

Performance

R is not a fast language. This is not an accident. R was purposely designed to make data analysis and statistics easier for you to do. It was not designed to make life easier for your computer. While R is slow compared to other programming languages, for most purposes, it's fast enough.

The goal of this part of the book is to give you a deeper understanding of R's performance characteristics. In this chapter, you'll learn about some of the trade-offs that R has made, valuing flexibility over performance. The following four chapters will give you the skills to improve the speed of your code when you need to:

- In Chapter 17, you'll learn how to systematically make your code faster. First you figure what's slow, and then you apply some general techniques to make the slow parts faster.
- In Chapter 18, you'll learn about how R uses memory, and how garbage collection and copy-on-modify affect performance and memory usage.
- For really high-performance code, you can move outside of R and use another programming language. Chapter 19 will teach you the absolute minimum you need to know about C++ so you can write fast code using the Rcpp package.
- To really understand the performance of built-in base functions, you'll need to learn a little bit about R's C API. In Chapter 20, you'll learn a little about R's C internals.

Let's get started by learning more about why R is slow.

16.1 Why is R slow?

To understand R's performance, it helps to think about R as both a language and as an implementation of that language. The R-language is abstract: it defines what R code means and how it should work. The implementation is concrete: it reads R code and computes a result. The most popular implementation is the one from r-project.org (<http://r-project.org>). I'll call that implementation GNU-R to distinguish it from R-language, and from the other implementations I'll discuss later in the chapter.

The distinction between R-language and GNU-R is a bit murky because the R-language is not formally defined. While there is the R language definition (<http://cran.r-project.org/doc/manuals/R-lang.html>), it is informal and incomplete. The R-language is mostly defined in terms of how GNU-R works. This is in contrast to other languages, like C++ (<http://isocpp.org/std/the-standard>) and javascript (<http://www.ecma-international.org/publications/standards/Ecma-262.htm>), that make a clear distinction between language and implementation by laying out formal specifications that describe in minute detail how every aspect of the language should work. Nevertheless, the distinction between R-language and GNU-R is still useful: poor performance due to the language is hard to fix without breaking existing code; fixing poor performance due to the implementation is easier.

In Section 16.3, I discuss some of the ways in which the design of the R-language imposes fundamental constraints on R's speed. In Section 16.4, I discuss why GNU-R is currently far from the theoretical maximum, and why improvements in performance happen so slowly. While it's hard to know exactly how much faster a better implementation could be, a >10x improvement in speed seems achievable. In Section 16.5, I discuss some of the promising new implementations of R, and describe one important technique they use to make R code run faster.

Beyond performance limitations due to design and implementation, it has to be said that a lot of R code is slow simply because it's poorly written. Few R users have any formal training in programming or software development. Fewer still write R code for a living. Most people use R to understand data: it's more important to get an answer quickly than to develop a system that will work in a wide variety of situations. This means that it's relatively easy to make most R code much faster, as we'll see in the following chapters.

Before we examine some of the slower parts of the R-language and GNU-R, we need to learn a little about benchmarking so that we can give our intuitions about performance a concrete foundation.

16.2 Microbenchmarking

A microbenchmark is a measurement of the performance of a very small piece of code, something that might take microseconds (μ s) or nanoseconds (ns) to run. I'm going to use microbenchmarks to demonstrate the performance of very low-level pieces of R code, which help develop your intuition for how R works. This intuition, by-and-large, is not useful for increasing the speed of real code. The observed differences in microbenchmarks will typically be dominated by higher-order effects in real code; a deep understanding of subatomic physics is not very helpful when baking. Don't change the way you code because of these microbenchmarks. Instead wait until you've read the practical advice in the following chapters.

The best tool for microbenchmarking in R is the `microbenchmark` (<http://cran.r-project.org/web/packages/microbenchmark/>) package. It provides very precise timings, making it possible to compare operations that only take a tiny amount of time. For example, the following code compares the speed of two ways of computing a square root.

```
library(microbenchmark)

x <- runif(100)
microbenchmark(
  sqrt(x),
  x ^ 0.5
)
#> Unit: nanoseconds
#>      expr    min      lq median      uq    max neval
#>  sqrt(x)   595    625    640    680  4,380   100
#>   x^0.5 3,660 3,700 3,730 3,770 33,600   100
```

By default, `microbenchmark()` runs each expression 100 times (controlled by the `times` parameter). In the process, it also randomises the order of the expressions. It summarises the results with a minimum (min), lower

quartile (1q), median, upper quartile (uq), and maximum (max). Focus on the median, and use the upper and lower quartiles (1q and uq) to get a feel for the variability. In this example, you can see that using the special purpose `sqrt()` function is faster than the general exponentiation operator.

As with all microbenchmarks, pay careful attention to the units: each computation takes about 800 ns, 800 billionths of a second. To help calibrate the impact of a microbenchmark on run time, it's useful to think about how many times a function needs to run before it takes a second. If a microbenchmark takes:

- 1 ms, then one thousand calls takes a second
- 1 μ s, then one million calls takes a second
- 1 ns, then one billion calls takes a second

The `sqrt()` function takes about 800 ns, or 0.8 μ s, to compute the square root of 100 numbers. That means if you repeated the operation a million times, it would take 0.8 s. So changing the way you compute the square root is unlikely to significantly affect real code.

16.2.1 Exercises

1. Instead of using `microbenchmark()`, you could use the built-in function `system.time()`. But `system.time()` is much less precise, so you'll need to repeat each operation many times with a loop, and then divide to find the average time of each operation, as in the code below.

```
n <- 1:1e6
system.time(for (i in n) sqrt(x)) / length(n)
system.time(for (i in n) x ^ 0.5) / length(n)
```

How do the estimates from `system.time()` compare to those from `microbenchmark()`? Why are they different?

2. Here are two other ways to compute the square root of a vector. Which do you think will be fastest? Which will be slowest? Use microbenchmarking to test your answers.

```
x ^ (1 / 2)
exp(log(x) / 2)
```

3. Use microbenchmarking to rank the basic arithmetic operators (+, -, *, /, and ^) in terms of their speed. Visualise the results. Compare the speed of arithmetic on integers vs. doubles.
4. You can change the units in which the microbenchmark results are expressed with the `unit` parameter. Use `unit = "eps"` to show the number of evaluations needed to take 1 second. Repeat the benchmarks above with the `eps` unit. How does this change your intuition for performance?

16.3 Language performance

In this section, I'll explore three trade-offs that limit the performance of the R-language: extreme dynamism, name lookup with mutable environments, and lazy evaluation of function arguments. I'll illustrate each trade-off with a microbenchmark, showing how it slows GNU-R down. I benchmark GNU-R because you can't benchmark the R-language (it can't run code). This means that the results are only suggestive of the cost of these design decisions, but are nevertheless useful. I've picked these three examples to illustrate some of the trade-offs that are key to language design: the designer must balance speed, flexibility, and ease of implementation.

If you'd like to learn more about the performance characteristics of the R-language and how they affect real code, I highly recommend "Evaluating the Design of the R Language" (<https://www.cs.purdue.edu/homes/jv/pubs/ecoop12.pdf>) by Floreal Morandat, Brandon Hill, Leo Osvald, and Jan Vitek. It uses a powerful methodology that combines a modified R interpreter and a wide set of code found in the wild.

16.3.1 Extreme dynamism

R is an extremely dynamic programming language. Almost anything can be modified after it is created. To give just a few examples, you can:

- Change the body, arguments, and environment of functions.
- Change the S4 methods for a generic.
- Add new fields to an S3 object, or even change its class.
- Modify objects outside of the local environment with `<<-`.

Pretty much the only things you can't change are objects in sealed namespaces, which are created when you load a package.

The advantage of dynamism is that you need minimal upfront planning. You can change your mind at any time, iterating your way to a solution without having to start afresh. The disadvantage of dynamism is that it's difficult to predict exactly what will happen with a given function call. This is a problem because the easier it is to predict what's going to happen, the easier it is for an interpreter or compiler to make an optimisation. (If you'd like more details, Charles Nutter expands on this idea at *On Languages, VMs, Optimization, and the Way of the World* (<http://blog.headius.com/2013/05/on-languages-vms-optimization-and-way.html>).) If an interpreter can't predict what's going to happen, it has to consider many options before it finds the right one. For example, the following loop is slow in R, because R doesn't know that `x` is always an integer. That means R has to look for the right `+` method (i.e., is it adding doubles, or integers?) in every iteration of the loop.

```
x <- 0L
for (i in 1:1e6) {
  x <- x + 1
}
```

The cost of finding the right method is higher for non-primitive functions. The following microbenchmark illustrates the cost of method dispatch for S3, S4, and RC. I create a generic and a method for each OO system, then call the generic and see how long it takes to find and call the method. I also time how long it takes to call the bare function for comparison.

```
f <- function(x) NULL

s3 <- function(x) UseMethod("s3")
s3.integer <- f

A <- setClass("A", representation(a = "list"))
setGeneric("s4", function(x) standardGeneric("s4"))
setMethod(s4, "A", f)

B <- setRefClass("B", methods = list(rc = f))

a <- A()
b <- B$new()
```



```
microbenchmark(
  fun = f(),
  S3 = s3(1L),
  S4 = s4(a),
  RC = b$rc()
)
#> Unit: nanoseconds
#>   expr      min       lq median      uq      max neval
#>   fun       155        201      242       300    1,670     100
#>   S3    1,960    2,460    2,790    3,150   32,900     100
#>   S4 10,000 11,800 12,500 13,500 19,800     100
#>   RC   9,650 10,600 11,200 11,700 568,000     100
```

On my computer, the bare function takes about 200 ns. S3 method dispatch takes an additional 2,000 ns; S4 dispatch, 11,000 ns; and RC dispatch, 10,000 ns. S3 and S4 method dispatch are expensive because R must search for the right method every time the generic is called; it might have changed between this call and the last. R could do better by caching methods between calls, but caching is hard to do correctly and a notorious source of bugs.

16.3.2 Name lookup with mutable environments

It's surprisingly difficult to find the value associated with a name in the R-language. This is due to combination of lexical scoping and extreme dynamism. Take the following example. Each time we print a it comes from a different environment:

```
a <- 1
f <- function() {
  g <- function() {
    print(a)
    assign("a", 2, envir = parent.frame())
    print(a)
    a <- 3
    print(a)
  }
  g()
}
f()
#> [1] 1
```

```
#> [1] 2
#> [1] 3
```

This means that you can't do name lookup just once: you have to start from scratch each time. This problem is exacerbated by the fact that almost every operation is a lexically scoped function call. You might think the following simple function calls two functions: `+` and `^`. In fact, it calls four because `{` and `()` are regular functions in R.

```
f <- function(x, y) {
  (x + y) ^ 2
}
```

Since these functions are in the global environment, R has to look through every environment in the search path, which could easily be 10 or 20 environments. The following microbenchmark hints at the performance costs. We create four versions of `f()`, each with one more environment (containing 26 bindings) between the environment of `f()` and the base environment where `+`, `^`, `()`, and `{` are defined.

```
random_env <- function(parent = globalenv()) {
  letter_list <- setNames(as.list(runif(26)), LETTERS)
  list2env(letter_list, envir = new.env(parent = parent))
}
set_env <- function(f, e) {
  environment(f) <- e
  f
}
f2 <- set_env(f, random_env())
f3 <- set_env(f, random_env(environment(f2)))
f4 <- set_env(f, random_env(environment(f3)))

microbenchmark(
  f(1, 2),
  f2(1, 2),
  f3(1, 2),
  f4(1, 2),
  times = 10000
)
#> Unit: nanoseconds
#>      expr min  lq median  uq      max neval
#>   f(1, 2) 591 643   730 876 711,000 10000
```

```
#> f2(1, 2) 616 690      778 920  56,700 10000
#> f3(1, 2) 666 722      808 958  32,600 10000
#> f4(1, 2) 690 762      850 995  846,000 10000
```

Each additional environment between `f()` and the base environment makes the function slower by about 30 ns.

It might be possible to implement a caching system so that R only needs to look up the value of each name once. This is hard because there are so many ways to change the value associated with a name: `<<-`, `assign()`, `eval()`, and so on. Any caching system would have to know about these functions to make sure the cache was correctly invalidated and you didn't get an out-of-date value.

Another simple fix would be to add more built-in constants that you can't override. This, for example, would mean that R always knew exactly what `+`, `-`, `{`, and `(` meant, and you wouldn't have to repeatedly look up their definitions. That would make the interpreter more complicated (because there are more special cases) and hence harder to maintain, and the language less flexible. This would change the R-language, but it would be unlikely to affect much existing code because it's such a bad idea to override functions like `{` and `(`.

16.3.3 Lazy evaluation overhead

In R, function arguments are evaluated lazily (as discussed in Section 6.4.4 and Section 13.1). To implement lazy evaluation, R uses a promise object that contains the expression needed to compute the result and the environment in which to perform the computation. Creating these objects has some overhead, so each additional argument to a function decreases its speed a little.

The following microbenchmark compares the runtime of a very simple function. Each version of the function has one additional argument. This suggests that adding an additional argument slows the function down by ~20 ns.

```
f0 <- function() NULL
f1 <- function(a = 1) NULL
f2 <- function(a = 1, b = 1) NULL
f3 <- function(a = 1, b = 2, c = 3) NULL
f4 <- function(a = 1, b = 2, c = 4, d = 4) NULL
f5 <- function(a = 1, b = 2, c = 4, d = 4, e = 5) NULL
```

```
microbenchmark(f0(), f1(), f2(), f3(), f4(), f5(), times = 10000)
#> Unit: nanoseconds
#>   expr min  lq median  uq      max neval
#>   f0() 129 149   153 220   8,830 10000
#>   f1() 153 174   181 290  19,800 10000
#>   f2() 170 196   214 367  30,400 10000
#>   f3() 195 216   258 454   7,520 10000
#>   f4() 206 237   324 534  59,400 10000
#>   f5() 219 256   372 589 865,000 10000
```

In most other programming languages there is little overhead for adding extra arguments. Many compiled languages will even warn you if arguments are never used (like in the above example), and automatically remove them from the function.

16.3.4 Exercises

1. `scan()` has the most arguments (21) of any base function. About how much time does it take to make 21 promises each time `scan` is called? Given a simple input (e.g., `scan(text = "1 2 3", quiet = T)`) what proportion of the total run time is due to creating those promises?
2. Read “Evaluating the Design of the R Language” (<https://www.cs.purdue.edu/homes/jv/pubs/ecoop12.pdf>). What other aspects of the R-language slow it down? Construct microbenchmarks to illustrate.
3. How does the performance of S3 method dispatch change with the length of the class vector? How does performance of S4 method dispatch change with number of superclasses? How about RC?
4. What is the cost of multiple inheritance and multiple dispatch on S4 method dispatch?
5. Why is the cost of name lookup less for functions in the base package?

16.4 Implementation performance

The design of the R language limits its maximum theoretical performance, but GNU-R is currently nowhere near that maximum. There are many things that can (and will) be done to improve performance. This section discusses some aspects of GNU-R that are slow not because of their definition, but because of their implementation.

R is over 20 years old. It contains nearly 800,000 lines of code (about 45% C, 19% R, and 17% Fortran). Changes to base R can only be made by members of the R Core Team (or R-core for short). Currently R-core has twenty members (<http://www.r-project.org/contributors.html>), but only six are active in day-to-day development. No one on R-core works full time on R. Most are statistics professors who can only spend a relatively small amount of their time on R. Because of the care that must be taken to avoid breaking existing code, R-core tends to be very conservative about accepting new code. It can be frustrating to see R-core reject proposals that would improve performance. However, the overriding concern for R-core is not to make R fast, but to build a stable platform for data analysis and statistics.

Below, I'll show two small, but illustrative, examples of parts of R that are currently slow but could, with some effort, be made faster. They are not critical parts of base R, but they have been sources of frustration for me in the past. As with all microbenchmarks, these won't affect the performance of most code, but can be important for special cases.

16.4.1 Extracting a single value from a data frame

The following microbenchmark shows seven ways to access a single value (the number in the bottom-right corner) from the built-in `mtcars` dataset. The variation in performance is startling: the slowest method takes 30x longer than the fastest. There's no reason that there has to be such a huge difference in performance. It's simply that no one has had the time to fix it.

```
microbenchmark(  
  "[32, 11]"      = mtcars[32, 11],  
  "$carb[32]"     = mtcars$carb[32],  
  "[[c(11, 32)]]" = mtcars[[c(11, 32)]],
```

```

"[[11]][32]" = mtcars[[11]][32],
".subset2" = .subset2(mtcars, 11)[32]
)
#> Unit: nanoseconds
#>      expr      min      lq median      uq      max neval
#>   [32, 11] 17,300 18,300 18,900 20,000 50,700   100
#>   $carb[32]  9,300 10,400 10,800 11,500 389,000   100
#>   [[c(11, 32)]] 7,350  8,460  8,970  9,640  19,300   100
#>   [[11]][32]  7,110  8,010  8,600  9,160  25,100   100
#>   .subset2    253    398    434    472  2,010   100

```

16.4.2 ifelse(), pmin(), and pmax()

Some base functions are known to be slow. For example, take the following three implementations of `squish()`, a function that ensures that the smallest value in a vector is at least `a` and its largest value is at most `b`. The first implementation, `squish_ife()`, uses `ifelse()`. `ifelse()` is known to be slow because it is relatively general and must evaluate all arguments fully. The second implementation, `squish_p()`, uses `pmin()` and `pmax()`. Because these two functions are so specialised, one might expect that they would be fast. However, they're actually rather slow. This is because they can take any number of arguments and they have to do some relatively complicated checks to determine which method to use. The final implementation uses basic subassignment.

```

squish_ife <- function(x, a, b) {
  ifelse(x <= a, a, ifelse(x >= b, b, x))
}
squish_p <- function(x, a, b) {
  pmax(pmin(x, b), a)
}
squish_in_place <- function(x, a, b) {
  x[x <= a] <- a
  x[x >= b] <- b
  x
}

x <- runif(100, -1.5, 1.5)
microbenchmark(
  squish_ife = squish_ife(x, -1, 1),
  squish_p = squish_p(x, -1, 1),
  squish_in_place = squish_in_place(x, -1, 1),

```

```

    unit = "us"
)
#> Unit: microseconds
#>      expr   min     lq median   uq    max neval
#>  squish_ife 78.8 83.90   85.1 87.0 151.0   100
#>    squish_p 18.8 21.50   22.5 24.6 426.0   100
#> squish_in_place  7.2  8.81   10.3 10.9  64.6   100

```

Using `pmin()` and `pmax()` is about 3x faster than `ifelse()`, and using subsetting directly is about twice as fast again. We can often do even better by using C++. The following example compares the best R implementation to a relatively simple, if verbose, implementation in C++. Even if you've never used C++, you should still be able to follow the basic strategy: loop over every element in the vector and perform a different action depending on whether or not the value is less than `a` and/or greater than `b`. The C++ implementation is around 3x faster than the best pure R implementation.

```

#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
NumericVector squish_cpp(NumericVector x, double a, double b) {
    int n = x.length();
    NumericVector out(n);

    for (int i = 0; i < n; ++i) {
        double xi = x[i];
        if (xi < a) {
            out[i] = a;
        } else if (xi > b) {
            out[i] = b;
        } else {
            out[i] = xi;
        }
    }

    return out;
}

```

(You'll learn how to access this C++ code from R in Chapter 19.)

```

microbenchmark(
  squish_in_place = squish_in_place(x, -1, 1),

```

```

squish_cpp      = squish_cpp(x, -1, 1),
unit = "us"
)
#> Unit: microseconds
#>           expr min   lq median    uq  max neval
#>  squish_in_place 7.45 8.33   9.82 10.30 43.8   100
#>      squish_cpp 2.49 2.98   3.27  3.47 33.7   100

```

16.4.3 Exercises

1. The performance characteristics of `squish_ife()`, `squish_p()`, and `squish_in_place()` vary considerably with the size of `x`. Explore the differences. Which sizes lead to the biggest and smallest differences?
2. Compare the performance costs of extracting an element from a list, a column from a matrix, and a column from a data frame. Do the same for rows.

