

Day 3

• Logic design:-

Boolean algebra:-

'0' @ '1'

→ cost of the circuit

→ Simple realization of a circuit

"In 1854, George Boole developed an algebra system is called boolean algebra"

→ "Boolean algebra is a system of mathematical logic"

→ It is defined with set of elements, a set of operators, and a no. of axioms @ postulates

→ Set of elements - (0, 1)

→ Two binary operators - OR and AND

'1' @ (u) @ (v) (+) (.) @ n @

→ Unary operator - NOT @ (invert)

• Axioms and laws of boolean algebra:-

→ Axioms @ postulates of boolean algebra were a logical expressions upon which we can build useful theory.

"AND operation" "OR operation"

"NOT operation"

$$\begin{aligned} \rightarrow 0 \cdot 0 &= 0 \\ \rightarrow 0 \cdot 1 &= 0 \\ \rightarrow 1 \cdot 0 &= 0 \\ \rightarrow 1 \cdot 1 &= 1 \end{aligned} \quad \left. \vphantom{\begin{aligned} \rightarrow 0 \cdot 0 &= 0 \\ \rightarrow 0 \cdot 1 &= 0 \\ \rightarrow 1 \cdot 0 &= 0 \\ \rightarrow 1 \cdot 1 &= 1 \end{aligned}} \right\} \text{AND operation}$$

$$\begin{aligned} \rightarrow 0 + 0 &= 0 \\ \rightarrow 0 + 1 &= 1 \\ \rightarrow 1 + 0 &= 1 \\ \rightarrow 1 + 1 &= 1 \end{aligned} \quad \left. \vphantom{\begin{aligned} \rightarrow 0 + 0 &= 0 \\ \rightarrow 0 + 1 &= 1 \\ \rightarrow 1 + 0 &= 1 \\ \rightarrow 1 + 1 &= 1 \end{aligned}} \right\} \text{OR operation}$$

DATE:

PAGE:

$$\begin{aligned} \rightarrow 0 \cdot 0 &= 0 \\ \rightarrow 0 \cdot 1 &= 0 \\ \rightarrow 1 \cdot 0 &= 0 \\ \rightarrow 1 \cdot 1 &= 1 \end{aligned} \quad \left. \vphantom{\begin{aligned} \rightarrow 0 \cdot 0 &= 0 \\ \rightarrow 0 \cdot 1 &= 0 \\ \rightarrow 1 \cdot 0 &= 0 \\ \rightarrow 1 \cdot 1 &= 1 \end{aligned}} \right\} \text{AND operation}$$

- Difference b/w boolean algebra, ordinary algebra and binary number system.

→ In boolean algebra

$$\begin{aligned} A + A &= A & A \cdot A &= A \\ 1 + 1 &= 1 & 1 \cdot 1 &= 1 \end{aligned}$$

→ In ordinary algebra

$$\begin{aligned} A + A &= 2A & A \cdot A &= A^2 \\ 1 + 1 &= 2 & 1 \cdot 1 &= 1 \end{aligned}$$

→ In binary number system

$$\begin{aligned} 1 + 1 &= (10) & 1 \cdot 1 &= 1 \end{aligned}$$

Axioms @ postulates

$$\begin{aligned} \rightarrow x + 0 &= x & x \cdot 0 &= 0 \\ \rightarrow x + 1 &= 1 & x \cdot 1 &= x \\ \rightarrow x + x &= x & x \cdot x &= x \\ \rightarrow x + \bar{x} &= 1 & x \cdot \bar{x} &= 0 \\ \rightarrow (\bar{x}) \cdot (x')' &= x \end{aligned}$$

• Identity element

$$\begin{aligned} \text{additive identity} &= 0 & \text{OR operation} & \text{AND operation} \\ & & x + 0 &= x & x \cdot 1 &= x = 1 \cdot x \end{aligned}$$

multiplicative identity = 1

$$x + 0 = x$$

$$0 + x = x$$

• Laws of boolean algebra:-

(i) Commutative: $x + y = y + x$

$$A + B = B + A \quad | \quad x \cdot y = y \cdot x$$

$$A \cdot B = B \cdot A$$

DATE:

PAGE:

(ii) Associative Law:-

$$x + (y + z) = (x + y) + z$$

$$x \cdot (y \cdot z) = (x \cdot y) \cdot z$$

$$A + (B + C) = (A + B) + C$$

$$A \cdot (B \cdot C) = (A \cdot B) \cdot C$$

(iii) Distributive law.

