# VALUING TIME-VARYING ATTRIBUTES USING THE HEDONIC MODEL: WHEN IS A DYNAMIC APPROACH NECESSARY?

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Abstract—We build on the intuitive (static) modeling framework of Rosen (1974) and specify a simple, forward-looking model of location choice. We use this model, along with a series of graphs, to describe the potential biases associated with the static model and relate these biases to the time series of the amenity of interest. We then derive an adjustment factor that allows the potentially biased static estimates to be converted into forward-looking estimates. Finally, we illustrate these concepts with two empirical applications: the marginal willingness to pay to avoid violent crime and the marginal willingness to pay to avoid air pollution.

# I. Introduction

THE standard hedonic model, drawing on Rosen's classic 1974 paper, provides the workhorse empirical approach used to value local public and private goods. It is straightforward to estimate, usually involving a single least-squares regression of house prices on housing characteristics and neighborhood amenities, and applying the model has become ever more feasible with the increasing availability of detailed housing transactions data. Given its appeal, a myriad of hedonic valuation exercises have been featured in the literature, focusing on applications such as school quality (Black, 1999; Downes & Zabel, 2002; Gibbons & Machin, 2003), climate (Albouy et al., 2016), safety (Gayer, Hamilton, & Viscusi, 2000; Davis, 2004; Greenstone & Gallagher, 2008), environmental quality (Palmquist, 1982; Chay & Greenstone, 2005; Bento, Freedman, & Lang, 2015).

An implicit assumption underlying the traditional model is that households are myopic: they do not account for the fact that housing and neighborhood amenities are likely to be time varying. In practice, though, given the significant costs associated with purchasing a house and moving, it is unlikely that households would not consider future levels of local amenities when making their decisions. When households are forward looking in this manner, the traditional model will yield biased estimates of willingness to pay in many, but not all, cases, and the degree of bias will vary substantially.

Recent literature has sought to quantify this bias empirically in specific applications, comparing results from the traditional model with those obtained using fully dynamic

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models of location choice.¹ Yet the estimation of dynamic models comes with substantial computational costs, even when drawing on recent advances in the literature. Furthermore, fully dynamic models often require very rich data that may exceed the detail of existing data sets. Thus, it would be useful if applied researchers could determine, in advance of a full-blown dynamic estimation, whether the resulting benefits were likely to outweigh the significant computational and data costs involved.

In this paper, we provide a framework that allows such a predetermination. Building on Rosen's (1974) static modeling framework, we specify a simple forward-looking model of location choice where households choose a residence based on the stream of associated utility flows for a fixed number of years. Using this framework, we characterize more fully the potential bias associated with the static approach and relate this bias to the time-series trend of the amenity of interest. In addition, we illustrate an empirically relevant example where the static model and the forward-looking model arrive at the same estimate of willingness to pay, despite the fact that the amenity of interest is time varying.

To understand the potential bias arising from a static model, it is worthwhile revisiting the intuitive identification strategy of the static Rosen model that allows researchers to recover estimates of marginal willingness to pay (MWTP) for an amenity using information on (a) the currently observed quantity of the amenity that the household chooses to consume and (b) the price schedule of the amenity that the household faces. However, if households are instead choosing a house based on some average stream of future amenities (and not solely on the currently observed levels), the traditional model will get both (a) and (b) wrong, resulting in potentially biased estimates of marginal willingness to pay. It is straightforward to see that by using an incorrect interpretation of quantity, the static model will either underor overattribute the true quantity "consumed." We refer to this as the quantity effect. Less obvious is what we refer to as the price effect: if the econometrician is recovering the implicit price schedule from housing price differentials using the incorrect interpretation of quantity, the implicit price of the amenity will also be under- or overstated.

Using these quantity- and price-effect notions, we seek to describe more fully the potential bias associated with the static approach and show that an adjustment factor may be easily derived for a given empirical application. This

<sup>&</sup>lt;sup>1</sup>For recent papers that estimate dynamic models of location choice, see Kennan and Walker (2011), Bishop (2012), Bayer et al. (2016), Bishop and Murphy (2015), Caetano (2016), Davis et al. (2017), and Mastromonaco (2014).

adjustment factor may be used to convert the estimates of marginal willingness to pay from a static model into those that one would have obtained using our forward-looking model. In the simplest case, this adjustment factor is a constant and can be recovered from a simple, ordinary least squares regression.