16.5 Alternative R implementations

There are some exciting new implementations of R. While they all try to stick as closely as possible to the existing language definition, they improve speed by using ideas from modern interpreter design. The four most mature open-source projects are:

- `pqR` (<http://www.pqr-project.org/>) (pretty quick R) by Radford Neal. Built on top of R 2.15.0, it fixes many obvious performance issues, and provides better memory management and some support for automatic multithreading.
- `Renjin` (<http://www.renjin.org/>) by BeDataDriven. Renjin uses the Java virtual machine, and has an extensive test suite (<http://packages.renjin.org/>).
- `FastR` (<https://github.com/allr/fastr>) by a team from Purdue. FastR is similar to Renjin, but it makes more ambitious optimisations and is somewhat less mature.
- `Riposte` (<https://github.com/jtalbot/riposte>) by Justin Talbot and

Zachary DeVito. Riposte is experimental and ambitious. For the parts of R it implements, it is extremely fast. Riposte is described in more detail in *Riposte: A Trace-Driven Compiler and Parallel VM for Vector Code in R* (<http://www.justintalbot.com/wp-content/uploads/2012/10/pact080talbot.pdf>).

These are roughly ordered from most practical to most ambitious. Another project, CXXR (<http://www.cs.kent.ac.uk/projects/cxxr/>) by Andrew Runnalls, does not provide any performance improvements. Instead, it aims to refactor R's internal C code in order to build a stronger foundation for future development, to keep behaviour identical to GNU-R, and to create better, more extensible documentation of its internals.

R is a huge language and it's not clear whether any of these approaches will ever become mainstream. It's a hard task to make an alternative implementation run all R code in the same way as GNU-R. Can you imagine having to reimplement every function in base R to be not only faster, but also to have exactly the same documented bugs? However, even if these implementations never make a dent in the use of GNU-R, they still provide benefits:

- Simpler implementations make it easy to validate new approaches before porting to GNU-R.
- Knowing which aspects of the language can be changed with minimal impact on existing code and maximal impact on performance can help to guide us to where we should direct our attention.
- Alternative implementations put pressure on the R-core to incorporate performance improvements.

One of the most important approaches that pqR, Renjin, FastR, and Riposte are exploring is the idea of deferred evaluation. As Justin Talbot, the author of Riposte, points out: “for long vectors, R's execution is completely memory bound. It spends almost all of its time reading and writing vector intermediates to memory”. If we could eliminate these intermediate vectors, we could improve performance and reduce memory usage.

The following example shows a very simple example of how deferred evaluation can help. We have three vectors, `x`, `y`, `z`, each containing 1 million elements, and we want to find the sum of `x + y` where `z` is TRUE. (This represents a simplification of a pretty common sort of data analysis question.)

```
x <- runif(1e6)
y <- runif(1e6)
z <- sample(c(T, F), 1e6, rep = TRUE)

sum((x + y)[z])
```

In R, this creates two big temporary vectors: `x + y`, 1 million elements long, and `(x + y)[z]`, about 500,000 elements long. This means you need to have extra memory available for the intermediate calculation, and you have to shuttle the data back and forth between the CPU and memory. This slows computation down because the CPU can't work at maximum efficiency if it's always waiting for more data to come in.

However, if we rewrote the function using a loop in a language like C++, we only need one intermediate value: the sum of all the values we've seen:

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
double cond_sum_cpp(NumericVector x, NumericVector y,
                    LogicalVector z) {
  double sum = 0;
  int n = x.length();

  for(int i = 0; i < n; i++) {
    if (!z[i]) continue;
    sum += x[i] + y[i];
  }

  return sum;
}
```

On my computer, this approach is about eight times faster than the vectorised R equivalent, which is already pretty fast.

```
cond_sum_r <- function(x, y, z) {
  sum((x + y)[z])
}

microbenchmark(
  cond_sum_cpp(x, y, z),
  cond_sum_r(x, y, z),
```

```
    unit = "ms"
  )
#> Unit: milliseconds
#>      expr    min      lq median      uq    max neval
#> cond_sum_cpp(x, y, z) 4.09  4.11   4.13  4.15  4.33   100
#>   cond_sum_r(x, y, z) 30.60 31.60  31.70 31.80 64.60   100
```

The goal of deferred evaluation is to perform this transformation automatically, so you can write concise R code and have it automatically translated into efficient machine code. Sophisticated translators can also figure out how to make the most of multiple cores. In the above example, if you have four cores, you could split `x`, `y`, and `z` into four pieces performing the conditional sum on each core, then adding together the four individual results. Deferred evaluation can also work with `for` loops, automatically discovering operations that can be vectorised.

This chapter has discussed some of the fundamental reasons that R is slow. The following chapters will give you the tools to do something about it when it impacts your code.

Optimising code

“Programmers waste enormous amounts of time thinking about, or worrying about, the speed of noncritical parts of their programs, and these attempts at efficiency actually have a strong negative impact when debugging and maintenance are considered.”

— Donald Knuth.

Optimising code to make it run faster is an iterative process:

1. Find the biggest bottleneck (the slowest part of your code).
2. Try to eliminate it (you may not succeed but that’s ok).
3. Repeat until your code is “fast enough.”

This sounds easy, but it’s not.

Even experienced programmers have a hard time identifying bottlenecks in their code. Instead of relying on your intuition, you should **profile** your code: use realistic inputs and measure the run-time of each individual operation. Only once you’ve identified the most important bottlenecks can you attempt to eliminate them. It’s difficult to provide general advice on improving performance, but I try my best with six techniques that can be applied in many situations. I’ll also suggest a general strategy for performance optimisation that helps ensure that your faster code will still be correct code.

It’s easy to get caught up in trying to remove all bottlenecks. Don’t! Your time is valuable and is better spent analysing your data, not eliminating possible inefficiencies in your code. Be pragmatic: don’t spend hours of your time to save seconds of computer time. To enforce this advice, you should set a goal time for your code and optimise only up to that goal. This means you will not eliminate all bottlenecks. Some you will not get to because you’ve met your goal. Others you may need to pass over and accept either because there is no quick and easy solution or because the code is already well optimised and no significant improvement is possible. Accept these possibilities and move on to the next candidate.

Outline

- Section 17.1 describes how to find the bottlenecks in your code using line profiling.
- Section 17.2 outlines seven general strategies for improving the performance of your code.
- Section 17.3 teaches you how to organise your code to make optimisation as easy, and bug free, as possible.
- Section 17.4 reminds you to look for existing solutions.
- Section 17.5 emphasises the importance of being lazy: often the easiest way to make a function faster is to let it to do less work.
- Section 17.6 concisely defines vectorisation, and shows you how to make the most of built-in functions.
- Section 17.7 discusses the performance perils of copying data.
- Section 17.8 shows you how to take advantage of R's byte code compiler.
- Section 17.9 pulls all the pieces together into a case study showing how to speed up repeated t-tests by ~1000x.
- Section 17.10 teaches you how to use parallelisation to spread computation across all the cores in your computer.
- Section 17.11 finishes the chapter with pointers to more resources that will help you write fast code.

Prerequisites

In this chapter we'll be using the `lineprof` package to understand the performance of R code. Get it with:

```
devtools::install_github("hadley/lineprof")
```

17.1 Measuring performance

To understand performance, you use a profiler. There are a number of different types of profilers. R uses a fairly simple type called a sampling

or statistical profiler. A sampling profiler stops the execution of code every few milliseconds and records which function is currently executing (along with which function called that function, and so on). For example, consider `f()`, below:

```
library(lineprof)
f <- function() {
  pause(0.1)
  g()
  h()
}
g <- function() {
  pause(0.1)
  h()
}
h <- function() {
  pause(0.1)
}
```

(I use `pause()` instead of `Sys.sleep()` because `Sys.sleep()` does not appear in profiling outputs because as far as R can tell, it doesn't use up any computing time.)

If we profiled the execution of `f()`, stopping the execution of code every 0.1 s, we'd see a profile like below. Each line represents one "tick" of the profiler (0.1 s in this case), and function calls are nested with `>`. It shows that the code spends 0.1 s running `f()`, then 0.2 s running `g()`, then 0.1 s running `h()`.

```
f()
f() > g()
f() > g() > h()
f() > h()
```

If we actually profile `f()`, using the code below, we're unlikely to get such a clear result.

```
tmp <- tempfile()
Rprof(tmp, interval = 0.1)
f()
Rprof(NULL)
```

That's because profiling is hard to do accurately without slowing your code down by many orders of magnitude. The compromise that `RProf()` makes, sampling, only has minimal impact on the overall performance, but is fundamentally stochastic. There's some variability in both the accuracy of the timer and in the time taken by each operation, so each time you profile you'll get a slightly different answer. Fortunately, pin-point accuracy is not needed to identify the slowest parts of your code.

Rather than focussing on individual calls, we'll visualise aggregates using the `lineprof` package. There are a number of other options, like `summaryRprof()`, the `proftools` package, and the `profr` package, but these tools are beyond the scope of this book. I wrote the `lineprof` package as a simpler way to visualise profiling data. As the name suggests, the fundamental unit of analysis in `lineprof()` is a line of code. This makes `lineprof` less precise than the alternatives (because a line of code can contain multiple function calls), but it's easier to understand the context.

To use `lineprof`, we first save the code in a file and `source()` it. Here `profiling-example.R` contains the definition of `f()`, `g()`, and `h()`. Note that you *must* use `source()` to load the code. This is because `lineprof` uses `srcrefs` to match up the code to the profile, and the needed `srcrefs` are only created when you load code from disk. We then use `lineprof()` to run our function and capture the timing output. Printing this object shows some basic information. For now, we'll just focus on the time column which estimates how long each line took to run and the `ref` column which tells us which line of code was run. The estimates aren't perfect, but the ratios look about right.

```
library(lineprof)
source("profiling-example.R")
l <- lineprof(f())
l
#>   time alloc release dups      ref      src
#> 1 0.074 0.001      0     0 profiling.R#2 f/pause
#> 2 0.143 0.002      0     0 profiling.R#3 f/g
#> 3 0.071 0.000      0     0 profiling.R#4 f/h
```

`lineprof` provides some functions to navigate through this data structure, but they're a bit clumsy. Instead, we'll start an interactive explorer using the `shiny` package. `shine(l)` will open a new web page (or if you're using RStudio, a new pane) that shows your source code annotated with information about how long each line took to run. `shine()` starts a


shiny app which “blocks” your R session. To exit, you’ll need to stop the process using escape or ctrl + c.

| # | Source code | t | r | a | d |
|----|-------------------|-------------|---|-------------|---|
| 1 | f <- function() { | | | | |
| 2 | pause(0.1) | <div></div> | | <div></div> | |
| 3 | g() | <div></div> | | <div></div> | |
| 4 | h() | <div></div> | | | |
| 5 | } | | | | |
| 6 | g <- function() { | | | | |
| 7 | pause(0.1) | | | | |
| 8 | h() | | | | |
| 9 | } | | | | |
| 10 | h <- function() { | | | | |
| 11 | pause(0.1) | | | | |
| 12 | } | | | | |

The t column visualises how much time is spent on each line. (You’ll learn about the other columns in Section 18.3.) While not precise, it allows you to spot bottlenecks, and you can get precise numbers by hovering over each bar. This shows that twice as much time is spent on g() as on h(), so it would make sense to drill down into g() for more details. To do so, click g():

| # | Source code | t | r | a | d |
|----|-------------------|-------------|---|-------------|---|
| 1 | f <- function() { | | | | |
| 2 | pause(0.1) | | | | |
| 3 | g() | | | | |
| 4 | h() | | | | |
| 5 | } | | | | |
| 6 | g <- function() { | | | | |
| 7 | pause(0.1) | <div></div> | | <div></div> | |
| 8 | h() | <div></div> | | <div></div> | |
| 9 | } | | | | |
| 10 | h <- function() { | | | | |
| 11 | pause(0.1) | | | | |
| 12 | } | | | | |

Then h():

| # | Source code | t | r | a | d |
|----|-------------------|---|---|---|---|
| 1 | f <- function() { | | | | |
| 2 | pause(0.1) | | | | |
| 3 | g() | | | | |
| 4 | h() | | | | |
| 5 | } | | | | |
| 6 | g <- function() { | | | | |
| 7 | pause(0.1) | | | | |
| 8 | h() | | | | |
| 9 | } | | | | |
| 10 | h <- function() { | | | | |
| 11 | pause(0.1) |  | |  | |
| 12 | } | | | | |

This technique should allow you to quickly identify the major bottlenecks in your code.

17.1.1 Limitations

There are some other limitations to profiling:

- Profiling does not extend to C code. You can see if your R code calls C/C++ code but not what functions are called inside of your C/C++ code. Unfortunately, tools for profiling compiled code are beyond the scope of this book (i.e., I have no idea how to do it).
- Similarly, you can't see what's going on inside primitive functions or byte code compiled code.
- If you're doing a lot of functional programming with anonymous functions, it can be hard to figure out exactly which function is being called. The easiest way to work around this is to name your functions.
- Lazy evaluation means that arguments are often evaluated inside another function. For example, in the following code, profiling would make it seem like `i()` was called by `j()` because the argument isn't evaluated until it's needed by `j()`.

```
i <- function() {
  pause(0.1)
  10
}
```

```
j <- function(x) {  
  x + 10  
}  
j(i())
```

If this is confusing, you can create temporary variables to force computation to happen earlier.

17.2 Improving performance

“We should forget about small efficiencies, say about 97% of the time: premature optimization is the root of all evil. Yet we should not pass up our opportunities in that critical 3%. A good programmer will not be lulled into complacency by such reasoning, he will be wise to look carefully at the critical code; but only after that code has been identified.”

— Donald Knuth.

Once you’ve used profiling to identify a bottleneck, you need to make it faster. The following sections introduce you to a number of techniques that I’ve found broadly useful:

1. Look for existing solutions.
2. Do less work.
3. Vectorise.
4. Parallelise.
5. Avoid copies.
6. Byte-code compile.

A final technique is to rewrite in a faster language, like C++. That’s a big topic and is covered in Chapter 19.

Before we get into specific techniques, I’ll first describe a general strategy and organisational style that’s useful when working on performance.

17.3 Code organisation

There are two traps that are easy to fall into when trying to make your code faster:

1. Writing faster but incorrect code.
2. Writing code that you think is faster, but is actually no better.

The strategy outlined below will help you avoid these pitfalls.

When tackling a bottleneck, you're likely to come up with multiple approaches. Write a function for each approach, encapsulating all relevant behaviour. This makes it easier to check that each approach returns the correct result and to time how long it takes to run. To demonstrate the strategy, I'll compare two approaches for computing the mean:

```
mean1 <- function(x) mean(x)
mean2 <- function(x) sum(x) / length(x)
```

I recommend that you keep a record of everything you try, even the failures. If a similar problem occurs in the future, it'll be useful to see everything you've tried. To do this I often use R Markdown, which makes it easy to intermingle code with detailed comments and notes.

Next, generate a representative test case. The case should be big enough to capture the essence of your problem but small enough that it takes only a few seconds to run. You don't want it to take too long because you'll need to run the test case many times to compare approaches. On the other hand, you don't want the case to be too small because then results might not scale up to the real problem.

Use this test case to quickly check that all variants return the same result. An easy way to do so is with `stopifnot()` and `all.equal()`. For real problems with fewer possible outputs, you may need more tests to make sure that an approach doesn't accidentally return the correct answer. That's unlikely for the mean.

```
x <- runif(100)
stopifnot(all.equal(mean1(x), mean2(x)))
```

Finally, use the `microbenchmark` package to compare how long each variation takes to run. For bigger problems, reduce the `times` parameter so that it only takes a couple of seconds to run. Focus on the median time, and use the upper and lower quartiles to gauge the variability of the measurement.

```
microbenchmark(
  mean1(x),
  mean2(x)
)
#> Unit: nanoseconds
#>      expr    min      lq median      uq     max neval
#> mean1(x) 5,030 5,260 5,400 5,660 47,100   100
#> mean2(x)   709   808 1,020 1,140 35,900   100
```

(You might be surprised by the results: `mean(x)` is considerably slower than `sum(x) / length(x)`. This is because, among other reasons, `mean(x)` makes two passes over the vector to be more numerically accurate.)

Before you start experimenting, you should have a target speed that defines when the bottleneck is no longer a problem. Setting such a goal is important because you don't want to spend valuable time over-optimising your code.

If you'd like to see this strategy in action, I've used it a few times on [stackoverflow](http://stackoverflow.com/questions/22515525#22518603):

- <http://stackoverflow.com/questions/22515525#22518603>
- <http://stackoverflow.com/questions/22515175#22515856>
- <http://stackoverflow.com/questions/3476015#22511936>

17.4 Has someone already solved the problem?

Once you've organised your code and captured all the variations you can think of, it's natural to see what others have done. You are part of a large community, and it's quite possible that someone has already tackled the same problem. If your bottleneck is a function in a package, it's worth looking at other packages that do the same thing. Two good places to start are:

- CRAN task views (<http://cran.rstudio.com/web/views/>). If there's a CRAN task view related to your problem domain, it's worth looking at the packages listed there.
- Reverse dependencies of Rcpp, as listed on its CRAN page (<http://cran.r-project.org/web/packages/Rcpp>). Since these packages use C++, it's possible to find a solution to your bottleneck written in a higher performance language.

Otherwise, the challenge is describing your bottleneck in a way that helps you find related problems and solutions. Knowing the name of the problem or its synonyms will make this search much easier. But because you don't know what it's called, it's hard to search for it! By reading broadly about statistics and algorithms, you can build up your own knowledge base over time. Alternatively, ask others. Talk to your colleagues and brainstorm some possible names, then search on Google and stackoverflow. It's often helpful to restrict your search to R related pages. For Google, try rseek (<http://www.rseek.org/>). For stackoverflow, restrict your search by including the R tag, [R], in your search.

As discussed above, record all solutions that you find, not just those that immediately appear to be faster. Some solutions might be initially slower, but because they are easier to optimise they end up being faster. You may also be able to combine the fastest parts from different approaches. If you've found a solution that's fast enough, congratulations! If appropriate, you may want to share your solution with the R community. Otherwise, read on.

17.4.1 Exercises

1. What are faster alternatives to `lm`? Which are specifically designed to work with larger datasets?
2. What package implements a version of `match()` that's faster for repeated lookups? How much faster is it?
3. List four functions (not just those in base R) that convert a string into a date time object. What are their strengths and weaknesses?
4. How many different ways can you compute a 1d density estimate in R?
5. Which packages provide the ability to compute a rolling mean?
6. What are the alternatives to `optim()`?

17.5 Do as little as possible

The easiest way to make a function faster is to let it do less work. One way to do that is use a function tailored to a more specific type of input or output, or a more specific problem. For example:

- `rowSums()`, `colSums()`, `rowMeans()`, and `colMeans()` are faster than equivalent invocations that use `apply()` because they are vectorised (the topic of the next section).
- `vapply()` is faster than `sapply()` because it pre-specifies the output type.
- If you want to see if a vector contains a single value, `any(x == 10)` is much faster than `10 %in% x`. This is because testing equality is simpler than testing inclusion in a set.

Having this knowledge at your fingertips requires knowing that alternative functions exist: you need to have a good vocabulary. Start with Chapter 4, and expand your vocab by regularly reading R code. Good places to read code are the R-help mailing list (<https://stat.ethz.ch/mailman/listinfo/r-help>) and stackoverflow (<http://stackoverflow.com/questions/tagged/r>).

Some functions coerce their inputs into a specific type. If your input is not the right type, the function has to do extra work. Instead, look for a function that works with your data as it is, or consider changing the way you store your data. The most common example of this problem is using `apply()` on a data frame. `apply()` always turns its input into a matrix. Not only is this error prone (because a data frame is more general than a matrix), it is also slower.

Other functions will do less work if you give them more information about the problem. It's always worthwhile to carefully read the documentation and experiment with different arguments. Some examples that I've discovered in the past include:

- `read.csv()`: specify known column types with `colClasses`.
- `factor()`: specify known levels with `levels`.

- `cut()`: don't generate labels with `labels = FALSE` if you don't need them, or, even better, use `findInterval()` as mentioned in the "see also" section of the documentation.
- `unlist(x, use.names = FALSE)` is much faster than `unlist(x)`.
- `interaction()`: if you only need combinations that exist in the data, use `drop = TRUE`.

Sometimes you can make a function faster by avoiding method dispatch. As we saw in (Section 16.3.1), method dispatch in R can be costly. If you're calling a method in a tight loop, you can avoid some of the costs by doing the method lookup only once:

- For S3, you can do this by calling `generic.class()` instead of `generic()`.
- For S4, you can do this by using `findMethod()` to find the method, saving it to a variable, and then calling that function.

For example, calling `mean.default()` quite a bit faster than calling `mean()` for small vectors:

```
x <- runif(1e2)

microbenchmark(
  mean(x),
  mean.default(x)
)
#> Unit: microseconds
#>          expr   min    lq median    uq   max neval
#>      mean(x)  4.38  4.56   4.70  4.89 43.70   100
#> mean.default(x) 1.32  1.44   1.52  1.66  6.92   100
```

This optimisation is a little risky. While `mean.default()` is almost twice as fast, it'll fail in surprising ways if `x` is not a numeric vector. You should only use it if you know for sure what `x` is.

Knowing that you're dealing with a specific type of input can be another way to write faster code. For example, `as.data.frame()` is quite slow because it coerces each element into a data frame and then `rbind()`s them together. If you have a named list with vectors of equal length, you can directly transform it into a data frame. In this case, if you're able to make strong assumptions about your input, you can write a method that's about 20x faster than the default.