① $x(y + z) = xy + xz$

$\rightarrow A = 0, B = 1, C = 0$

$A(B + C) = AB + AC$

LHS: $A(B + C) = 0(1 + 0) = 0$

RHS: $AB + AC = 0$

② $x + yz = (x + y)(x + z)$

$A + BC = (A + B)(A + C)$

③ $x + yz = (x + y)(x + z)$

$= x \cdot x + xz + xy + yz$

$= x + xz + xy + yz$

$= x(1 + z + y) = yz \Rightarrow x + yz$ hence proved

• Theorems of boolean algebra:-

① Absorption theorem: $x + xy = x$, $A + AB = A$

$\rightarrow x(1 + y) = x \cdot 1 = x$

② $x + \bar{x}y = x + y$

$(x + \bar{x})(x + y) = 1 \cdot (x + y) = (x + y)$

③ $A + BC = (A + B)(A + C)$

$= A \cdot A + A \cdot C + B \cdot A + B \cdot C$

$= A(1 + C) + AB + BC \Rightarrow A + BC$

$A + \bar{A}B = A + B$

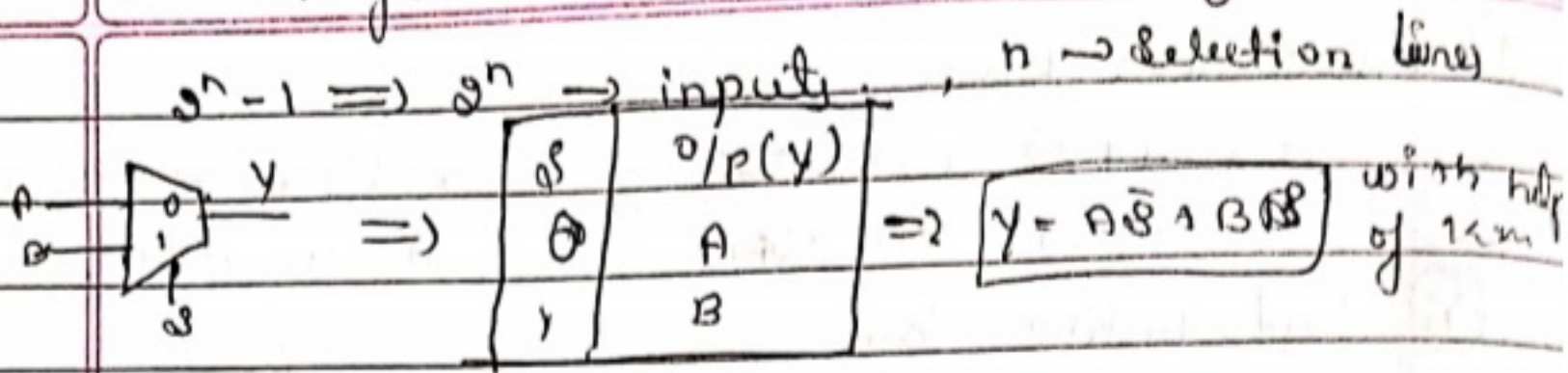
• More to logic gates:-

① NAND, NOR - universal gates

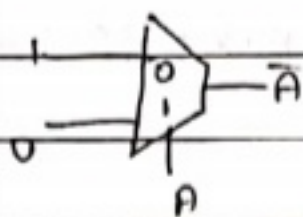
② "universal logic"

③ Mux & decoder are called "universal logic"

Multiplexer :- It is a device that selects one of several analog or digital signals and it will forward to o/p line, i.e. single o/p line.

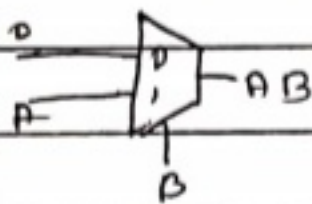


Inverter designs help of mux.



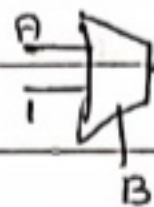
$$Y = A\bar{S} + BS \Rightarrow 1\bar{A} + 0A$$

$$Y = \bar{A}$$



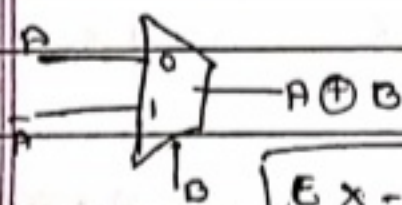
$$Y = 0\bar{B} + AB$$

$$Y = A \cdot B$$

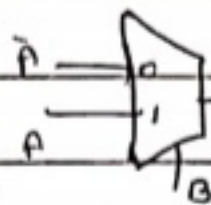


$$Y = A+B$$

@ gate

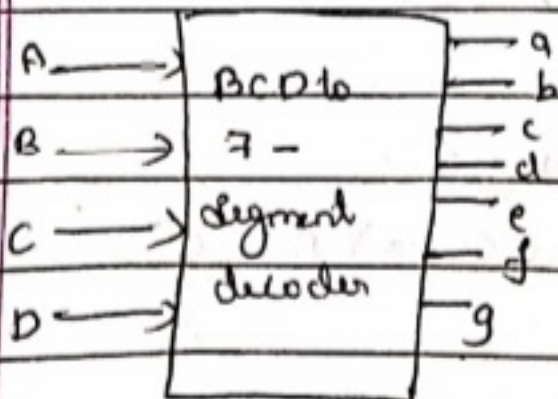


$$Y = A \oplus B$$



$$Y = A \odot B$$

BCD to 7-Segment decoder :-



4 i/p lines & 7 o/p lines

 light emitting diode.

Python:

Application 5:- build a desktop database application.

@ Desktop database App - How the app will look like.

→ How to build a program which is used store the information of books.

→ user interface design.

→ build a graphical user interface.

→ frontend interface

we use grid method make things easier

1. from tkinter import.

2.

3. window Tk()

4. window-r

5. window main loop()

l1 = Label(window, text = 'Title')

l1 = grid(row=0, column=0)

copy for more row & column indicating
"Title", "author", "year", "ISBN"

title - text - string var()

e1 = entry(window, textvariable = title_text)

e1 = grid(row=0, column=1)

This should be applied for author, year, ISBN to get a row & column table.

→ Backend :- we got to know to create table @ exist book.

→ connecting the frontend to the backend.

→ fixing the bug.

→ creating a standalone executable version of the program.