In the first of our empirical applications, we use a rich data set on housing transactions to apply our adjustment factor to illustrate an example with large heterogeneity in the size of the bias associated with the static model. In particular, we use data from the San Francisco Bay Area to estimate the marginal willingness to pay to avoid violent crime. We calculate the adjustment factor separately by county and find that the static model produces a small bias in Alameda County and large biases in both Marin and San Mateo counties. The heterogeneity across counties is driven by the fact that there is only a small amount of mean reversion in Alameda County, while crime mean-reverts quickly in Marin and San Mateo counties. This geographic heterogeneity provides an empirical example that supports our assertions that, depending on the application, the bias generated by specifying a static model may be large or small and that it is straightforward to get a sense of this bias without estimating a fully dynamic model.

In our second application, we illustrate how our adjustment factor approach may easily be applied to existing estimates of the hedonic price function. In particular, we transform the housing market estimates from Chay and Greenstone's well-known 2005 paper to recover static and forward-looking measures of marginal willingness to pay to avoid air pollution in the years following the Clean Air Act Amendments of 1970. This application, which focuses on a period with a policy-driven, mean-reverting decline in air pollution, also serves as an example of a case with a large adjustment factor.

The remainder of the paper is organized as follows: Section II describes the traditional static model, as well as a simple forward-looking model of hedonic demand; section III describes the bias induced by the static model under various transitions of the amenity of interest and provides guidance when trying to answer the question, "When is the static model sufficient?"; section IV applies the framework in the two empirical settings; and section V concludes.

## II. Model

In this section, we provide an overview of the traditional, static model of Rosen (1974), as well as a simple, forward-looking model of marginal willingness to pay.

## A. The Traditional, Static Model of Willingness to Pay

We first consider the static model of marginal willingness to pay for a house or neighborhood amenity. In this model, households maximize current utility with respect to

their choice of amenity consumption. We choose a simple specification of household utility where household i has an individual-specific preference parameter,  $\alpha_i$ , describing their preference for consumption of the amenity of interest,  $x_i$ . The household also receives utility from the consumption of the numeraire good,  $C_i$ :

$$U(x_i) = \alpha_i x_i + C_i. \tag{1}$$

For simplicity, we consider a model where utility is increasing at a linear rate in the amenity x.<sup>2</sup> Broadly speaking, the intuition developed here applies to nonlinear specifications, which we present in the appendix.

Households purchase x as part of the bundle of goods described by housing. They must pay an annual user cost for housing, which we denote  $r_i$ . One could think of the annual user cost of housing as capturing either a rent or mortgage payment.<sup>3</sup> The function that relates the level of amenity consumption, x, to the annual user cost of housing, r, is the housing price function,  $r_i = r(x_i)$ . We do not need to make any assumptions regarding the functional form of the housing price function, r(x).<sup>4</sup>

Incorporating the household's budget constraint—that their numeraire consumption,  $C_i$ , is equal to income,  $I_i$ , minus the annual user cost of housing,  $r_i$ —yields

$$U(x_i) = \alpha_i x_i + I_i - r(x_i). \tag{2}$$

According to the assumptions underlying the static model, households consider only current levels of the amenity x and therefore maximize current utility with respect to their current choice of x.<sup>5</sup> Thus, the first-order condition for the optimal choice of x is given by

$$U'(x_i) = \alpha_i - r'(x_i) = 0.$$
(3)

The first-order condition described by equation (3) may then be used to solve for  $\alpha_i$ , household i's marginal willingness to pay for the amenity x. In other words, at their chosen level of x consumption, household i's marginal utility of x

<sup>2</sup> While this is done to simplify the analysis, it also means that the identification issues discussed in Brown and Rosen (1982), Mendelsohn (1985), and Ekeland, Heckman, and Nesheim (2004), as well as the estimation issues discussed in Epple (1987) and Bartik (1987), do not apply here.

<sup>3</sup> The annual user cost of housing could also capture other costs of home ownership such as taxes, maintenance, and depreciation. See Poterba (1984) for a discussion of user cost.

<sup>4</sup>Because we do not specify the preferences of housing suppliers, the linear-utility assumption could be consistent with any equilibrium price function that is strictly convex. See Bajari and Benkard (2005) for a discussion. Furthermore, the results derived here hold for any such price function. When we draw the price function, we must show a particular form, and, for simplicity, we illustrate a quadratic housing price function (linear implicit price function) in figures 1, 2, and 3.

<sup>5</sup> If x were time varying, this assumption is analogous to an assumption regarding households' moving costs; in a world with zero moving costs, households may costlessly reoptimize in every period (so looking to the future yields no benefit). However, many papers, including Kennan and Walker (2011), find evidence of substantial moving costs.

will equal the implicit price of x—the marginal cost.<sup>6</sup> This naturally suggests the (static) estimator,

$$\hat{\alpha}_i^s = \hat{r}'(x)_{|x=x_i^*},\tag{4}$$

for the per annum marginal willingness to pay for a one-unit increase in the amenity x.