```

quickdf <- function(l) {
  class(l) <- "data.frame"
  attr(l, "row.names") <- .set_row_names(length(l[[1]]))
  l
}

l <- lapply(1:26, function(i) runif(1e3))
names(l) <- letters

microbenchmark(
  quick_df      = quickdf(l),
  as.data.frame = as.data.frame(l)
)
#> Unit: microseconds
#>      expr      min       lq   median       uq      max neval
#>   quick_df    13.9    15.9    20.6    23.1    35.3   100
#> as.data.frame 1,410.0 1,470.0 1,510.0 1,540.0 31,500.0  100

```

Again, note the trade-off. This method is fast because it's dangerous. If you give it bad inputs, you'll get a corrupt data frame:

```

quickdf(list(x = 1, y = 1:2))
#> Warning: corrupt data frame: columns will be truncated or
#> padded with NAs
#>    x y
#> 1 1 1

```

To come up with this minimal method, I carefully read through and then rewrote the source code for `as.data.frame.list()` and `data.frame()`. I made many small changes, each time checking that I hadn't broken existing behaviour. After several hours work, I was able to isolate the minimal code shown above. This is a very useful technique. Most base R functions are written for flexibility and functionality, not performance. Thus, rewriting for your specific need can often yield substantial improvements. To do this, you'll need to read the source code. It can be complex and confusing, but don't give up!

The following example shows a progressive simplification of the `diff()` function if you only want computing differences between adjacent values. At each step, I replace one argument with a specific case, and then check to see that the function still works. The initial function is long and complicated, but by restricting the arguments I not only make it around twice as fast, I also make it easier to understand.

First, I take the code of `diff()` and reformat it to my style:

```
diff1 <- function (x, lag = 1L, differences = 1L) {
  ismat <- is.matrix(x)
  xlen <- if (ismat) dim(x)[1L] else length(x)
  if (length(lag) > 1L || length(differences) > 1L ||
      lag < 1L || differences < 1L)
    stop("'lag' and 'differences' must be integers >= 1")

  if (lag * differences >= xlen) {
    return(x[0L])
  }

  r <- unclass(x)
  i1 <- -seq_len(lag)
  if (ismat) {
    for (i in seq_len(differences)) {
      r <- r[i1, , drop = FALSE] -
        r[-nrow(r):-(nrow(r) - lag + 1L), , drop = FALSE]
    }
  } else {
    for (i in seq_len(differences)) {
      r <- r[i1] - r[-length(r):-(length(r) - lag + 1L)]
    }
  }
  class(r) <- oldClass(x)
  r
}
```

Next, I assume vector input. This allows me to remove the `is.matrix()` test and the method that uses matrix subsetting.

```
diff2 <- function (x, lag = 1L, differences = 1L) {
  xlen <- length(x)
  if (length(lag) > 1L || length(differences) > 1L ||
      lag < 1L || differences < 1L)
    stop("'lag' and 'differences' must be integers >= 1")

  if (lag * differences >= xlen) {
    return(x[0L])
  }
}
```

```

i1 <- -seq_len(lag)
for (i in seq_len(differences)) {
  x <- x[i1] - x[-length(x):- (length(x) - lag + 1L)]
}
x
}
diff2(cumsum(0:10))
#> [1] 1 2 3 4 5 6 7 8 9 10

```

I now assume that $\text{difference} = 1L$. This simplifies input checking and eliminates the for loop:

```

diff3 <- function (x, lag = 1L) {
  xlen <- length(x)
  if (length(lag) > 1L || lag < 1L)
    stop("'lag' must be integer >= 1")

  if (lag >= xlen) {
    return(x[0L])
  }

  i1 <- -seq_len(lag)
  x[i1] - x[-length(x):- (length(x) - lag + 1L)]
}
diff3(cumsum(0:10))
#> [1] 1 2 3 4 5 6 7 8 9 10

```

Finally I assume $\text{lag} = 1L$. This eliminates input checking and simplifies subsetting.

```

diff4 <- function (x) {
  xlen <- length(x)
  if (xlen <= 1) return(x[0L])

  x[-1] - x[-xlen]
}
diff4(cumsum(0:10))
#> [1] 1 2 3 4 5 6 7 8 9 10

```

Now `diff4()` is both considerably simpler and considerably faster than `diff1()`:

```
x <- runif(100)
microbenchmark(
  diff1(x),
  diff2(x),
  diff3(x),
  diff4(x)
)
#> Unit: microseconds
#>      expr    min      lq  median      uq   max neval
#>  diff1(x) 10.90 12.60 13.90 14.20 28.4   100
#>  diff2(x)  9.42 10.30 12.00 12.40 65.7   100
#>  diff3(x)  8.00  9.11 10.80 11.10 44.4   100
#>  diff4(x)  6.56  7.21  8.95  9.24 15.0   100
```

You'll be able to make `diff()` even faster for this special case once you've read Chapter 19.

A final example of doing less work is to use simpler data structures. For example, when working with rows from a data frame, it's often faster to work with row indices than data frames. For instance, if you wanted to compute a bootstrap estimate of the correlation between two columns in a data frame, there are two basic approaches: you can either work with the whole data frame or with the individual vectors. The following example shows that working with vectors is about twice as fast.

```
sample_rows <- function(df, i) sample.int(nrow(df), i,
  replace = TRUE)

# Generate a new data frame containing randomly selected rows
boot_cor1 <- function(df, i) {
  sub <- df[sample_rows(df, i), , drop = FALSE]
  cor(sub$x, sub$y)
}

# Generate new vectors from random rows
boot_cor2 <- function(df, i) {
  idx <- sample_rows(df, i)
  cor(df$x[idx], df$y[idx])
}

df <- data.frame(x = runif(100), y = runif(100))
microbenchmark(
  boot_cor1(df, 10),
```

```

boot_cor2(df, 10)
)
#> Unit: microseconds
#>      expr    min      lq  median      uq   max neval
#> boot_cor1(df, 10) 123.0 132.0 137.0 149.0 665   100
#> boot_cor2(df, 10)  74.7  78.5  80.2  86.1 109   100

```

17.5.1 Exercises

1. How do the results change if you compare `mean()` and `mean.default()` on 10,000 observations, rather than on 100?
2. The following code provides an alternative implementation of `rowSums()`. Why is it faster for this input?

```

rowSums2 <- function(df) {
  out <- df[[1L]]
  if (ncol(df) == 1) return(out)

  for (i in 2:ncol(df)) {
    out <- out + df[[i]]
  }
  out
}

df <- as.data.frame(
  replicate(1e3, sample(100, 1e4, replace = TRUE))
)
system.time(rowSums(df))
#>   user  system elapsed
#>  0.063   0.001   0.063
system.time(rowSums2(df))
#>   user  system elapsed
#>  0.039   0.009   0.049

```

3. What's the difference between `rowSums()` and `.rowSums()`?
4. Make a faster version of `chisq.test()` that only computes the chi-square test statistic when the input is two numeric vectors with no missing values. You can try simplifying `chisq.test()` or by coding from the mathematical definition (http://en.wikipedia.org/wiki/Pearson%27s_chi-squared_test).
5. Can you make a faster version of `table()` for the case of an

input of two integer vectors with no missing values? Can you use it to speed up your chi-square test?

6. Imagine you want to compute the bootstrap distribution of a sample correlation using `cor_df()` and the data in the example below. Given that you want to run this many times, how can you make this code faster? (Hint: the function has three components that you can speed up.)

```
n <- 1e6
df <- data.frame(a = rnorm(n), b = rnorm(n))

cor_df <- function(i) {
  i <- sample(seq(n), n * 0.01)
  cor(q[i, , drop = FALSE])[2,1]
}
```

Is there a way to vectorise this procedure?

17.6 Vectorise

If you’ve used R for any length of time, you’ve probably heard the admonishment to “vectorise your code”. But what does that actually mean? Vectorising your code is not just about avoiding for loops, although that’s often a step. Vectorising is about taking a “whole object” approach to a problem, thinking about vectors, not scalars. There are two key attributes of a vectorised function:

- It makes many problems simpler. Instead of having to think about the components of a vector, you only think about entire vectors.
- The loops in a vectorised function are written in C instead of R. Loops in C are much faster because they have much less overhead.

Chapter 11 stressed the importance of vectorised code as a higher level abstraction. Vectorisation is also important for writing fast R code. This doesn’t mean simply using `apply()` or `lapply()`, or even `Vectorise()`. Those functions improve the interface of a function, but don’t fundamentally change performance. Using vectorisation for performance means finding the existing R function that is implemented in C and most closely applies to your problem.

Vectorised functions that apply to many common performance bottlenecks include:

- `rowSums()`, `colSums()`, `rowMeans()`, and `colMeans()`. These vectorised matrix functions will always be faster than using `apply()`. You can sometimes use these functions to build other vectorised functions.

```
rowAny <- function(x) rowSums(x) > 0
rowAll <- function(x) rowSums(x) == ncol(x)
```

- Vectorised subsetting can lead to big improvements in speed. Remember the techniques behind lookup tables (Section 3.4.1) and matching and merging by hand (Section 3.4.2). Also remember that you can use subsetting assignment to replace multiple values in a single step. If `x` is a vector, matrix or data frame then `x[is.na(x)] <- 0` will replace all missing values with 0.
- If you're extracting or replacing values in scattered locations in a matrix or data frame, subset with an integer matrix. See Section 3.1.3 for more details.
- If you're converting continuous values to categorical make sure you know how to use `cut()` and `findInterval()`.
- Be aware of vectorised functions like `cumsum()` and `diff()`.

Matrix algebra is a general example of vectorisation. There loops are executed by highly tuned external libraries like BLAS. If you can figure out a way to use matrix algebra to solve your problem, you'll often get a very fast solution. The ability to solve problems with matrix algebra is a product of experience. While this skill is something you'll develop over time, a good place to start is to ask people with experience in your domain.

The downside of vectorisation is that it makes it harder to predict how operations will scale. The following example measures how long it takes to use character subsetting to lookup 1, 10, and 100 elements from a list. You might expect that looking up 10 elements would take 10x as long as looking up 1, and that looking up 100 elements would take 10x longer again. In fact, the following example shows that it only takes about 9 times longer to look up 100 elements than it does to look up 1.

```
lookup <- setNames(as.list(sample(100, 26)), letters)
```

```

x1 <- "j"
x10 <- sample(letters, 10)
x100 <- sample(letters, 100, replace = TRUE)

microbenchmark(
  lookup[x1],
  lookup[x10],
  lookup[x100]
)
#> Unit: nanoseconds
#>      expr    min      lq  median      uq    max neval
#>  lookup[x1]   549    616     709    818  2,040    100
#>  lookup[x10] 1,580  1,680  1,840  2,090 34,900    100
#>  lookup[x100] 5,450  5,570  7,670  8,160 25,900    100

```

Vectorisation won't solve every problem, and rather than torturing an existing algorithm into one that uses a vectorised approach, you're often better off writing your own vectorised function in C++. You'll learn how to do so in Chapter 19.

17.6.1 Exercises

1. The density functions, e.g., `dnorm()`, have a common interface. Which arguments are vectorised over? What does `rnorm(10, mean = 10:1)` do?
2. Compare the speed of `apply(x, 1, sum)` with `rowSums(x)` for varying sizes of `x`.
3. How can you use `crossprod()` to compute a weighted sum? How much faster is it than the naive `sum(x * w)`?

17.7 Avoid copies

A pernicious source of slow R code is growing an object with a loop. Whenever you use `c()`, `append()`, `cbind()`, `rbind()`, or `paste()` to create a bigger object, R must first allocate space for the new object and then copy the old object to its new home. If you're repeating this many times, like in a `for` loop, this can be quite expensive. You've entered Circle 2

of the “R inferno” (http://www.burns-stat.com/pages/Tutor/R_inferno.pdf).

Here’s a little example that shows the problem. We first generate some random strings, and then combine them either iteratively with a loop using `collapse()`, or in a single pass using `paste()`. Note that the performance of `collapse()` gets relatively worse as the number of strings grows: combining 100 strings takes almost 30 times longer than combining 10 strings.

```
random_string <- function() {
  paste(sample(letters, 50, replace = TRUE), collapse = "")
}
strings10 <- replicate(10, random_string())
strings100 <- replicate(100, random_string())

collapse <- function(xs) {
  out <- ""
  for (x in xs) {
    out <- paste0(out, x)
  }
  out
}

microbenchmark(
  loop10 = collapse(strings10),
  loop100 = collapse(strings100),
  vec10 = paste(strings10, collapse = ""),
  vec100 = paste(strings100, collapse = "")
)
#> Unit: microseconds
#>      expr      min      lq median      uq      max neval
#>   loop10   22.50   24.70   25.80   27.70    69.6   100
#>  loop100  866.00  894.00  900.00  919.00  1,350.0   100
#>    vec10    5.67    6.13    6.62    7.33    40.7   100
#>   vec100   45.90   47.70   48.80   52.60    74.7   100
```

Modifying an object in a loop, e.g., `x[i] <- y`, can also create a copy, depending on the class of `x`. Section 18.4 discusses this issue in more depth and gives you some tools to determine when you’re making copies.

17.8 Byte code compilation

R 2.13.0 introduced a byte code compiler which can increase the speed of some code. Using the compiler is an easy way to get improvements in speed. Even if it doesn't work well for your function, you won't have invested a lot of time in the effort. The following example shows the pure R version of `lapply()` from Section 11.1. Compiling it gives a considerable speedup, although it's still not quite as fast as the C version provided by base R.

```
lapply2 <- function(x, f, ...) {
  out <- vector("list", length(x))
  for (i in seq_along(x)) {
    out[[i]] <- f(x[[i]], ...)
  }
  out
}

lapply2_c <- compiler::cmpfun(lapply2)

x <- list(1:10, letters, c(F, T), NULL)
microbenchmark(
  lapply2(x, is.null),
  lapply2_c(x, is.null),
  lapply(x, is.null)
)
#> Unit: microseconds
#>           expr   min    lq median    uq   max neval
#>  lapply2(x, is.null) 5.49 5.88   6.15 6.83 17.2   100
#> lapply2_c(x, is.null) 3.06 3.30   3.47 3.79 34.8   100
#>    lapply(x, is.null) 2.25 2.49   2.67 2.92 38.5   100
```

Byte code compilation really helps here, but in most cases you're more likely to get a 5-10% improvement. All base R functions are byte code compiled by default.

17.9 Case study: t-test

The following case study shows how to make t-tests faster using some of the techniques described above. It's based on an example in "Computing thousands of test statistics simultaneously in R" (<http://stat-computing.org/newsletter/issues/scgn-18-1.pdf>) by Holger Schwender and Tina Müller. I thoroughly recommend reading the paper in full to see the same idea applied to other tests.

Imagine we have run 1000 experiments (rows), each of which collects data on 50 individuals (columns). The first 25 individuals in each experiment are assigned to group 1 and the rest to group 2. We'll first generate some random data to represent this problem:

```
m <- 1000
n <- 50
X <- matrix(rnorm(m * n, mean = 10, sd = 3), nrow = m)
grp <- rep(1:2, each = n / 2)
```

For data in this form, there are two ways to use `t.test()`. We can either use the formula interface or provide two vectors, one for each group. Timing reveals that the formula interface is considerably slower.

```
system.time(for(i in 1:m) t.test(X[i, ] ~ grp)$stat)
#>    user  system elapsed
#>  0.975   0.005   0.980
system.time(
  for(i in 1:m) t.test(X[i, grp == 1], X[i, grp == 2])$stat
)
#>    user  system elapsed
#>  0.210   0.001   0.211
```

Of course, a for loop computes, but doesn't save the values. We'll use `apply()` to do that. This adds a little overhead:

```
compT <- function(x, grp){
  t.test(x[grp == 1], x[grp == 2])$stat
}
system.time(t1 <- apply(X, 1, compT, grp = grp))
#>    user  system elapsed
#>  0.223   0.001   0.224
```

How can we make this faster? First, we could try doing less work. If you look at the source code of `stats::t.test.default()`, you'll see that it does a lot more than just compute the t-statistic. It also computes the p-value and formats the output for printing. We can try to make our code faster by stripping out those pieces.

```
my_t <- function(x, grp) {
  t_stat <- function(x) {
    m <- mean(x)
    n <- length(x)
    var <- sum((x - m) ^ 2) / (n - 1)

    list(m = m, n = n, var = var)
  }

  g1 <- t_stat(x[grp == 1])
  g2 <- t_stat(x[grp == 2])

  se_total <- sqrt(g1$var / g1$n + g2$var / g2$n)
  (g1$m - g2$m) / se_total
}
system.time(t2 <- apply(X, 1, my_t, grp = grp))
#>    user  system elapsed
#>  0.035   0.000   0.036
stopifnot(all.equal(t1, t2))
```

This gives us about a 6x speed improvement.

Now that we have a fairly simple function, we can make it faster still by vectorising it. Instead of looping over the array outside the function, we will modify `t_stat()` to work with a matrix of values. Thus, `mean()` becomes `rowMeans()`, `length()` becomes `ncol()`, and `sum()` becomes `rowSums()`. The rest of the code stays the same.

```
rowtstat <- function(X, grp){
  t_stat <- function(X) {
    m <- rowMeans(X)
    n <- ncol(X)
    var <- rowSums((X - m) ^ 2) / (n - 1)

    list(m = m, n = n, var = var)
  }
}
```

```

g1 <- t_stat(X[, grp == 1])
g2 <- t_stat(X[, grp == 2])

se_total <- sqrt(g1$var / g1$n + g2$var / g2$n)
(g1$m - g2$m) / se_total
}
system.time(t3 <- rowtstat(X, grp))
#>      user  system elapsed
#>  0.001    0.000    0.001
stopifnot(all.equal(t1, t3))

```

That's much faster! It's at least 40x faster than our previous effort, and around 1000x faster than where we started.

Finally, we could try byte code compilation. Here we'll need to use `microbenchmark()` instead of `system.time()` in order to get enough accuracy to see a difference:

```

rowtstat_bc <- compiler::cmpfun(rowtstat)

microbenchmark(
  rowtstat(X, grp),
  rowtstat_bc(X, grp),
  unit = "ms"
)
#> Unit: milliseconds
#>      expr    min    lq median    uq   max neval
#> rowtstat(X, grp) 0.819 1.11   1.16 1.19 14.0   100
#> rowtstat_bc(X, grp) 0.788 1.12   1.16 1.19 14.6   100

```

In this example, byte code compilation doesn't help at all.

17.10 Parallelise

Parallelisation uses multiple cores to work simultaneously on different parts of a problem. It doesn't reduce the computing time, but it saves your time because you're using more of your computer's resources. Parallel computing is a complex topic, and there's no way to cover it in depth here. Some resources I recommend are:

- *Parallel R* (<http://amazon.com/B005Z29QT4>) by Q. Ethan McCallum and Stephen Weston.
- *Parallel Computing for Data Science* (<http://heather.cs.ucdavis.edu/paralleldatasci.pdf>) by Norm Matloff.

What I want to show is a simple application of parallel computing to what are called “embarrassingly parallel problems”. An embarrassingly parallel problem is one that’s made up of many simple problems that can be solved independently. A great example of this is `lapply()` because it operates on each element independently of the others. It’s very easy to parallelise `lapply()` on Linux and the Mac because you simply substitute `mclapply()` for `lapply()`. The following code snippet runs a trivial (but slow) function on all cores of your computer.

```
library(parallel)

cores <- detectCores()
cores
#> [1] 8

pause <- function(i) {
  function(x) Sys.sleep(i)
}

system.time(lapply(1:10, pause(0.25)))
#>   user  system elapsed
#>  0.0    0.0    2.5
system.time(mclapply(1:10, pause(0.25), mc.cores = cores))
#>   user  system elapsed
#> 0.018  0.041  0.517
```

Life is a bit harder in Windows. You need to first set up a local cluster and then use `parLapply()`:

```
cluster <- makePSOCKcluster(cores)
system.time(parLapply(cluster, 1:10, function(i) Sys.sleep(1)))
#>   user  system elapsed
#> 0.003  0.000  2.004
```

The main difference between `mclapply()` and `makePSOCKcluster()` is that the individual processes generated by `mclapply()` inherit from the current

process, while those generated by `makePSOCKcluster()` start with a fresh session. This means that most real code will need some setup. Use `clusterEvalQ()` to run arbitrary code on each cluster and load needed packages, and `clusterExport()` to copy objects in the current session to the remote sessions.

