

$$1. \quad n = \sum (d_i \times \text{base}^i)$$

a. $0x\text{BABE}$ $\xrightarrow{\text{binary}}$ $(1)011010101110$ $\xrightarrow{\text{invert all bits} + 1}$

negative integer

$$\begin{aligned} &\rightarrow 0100010101000010 \\ &= 1 \times 2^{14} + 1 \times 2^{10} + 1 \times 2^8 + 1 \times 2^6 + 1 \times 2^1 \\ &= (1 \times 16384) + (1 \times 1024) + (1 \times 256) + (1 \times 64) + (1 \times 2) \\ &= 17730 \quad \therefore \text{answer} = -17730 \end{aligned}$$

b. $0x\text{DAD E}$ $\xrightarrow{\text{binary}}$ $(1)0110101101110$ $\xrightarrow{\text{invert all bits} + 1}$

negative integer

$$\begin{aligned} &\rightarrow 0010010100100010 \\ &= 1 \times 2^{13} + 1 \times 2^{10} + 1 \times 2^8 + 1 \times 2^5 + 1 \times 2^1 \\ &= (1 \times 8192) + (1 \times 1024) + (1 \times 256) + (1 \times 32) + (1 \times 2) \\ &= 9506 \quad \therefore \text{answer} = -9506 \end{aligned}$$

c. $0x4ACE$ $\xrightarrow{\text{binary}}$ 0100101011001110

$$\begin{aligned} &= 1 \times 2^{14} + 1 \times 2^{11} + 1 \times 2^9 + 1 \times 2^7 + 1 \times 2^6 + 1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 \\ &= (1 \times 16384) + (1 \times 2048) + (1 \times 512) + (1 \times 128) + (1 \times 64) + (1 \times 8) + (1 \times 4) + (1 \times 2) \\ &= 19150 \# \end{aligned}$$

2. Using Horner's nest form

a. -2011 , try to calculate 2011 first, minus 1 and invert all bits

in binary

2011	2011/2	1	2011 $\xrightarrow{\text{hex}}$ $0x\text{FFF F F825}$ #
	1005/2	1	
	502/2	0	
	251/2	1	
	125/2	1	
	62/2	0	
	31/2	1	
	15/2	1	
	7/2	1	
	3/2	1	
	1/2	1	

result = 1111101111, extension to 32 bits

0000 0000 0000 0000 0000 0000 0111 1101 1011

1111 1111 1111 1111 1111 1000 0010 0101

b. 9804	9804/2	remainder	9804 in binary
	4902/2	0	= 10011001001100, extension to 32 bits
	2451/2	1	
	1225/2	1	0000 0000 0000 0000 0010 0110 0100 1100
	612/2	0	
	306/2	0	hex → 0x 0000 264C
	153/2	1	
	76/2	0	
	38/2	0	
	19/2	1	
	9/2	1	
	4/2	0	
	2/2	0	
	1/2	1	

3. a. -0.1875

$S = 1$

$$-0.1875 = \left(-\frac{1}{8}\right) + \left(-\frac{1}{16}\right) = \left(-\frac{3}{16}\right) = -1 \times 11_2 \times 2^{-4}$$

$$= -1 \times 1/2 \times 2^{-3}$$

Fraction = 100...00₂

Exponent = $-3 + \text{bias} = -3 + 127 = 124 = 01111100_2$

answer = 101111001000000000000000000000

b. 0.46875

$S = 0$

$$0.46875 = \left(\frac{1}{4}\right) + \left(\frac{1}{8}\right) + \left(\frac{1}{16}\right) + \left(\frac{1}{32}\right) = \left(\frac{15}{32}\right) = 1 \times 1111_2 \times 2^{-5}$$

$$= 1 \times 1.111_2 \times 2^{-2}$$

Fraction = 1110.00₂

Exponent = $2 + 127 = 129 = 10000001_2$

answer = 010000001110000000000000000000

4. a. 3F000000 $\xrightarrow{\text{binary}}$ $\underbrace{0011111}_{\text{exponent}} \underbrace{0000000000000000}_{\text{fraction}} \dots 0000$

$$\text{exponent} = 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 = 126$$

$$\begin{aligned} \text{Fraction} &= 0 \\ \text{decimal} &= (-1)^0 \times (1 + 0.0_2) \times 2^{(126-127)} \\ &= 1 \times 1 \times 2^{-1} = 0.5 \end{aligned}$$

b. BF000000 $\xrightarrow{\text{binary}}$ $\underbrace{0111110}_{\text{exponent}} \underbrace{0000000000000000}_{\text{fraction}} \dots 0000$

$$\text{exponent} = 2^6 + 2^5 + 2^4 + 2^3 + 2^2 = 124$$

$$\begin{aligned} \text{Fraction} &= 0 \\ \text{decimal} &= (-1)^1 \times (1 + 0.0_2) \times 2^{(124-127)} \\ &= -0.125 \end{aligned}$$

5. "Comets are awesome!"

in memory, a char is 8 bits = 1 byte
in mips, we use big endian
Msb start from lowest bit