In addition to this analytical solution, the estimation framework may be described intuitively through a series of graphs. The parameters of the housing price function and, at the same time, the parameters of the implicit price function (the hedonic price gradient), r'(x), are recovered through a regression of annual user costs of housing on amenity levels. These relationships are shown in figures 1a and 1b, respectively.

Using each family's observed consumption of x and the implicit price function, the econometrician is able to construct the implicit price of x that each family actually paid. This information, paired with the first-order condition for utility maximization, allows the econometrician to invert the implicit price and recover the household-specific preference parameter,  $\alpha_i$ . This inversion is depicted in figure 1b.<sup>7</sup>

It is important to note that this static model will return unbiased estimates of  $\alpha_i$  only when either moving is costless or amenity levels are fixed through time. However, in any realistic application, a household would face positive moving costs and time-varying amenities. Thus, we describe a forward-looking model in the next section.<sup>8</sup>

# B. A Simple, Forward-Looking Model of Willingness to Pay

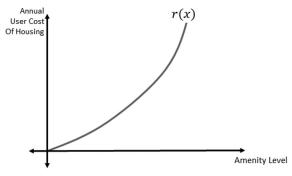
We now move to a forward-looking framework where households maximize the discounted sum of annual utility flows with respect to their current choice of x. Our goal is to specify a model that captures the key determinants of forward-looking behavior but is still simple enough to retain analytical tractability. To do this, we abstract away from

<sup>6</sup> The approach is simple as it requires only interpreting the estimated implicit price function as the menu of prices households face. Given this menu of prices, each household's amenity choice reveals its preferences, which are recovered separately for each household in the data. The approach is limited, however, as without modeling the preferences of housing suppliers, we cannot speak to the equilibrium-price effects of counterfactual amenity changes, as in Cellini, Ferreira, and Rothstein (2010).

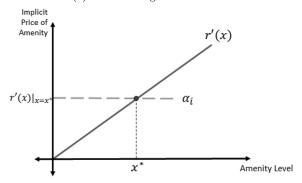
<sup>7</sup>Note that the recovery of the implicit price function and mapping into a local measure of willingness to pay for each household is commonly referred to as the first stage of Rosen's (1974) two-stage model. Applying the assumption that each household has a flat marginal willingness-to-pay function, this inversion would also serve as the second stage of Rosen's model: the recovery of a global measure of willingness to pay. Bajari and Benkard (2005) and Bajari and Kahn (2005) provide an insightful discussion of the interpretations of  $\alpha_i$  as either a structural parameter of the utility function or a local estimate of marginal willingness to pay at the point of consumption.

<sup>8</sup> If agents are actually myopic (for whatever reason), we assume that the static framework presented here yields the correct estimate of  $\alpha_i$ . However, an alternative view of this modeling framework might be that x serves as a proxy for the associated future stream of amenities, and the recovered  $\widehat{\alpha}_i$  may be interpreted as the per period marginal willingness to pay when households are forward looking. In this case, x would suffer from measurement error, and the insights in Chalfin and McCrary (2018), for example, would apply.

FIGURE 1.—GRAPHICAL REPRESENTATION OF THE MODEL



(a) The Housing Price Function



(b) The Implicit Price Function and Household i's MWTP

some of the finer details of dynamic behavior that would substantially complicate the analysis and preclude an analytical decomposition of the bias. In an empirical application of section IV, we compare results from the simple forward-looking model presented here with those found in the fully dynamic model of Bishop and Murphy (2011).

We assume that households choose a residence based on the stream of associated utility flows for the next T years. This is akin to assuming prohibitively high moving costs for the next T years. For simplicity, we assume households cannot reoptimize within the period of T years, and we abstract away from any considerations about the post-T utility. In the specification laid out here, we do not consider future reoptimization in order to simplify the problem, yet we retain the primary insights and intuition of a fully dynamic model—households know that amenities are time varying and that their choice of amenity today will influence the amount of the amenity they consume in subsequent periods.