```
x <- 10
psock <- parallel::makePSOCKcluster(1L)
clusterEvalQ(psock, x)
#> Error: one node produced an error: object 'x' not found

clusterExport(psock, "x")
clusterEvalQ(psock, x)
#> [[1]]
#> [1] 10
```

There is some communication overhead with parallel computing. If the subproblems are very small, then parallelisation might hurt rather than help. It's also possible to distribute computation over a network of computers (not just the cores on your local computer) but that's beyond the scope of this book, because it gets increasingly complicated to balance computation and communication costs. A good place to start for more information is the high performance computing CRAN task view (<http://cran.r-project.org/web/views/HighPerformanceComputing.html>).

17.11 Other techniques

Being able to write fast R code is part of being a good R programmer. Beyond the specific hints in this chapter, if you want to write fast R code, you'll need to improve your general programming skills. Some ways to do this are to:

- Read R blogs (<http://www.r-bloggers.com/>) to see what performance problems other people have struggled with, and how they have made their code faster.
- Read other R programming books, like Norm Matloff's *The Art of R Programming* (<http://amazon.com/1593273843>) or Patrick Burns' *R Inferno* (<http://www.burns-stat.com/documents/books/the-r-inferno/>) to learn about common traps.

- Take an algorithms and data structure course to learn some well known ways of tackling certain classes of problems. I have heard good things about Princeton's Algorithms course (<https://www.coursera.org/course/algs4partI>) offered on Coursera.
- Read general books about optimisation like *Mature optimisation* (<http://carlos.bueno.org/optimization/mature-optimization.pdf>) by Carlos Bueno, or the *Pragmatic Programmer* (<http://amazon.com/020161622X>) by Andrew Hunt and David Thomas.

You can also reach out to the community for help. Stackoverflow can be a useful resource. You'll need to put some effort into creating an easily digestible example that also captures the salient features of your problem. If your example is too complex, few people will have the time and motivation to attempt a solution. If it's too simple, you'll get answers that solve the toy problem but not the real problem. If you also try to answer questions on stackoverflow, you'll quickly get a feel for what makes a good question.

18

Memory

A solid understanding of R's memory management will help you predict how much memory you'll need for a given task and help you to make the most of the memory you have. It can even help you write faster code because accidental copies are a major cause of slow code. The goal of this chapter is to help you understand the basics of memory management in R, moving from individual objects to functions to larger blocks of code. Along the way, you'll learn about some common myths, such as that you need to call `gc()` to free up memory, or that for loops are always slow.

Outline

- Section 18.1 shows you how to use `object_size()` to see how much memory an object occupies, and uses that as a launching point to improve your understanding of how R objects are stored in memory.
- Section 18.2 introduces you to the `mem_used()` and `mem_changed()` functions that will help you understand how R allocates and frees memory.
- Section 18.3 shows you how to use the `lineprof` package to understand how memory is allocated and released in larger code blocks.
- Section 18.4 introduces you to the `address()` and `refs()` functions so that you can understand when R modifies in place and when R modifies a copy. Understanding when objects are copied is very important for writing efficient R code.

Prerequisites

In this chapter, we'll use tools from the `pryr` and `lineprof` packages to understand memory usage, and a sample dataset from `ggplot2`. If you don't already have them, run this code to get the packages you need:

```
install.packages("ggplot2")
install.packages("pryr")
devtools::install_github("hadley/lineprof")
```

Sources

The details of R's memory management are not documented in a single place. Most of the information in this chapter was gleaned from a close reading of the documentation (particularly `?Memory` and `?gc`), the memory profiling (<http://cran.r-project.org/doc/manuals/R-exts.html#Profiling-R-code-for-memory-use>) section of `R-exts`, and the `SEXP`s (<http://cran.r-project.org/doc/manuals/R-ints.html#SEXP>s) section of `R-ints`. The rest I figured out by reading the C source code, performing small experiments, and asking questions on `R-devel`. Any mistakes are entirely mine.

18.1 Object size

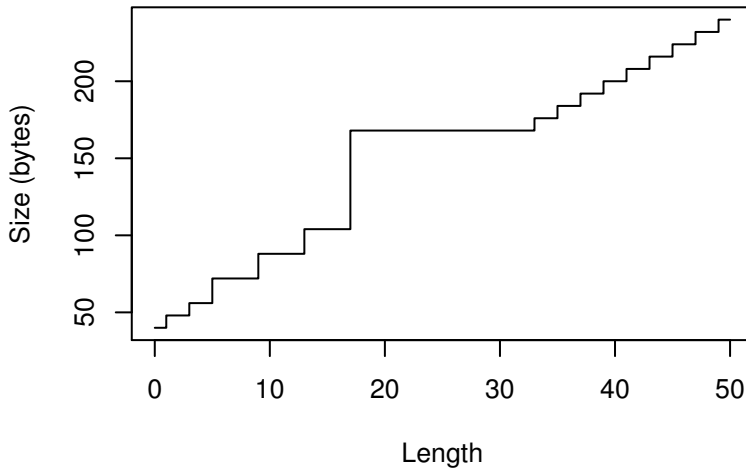
To understand memory usage in R, we will start with `pryr::object_size()`. This function tells you how many bytes of memory an object occupies:

```
library(pryr)
object_size(1:10)
#> 88 B
object_size(mean)
#> 832 B
object_size(mtcars)
#> 6.74 kB
```

(This function is better than the built-in `object.size()` because it accounts for shared elements within an object and includes the size of environments.)

Something interesting occurs if we use `object_size()` to systematically explore the size of an integer vector. The code below computes and plots the memory usage of integer vectors ranging in length from 0 to 50 elements. You might expect that the size of an empty vector would be zero and that memory usage would grow proportionately with length. Neither of those things are true!

```
sizes <- sapply(0:50, function(n) object_size(seq_len(n)))
plot(0:50, sizes, xlab = "Length", ylab = "Size (bytes)",
     type = "s")
```



This isn't just an artefact of integer vectors. Every length 0 vector occupies 40 bytes of memory:

```
object_size(numeric())
#> 40 B
object_size(logical())
#> 40 B
object_size(raw())
#> 40 B
object_size(list())
#> 40 B
```

Those 40 bytes are used to store four components possessed by every object in R:

- Object metadata (4 bytes). These metadata store the base type (e.g. integer) and information used for debugging and memory management.
- Two pointers: one to the next object in memory and one to the previous object (2 * 8 bytes). This doubly-linked list makes it easy for internal R code to loop through every object in memory.
- A pointer to the attributes (8 bytes).

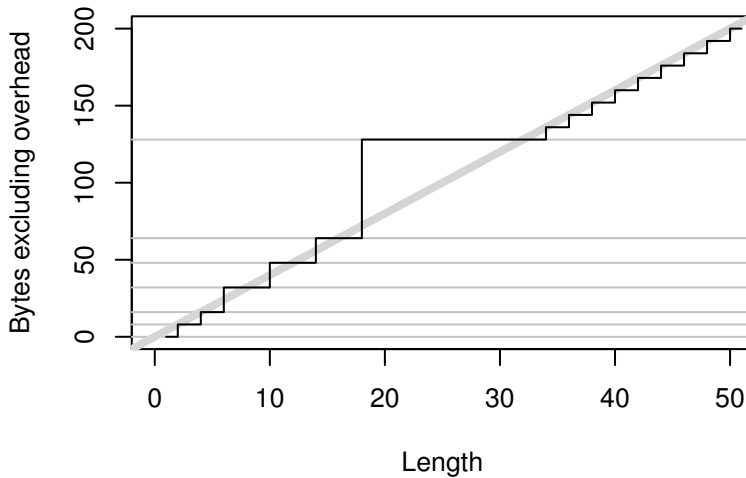
All vectors have three additional components:

- The length of the vector (4 bytes). By using only 4 bytes, you might expect that R could only support vectors up to $2^{4 \times 8 - 1}$ (2^{31} , about two billion) elements. But in R 3.0.0 and later, you can actually have vectors up to 2^{52} elements. Read R-internals (<http://cran.r-project.org/doc/manuals/R-ints.html#Long-vectors>) to see how support for long vectors was added without having to change the size of this field.
- The “true” length of the vector (4 bytes). This is basically never used, except when the object is the hash table used for an environment. In that case, the true length represents the allocated space, and the length represents the space currently used.
- The data (?? bytes). An empty vector has 0 bytes of data, but it’s obviously very important otherwise! Numeric vectors occupy 8 bytes for every element, integer vectors 4, and complex vectors 16.

If you’re keeping count you’ll notice that this only adds up to 36 bytes. The remaining 4 bytes are used for padding so that each component starts on an 8 byte (= 64-bit) boundary. Most cpu architectures require pointers to be aligned in this way, and even if they don’t require it, accessing non-aligned pointers tends to be rather slow. (If you’re interested, you can read more about it in C structure packing (<http://www.catb.org/esr/structure-packing/>).)

This explains the intercept on the graph. But why does the memory size grow irregularly? To understand why, you need to know a little bit about how R requests memory from the operating system. Requesting memory (with `malloc()`) is a relatively expensive operation. Having to request memory every time a small vector is created would slow R down considerably. Instead, R asks for a big block of memory and then manages that block itself. This block is called the small vector pool and is used for vectors less than 128 bytes long. For efficiency and simplicity, it only allocates vectors that are 8, 16, 32, 48, 64, or 128 bytes long. If we adjust our previous plot to remove the 40 bytes of overhead, we can see that those values correspond to the jumps in memory use.

```
plot(0:50, sizes - 40, xlab = "Length",
     ylab = "Bytes excluding overhead", type = "n")
abline(h = 0, col = "grey80")
abline(h = c(8, 16, 32, 48, 64, 128), col = "grey80")
abline(a = 0, b = 4, col = "grey90", lwd = 4)
lines(sizes - 40, type = "s")
```



Beyond 128 bytes, it no longer makes sense for R to manage vectors. After all, allocating big chunks of memory is something that operating systems are very good at. Beyond 128 bytes, R will ask for memory in multiples of 8 bytes. This ensures good alignment.

A subtlety of the size of an object is that components can be shared across multiple objects. For example, look at the following code:

```
x <- 1:1e6
object_size(x)
#> 4 MB

y <- list(x, x, x)
object_size(y)
#> 4 MB
```

`y` isn't three times as big as `x` because R is smart enough to not copy `x` three times; instead it just points to the existing `x`.

It's misleading to look at the sizes of `x` and `y` individually. If you want to know how much space they take up together, you have to supply them to the same `object_size()` call:

```
object_size(x, y)
#> 4 MB
```

In this case, `x` and `y` together take up the same amount of space as `y` alone. This is not always the case. If there are no shared components,

as in the following example, then you can add up the sizes of individual components to find out the total size:

```
x1 <- 1:1e6
y1 <- list(1:1e6, 1:1e6, 1:1e6)

object_size(x1)
#> 4 MB
object_size(y1)
#> 12 MB
object_size(x1, y1)
#> 16 MB
object_size(x1) + object_size(y1) == object_size(x1, y1)
#> [1] TRUE
```

The same issue also comes up with strings, because R has a global string pool. This means that each unique string is only stored in one place, and therefore character vectors take up less memory than you might expect:

```
object_size("banana")
#> 96 B
object_size(rep("banana", 10))
#> 216 B
```

18.1.1 Exercises

1. Repeat the analysis above for numeric, logical, and complex vectors.
2. If a data frame has one million rows, and three variables (two numeric, and one integer), how much space will it take up? Work out it out from theory, then verify your work by creating a data frame and measuring its size.
3. Compare the sizes of the elements in the following two lists. Each contains basically the same data, but one contains vectors of small strings while the other contains a single long string.

```
vec <- lapply(0:50, function(i) c("ba", rep("na", i)))
str <- lapply(vec, paste0, collapse = "")
```

4. Which takes up more memory: a factor (`x`) or the equivalent character vector (`as.character(x)`)? Why?
5. Explain the difference in size between `1:5` and `list(1:5)`.

18.2 Memory usage and garbage collection

While `object_size()` tells you the size of a single object, `pryr::mem_used()` tells you the total size of all objects in memory:

```
library(pryr)
mem_used()
#> 45.4 MB
```

This number won't agree with the amount of memory reported by your operating system for a number of reasons:

1. It only includes objects created by R, not the R interpreter itself.
2. Both R and the operating system are lazy: they won't reclaim memory until it's actually needed. R might be holding on to memory because the OS hasn't yet asked for it back.
3. R counts the memory occupied by objects but there may be gaps due to deleted objects. This problem is known as memory fragmentation.

`mem_change()` builds on top of `mem_used()` to tell you how memory changes during code execution. Positive numbers represent an increase in the memory used by R, and negative numbers represent a decrease.

```
# Need about 4 mb to store 1 million integers
mem_change(x <- 1:1e6)
#> 4.01 MB
# We get that memory back when we delete it
mem_change(rm(x))
#> -4 MB
```

Even operations that don't do anything use up a little memory. This is because R is tracking the history of everything you do. You can ignore anything on the order of around 2 kB.

```
mem_change(NULL)
#> 1.47 kB
mem_change(NULL)
#> 1.47 kB
```

In some languages, you have to explicitly delete unused objects for their memory to be returned. R uses an alternative approach: garbage collection (or GC for short). GC automatically releases memory when an object is no longer used. It does this by tracking how many names point to each object, and when there are no names pointing to an object, it deletes that object.

```
# Create a big object
mem_change(x <- 1:1e6)
#> 4 MB
# Also point to 1:1e6 from y
mem_change(y <- x)
#> -4 MB
# Remove x, no memory freed because y is still pointing to it
mem_change(rm(x))
#> 1.42 kB
# Now nothing points to it and the memory can be freed
mem_change(rm(y))
#> -4 MB
```

Despite what you might have read elsewhere, there's never any need to call `gc()` yourself. R will automatically run garbage collection whenever it needs more space; if you want to see when that is, call `gcinfo(TRUE)`. The only reason you *might* want to call `gc()` is to ask R to return memory to the operating system. However, even that might not have any effect: older versions of Windows had no way for a program to return memory to the OS.

GC takes care of releasing objects that are no longer used. However, you do need to be aware of possible memory leaks. A memory leak occurs when you keep pointing to an object without realising it. In R, the two main causes of memory leaks are formulas and closures because they both capture the enclosing environment. The following code illustrates the problem. In `f1()`, `1:1e6` is only referenced inside the function, so when the function completes the memory is returned and the net change is 0. The net memory change will be 0. `f2()` and `f3()` both return objects that capture environments, so that `x` is not freed when the function completes.


```
f1 <- function() {  
  x <- 1:1e6  
  10  
}  
mem_change(x <- f1())  
#> 1.38 kB  
object_size(x)  
#> 48 B  
  
f2 <- function() {  
  x <- 1:1e6  
  a ~ b  
}  
mem_change(y <- f2())  
#> 4 MB  
object_size(y)  
#> 4 MB  
  
f3 <- function() {  
  x <- 1:1e6  
  function() 10  
}  
mem_change(z <- f3())  
#> 4 MB  
object_size(z)  
#> 4.01 MB
```

18.3 Memory profiling with lineprof

`mem_change()` captures the net change in memory when running a block of code. Sometimes, however, we may want to measure incremental change. One way to do this is to use memory profiling to capture usage every few milliseconds. This functionality is provided by `utils::Rprof()` but it doesn't provide a very useful display of the results. Instead we'll use the `lineprof` (<https://github.com/hadley/lineprof>) package. It is powered by `Rprof()`, but displays the results in a more informative manner.

To demonstrate `lineprof`, we're going to explore a bare-bones implementation of `read.delim()` with only three arguments:

```

read_delim <- function(file, header = TRUE, sep = ",") {
  # Determine number of fields by reading first line
  first <- scan(file, what = character(1), nlines = 1,
    sep = sep, quiet = TRUE)
  p <- length(first)

  # Load all fields as character vectors
  all <- scan(file, what = as.list(rep("character", p)),
    sep = sep, skip = if (header) 1 else 0, quiet = TRUE)

  # Convert from strings to appropriate types (never to factors)
  all[] <- lapply(all, type.convert, as.is = TRUE)

  # Set column names
  if (header) {
    names(all) <- first
  } else {
    names(all) <- paste0("V", seq_along(all))
  }

  # Convert list into data frame
  as.data.frame(all)
}

```

We'll also create a sample csv file:

```

library(ggplot2)
write.csv(diamonds, "diamonds.csv", row.names = FALSE)

```












Using `lineprof` is straightforward. `source()` the code, apply `lineprof()` to an expression, then use `shine()` to view the results. Note that you *must* use `source()` to load the code. This is because `lineprof` uses `srcrefs` to match up the code and run times. The needed `srcrefs` are only created when you load code from disk.

```

library(lineprof)

source("code/read-delim.R")
prof <- lineprof(read_delim("diamonds.csv"))
shine(prof)

```

| # | Source code | t | r | a | d |
|----|--|---|---|---|---|
| 1 | # ---- read_delim | | | | |
| 2 | read_delim <- function(file, header = TRUE, sep = ",") { | | | | |
| 3 | # Determine number of fields by reading first line | | | | |
| 4 | first <- scan(file, what = character(1), nlines = 1, se... | | | | |
| 5 | p <- length(first) | | | | |
| 6 | | | | | |
| 7 | # Load all fields as character vectors | | | | |
| 8 | all <- scan(file, what = as.list(rep("character", p)), ... |  |  |  |  |
| 9 | skip = if (header) 1 else 0, quiet = TRUE) | | | | |
| 10 | | | | | |
| 11 | # Convert from strings to appropriate types (never to f... | | | | |
| 12 | all[] <- lapply(all, type.convert, as.is = TRUE) |  |  |  | |
| 13 | | | | | |
| 14 | # Set column names | | | | |
| 15 | if (header) { | | | | |
| 16 | names(all) <- first | | | | |
| 17 | } else { | | | | |
| 18 | names(all) <- paste0("V", seq_along(all)) | | | | |
| 19 | } | | | | |
| 20 | | | | | |
| 21 | # Convert list into data frame | | | | |
| 22 | as.data.frame(all) |  |  |  |  |
| 23 | } | | | | |

shine() will also open a new web page (or if you're using RStudio, a new pane) that shows your source code annotated with information about memory usage. shine() starts a shiny app which will "block" your R session. To exit, press escape or ctrl + break.

Next to the source code, four columns provide details about the performance of the code:

- t, the time (in seconds) spent on that line of code (explained in Section 17.1).
- a, the memory (in megabytes) allocated by that line of code.
- r, the memory (in megabytes) released by that line of code. While memory allocation is deterministic, memory release is stochastic: it depends on when the GC was run. This means that memory release only tells you that the memory released was no longer needed before this line.

- `d`, the number of vector duplications that occurred. A vector duplication occurs when R copies a vector as a result of its copy on modify semantics.

You can hover over any of the bars to get the exact numbers. In this example, looking at the allocations tells us most of the story:

- `scan()` allocates about 2.5 MB of memory, which is very close to the 2.8 MB of space that the file occupies on disk. You wouldn't expect the two numbers to be identical because R doesn't need to store the commas and because the global string pool will save some memory.
- Converting the columns allocates another 0.6 MB of memory. You'd also expect this step to free some memory because we've converted string columns into integer and numeric columns (which occupy less space), but we can't see those releases because GC hasn't been triggered yet.
- Finally, calling `as.data.frame()` on a list allocates about 1.6 megabytes of memory and performs over 600 duplications. This is because `as.data.frame()` isn't terribly efficient and ends up copying the input multiple times. We'll discuss duplication more in the next section.

There are two downsides to profiling:

1. `read_delim()` only takes around half a second, but profiling can, at best, capture memory usage every 1 ms. This means we'll only get about 500 samples.
2. Since GC is lazy, we can never tell exactly when memory is no longer needed.

You can work around both problems by using `torture = TRUE`, which forces R to run GC after every allocation (see `gctorture()` for more details). This helps with both problems because memory is freed as soon as possible, and R runs 10–100x slower. This effectively makes the resolution of the timer greater, so that you can see smaller allocations and exactly when memory is no longer needed.

18.3.1 Exercises

1. When the input is a list, we can make a more efficient `as.data.frame()` by using special knowledge. A data frame is

a list with class `data.frame` and `row.names` attribute. `row.names` is either a character vector or vector of sequential integers, stored in a special format created by `.set_row_names()`. This leads to an alternative `as.data.frame()`:

```
to_df <- function(x) {
  class(x) <- "data.frame"
  attr(x, "row.names") <- .set_row_names(length(x[[1]]))
  x
}
```

What impact does this function have on `read_delim()`? What are the downsides of this function?

2. Line profile the following function with `torture = TRUE`. What is surprising? Read the source code of `rm()` to figure out what's going on.

