

Date:- 25-05-20

Name:- G. Raviteja

Course:- Digital signal processing

USN:- 4AL16EC101

Topic:- Day 1

Sem:- 6th 'B'

- \* Fourier transform and Wavelet's co-ordinate system transform:-

$$u(x, y, t)$$

$$u_t = \alpha \nabla^2 u$$

$$SVD = \text{data-drive FFT}$$

- \* FFT:- Fast Fourier transform is used to process audio signals, video, etc:- by compressing and representing efficiently by using FFT.

$$f(t) = \frac{a_0}{2} + \sum_{k=1}^{\infty} (a_k \cos 2\pi k t + b_k \sin 2\pi k t)$$

Like  $k \rightarrow$  Frequency

$a_k, b_k \rightarrow$  coefficients.

- \* It consists of cosine & sine components.

- \* Fourier transform:-

$$X_a(F) = \int_{-\infty}^{\infty} x(t) \cos 2\pi f t dt$$

$$X_b(F) = \int_{-\infty}^{\infty} x(t) \sin 2\pi f t dt.$$

$$X(F) = \int_{-\infty}^{\infty} x(t) e^{-j2\pi f t} dt$$

- \* Continuous Fourier Transform:-

$$X(f) = \int_{-\infty}^{\infty} x(t) e^{-j2\pi f t} dt.$$

- \* Discrete Fourier Transform:-

$$X_k = \sum_{n=0}^{N-1} x_n e^{-j2\pi k n / N}$$

\* Inner products in Hilbert space:-

$$\langle f(x), g(x) \rangle = \int_a^b f(x)g(x)dx.$$

\* Fourier series using Matlab:-

clear all, close all, clc

figure

set(gcf, 'position', [1500, 200, 2000, 1200])

L=pi;

N=1024;

dx = 2+L/(N-1);

f = 0.2;

f(N/4:N/2) = 4\*(1:N/4+1)/N;

f(N/2+1:3\*N/4) = 1-4\*(0:N/4-1)/N;

plot(x, f, '-k', 'line width', 3:5), hold on

cc = jet(20);

A0 = sum(f.\*ones(size(x))\*dx/pi);

fFs = A0/2

for k=1:20

A(k) = sum(z.\*cos(pi\*x/L)\*dx/pi);

B(k) = sum(z.\*sin(pi\*k\*x/L)\*dx/pi);

ZFs = fFs + A(k)\*cos(k\*pi\*x/L) + B(k)\*sin(k\*pi\*x/L);

plot(x, fFs, '-', 'colour', cc(k,i)): line width=2)

pause(.1)

end.

## \* Fourier series using Python:-

```
=> In [c]: import numpy as np
            import matplotlib.pyplot as plt
            from matplotlib import cm
            plt.rcParams['figure.figsize'] = [8,8]
            plt.rcParams.update({'font.size': 18})
            dx = 0.001
            L = np.pi
            x = L * np.arange(1+dx, 1+dx, dx)
            n = len(x)
            nquist = int(np.floor(n/4))
            f = np.zeros_like(x)
            f[nquist:2+nquist] = (4/n) * np.arange(1, nquist+1)
            f[2*nquist:3*nquist] = np.ones(nquist) - (2/c0) * np.arange(0, nquist+1)
            fig, ax = plt.subplots()
            ax.plot(x, f, '-', color='k', linewidth=2)
```