```
f <- function(n = 1e5) {
  x <- rep(1, n)
  rm(x)
}
```

18.4 Modification in place

What happens to `x` in the following code?

```
x <- 1:10
x[5] <- 10
x
#> [1] 1 2 3 4 10 6 7 8 9 10
```

There are two possibilities:

1. R modifies `x` in place.
2. R makes a copy of `x` to a new location, modifies the copy, and then uses the name `x` to point to the new location.

It turns out that R can do either depending on the circumstances. In the example above, it will modify in place. But if another variable also points to `x`, then R will copy it to a new location. To explore what's going on in greater detail, we use two tools from the `pryr` package. Given the name of a variable, `address()` will tell us the variable's location in memory and `refs()` will tell us how many names point to that location.

```
library(pryr)
x <- 1:10
c(address(x), refs(x))
# [1] "0x103100060" "1"

y <- x
c(address(y), refs(y))
# [1] "0x103100060" "2"
```

(Note that if you're using RStudio, `refs()` will always return 2: the environment browser makes a reference to every object you create on the command line.)

`refs()` is only an estimate. It can only distinguish between one and more than one reference (future versions of R might do better). This means that `refs()` returns 2 in both of the following cases:

```
x <- 1:5
y <- x
rm(y)
# Should really be 1, because we've deleted y
refs(x)
#> [1] 2

x <- 1:5
y <- x
z <- x
# Should really be 3
refs(x)
#> [1] 2
```

When `refs(x)` is 1, modification will occur in place. When `refs(x)` is 2, R will make a copy (this ensures that other pointers to the object remain unaffected). Note that in the following example, `y` keeps pointing to the same location while `x` changes.

```
x <- 1:10
y <- x
c(address(x), address(y))
#> [1] "0x7fa9239c65b0" "0x7fa9239c65b0"

x[5] <- 6L
c(address(x), address(y))
#> [1] "0x7fa926be6a08" "0x7fa9239c65b0"
```

Another useful function is `tracemem()`. It prints a message every time the traced object is copied:

```
x <- 1:10
# Prints the current memory location of the object
tracemem(x)
# [1] "<0x7feeaaa1c6b8>"

x[5] <- 6L

y <- x
# Prints where it has moved from and to
x[5] <- 6L
# tracemem[0x7feeaaa1c6b8 -> 0x7feeaaa1c768]:
```

For interactive use, `tracemem()` is slightly more useful than `refs()`, but because it just prints a message, it's harder to program with. I don't use it in this book because it interacts poorly with `knitr` (<http://yihui.name/knitr/>), the tool I use to interleave text and code.

Non-primitive functions that touch the object always increment the ref count. Primitive functions usually don't. (The reasons are a little complicated, but see the R-devel thread confused about NAMED (<http://r.789695.n4.nabble.com/Confused-about-NAMED-td4103326.html>)).

```
# Touching the object forces an increment
f <- function(x) x
{x <- 1:10; f(x); refs(x)}
#> [1] 2

# Sum is primitive, so no increment
{x <- 1:10; sum(x); refs(x)}
#> [1] 1
```

```
# f() and g() never evaluate x, so refs don't increment
f <- function(x) 10
g <- function(x) substitute(x)

{x <- 1:10; f(x); refs(x)}
#> [1] 1
{x <- 1:10; g(x); refs(x)}
#> [1] 1
```

Generally, provided that the object is not referred to elsewhere, any primitive replacement function will modify in place. This includes `[[<-`, `[<-`, `@<-`, `$<-`, `attr<-`, `attributes<-`, `class<-`, `dim<-`, `dimnames<-`, `names<-`, and `levels<-`. To be precise, all non-primitive functions increment refs, but a primitive function may be written in such a way that it doesn't. The rules are sufficiently complicated that there's little point in trying to memorise them. Instead, you should approach the problem practically by using `refs()` and `address()` to figure out when objects are being copied.

While determining that copies are being made is not hard, preventing such behaviour is. If you find yourself resorting to exotic tricks to avoid copies, it may be time to rewrite your function in C++, as described in Chapter 19.

18.4.1 Loops

For loops in R have a reputation for being slow. Often that slowness is because you're modifying a copy instead of modifying in place. Consider the following code. It subtracts the median from each column of a large data frame:

```
x <- data.frame(matrix(runif(100 * 1e4), ncol = 100))
medians <- vapply(x, median, numeric(1))

for(i in seq_along(medians)) {
  x[, i] <- x[, i] - medians[i]
}
```

You may be surprised to realise that every iteration of the loop copies the data frame. We can see that more clearly by using `address()` and `refs()` for a small sample of the loop:


```

for(i in 1:5) {
  x[, i] <- x[, i] - medians[i]
  print(c(address(x), refs(x)))
}
#> [1] "0x7fa92502c3e0" "2"
#> [1] "0x7fa92502cdd0" "2"
#> [1] "0x7fa92502d7c0" "2"
#> [1] "0x7fa92502e1b0" "2"
#> [1] "0x7fa92500bfe0" "2"

```

For each iteration, `x` is moved to a new location so `refs(x)` is always 2. This occurs because `[<- .data.frame` is not a primitive function, so it always increments the refs. We can make the function substantially more efficient by using a list instead of a data frame. Modifying a list uses primitive functions, so the refs are not incremented and all modifications occur in place:

```

y <- as.list(x)

for(i in 1:5) {
  y[[i]] <- y[[i]] - medians[i]
  print(c(address(y), refs(y)))
}
#> [1] "0x7fa9250238d0" "2"
#> [1] "0x7fa925016850" "2"
#> [1] "0x7fa9250027e0" "2"
#> [1] "0x7fa92501fd60" "2"
#> [1] "0x7fa925006be0" "2"

```

This behaviour was substantially more problematic prior to R 3.1.0, because every copy of the data frame was a deep copy. This made the motivating example take around 5 s, compared to 0.01 s today.

18.4.2 Exercises

1. The code below makes one duplication. Where does it occur and why? (Hint: look at `refs(y)`.)

```

y <- as.list(x)
for(i in seq_along(medians)) {
  y[[i]] <- y[[i]] - medians[i]
}

```

2. The implementation of `as.data.frame()` in the previous section has one big downside. What is it and how could you avoid it?

19

High performance functions with Rcpp

Sometimes R code just isn't fast enough. You've used profiling to figure out where your bottlenecks are, and you've done everything you can in R, but your code still isn't fast enough. In this chapter you'll learn how to improve performance by rewriting key functions in C++. This magic comes by way of the Rcpp (<http://www.rcpp.org/>) package, a fantastic tool written by Dirk Eddelbuettel and Romain Francois (with key contributions by Doug Bates, John Chambers, and JJ Allaire). Rcpp makes it very simple to connect C++ to R. While it is *possible* to write C or Fortran code for use in R, it will be painful by comparison. Rcpp provides a clean, approachable API that lets you write high-performance code, insulated from R's arcane C API.

Typical bottlenecks that C++ can address include:

- Loops that can't be easily vectorised because subsequent iterations depend on previous ones.
- Recursive functions, or problems which involve calling functions millions of times. The overhead of calling a function in C++ is much lower than that in R.
- Problems that require advanced data structures and algorithms that R doesn't provide. Through the standard template library (STL), C++ has efficient implementations of many important data structures, from ordered maps to double-ended queues.

The aim of this chapter is to discuss only those aspects of C++ and Rcpp that are absolutely necessary to help you eliminate bottlenecks in your code. We won't spend much time on advanced features like object oriented programming or templates because the focus is on writing small, self-contained functions, not big programs. A working knowledge of C++ is helpful, but not essential. Many good tutorials and references are freely available, including <http://www.learnrcpp.com/> and <http://www.cplusplus.com/>. For more advanced topics, the *Effective C++* series by

Scott Meyers is popular choice. You may also enjoy Dirk Eddelbuettel's *Seamless R and C++ integration with Rcpp* (<http://www.springer.com/statistics/computational+statistics/book/978-1-4614-6867-7>), which goes into much greater detail into all aspects of Rcpp.

Outline

- Section 19.1 teaches you how to write C++ by converting simple R functions to their C++ equivalents. You'll learn how C++ differs from R, and what the key scalar, vector, and matrix classes are called.
- Section 19.1.6 shows you how to use `sourceCpp()` to load a C++ file from disk in the same way you use `source()` to load a file of R code.
- Section 19.2 discusses how to modify attributes from Rcpp, and mentions some of the other important classes.
- Section 19.3 teaches you how to work with R's missing values in C++.
- Section 19.4 discusses Rcpp "sugar", which allows you to avoid loops in C++ and write code that looks very similar to vectorised R code.
- Section 19.5 shows you how to use some of the most important data structures and algorithms from the standard template library, or STL, built-in to C++.
- Section 19.6 shows two real case studies where Rcpp was used to get considerable performance improvements.
- Section 19.7 teaches you how to add C++ code to a package.
- Section 19.8 concludes the chapter with pointers to more resources to help you learn Rcpp and C++.

Prerequisites

All examples in this chapter need version 0.10.1 or above of the Rcpp package. This version includes `cppFunction()` and `sourceCpp()`, which makes it very easy to connect C++ to R. Install the latest version of Rcpp from CRAN with `install.packages("Rcpp")`.

You'll also need a working C++ compiler. To get it:

- On Windows, install Rtools (<http://cran.r-project.org/bin/windows/Rtools/>).
- On Mac, install Xcode from the app store.
- On Linux, `sudo apt-get install r-base-dev` or similar.

19.1 Getting started with C++

`cppFunction()` allows you to write C++ functions in R:

```
library(Rcpp)
#>
#> Attaching package: 'Rcpp'
#>
#> The following object is masked from 'package:inline':
#>
#>     registerPlugin
cppFunction('int add(int x, int y, int z) {
  int sum = x + y + z;
  return sum;
}')
# add works like a regular R function
add
#> function (x, y, z)
#> .Primitive(".Call")(<pointer: 0x10fff9e10>, x, y, z)
add(1, 2, 3)
#> [1] 6
```

When you run this code, Rcpp will compile the C++ code and construct an R function that connects to the compiled C++ function. We're going to use this simple interface to learn how to write C++. C++ is a large language, and there's no way to cover it all in just one chapter. Instead, you'll get the basics so that you can start writing useful functions to address bottlenecks in your R code.

The following sections will teach you the basics by translating simple R functions to their C++ equivalents. We'll start simple with a function that has no inputs and a scalar output, and then get progressively more complicated:

- Scalar input and scalar output
- Vector input and scalar output
- Vector input and vector output
- Matrix input and vector output

19.1.1 No inputs, scalar output

Let's start with a very simple function. It has no arguments and always returns the integer 1:

```
one <- function() 1L
```

The equivalent C++ function is:

```
int one() {  
    return 1;  
}
```

We can compile and use this from R with `cppFunction`

```
cppFunction('int one() {  
    return 1;  
}')
```

This small function illustrates a number of important differences between R and C++:

- The syntax to create a function looks like the syntax to call a function; you don't use assignment to create functions as you do in R.
- You must declare the type of output the function returns. This function returns an `int` (a scalar integer). The classes for the most common types of R vectors are: `NumericVector`, `IntegerVector`, `CharacterVector`, and `LogicalVector`.
- Scalars and vectors are different. The scalar equivalents of numeric, integer, character, and logical vectors are: `double`, `int`, `String`, and `bool`.
- You must use an explicit `return` statement to return a value from a function.
- Every statement is terminated by a `;`.

19.1.2 Scalar input, scalar output

The next example function implements a scalar version of the `sign()` function which returns 1 if the input is positive, and -1 if it's negative:

```
signR <- function(x) {  
  if (x > 0) {  
    1  
  } else if (x == 0) {  
    0  
  } else {  
    -1  
  }  
}  
  
cppFunction('int signC(int x) {  
  if (x > 0) {  
    return 1;  
  } else if (x == 0) {  
    return 0;  
  } else {  
    return -1;  
  }  
}')  
}
```

In the C++ version:

- We declare the type of each input in the same way we declare the type of the output. While this makes the code a little more verbose, it also makes it very obvious what type of input the function needs.
- The `if` syntax is identical — while there are some big differences between R and C++, there are also lots of similarities! C++ also has a `while` statement that works the same way as R's. As in R you can use `break` to exit the loop, but to skip one iteration you need to use `continue` instead of `next`.

19.1.3 Vector input, scalar output

One big difference between R and C++ is that the cost of loops is much lower in C++. For example, we could implement the `sum` function in R using a loop. If you've been programming in R a while, you'll probably have a visceral reaction to this function!

```
sumR <- function(x) {
  total <- 0
  for (i in seq_along(x)) {
    total <- total + x[i]
  }
  total
}
```

In C++, loops have very little overhead, so it's fine to use them. In Section 19.5, you'll see alternatives to `for` loops that more clearly express your intent; they're not faster, but they can make your code easier to understand.

```
cppFunction('double sumC(NumericVector x) {
  int n = x.size();
  double total = 0;
  for(int i = 0; i < n; ++i) {
    total += x[i];
  }
  return total;
}')
```

The C++ version is similar, but:

- To find the length of the vector, we use the `.size()` method, which returns an integer. C++ methods are called with `.` (i.e., a full stop).
- The `for` statement has a different syntax: `for(init; check; increment)`. This loop is initialised by creating a new variable called `i` with value 0. Before each iteration we check that `i < n`, and terminate the loop if it's not. After each iteration, we increment the value of `i` by one, using the special prefix operator `++` which increases the value of `i` by 1.
- In C++, vector indices start at 0. I'll say this again because it's so important: **IN C++, VECTOR INDICES START AT 0!** This is a very common source of bugs when converting R functions to C++.
- Use `=` for assignment, not `<-`.
- C++ provides operators that modify in-place: `total += x[i]` is equivalent to `total = total + x[i]`. Similar in-place operators are `-=`, `*=`, and `/=`.

This is a good example of where C++ is much more efficient than R. As shown by the following microbenchmark, `sumC()` is competitive with the built-in (and highly optimised) `sum()`, while `sumR()` is several orders of magnitude slower.

```
x <- runif(1e3)
microbenchmark(
  sum(x),
  sumC(x),
  sumR(x)
)
#> Unit: microseconds
#>      expr      min       lq  median       uq      max neval
#>   sum(x)    1.07    1.33    1.66    1.95    6.24   100
#>  sumC(x)    2.49    2.99    3.54    4.36   21.50   100
#>  sumR(x) 333.00 367.00 388.00 428.00 1,390.00   100
```

19.1.4 Vector input, vector output

Next we'll create a function that computes the Euclidean distance between a value and a vector of values:

```
pdistR <- function(x, ys) {
  sqrt((x - ys) ^ 2)
}
```

It's not obvious that we want `x` to be a scalar from the function definition. We'd need to make that clear in the documentation. That's not a problem in the C++ version because we have to be explicit about types:

```
cppFunction('NumericVector pdistC(double x, NumericVector ys) {
  int n = ys.size();
  NumericVector out(n);

  for(int i = 0; i < n; ++i) {
    out[i] = sqrt(pow(ys[i] - x, 2.0));
  }
  return out;
}')
```

This function introduces only a few new concepts:

- We create a new numeric vector of length `n` with a constructor: `NumericVector out(n)`. Another useful way of making a vector is to copy an existing one: `NumericVector zs = clone(ys)`.
- C++ uses `pow()`, not `^`, for exponentiation.

Note that because the R version is fully vectorised, it's already going to be fast. On my computer, it takes around 8 ms with a 1 million element `y` vector. The C++ function is twice as fast, ~4 ms, but assuming it took you 10 minutes to write the C++ function, you'd need to run it ~150,000 times to make rewriting worthwhile. The reason why the C++ function is faster is subtle, and relates to memory management. The R version needs to create an intermediate vector the same length as `y` (`x - ys`), and allocating memory is an expensive operation. The C++ function avoids this overhead because it uses an intermediate scalar.

In the sugar section, you'll see how to rewrite this function to take advantage of Rcpp's vectorised operations so that the C++ code is almost as concise as R code.

19.1.5 Matrix input, vector output

Each vector type has a matrix equivalent: `NumericMatrix`, `IntegerMatrix`, `CharacterMatrix`, and `LogicalMatrix`. Using them is straightforward. For example, we could create a function that reproduces `rowSums()`:

```
cppFunction('NumericVector rowSumsC(NumericMatrix x) {
  int nrow = x.nrow(), ncol = x.ncol();
  NumericVector out(nrow);

  for (int i = 0; i < nrow; i++) {
    double total = 0;
    for (int j = 0; j < ncol; j++) {
      total += x(i, j);
    }
    out[i] = total;
  }
  return out;
}')
set.seed(1014)
x <- matrix(sample(100), 10)
rowSums(x)
```

```
#> [1] 458 558 488 458 536 537 488 491 508 528
rowSumsC(x)
#> [1] 458 558 488 458 536 537 488 491 508 528
```

The main differences:

- In C++, you subset a matrix with `()`, not `[]`.
- Use `.nrow()` and `.ncol()` *methods* to get the dimensions of a matrix.

19.1.6 Using sourceCpp

So far, we've used inline C++ with `cppFunction()`. This makes presentation simpler, but for real problems, it's usually easier to use stand-alone C++ files and then source them into R using `sourceCpp()`. This lets you take advantage of text editor support for C++ files (e.g., syntax highlighting) as well as making it easier to identify the line numbers in compilation errors.

Your stand-alone C++ file should have extension `.cpp`, and needs to start with:

```
#include <Rcpp.h>
using namespace Rcpp;
```

And for each function that you want available within R, you need to prefix it with:

```
// [[Rcpp::export]]
```

Note that the space is mandatory.

If you're familiar with `roxygen2`, you might wonder how this relates to `@export`. `Rcpp::export` controls whether a function is exported from C++ to R; `@export` controls whether a function is exported from a package and made available to the user.

You can embed R code in special C++ comment blocks. This is really convenient if you want to run some test code:

```
/** R
# This is R code
*/
```

The R code is run with `source(echo = TRUE)` so you don't need to explicitly print output.

To compile the C++ code, use `sourceCpp("path/to/file.cpp")`. This will create the matching R functions and add them to your current session. Note that these functions can not be saved in a `.Rdata` file and reloaded in a later session; they must be recreated each time you restart R. For example, running `sourceCpp()` on the following file implements `mean` in C++ and then compares it to the built-in `mean()`:

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
double meanC(NumericVector x) {
  int n = x.size();
  double total = 0;

  for(int i = 0; i < n; ++i) {
    total += x[i];
  }
  return total / n;
}

/*** R
library(microbenchmark)
x <- runif(1e5)
microbenchmark(
  mean(x),
  meanC(x)
)
*/
```

NB: if you run this code yourself, you'll notice that `meanC()` is much faster than the built-in `mean()`. This is because it trades numerical accuracy for speed.

For the remainder of this chapter C++ code will be presented stand-alone rather than wrapped in a call to `cppFunction`. If you want to try compiling and/or modifying the examples you should paste them into a C++ source file that includes the elements described above.

19.1.7 Exercises

With the basics of C++ in hand, it's now a great time to practice by reading and writing some simple C++ functions. For each of the following functions, read the code and figure out what the corresponding base R function is. You might not understand every part of the code yet, but you should be able to figure out the basics of what the function does.

```
double f1(NumericVector x) {
  int n = x.size();
  double y = 0;

  for(int i = 0; i < n; ++i) {
    y += x[i] / n;
  }
  return y;
}

NumericVector f2(NumericVector x) {
  int n = x.size();
  NumericVector out(n);

  out[0] = x[0];
  for(int i = 1; i < n; ++i) {
    out[i] = out[i - 1] + x[i];
  }
  return out;
}

bool f3(LogicalVector x) {
  int n = x.size();

  for(int i = 0; i < n; ++i) {
    if (x[i]) return true;
  }
  return false;
}

int f4(Function pred, List x) {
  int n = x.size();

  for(int i = 0; i < n; ++i) {
    LogicalVector res = pred(x[i]);
```

```

    if (res[0]) return i + 1;
  }
  return 0;
}

NumericVector f5(NumericVector x, NumericVector y) {
  int n = std::max(x.size(), y.size());
  NumericVector x1 = rep_len(x, n);
  NumericVector y1 = rep_len(y, n);

  NumericVector out(n);

  for (int i = 0; i < n; ++i) {
    out[i] = std::min(x1[i], y1[i]);
  }

  return out;
}

```

To practice your function writing skills, convert the following functions into C++. For now, assume the inputs have no missing values.

1. `all()`
2. `cumprod()`, `cummin()`, `cummax()`.
3. `diff()`. Start by assuming lag 1, and then generalise for lag `n`.
4. `range`.
5. `var`. Read about the approaches you can take on wikipedia (http://en.wikipedia.org/wiki/Algorithms_for_calculating_variance). Whenever implementing a numerical algorithm, it's always good to check what is already known about the problem.

19.2 Attributes and other classes

You've already seen the basic vector classes (`IntegerVector`, `NumericVector`, `LogicalVector`, `CharacterVector`) and their scalar

(int, double, bool, String) and matrix (IntegerMatrix, NumericMatrix, LogicalMatrix, CharacterMatrix) equivalents.

All R objects have attributes, which can be queried and modified with `.attr()`. Rcpp also provides `.names()` as an alias for the name attribute. The following code snippet illustrates these methods. Note the use of `::create()`, a *class* method. This allows you to create an R vector from C++ scalar values:

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
NumericVector attribs() {
  NumericVector out = NumericVector::create(1, 2, 3);

  out.names() = CharacterVector::create("a", "b", "c");
  out.attr("my-attr") = "my-value";
  out.attr("class") = "my-class";

  return out;
}
```

For S4 objects, `.slot()` plays a similar role to `.attr()`.

19.2.1 Lists and data frames

Rcpp also provides classes `List` and `DataFrame`, but they are more useful for output than input. This is because lists and data frames can contain arbitrary classes but C++ needs to know their classes in advance. If the list has known structure (e.g., it's an S3 object), you can extract the components and manually convert them to their C++ equivalents with `as()`. For example, the object created by `lm()`, the function that fits a linear model, is a list whose components are always of the same type. The following code illustrates how you might extract the mean percentage error (`mpe()`) of a linear model. This isn't a good example of when to use C++, because it's so easily implemented in R, but it shows how to work with an important S3 class. Note the use of `.inherits()` and the `stop()` to check that the object really is a linear model.

```
#include <Rcpp.h>
using namespace Rcpp;
```

```
// [[Rcpp::export]]
double mpe(List mod) {
  if (!mod.inherits("lm")) stop("Input must be a linear model");

  NumericVector resid = as<NumericVector>(mod["residuals"]);
  NumericVector fitted = as<NumericVector>(mod["fitted.values"]);

  int n = resid.size();
  double err = 0;
  for(int i = 0; i < n; ++i) {
    err += resid[i] / (fitted[i] + resid[i]);
  }
  return err / n;
}

mod <- lm(mpg ~ wt, data = mtcars)
mpe(mod)
#> [1] -0.0154
```

19.2.2 Functions

You can put R functions in an object of type `Function`. This makes calling an R function from C++ straightforward. We first define our C++ function:

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
RObject callWithOne(Function f) {
  return f(1);
}
```

Then call it from R:

```
callWithOne(function(x) x + 1)
#> [1] 2
callWithOne(paste)
#> [1] "1"
```


What type of object does an R function return? We don't know, so we use the catchall type `RObject`. An alternative is to return a `List`. For example, the following code is a basic implementation of `lapply` in C++:

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
List lapply1(List input, Function f) {
    int n = input.size();
    List out(n);

    for(int i = 0; i < n; i++) {
        out[i] = f(input[i]);
    }

    return out;
}
```

Calling R functions with positional arguments is obvious:

```
f("y", 1);
```

But to use named arguments, you need a special syntax:

```
f(_["x"] = "y", _["value"] = 1);
```

19.2.3 Other types

There are also classes for many more specialised language objects: `Environment`, `ComplexVector`, `RawVector`, `DottedPair`, `Language`, `Promise`, `Symbol`, `WeakReference`, and so on. These are beyond the scope of this chapter and won't be discussed further.

19.3 Missing values

If you're working with missing values, you need to know two things:

- how R's missing values behave in C++'s scalars (e.g., `double`).
- how to get and set missing values in vectors (e.g., `NumericVector`).

19.3.1 Scalars

The following code explores what happens when you take one of R's missing values, coerce it into a scalar, and then coerce back to an R vector. Note that this kind of experimentation is a useful way to figure out what any operation does.

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
List scalar_missings() {
  int int_s = NA_INTEGER;
  String chr_s = NA_STRING;
  bool lgl_s = NA_LOGICAL;
  double num_s = NA_REAL;

  return List::create(int_s, chr_s, lgl_s, num_s);
}

str(scalar_missings())
#> List of 4
#> $ : int NA
#> $ : chr NA
#> $ : logi TRUE
#> $ : num NA
```

With the exception of `bool`, things look pretty good here: all of the missing values have been preserved. However, as we'll see in the following sections, things are not quite as straightforward as they seem.

19.3.1.1 Integers

With integers, missing values are stored as the smallest integer. If you don't do anything to them, they'll be preserved. But, since C++ doesn't know that the smallest integer has this special behaviour, if you do anything to it you're likely to get an incorrect value: for example, `evalCpp('NA_INTEGER + 1')` gives `-2147483647`.

So if you want to work with missing values in integers, either use a length one `IntegerVector` or be very careful with your code.

19.3.1.2 Doubles

With doubles, you may be able to get away with ignoring missing values and working with NaNs (not a number). This is because R's NA is a special type of IEEE 754 floating point number NaN. So any logical expression that involves a NaN (or in C++, NAN) always evaluates as FALSE:

```
evalCpp("NAN == 1")
#> [1] FALSE
evalCpp("NAN < 1")
#> [1] FALSE
evalCpp("NAN > 1")
#> [1] FALSE
evalCpp("NAN == NAN")
#> [1] FALSE
```

But be careful when combining then with boolean values:

```
evalCpp("NAN && TRUE")
#> [1] TRUE
evalCpp("NAN || FALSE")
#> [1] TRUE
```

However, in numeric contexts NaNs will propagate NAs:

```
evalCpp("NAN + 1")
#> [1] NaN
evalCpp("NAN - 1")
#> [1] NaN
evalCpp("NAN / 1")
#> [1] NaN
evalCpp("NAN * 1")
#> [1] NaN
```

19.3.2 Strings

`String` is a scalar string class introduced by Rcpp, so it knows how to deal with missing values.

19.3.3 Boolean

While C++’s `bool` has two possible values (`true` or `false`), a logical vector in R has three (`TRUE`, `FALSE`, and `NA`). If you coerce a length 1 logical vector, make sure it doesn’t contain any missing values otherwise they will be converted to `TRUE`.

19.3.4 Vectors

With vectors, you need to use a missing value specific to the type of vector, `NA_REAL`, `NA_INTEGER`, `NA_LOGICAL`, `NA_STRING`:

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
List missing_sampler() {
  return List::create(
    NumericVector::create(NA_REAL),
    IntegerVector::create(NA_INTEGER),
    LogicalVector::create(NA_LOGICAL),
    CharacterVector::create(NA_STRING));
}

str(missing_sampler())
#> List of 4
#> $ : num NA
#> $ : int NA
#> $ : logi NA
#> $ : chr NA
```

To check if a value in a vector is missing, use the class method `::is_na()`:

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
LogicalVector is_naC(NumericVector x) {
  int n = x.size();
  LogicalVector out(n);
```

```

    for (int i = 0; i < n; ++i) {
        out[i] = NumericVector::is_na(x[i]);
    }
    return out;
}

```

```

is_naC(c(NA, 5.4, 3.2, NA))
#> [1] TRUE FALSE FALSE TRUE

```

Another alternative is the sugar function `is_na()`, which takes a vector and returns a logical vector.

```

#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
LogicalVector is_naC2(NumericVector x) {
    return is_na(x);
}

is_naC2(c(NA, 5.4, 3.2, NA))
#> [1] TRUE FALSE FALSE TRUE

```

19.3.5 Exercises

1. Rewrite any of the functions from the first exercise to deal with missing values. If `na.rm` is true, ignore the missing values. If `na.rm` is false, return a missing value if the input contains any missing values. Some good functions to practice with are `min()`, `max()`, `range()`, `mean()`, and `var()`.
2. Rewrite `cumsum()` and `diff()` so they can handle missing values. Note that these functions have slightly more complicated behaviour.

19.4 Rcpp sugar

Rcpp provides a lot of syntactic “sugar” to ensure that C++ functions work very similarly to their R equivalents. In fact, Rcpp sugar makes

it possible to write efficient C++ code that looks almost identical to its R equivalent. If there's a sugar version of the function you're interested in, you should use it: it'll be both expressive and well tested. Sugar functions aren't always faster than a handwritten equivalent, but they will get faster in the future as more time is spent on optimising Rcpp.

Sugar functions can be roughly broken down into

- arithmetic and logical operators
- logical summary functions
- vector views
- other useful functions

19.4.1 Arithmetic and logical operators

All the basic arithmetic and logical operators are vectorised: `+`, `*`, `-`, `/`, `pow`, `<`, `<=`, `>`, `>=`, `==`, `!=`, `!`. For example, we could use sugar to considerably simplify the implementation of `pdistC()`.

```
pdistR <- function(x, ys) {
  sqrt((x - ys) ^ 2)
}

#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
NumericVector pdistC2(double x, NumericVector ys) {
  return sqrt(pow((x - ys), 2));
}
```

19.4.2 Logical summary functions

The sugar function `any()` and `all()` are fully lazy so that `any(x == 0)`, for example, might only need to evaluate one element of a vector, and return a special type that can be converted into a `bool` using `.is_true()`, `.is_false()`, or `.is_na()`. We could also use this sugar to write an efficient function to determine whether or not a numeric vector contains any missing values. To do this in R, we could use `any(is.na(x))`:

```
any_naR <- function(x) any(is.na(x))
```

However, this will do the same amount of work regardless of the location of the missing value. Here’s the C++ implementation:

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
bool any_naC(NumericVector x) {
  return is_true(any(is_na(x)));
}

x0 <- runif(1e5)
x1 <- c(x0, NA)
x2 <- c(NA, x0)

microbenchmark(
  any_naR(x0), any_naC(x0),
  any_naR(x1), any_naC(x1),
  any_naR(x2), any_naC(x2)
)
#> Unit: microseconds
#>      expr      min      lq median      uq      max neval
#> any_naR(x0) 253.00 255.00 262.00 295.00 1,370   100
#> any_naC(x0) 308.00 309.00 310.00 324.00 1,050   100
#> any_naR(x1) 253.00 256.00 260.00 351.00 1,160   100
#> any_naC(x1) 308.00 309.00 312.00 322.00 1,350   100
#> any_naR(x2)  86.50  91.50  94.00 111.00 1,070   100
#> any_naC(x2)   1.79   2.32   2.93   3.69    10   100
```

19.4.3 Vector views

A number of helpful functions provide a “view” of a vector: `head()`, `tail()`, `rep_each()`, `rep_len()`, `rev()`, `seq_along()`, and `seq_len()`. In R these would all produce copies of the vector, but in Rcpp they simply point to the existing vector and override the subsetting operator (`[]`) to implement special behaviour. This makes them very efficient: for instance, `rep_len(x, 1e6)` does not have to make a million copies of `x`.

19.4.4 Other useful functions

Finally, there's a grab bag of sugar functions that mimic frequently used R functions:

- Math functions: `abs()`, `acos()`, `asin()`, `atan()`, `beta()`, `ceil()`, `ceiling()`, `choose()`, `cos()`, `cosh()`, `digamma()`, `exp()`, `expm1()`, `factorial()`, `floor()`, `gamma()`, `lbeta()`, `lchoose()`, `lfactorial()`, `lgamma()`, `log()`, `log10()`, `log1p()`, `pentagamma()`, `psigamma()`, `round()`, `signif()`, `sin()`, `sinh()`, `sqrt()`, `tan()`, `tanh()`, `tetragamma()`, `trigamma()`, `trunc()`.
- Scalar summaries: `mean()`, `min()`, `max()`, `sum()`, `sd()`, and (for vectors) `var()`.
- Vector summaries: `cumsum()`, `diff()`, `pmin()`, and `pmax()`.
- Finding values: `match()`, `self_match()`, `which_max()`, `which_min()`.
- Dealing with duplicates: `duplicated()`, `unique()`.
- `d/q/p/r` for all standard distributions.

Finally, `noNA(x)` asserts that the vector `x` does not contain any missing values, and allows optimisation of some mathematical operations.

19.5 The STL

The real strength of C++ shows itself when you need to implement more complex algorithms. The standard template library (STL) provides a set of extremely useful data structures and algorithms. This section will explain some of the most important algorithms and data structures and point you in the right direction to learn more. I can't teach you everything you need to know about the STL, but hopefully the examples will show you the power of the STL, and persuade you that it's useful to learn more.

If you need an algorithm or data structure that isn't implemented in STL, a good place to look is boost (<http://www.boost.org/doc/>). Installing boost on your computer is beyond the scope of this chapter, but once you have it installed, you can use boost data structures and algorithms by including the appropriate header file with (e.g.) `#include <boost/array.hpp>`.

19.5.1 Using iterators

Iterators are used extensively in the STL: many functions either accept or return iterators. They are the next step up from basic loops, abstracting away the details of the underlying data structure. Iterators have three main operators:

1. Advance with ++.
2. Get the value they refer to, or **dereference**, with *.
3. Compare with ==.

For example we could re-write our sum function using iterators:

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
double sum3(NumericVector x) {
    double total = 0;

    NumericVector::iterator it;
    for(it = x.begin(); it != x.end(); ++it) {
        total += *it;
    }
    return total;
}
```

The main changes are in the for loop:

- We start at `x.begin()` and loop until we get to `x.end()`. A small optimization is to store the value of the end iterator so we don't need to look it up each time. This only saves about 2 ns per iteration, so it's only important when the calculations in the loop are very simple.
- Instead of indexing into `x`, we use the dereference operator to get its current value: `*it`.
- Notice the type of the iterator: `NumericVector::iterator`. Each vector type has its own iterator type: `LogicalVector::iterator`, `CharacterVector::iterator`, etc.

Iterators also allow us to use the C++ equivalents of the apply family of functions. For example, we could again rewrite `sum()` to use the

`accumulate()` function, which takes a starting and an ending iterator, and adds up all the values in the vector. The third argument to `accumulate` gives the initial value: it's particularly important because this also determines the data type that `accumulate` uses (so we use `0.0` and not `0` so that `accumulate` uses a double, not an int.). To use `accumulate()` we need to include the `<numeric>` header.

```
#include <numeric>
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
double sum4(NumericVector x) {
    return std::accumulate(x.begin(), x.end(), 0.0);
}
```

`accumulate()` (along with the other functions in `<numeric>`, like `adjacent_difference()`, `inner_product()`, and `partial_sum()`) is not that important in Rcpp because Rcpp sugar provides equivalents.

19.5.2 Algorithms

The `<algorithm>` header provides a large number of algorithms that work with iterators. A good reference is available at <http://www.cplusplus.com/reference/algorithm/>. For example, we could write a basic Rcpp version of `findInterval()` that takes two arguments a vector of values and a vector of breaks, and locates the bin that each `x` falls into. This shows off a few more advanced iterator features. Read the code below and see if you can figure out how it works.

```
#include <algorithm>
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
IntegerVector findInterval2(NumericVector x, NumericVector breaks) {
    IntegerVector out(x.size());

    NumericVector::iterator it, pos;
    IntegerVector::iterator out_it;
```

```

for(it = x.begin(), out_it = out.begin(); it != x.end();
    ++it, ++out_it) {
    pos = std::upper_bound(breaks.begin(), breaks.end(), *it);
    *out_it = std::distance(breaks.begin(), pos);
}

return out;
}

```

The key points are:

- We step through two iterators (input and output) simultaneously.
- We can assign into an dereferenced iterator (`out_it`) to change the values in `out`.
- `upper_bound()` returns an iterator. If we wanted the value of the `upper_bound()` we could dereference it; to figure out its location, we use the `distance()` function.
- Small note: if we want this function to be as fast as `findInterval()` in R (which uses handwritten C code), we need to compute the calls to `.begin()` and `.end()` once and save the results. This is easy, but it distracts from this example so it has been omitted. Making this change yields a function that's slightly faster than R's `findInterval()` function, but is about 1/10 of the code.

It's generally better to use algorithms from the STL than hand rolled loops. In *Effective STL*, Scott Meyers gives three reasons: efficiency, correctness, and maintainability. Algorithms from the STL are written by C++ experts to be extremely efficient, and they have been around for a long time so they are well tested. Using standard algorithms also makes the intent of your code more clear, helping to make it more readable and more maintainable.

19.5.3 Data structures

The STL provides a large set of data structures: `array`, `bitset`, `list`, `forward_list`, `map`, `multimap`, `multiset`, `priority_queue`, `queue`, `dequeue`, `set`, `stack`, `unordered_map`, `unordered_set`, `unordered_multimap`, `unordered_multiset`, and `vector`. The most important of these data structures are the `vector`, the `unordered_set`, and the `unordered_map`.

We'll focus on these three in this section, but using the others is similar: they just have different performance trade-offs. For example, the deque (pronounced “deck”) has a very similar interface to vectors but a different underlying implementation that has different performance trade-offs. You may want to try them for your problem. A good reference for STL data structures is <http://www.cplusplus.com/reference/stl/> — I recommend you keep it open while working with the STL.

Rcpp knows how to convert from many STL data structures to their R equivalents, so you can return them from your functions without explicitly converting to R data structures.

19.5.4 Vectors

An STL vector is very similar to an R vector, except that it grows efficiently. This makes vectors appropriate to use when you don't know in advance how big the output will be. Vectors are templated, which means that you need to specify the type of object the vector will contain when you create it: `vector<int>`, `vector<bool>`, `vector<double>`, `vector<String>`. You can access individual elements of a vector using the standard `[]` notation, and you can add a new element to the end of the vector using `.push_back()`. If you have some idea in advance how big the vector will be, you can use `.reserve()` to allocate sufficient storage.

The following code implements run length encoding (`rle()`). It produces two vectors of output: a vector of values, and a vector `lengths` giving how many times each element is repeated. It works by looping through the input vector `x` comparing each value to the previous: if it's the same, then it increments the last value in `lengths`; if it's different, it adds the value to the end of `values`, and sets the corresponding length to 1.

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
List rleC(NumericVector x) {
  std::vector<int> lengths;
  std::vector<double> values;

  // Initialise first value
  int i = 0;
  double prev = x[0];
```

```

    values.push_back(prev);
    lengths.push_back(1);

    NumericVector::iterator it;
    for(it = x.begin() + 1; it != x.end(); ++it) {
        if (prev == *it) {
            lengths[i]++;
        } else {
            values.push_back(*it);
            lengths.push_back(1);

            i++;
            prev = *it;
        }
    }

    return List::create(
        _["lengths"] = lengths,
        _["values"] = values
    );
}

```

(An alternative implementation would be to replace `i` with the iterator `lengths.rbegin()` which always points to the last element of the vector. You might want to try implementing that yourself.)

Other methods of a vector are described at <http://www.cplusplus.com/reference/vector/vector/>.

19.5.5 Sets

Sets maintain a unique set of values, and can efficiently tell if you've seen a value before. They are useful for problems that involve duplicates or unique values (like `unique`, `duplicated`, or `in`). C++ provides both ordered (`std::set`) and unordered sets (`std::unordered_set`), depending on whether or not order matters for you. Unordered sets tend to be much faster (because they use a hash table internally rather than a tree), so even if you need an ordered set, you should consider using an unordered set and then sorting the output. Like vectors, sets are templated, so you need to request the appropriate type of set for your purpose: `unordered_set<int>`, `unordered_set<bool>`, etc. More details are available at <http://www.cplusplus.com/reference/set/set/> and http://www.cplusplus.com/reference/unordered_set/unordered_set/.

The following function uses an unordered set to implement an equivalent to `duplicated()` for integer vectors. Note the use of `seen.insert(x[i]).second`. `insert()` returns a pair, the `.first` value is an iterator that points to element and the `.second` value is a boolean that's true if the value was a new addition to the set.

```
// [[Rcpp::plugins(cpp11)]]
#include <Rcpp.h>
#include <unordered_set>
using namespace Rcpp;

// [[Rcpp::export]]
LogicalVector duplicatedC(IntegerVector x) {
  std::unordered_set<int> seen;
  int n = x.size();
  LogicalVector out(n);

  for (int i = 0; i < n; ++i) {
    out[i] = !seen.insert(x[i]).second;
  }

  return out;
}
```

Note that unordered sets are only available in C++ 11, which means we need to use the `cpp11` plugin, `[[Rcpp::plugins(cpp11)]]`.

19.5.6 Map

A map is similar to a set, but instead of storing presence or absence, it can store additional data. It's useful for functions like `table()` or `match()` that need to look up a value. As with sets, there are ordered (`std::map`) and unordered (`std::unordered_map`) versions. Since maps have a value and a key, you need to specify both types when initialising a map: `map<double, int>`, `unordered_map<int, double>`, and so on. The following example shows how you could use a map to implement `table()` for numeric vectors:

```
#include <Rcpp.h>
using namespace Rcpp;
```

```
// [[Rcpp::export]]
std::map<double, int> tableC(NumericVector x) {
  std::map<double, int> counts;

  int n = x.size();
  for (int i = 0; i < n; i++) {
    counts[x[i]]++;
  }

  return counts;
}
```

Note that unordered maps are only available in C++ 11, so to use them, you'll again need `[[Rcpp::plugins(cpp11)]]`.

19.5.7 Exercises

To practice using the STL algorithms and data structures, implement the following using R functions in C++, using the hints provided:

1. `median.default()` using `partial_sort`.
2. `%in%` using `unordered_set` and the `find()` or `count()` methods.
3. `unique()` using an `unordered_set` (challenge: do it in one line!).
4. `min()` using `std::min()`, or `max()` using `std::max()`.
5. `which.min()` using `min_element`, or `which.max()` using `max_element`.
6. `setdiff()`, `union()`, and `intersect()` for integers using sorted ranges and `set_union`, `set_intersection` and `set_difference`.

19.6 Case studies

The following case studies illustrate some real life uses of C++ to replace slow R code.

19.6.1 Gibbs sampler

The following case study updates an example blogged about (<http://dirk.eddelbuettel.com/blog/2011/07/14/>) by Dirk Eddelbuettel, illustrating the conversion of a Gibbs sampler in R to C++. The R and C++ code shown below is very similar (it only took a few minutes to convert the R version to the C++ version), but runs about 20 times faster on my computer. Dirk's blog post also shows another way to make it even faster: using the faster random number generator functions in GSL (easily accessible from R through the RcppGSL package) can make it another 2–3x faster.

The R code is as follows:

```
gibbs_r <- function(N, thin) {
  mat <- matrix(nrow = N, ncol = 2)
  x <- y <- 0

  for (i in 1:N) {
    for (j in 1:thin) {
      x <- rgamma(1, 3, y * y + 4)
      y <- rnorm(1, 1 / (x + 1), 1 / sqrt(2 * (x + 1)))
    }
    mat[i, ] <- c(x, y)
  }
  mat
}
```

This is straightforward to convert to C++. We:

- add type declarations to all variables
- use `()` instead of `[]` to index into the matrix
- subscript the results of `rgamma` and `rnorm` to convert from a vector into a scalar

```
#include <Rcpp.h>
using namespace Rcpp;

// [[Rcpp::export]]
NumericMatrix gibbs_cpp(int N, int thin) {
  NumericMatrix mat(N, 2);
```



```

double x = 0, y = 0;

for(int i = 0; i < N; i++) {
  for(int j = 0; j < thin; j++) {
    x = rgamma(1, 3, 1 / (y * y + 4))[0];
    y = rnorm(1, 1 / (x + 1), 1 / sqrt(2 * (x + 1)))[0];
  }
  mat(i, 0) = x;
  mat(i, 1) = y;
}

return(mat);
}

```

Benchmarking the two implementations yields:

```

microbenchmark(
  gibbs_r(100, 10),
  gibbs_cpp(100, 10)
)
#> Unit: microseconds
#>      expr      min      lq  median      uq      max neval
#>  gibbs_r(100, 10) 6,980 8,150  8,430 8,740 44,100   100
#>  gibbs_cpp(100, 10)   258   273    279   293  1,330   100

```

19.6.2 R vectorisation vs. C++ vectorisation

This example is adapted from “Rcpp is smoking fast for agent-based models in data frames” (<http://www.babelgraph.org/wp/?p=358>). The challenge is to predict a model response from three inputs. The basic R version of the predictor looks like:

```

vacc1a <- function(age, female, ily) {
  p <- 0.25 + 0.3 * 1 / (1 - exp(0.04 * age)) + 0.1 * ily
  p <- p * if (female) 1.25 else 0.75
  p <- max(0, p)
  p <- min(1, p)
  p
}

```

We want to be able to apply this function to many inputs, so we might write a vector-input version using a for loop.

```

vacc1 <- function(age, female, ily) {
  n <- length(age)
  out <- numeric(n)
  for (i in seq_len(n)) {
    out[i] <- vacc1a(age[i], female[i], ily[i])
  }
  out
}

```

If you're familiar with R, you'll have a gut feeling that this will be slow, and indeed it is. There are two ways we could attack this problem. If you have a good R vocabulary, you might immediately see how to vectorise the function (using `ifelse()`, `pmin()`, and `pmax()`). Alternatively, we could rewrite `vacc1a()` and `vacc1()` in C++, using our knowledge that loops and function calls have much lower overhead in C++.

Either approach is fairly straightforward. In R:

```

vacc2 <- function(age, female, ily) {
  p <- 0.25 + 0.3 * 1 / (1 - exp(0.04 * age)) + 0.1 * ily
  p <- p * ifelse(female, 1.25, 0.75)
  p <- pmax(0, p)
  p <- pmin(1, p)
  p
}

```

(If you've worked R a lot you might recognise some potential bottlenecks in this code: `ifelse`, `pmin`, and `pmax` are known to be slow, and could be replaced with `p + 0.75 + 0.5 * female`, `p[p < 0] <- 0`, `p[p > 1] <- 1`. You might want to try timing those variations yourself.)

Or in C++:

```

#include <Rcpp.h>
using namespace Rcpp;

double vacc3a(double age, bool female, bool ily){
  double p = 0.25 + 0.3 * 1 / (1 - exp(0.04 * age)) + 0.1 * ily;
  p = p * (female ? 1.25 : 0.75);
  p = std::max(p, 0.0);
  p = std::min(p, 1.0);
  return p;
}

```

```
// [[Rcpp::export]]
NumericVector vacc3(NumericVector age, LogicalVector female,
                    LogicalVector ily) {
  int n = age.size();
  NumericVector out(n);

  for(int i = 0; i < n; ++i) {
    out[i] = vacc3a(age[i], female[i], ily[i]);
  }

  return out;
}
```

We next generate some sample data, and check that all three versions return the same values:

```
n <- 1000
age <- rnorm(n, mean = 50, sd = 10)
female <- sample(c(T, F), n, rep = TRUE)
ily <- sample(c(T, F), n, prob = c(0.8, 0.2), rep = TRUE)

stopifnot(
  all.equal(vacc1(age, female, ily), vacc2(age, female, ily)),
  all.equal(vacc1(age, female, ily), vacc3(age, female, ily))
)
```

The original blog post forgot to do this, and introduced a bug in the C++ version: it used 0.004 instead of 0.04. Finally, we can benchmark our three approaches:

```
microbenchmark(
  vacc1 = vacc1(age, female, ily),
  vacc2 = vacc2(age, female, ily),
  vacc3 = vacc3(age, female, ily)
)
#> Unit: microseconds
#>   expr      min       lq   median       uq    max neval
#> vacc1 4,210.0 4,680.0 5,150.0 6,050.0 11,800   100
#> vacc2  327.0   373.0   403.0   449.0   750    100
#> vacc3   16.6    20.1    27.5    34.1    82    100
```

Not surprisingly, our original approach with loops is very slow. Vectorising in R gives a huge speedup, and we can eke out even more performance (~10x) with the C++ loop. I was a little surprised that the C++ was so much faster, but it is because the R version has to create 11 vectors to store intermediate results, where the C++ code only needs to create 1.

19.7 Using Rcpp in a package

The same C++ code that is used with `sourceCpp()` can also be bundled into a package. There are several benefits of moving code from a stand-alone C++ source file to a package:

1. Your code can be made available to users without C++ development tools.
2. Multiple source files and their dependencies are handled automatically by the R package build system.
3. Packages provide additional infrastructure for testing, documentation, and consistency.

To add Rcpp to an existing package, you put your C++ files in the `src/` directory and modify/create the following configuration files:

- In DESCRIPTION add

```
LinkingTo: Rcpp
Imports: Rcpp
```

- Make sure your NAMESPACE includes:

```
useDynLib(mypackage)
importFrom(Rcpp, sourceCpp)
```

We need to import something (anything) from Rcpp so that internal Rcpp code is properly loaded. This is a bug in R and hopefully will be fixed in the future.

To generate a new Rcpp package that includes a simple “hello world” function you can use `Rcpp.package.skeleton()`:

```
Rcpp.package.skeleton("NewPackage", attributes = TRUE)
```

To generate a package based on C++ files that you’ve been using with `sourceCpp()`, use the `cpp_files` parameter:

```
Rcpp.package.skeleton("NewPackage", example_code = FALSE,  
                      cpp_files = c("convolve.cpp"))
```

Before building the package, you’ll need to run `Rcpp::compileAttributes()`. This function scans the C++ files for `Rcpp::export` attributes and generates the code required to make the functions available in R. Re-run `compileAttributes()` whenever functions are added, removed, or have their signatures changed. This is done automatically by the devtools package and by Rstudio.

For more details see the Rcpp package vignette, `vignette("Rcpp-package")`.

19.8 Learning more

This chapter has only touched on a small part of Rcpp, giving you the basic tools to rewrite poorly performing R code in C++. The Rcpp book (<http://www.rcpp.org/book>) is the best reference to learn more about Rcpp. As noted, Rcpp has many other capabilities that make it easy to interface R to existing C++ code, including:

- Additional features of attributes including specifying default arguments, linking in external C++ dependencies, and exporting C++ interfaces from packages. These features and more are covered in the Rcpp attributes vignette, `vignette("Rcpp-attributes")`.
- Automatically creating wrappers between C++ data structures and R data structures, including mapping C++ classes to reference classes. A good introduction to this topic is Rcpp modules vignette, `vignette("Rcpp-modules")`
- The Rcpp quick reference guide, `vignette("Rcpp-quickref")`, contains a useful summary of Rcpp classes and common programming idioms.

I strongly recommend keeping an eye on the Rcpp homepage (<http://www.rcpp.org>) and Dirk's Rcpp page (<http://dirk.eddelbuettel.com/code/rcpp.html>) as well as signing up for the Rcpp mailing list (<http://lists.r-forge.r-project.org/cgi-bin/mailman/listinfo/rcpp-devel>). Rcpp is still under active development, and is getting better with every release.

Other resources I've found helpful in learning C++ are:

- *Effective C++* (<http://amzn.com/0321334876?tag=devtools-20>) and *Effective STL* (<http://amzn.com/0201749629?tag=devtools-20>) by Scott Meyers.
- *C++ Annotations* (<http://www.icce.rug.nl/documents/cplusplus/cplusplus.html>), aimed at “knowledgeable users of C (or any other language using a C-like grammar, like Perl or Java) who would like to know more about, or make the transition to, C++”.
- *Algorithm Libraries* (<http://www.cs.helsinki.fi/u/tpkarkka/alglib/k06/>), which provides a more technical, but still concise, description of important STL concepts. (Follow the links under notes).

Writing performant code may also require you to rethink your basic approach: a solid understanding of basic data structures and algorithms is very helpful here. That's beyond the scope of this book, but I'd suggest the *Algorithm Design Manual* (<http://amzn.com/0387948600?tag=devtools-20>), MIT's *Introduction to Algorithms* (<http://ocw.mit.edu/courses/electrical-engineering-and-computer-science/6-046j-introduction-to-algorithms-sma-5503-fall-2005/>), *Algorithms* by Robert Sedgewick and Kevin Wayne which has a free online textbook (<http://algs4.cs.princeton.edu/home/>) and a matching coursera course (<https://www.coursera.org/course/algs4partI>).

19.9 Acknowledgments

I'd like to thank the Rcpp-mailing list for many helpful conversations, particularly Romain Francois and Dirk Eddelbuettel who have not only provided detailed answers to many of my questions, but have been incredibly responsive at improving Rcpp. This chapter would not have been possible without JJ Allaire; he encouraged me to learn C++ and then answered many of my dumb questions along the way.

20

R's C interface

Reading R's source code is an extremely powerful technique for improving your programming skills. However, many base R functions, and many functions in older packages, are written in C. It's useful to be able to figure out how those functions work, so this chapter will introduce you to R's C API. You'll need some basic C knowledge, which you can get from a standard C text (e.g., *The C Programming Language* (<http://amzn.com/0131101633?tag=devtools-20>) by Kernigan and Ritchie), or from Chapter 19. You'll need a little patience, but it is possible to read R's C source code, and you will learn a lot doing it.

The contents of this chapter draw heavily from Section 5 (“System and foreign language interfaces”) of Writing R extensions (<http://cran.r-project.org/doc/manuals/R-exts.html>), but focus on best practices and modern tools. This means it does not cover the old .C interface, the old API defined in `Rdefines.h`, or rarely used language features. To see R's complete C API, look at the header file `Rinternals.h`. It's easiest to find and display this file from within R:

```
rinternals <- file.path(R.home("include"), "Rinternals.h")
file.show(rinternals)
```

All functions are defined with either the prefix `Rf_` or `R_` but are exported without it (unless `#define R_NO_REMAP` has been used).

I do not recommend using C for writing new high-performance code. Instead write C++ with `Rcpp`. The `Rcpp` API protects you from many of the historical idiosyncracies of the R API, takes care of memory management for you, and provides many useful helper methods.

Outline

- Section 20.1 shows the basics of creating and calling C functions with the inline package.

- Section 20.2 shows how to translate data structure names from R to C.
- Section 20.3 teaches you how to create, modify, and coerce vectors in C.
- Section 20.4 shows you how to work with pairlists. You need to know this because the distinction between pairlists and list is more important in C than R.
- Section 20.5 talks about the importance of input validation so that your C function doesn't crash R.
- Section 20.6 concludes the chapter by showing you how to find the C source code for internal and primitive R functions.

Prerequisites

To understand existing C code, it's useful to generate simple examples of your own that you can experiment with. To that end, all examples in this chapter use the `inline` package, which makes it extremely easy to compile and link C code to your current R session. Get it by running `install.packages("inline")`. To easily find the C code associated with internal and primitive functions, you'll need a function from `pryr`. Get the package with `install.packages("pryr")`.

You'll also need a C compiler. Windows users can use Rtools (<http://cran.r-project.org/bin/windows/Rtools/>). Mac users will need the Xcode command line tools (<http://developer.apple.com/>). Most Linux distributions will come with the necessary compilers.

In Windows, it's necessary that the Rtools executables directory (typically `C:\Rtools\bin`) and the C compiler executables directory (typically `C:\Rtools\gcc-4.6.3\bin`) are included in the Windows PATH environment variable. You may need to reboot Windows before R can recognise these values.

20.1 Calling C functions from R

Generally, calling a C function from R requires two pieces: a C function and an R wrapper function that uses `.Call()`. The simple function below

adds two numbers together and illustrates some of the complexities of coding in C:

```
// In C -----
#include <R.h>
#include <Rinternals.h>

SEXP add(SEXP a, SEXP b) {
    SEXP result = PROTECT(allocVector(REALSXP, 1));
    REAL(result)[0] = asReal(a) + asReal(b);
    UNPROTECT(1);

    return result;
}

# In R -----
add <- function(a, b) {
    .Call("add", a, b)
}
```

(An alternative to using `.Call` is to use `.External`. It is used almost identically, except that the C function will receive a single argument containing a `LISTSXP`, a pairlist from which the arguments can be extracted. This makes it possible to write functions that take a variable number of arguments. However, it's not commonly used in base R and `inline` does not currently support `.External` functions so I don't discuss it further in this chapter.)

In this chapter we'll produce the two pieces in one step by using the `inline` package. This allows us to write:

```
add <- cfunction(c(a = "integer", b = "integer"), "
    SEXP result = PROTECT(allocVector(REALSXP, 1));
    REAL(result)[0] = asReal(a) + asReal(b);
    UNPROTECT(1);

    return result;
")
add(1, 5)
#> [1] 6
```

Before we begin reading and writing C code, we need to know a little about the basic data structures.

20.2 C data structures

At the C-level, all R objects are stored in a common datatype, the `SEXP`, or S-expression. All R objects are S-expressions so every C function that you create must return a `SEXP` as output and take `SEXPs` as inputs. (Technically, this is a pointer to a structure with typedef `SEXPREC`.) A `SEXP` is a variant type, with subtypes for all R's data structures. The most important types are:

- `REALSXP`: numeric vector
- `INTSXP`: integer vector
- `LGLSXP`: logical vector
- `STRSXP`: character vector
- `VECSXP`: list
- `CLOSXP`: function (closure)
- `ENVSXP`: environment

Beware: In C, lists are called `VECSXPs` not `LISTSXPs`. This is because early implementations of lists were Lisp-like linked lists, which are now known as “pairlists”.

Character vectors are a little more complicated than the other atomic vectors. A `STRSXP` contains a vector of `CHARSXPs`, where each `CHARSXP` points to C-style string stored in a global pool. This design allows individual `CHARSXP`'s to be shared between multiple character vectors, reducing memory usage. See Section 18.1 for more details.

There are also `SEXPs` for less common object types:

- `CPLXSXP`: complex vectors
- `LISTSXP`: “pair” lists. At the R level, you only need to care about the distinction lists and pairlists for function arguments, but internally they are used in many more places
- `DOTSXP`: ‘...’
- `SYMSXP`: names/symbols
- `NILSXP`: NULL

And `SEXPs` for internal objects, objects that are usually only created and used by C functions, not R functions:

- LANGSXP: language constructs
- CHARSXP: “scalar” strings
- PROMSXP: promises, lazily evaluated function arguments
- EXPRSXP: expressions

There’s no built-in R function to easily access these names, but `pryr` provides `sexp_type()`:

```
library(pryr)

sexp_type(10L)
#> [1] "INTSXP"
sexp_type("a")
#> [1] "STRSXP"
sexp_type(T)
#> [1] "LGLSXP"
sexp_type(list(a = 1))
#> [1] "VECSXP"
sexp_type(pairlist(a = 1))
#> [1] "LISTSXP"
```

20.3 Creating and modifying vectors

At the heart of every C function are conversions between R data structures and C data structures. Inputs and output will always be R data structures (SEXPs) and you will need to convert them to C data structures in order to do any work. This section focusses on vectors because they’re the type of object you’re most likely to work with.

An additional complication is the garbage collector: if you don’t protect every R object you create, the garbage collector will think they are unused and delete them.

20.3.1 Creating vectors and garbage collection

The simplest way to create a new R-level object is to use `allocVector()`. It takes two arguments, the type of SEXP (or SEXPTYPE) to create, and the length of the vector. The following code creates a three element list

containing a logical vector, a numeric vector, and an integer vector, all of length four:

```
dummy <- cfunction(body = '
  SEXP dbls = PROTECT(allocVector(REALSXP, 4));
  SEXP lgls = PROTECT(allocVector(LGLSXP, 4));
  SEXP ints = PROTECT(allocVector(INTSXP, 4));

  SEXP vec = PROTECT(allocVector(VECSXP, 3));
  SET_VECTOR_ELT(vec, 0, dbls);
  SET_VECTOR_ELT(vec, 1, lgls);
  SET_VECTOR_ELT(vec, 2, ints);

  UNPROTECT(4);
  return vec;
')
dummy()
#> [[1]]
#> [1] 6.941e-310 6.941e-310 6.941e-310 0.000e+00
#>
#> [[2]]
#> [1] TRUE TRUE TRUE TRUE
#>
#> [[3]]
#> [1]      2      4      8 32710
```

You might wonder what all the `PROTECT()` calls do. They tell R that the object is in use and shouldn't be deleted if the garbage collector is activated. (We don't need to protect objects that R already knows we're using, like function arguments.)

You also need to make sure that every protected object is unprotected. `UNPROTECT()` takes a single integer argument, `n`, and unprotects the last `n` objects that were protected. The number of protects and unprotects must match. If not, R will warn about a "stack imbalance in `.Call`". Other specialised forms of protection are needed in some circumstances:

- `UNPROTECT_PTR()` unprotects the object pointed to by the SEXPs.
- `PROTECT_WITH_INDEX()` saves an index of the protection location that can be used to replace the protected value using `REPROTECT()`.

Consult the R externals section on garbage collection (<http://cran.r-project.org/doc/manuals/R-exts.html#Garbage-Collection>) for more details.

Properly protecting the R objects you allocate is extremely important! Improper protection leads to difficulty diagnosing errors, typically seg-faults, but other corruption is possible as well. In general, if you allocate a new R object, you must PROTECT it.

If you run `dummy()` a few times, you'll notice the output varies. This is because `allocVector()` assigns memory to each output, but it doesn't clean it out first. For real functions, you may want to loop through each element in the vector and set it to a constant. The most efficient way to do that is to use `memset()`:

```
zeroes <- cfunction(c(n_ = "integer"), '
    int n = asInteger(n_);

    SEXP out = PROTECT(allocVector(INTSXP, n));
    memset(INTEGER(out), 0, n * sizeof(int));
    UNPROTECT(1);

    return out;
')
zeroes(10);
#> [1] 0 0 0 0 0 0 0 0 0 0
```

20.3.2 Missing and non-finite values

Each atomic vector has a special constant for getting or setting missing values:

- INTSXP: NA_INTEGER
- LGLSXP: NA_LOGICAL
- STRSXP: NA_STRING

Missing values are somewhat more complicated for REALSXP because there is an existing protocol for missing values defined by the floating point standard (IEEE 754 (http://en.wikipedia.org/wiki/IEEE_floating_point)). In doubles, an NA is NaN with a special bit pattern (the lowest word is 1954, the year Ross Ihaka was born), and there are other special values for positive and negative infinity. Use `ISNA()`, `ISNAN()`, and `!R_FINITE()` macros to check for missing, NaN, or non-finite values. Use the constants `NA_REAL`, `R_NaN`, `R_PosInf`, and `R_NegInf` to set those values.

We can use this knowledge to make a simple version of `is.NA()`:

```

is_na <- cfunction(c(x = "ANY"), '
  int n = length(x);

  SEXP out = PROTECT(allocVector(LGLSXP, n));

  for (int i = 0; i < n; i++) {
    switch(TYPEOF(x)) {
      case LGLSXP:
        LOGICAL(out)[i] = (LOGICAL(x)[i] == NA_LOGICAL);
        break;
      case INTSXP:
        LOGICAL(out)[i] = (INTEGER(x)[i] == NA_INTEGER);
        break;
      case REALSXP:
        LOGICAL(out)[i] = ISNA-REAL(x)[i]);
        break;
      case STRSXP:
        LOGICAL(out)[i] = (STRING_ELT(x, i) == NA_STRING);
        break;
      default:
        LOGICAL(out)[i] = NA_LOGICAL;
    }
  }
  UNPROTECT(1);

  return out;
')
is_na(c(NA, 1L))
#> [1] TRUE FALSE
is_na(c(NA, 1))
#> [1] TRUE FALSE
is_na(c(NA, "a"))
#> [1] TRUE FALSE
is_na(c(NA, TRUE))
#> [1] TRUE FALSE

```

Note that `base::is.na()` returns `TRUE` for both `NA` and `NaN`s in a numeric vector, as opposed to the C `ISNA()` macro, which returns `TRUE` only for `NA_REAL`s.

20.3.3 Accessing vector data

There is a helper function for each atomic vector that allows you to access the C array which stores the data in a vector. Use `REAL()`, `INTEGER()`, `LOGICAL()`, `COMPLEX()`, and `RAW()` to access the C array inside numeric, integer, logical, complex, and raw vectors. The following example shows how to use `REAL()` to inspect and modify a numeric vector:

```
add_one <- cfunction(c(x = "numeric"), "  
  int n = length(x);  
  SEXP out = PROTECT(allocVector(REALSXP, n));  
  
  for (int i = 0; i < n; i++) {  
    REAL(out)[i] = REAL(x)[i] + 1;  
  }  
  UNPROTECT(1);  
  
  return out;  
")  
add_one(as.numeric(1:10))  
#> [1]  2  3  4  5  6  7  8  9 10 11
```

When working with longer vectors, there's a performance advantage to using the helper function once and saving the result in a pointer:

```
add_two <- cfunction(c(x = "numeric"), "  
  int n = length(x);  
  double *px, *pout;  
  
  SEXP out = PROTECT(allocVector(REALSXP, n));  
  
  px = REAL(x);  
  pout = REAL(out);  
  for (int i = 0; i < n; i++) {  
    pout[i] = px[i] + 2;  
  }  
  UNPROTECT(1);  
  
  return out;  
")  
add_two(as.numeric(1:10))  
#> [1]  3  4  5  6  7  8  9 10 11 12
```

```

library(microbenchmark)
x <- as.numeric(1:1e6)
microbenchmark(
  add_one(x),
  add_two(x)
)
#> Unit: milliseconds
#>      expr    min      lq  median      uq    max neval
#>  add_one(x) 4.950 5.093  6.199 7.571 41.81   100
#>  add_two(x) 1.106 1.220  2.309 3.673 34.88   100

```

On my computer, `add_two()` is about twice as fast as `add_one()` for a million element vector. This is a common idiom in base R.

20.3.4 Character vectors and lists

Strings and lists are more complicated because the individual elements of a vector are SEXPs, not basic C data structures. Each element of a STRSXP is a CHARSEXPs, an immutable object that contains a pointer to C string stored in a global pool. Use `STRING_ELT(x, i)` to extract the CHARSXP, and `CHAR(STRING_ELT(x, i))` to get the actual `const char*` string. Set values with `SET_STRING_ELT(x, i, value)`. Use `mkChar()` to turn a C string into a CHARSXP and `mkString()` to turn a C string into a STRSXP. Use `mkChar()` to create strings to insert in an existing vector, use `mkString()` to create a new (length 1) vector.

The following function shows how to make a character vector containing known strings:

```

abc <- cfunction(NULL, '
  SEXP out = PROTECT(allocVector(STRSXP, 3));

  SET_STRING_ELT(out, 0, mkChar("a"));
  SET_STRING_ELT(out, 1, mkChar("b"));
  SET_STRING_ELT(out, 2, mkChar("c"));

  UNPROTECT(1);

  return out;
')
abc()
#> [1] "a" "b" "c"

```


Things are a little harder if you want to modify the strings in the vector because you need to know a lot about string manipulation in C (which is hard, and harder to do right). For any problem that involves any kind of string modification, you're better off using Rcpp.

The elements of a list can be any other SEXP, which generally makes them hard to work with in C (you'll need lots of `switch` statements to deal with the possibilities). The accessor functions for lists are `VECTOR_ELT(x, i)` and `SET_VECTOR_ELT(x, i, value)`.

20.3.5 Modifying inputs

You must be very careful when modifying function inputs. The following function has some rather unexpected behaviour:

```
add_three <- cfunction(c(x = "numeric"), '
  REAL(x)[0] = REAL(x)[0] + 3;
  return x;
')
x <- 1
y <- x
add_three(x)
#> [1] 4
x
#> [1] 4
y
#> [1] 4
```

Not only has it modified the value of `x`, it has also modified `y`! This happens because of R's lazy copy-on-modify semantics. To avoid problems like this, always `duplicate()` inputs before modifying them:

```
add_four <- cfunction(c(x = "numeric"), '
  SEXP x_copy = PROTECT(duplicate(x));
  REAL(x_copy)[0] = REAL(x_copy)[0] + 4;
  UNPROTECT(1);
  return x_copy;
')
x <- 1
y <- x
add_four(x)
#> [1] 5
```

```
x
#> [1] 1
y
#> [1] 1
```

If you're working with lists, use `shallow_duplicate()` to make a shallow copy; `duplicate()` will also copy every element in the list.

20.3.6 Coercing scalars

There are a few helper functions that turn length one R vectors into C scalars:

- `asLogical(x)`: `INTSXP` \rightarrow `int`
- `asInteger(x)`: `INTSXP` \rightarrow `int`
- `asReal(x)`: `REALSXP` \rightarrow `double`
- `CHAR(asChar(x))`: `STRSXP` \rightarrow `const char*`

And helpers to go in the opposite direction:

- `ScalarLogical(x)`: `int` \rightarrow `LGLSXP`
- `ScalarInteger(x)`: `int` \rightarrow `INTSXP`
- `ScalarReal(x)`: `double` \rightarrow `REALSXP`
- `mkString(x)`: `const char*` \rightarrow `STRSXP`

These all create R-level objects, so they need to be `PROTECT()`ed.

20.3.7 Long vectors

As of R 3.0.0, R vectors can have length greater than 2^{32} . This means that vector lengths can no longer be reliably stored in an `int` and if you want your code to work with long vectors, you can't write code like `int n = length(x)`. Instead use the `R_xlen_t` type and the `xlength()` function, and write `R_xlen_t n = xlength(x)`.

20.4 Pairlists

In R code, there are only a few instances when you need to care about the difference between a pairlist and a list (as described in Section 14.5). In C, pairlists play much more important role because they are used for calls, unevaluated arguments, attributes, and in In C, lists and pairlists differ primarily in how you access and name elements.

Unlike lists (VECSXPs), pairlists (LISTSXPs) have no way to index into an arbitrary location. Instead, R provides a set of helper functions that navigate along a linked list. The basic helpers are `CAR()`, which extracts the first element of the list, and `CDR()`, which extracts the rest of the list. These can be composed to get `CAAR()`, `CDAR()`, `CADDR()`, `CADDDR()`, and so on. Corresponding to the getters, R provides setters `SETCAR()`, `SETCDR()`, etc.

The following example shows how `CAR()` and `CDR()` can pull out pieces of a quoted function call:

```
car <- cfunction(c(x = "ANY"), 'return CAR(x);')
cdr <- cfunction(c(x = "ANY"), 'return CDR(x);')
cadr <- cfunction(c(x = "ANY"), 'return CADR(x);')
```

```
x <- quote(f(a = 1, b = 2))
# The first element
car(x)
#> f
# Second and third elements
cdr(x)
#> $a
#> [1] 1
#>
#> $b
#> [1] 2
# Second element
car(cdr(x))
#> [1] 1
cadr(x)
#> [1] 1
```

Pairlists are always terminated with `R_NilValue`. To loop over all elements of a pairlist, use this template:

```

count <- cfunction(c(x = "ANY"), '
  SEXP e1, nxt;
  int i = 0;

  for(nxt = x; nxt != R_NilValue; e1 = CAR(nxt), nxt = CDR(nxt)) {
    i++;
  }
  return ScalarInteger(i);
')
count(quote(f(a, b, c)))
#> [1] 4
count(quote(f()))
#> [1] 1

```

You can make new pairlists with `CONS()` and new calls with `LCONS()`. Remember to set the last value to `R_NilValue`. Since these are R objects as well, they are eligible for garbage collection and must be `PROTECTED`. In fact, it is unsafe to write code like the following:

```

new_call <- cfunction(NULL, '
  return LCONS(install("+"), LCONS(
    ScalarReal(10), LCONS(
      ScalarReal(5), R_NilValue
    )
  ));
')
gctorture(TRUE)
new_call()
#> 5 + 5
gctorture(FALSE)

```

On my machine, I get the result `5 + 5` — highly unexpected! In fact, to be safe, we must `PROTECT` each `ScalarReal` that is generated, as every R object allocation can trigger the garbage collector.

```

new_call <- cfunction(NULL, '
  SEXP REALSXP_10 = PROTECT(ScalarReal(10));
  SEXP REALSXP_5 = PROTECT(ScalarReal(5));
  SEXP out = PROTECT(LCONS(install("+"), LCONS(
    REALSXP_10, LCONS(
      REALSXP_5, R_NilValue
    )
  ));
')

```

```

    ));
    UNPROTECT(3);
    return out;
  )
  gctorture(TRUE)
  new_call()
  #> 10 + 5
  gctorture(FALSE)

```

TAG() and SET_TAG() allow you to get and set the tag (aka name) associated with an element of a pairlist. The tag should be a symbol. To create a symbol (the equivalent of `as.symbol()` in R), use `install()`.

Attributes are also pairlists, but come with the helper functions `setAttrib()` and `getAttrib()`:

```

set_attr <- cfunction(c(obj = "SEXP", attr = "SEXP", value = "SEXP"), '
  const char* attr_s = CHAR(asChar(attr));

  duplicate(obj);
  setAttrib(obj, install(attr_s), value);
  return obj;
')
x <- 1:10
set_attr(x, "a", 1)
#> [1] 1 2 3 4 5 6 7 8 9 10
#> attr("a")
#> [1] 1

```

(Note that `setAttrib()` and `getAttrib()` must do a linear search over the attributes pairlist.)

There are some (confusingly named) shortcuts for common setting operations: `classgets()`, `namesgets()`, `dimgets()`, and `dimnamesgets()` are the internal versions of the default methods of `class<-`, `names<-`, `dim<-`, and `dimnames<-`.

20.5 Input validation

If the user provides unexpected input to your function (e.g., a list instead of a numeric vector), it's very easy to crash R. For this reason, it's a good

idea to write a wrapper function that checks arguments are of the correct type. It's usually easier to do this at the R level. For example, going back to our first example of C code, we might rename the C function to `add_` and write a wrapper around it to check that the inputs are ok:

```
add_ <- cfunction(signature(a = "integer", b = "integer"), "
  SEXP result = PROTECT(allocVector(REALSXP, 1));
  REAL(result)[0] = asReal(a) + asReal(b);
  UNPROTECT(1);

  return result;
")
add <- function(a, b) {
  stopifnot(is.numeric(a), is.numeric(b))
  stopifnot(length(a) == 1, length(b) == 1)
  add_(a, b)
}
```

Alternatively, if we wanted to be more accepting of diverse inputs we could do the following:

```
add <- function(a, b) {
  a <- as.numeric(a)
  b <- as.numeric(b)

  if (length(a) > 1) warning("Only first element of a used")
  if (length(b) > 1) warning("Only first element of b used")

  add_(a, b)
}
```

To coerce objects at the C level, use `PROTECT(new = coerceVector(old, SEXPTYPE))`. This will return an error if the SEXP can not be converted to the desired type.

To check if an object is of a specified type, you can use `TYPEOF`, which returns a `SEXPTYPE`:

```
is_numeric <- cfunction(c("x" = "ANY"), "
  return ScalarLogical(TYPEOF(x) == REALSXP);
")
is_numeric(7)
```

```
#> [1] TRUE
is_numeric("a")
#> [1] FALSE
```

There are also a number of helper functions which return 0 for FALSE and 1 for TRUE:

- For atomic vectors: `isInteger()`, `isReal()`, `isComplex()`, `isLogical()`, `isString()`.
- For combinations of atomic vectors: `isNumeric()` (integer, logical, real), `isNumber()` (integer, logical, real, complex), `isVectorAtomic()` (logical, integer, numeric, complex, string, raw).
- For matrices (`isMatrix()`) and arrays (`isArray()`).
- For more esoteric objects: `isEnvironment()`, `isExpression()`, `isList()` (a pair list), `isNewList()` (a list), `isSymbol()`, `isNull()`, `isObject()` (S4 objects), `isVector()` (atomic vectors, lists, expressions).

Note that some of these functions behave differently to similarly named R functions with similar names. For example `isVector()` is true for atomic vectors, lists, and expressions, where `is.vector()` returns TRUE only if its input has no attributes apart from names.

20.6 Finding the C source code for a function

In the base package, R doesn't use `.Call()`. Instead, it uses two special functions: `.Internal()` and `.Primitive()`. Finding the source code for these functions is a an arduous task: you first need to look for their C function name in `src/main/names.c` and then search the R source code. `pryr::show_c_source()` automates this task using GitHub code search:

```
tabulate
#> function (bin, nbins = max(1L, bin, na.rm = TRUE))
#> {
#>   if (!is.numeric(bin) && !is.factor(bin))
#>     stop("'bin' must be numeric or a factor")
#>   if (typeof(bin) != "integer")
```

```
#>      bin <- as.integer(bin)
#>      if (nbins > .Machine$integer.max)
#>        stop("attempt to make a table with >= 2^31 elements")
#>      nbins <- as.integer(nbins)
#>      if (is.na(nbins))
#>        stop("invalid value of 'nbins'")
#>      .Internal(tabulate(bin, nbins))
#> }
#> <bytecode: 0x7fc69d9930b0>
#> <environment: namespace:base>
```

```
pryr::show_c_source(.Internal(tabulate(bin, nbins)))
#> tabulate is implemented by do_tabulate with op = 0
```

This reveals the following C source code (slightly edited for clarity):

```
SEXP attribute_hidden do_tabulate(SEXP call, SEXP op, SEXP args,
                                SEXP rho) {
    checkArity(op, args);
    SEXP in = CAR(args), nbin = CADR(args);
    if (TYPEOF(in) != INTSXP) error("invalid input");

    R_xlen_t n = XLENGTH(in);
    /* FIXME: could in principle be a long vector */
    int nb = asInteger(nbin);
    if (nb == NA_INTEGER || nb < 0)
        error(_("invalid '%s' argument"), "nbin");

    SEXP ans = allocVector(INTSXP, nb);
    int *x = INTEGER(in), *y = INTEGER(ans);
    memset(y, 0, nb * sizeof(int));
    for(R_xlen_t i = 0 ; i < n ; i++) {
        if (x[i] != NA_INTEGER && x[i] > 0 && x[i] <= nb) {
            y[x[i] - 1]++;
        }
    }

    return ans;
}
```

Internal and primitive functions have a somewhat different interface than `.Call()` functions. They always have four arguments:

- **SEXP call**: the complete call to the function. `CAR(call)` gives the name of the function (as a symbol); `CDR(call)` gives the arguments.
- **SEXP op**: an “offset pointer”. This is used when multiple R functions use the same C function. For example `do_logic()` implements `&`, `|`, and `!`. `show_c_source()` prints this out for you.
- **SEXP args**: a pairlist containing the unevaluated arguments to the function.
- **SEXP rho**: the environment in which the call was executed.

This gives internal functions an incredible amount of flexibility as to how and when the arguments are evaluated. For example, internal S3 generics call `DispatchOrEval()` which either calls the appropriate S3 method or evaluates all the arguments in place. This flexibility come at a price, because it makes the code harder to understand. However, evaluating the arguments is usually the first step and the rest of the function is straightforward.

The following code shows `do_tabulate()` converted into standard a `.Call()` interface:

```
tabulate2 <- cfunction(c(bin = "SEXP", nbins = "SEXP"), '
    if (TYPEOF(bin) != INTSXP) error("invalid input");

    R_xlen_t n = XLENGTH(bin);
    /* FIXME: could in principle be a long vector */
    int nb = asInteger(nbins);
    if (nb == NA_INTEGER || nb < 0)
        error("invalid \'%s\' argument", "nbins");

    SEXP ans = allocVector(INTSXP, nb);
    int *x = INTEGER(bin), *y = INTEGER(ans);
    memset(y, 0, nb * sizeof(int));
    for(R_xlen_t i = 0 ; i < n ; i++) {
        if (x[i] != NA_INTEGER && x[i] > 0 && x[i] <= nb) {
            y[x[i] - 1]++;
        }
    }

    return ans;
')
tabulate2(c(1L, 1L, 1L, 2L, 2L), 3)
#> [1] 3 2 0
```

To get this to compile, I also removed the call to `_()` which is an internal R function used to translate error messages between different languages.

The final version below moves more of the coercion logic into an accompanying R function, and does some minor restructuring to make the code a little easier to understand. I also added a `PROTECT()`; this is probably missing in the original because the author knew that it would be safe.

```
tabulate_ <- cfunction(c(bin = "SEXP", nbins = "SEXP"), '
  int nb = asInteger(nbins);

  // Allocate vector for output - assumes that there are
  // less than 2^32 bins, and that each bin has less than
  // 2^32 elements in it.
  SEXP out = PROTECT(allocVector(INTSXP, nb));
  int *pbin = INTEGER(bin), *pout = INTEGER(out);
  memset(pout, 0, nb * sizeof(int));

  R_xlen_t n = xlength(bin);
  for(R_xlen_t i = 0; i < n; i++) {
    int val = pbin[i];
    if (val != NA_INTEGER && val > 0 && val <= nb) {
      pout[val - 1]++; // C is zero-indexed
    }
  }
  UNPROTECT(1);

  return out;
')

tabulate3 <- function(bin, nbins) {
  bin <- as.integer(bin)
  if (length(nbins) != 1 || nbins <= 0 || is.na(nbins)) {
    stop("nbins must be a positive integer", call. = FALSE)
  }
  tabulate_(bin, nbins)
}
tabulate3(c(1, 1, 1, 2, 2), 3)
#> [1] 3 2 0
```

“The author has become one of the foremost authorities on this topic and is well known and appreciated throughout the entire R community. This is the great strength of the book and the primary reason it deserves to be published. It addresses a topic where there is already a growing number of books, but few have the depth, the technical accuracy, and the authority of this one.”

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ISBN: 978-1-4665-8696-3

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