The housing price function still maps the consumption of the amenity into the annual user cost of housing. As this price is determined in the current period, t, it is a function of the current choice of amenity levels and denoted  $r(x_{i,t})$ . For homeowners, our group of interest, it is natural to think of this annualized user cost of housing as a mortgage payment:

<sup>&</sup>lt;sup>9</sup>In a fully dynamic model, households would also maximize the discounted sum of annual utility flows (i.e., lifetime utility) but would face positive, yet feasible, moving costs in each period. Households would then account not only for future utility flows but for possible future endogenous reoptimization from their current choice.

determined at the time of sale, it is a function of amenity levels in the period in which a household buys.<sup>10</sup>

The amenity of interest, x, is evolving through time, and households form expectations over future levels of x. We write the discounted sum of annual utility flows over the next T years (i.e., the value function) as

$$v(x_{i,t}) = E\left[\sum_{s=1}^{T} \beta^{s-1} (\alpha_i x_{i,t+s-1} + I_i - r(x_{i,t})) | x_{i,t}\right]. \quad (5)$$

For expositional purposes, we define a measure of expected average x consumption over the horizon T with the following weighted average:

$$\bar{x}_{i,t} = \bar{x}(x_{i,t}) = \frac{\sum_{s=1}^{T} \beta^{s-1} E[x_{i,t+s-1} | x_{i,t}]}{\sum_{s=1}^{T} \beta^{s-1}}.$$

We also define the function  $\tilde{r}(\bar{x})$ , which maps the expected average stream of amenity flows into the annual user cost of housing,  $r_{i,t}$ :

$$r_{i,t} = \tilde{r}(\bar{x}(x_{i,t})) = r(x_{i,t}). \tag{6}$$

To make this concrete, consider a house with an annual user cost of \$10,000:  $r_{i,t} = 10,000$ . If this house has a current amenity level of 90 and an expected average amenity level of 115, then  $r_{i,t} = \tilde{r}(115) = r(90) = 10,000$ .

Defining  $\tilde{v}(\bar{x})$  analogously (i.e.,  $\tilde{v}(\bar{x}(x_{i,t})) = v(x_{i,t})$ ) allows us to rewrite equation (5) in terms of  $\bar{x}_{i,t}$ ,

$$\tilde{v}(\bar{x}_{i,t}) = \alpha_i \sum_{s=1}^{T} \beta^{s-1} \bar{x}_{i,t} + \sum_{s=1}^{T} \beta^{s-1} I_i - \sum_{s=1}^{T} \beta^{s-1} \tilde{r}(\bar{x}_{i,t}),$$
 (7)

and the household's problem is then equivalent to choosing  $\bar{x}_{i,t}$  to maximize  $\tilde{v}(\bar{x}_{i,t})$ , yielding the first-order condition:<sup>11</sup>

$$\tilde{v}'(\bar{x}_{i,t}) = \alpha_i \sum_{s=1}^T \beta^{s-1} - \sum_{s=1}^T \beta^{s-1} \tilde{r}'(\bar{x}_{i,t}) = 0.$$
 (8)

The first-order condition described by equation (8) may then be used to solve for household i's marginal willingness to pay for amenity x. This naturally suggests the (forward-looking) estimator

$$\hat{\alpha}_i^f = \hat{\bar{r}}'(\bar{x})_{\left|\bar{x} = \bar{x}_{i,t}^*\right|} \tag{9}$$

for the per annum marginal willingness to pay for a one-unit increase in the amenity, x.

<sup>10</sup> A more general model would allow the user cost to vary over time, which would complicate the model and analysis. As discussed above, the goal of the paper is to derive simple analytical results for the simplest model that still captures the key component of dynamic behavior. In that spirit, it is natural to restrict the user cost to be time invariant but to allow utility from the amenity to vary over time.

<sup>11</sup> If one were to work with  $x_{i,t}$  instead of  $\bar{x}_{i,t}$ , the first-order condition would be given by  $\partial \tilde{v}(\bar{x}_{i,t})/\partial x_{i,t} = \alpha_i \partial \bar{x}_{i,t}/\partial x_{i,t} - \tilde{r}'(\bar{x}_{i,t})\partial \bar{x}_{i,t}/\partial x_{i,t} = 0$ , which is equivalent to equation (8).

When compared with the analogous solution from the static model, described by equation (4), equation (9) highlights the two effects that we previously referred to as the price effect and the quantity effect. The price effect is captured by the use of  $\tilde{r}(\cdot)$  rather than  $r(\cdot)$ . The quantity effect is captured by the fact that we evaluate the function at  $\bar{x}_{i,t}$  rather than  $x_{i,t}$ . In the following section, we discuss the bias induced by each of these effects and show an interesting result where these two effects cancel one another out.

Note that graphically, the recovery of  $\alpha_i$  for the forward-looking model appears similar to that of the static model depicted in figure 1 but defined in  $(\tilde{r}'(\bar{x}), \bar{x})$  space.

## III. Understanding and Predicting the Bias

When the amenity of interest is time varying and reoptimization is not without cost, estimates of marginal willingness to pay recovered using the static model may be biased. In this section, we provide a detailed decomposition of the bias by relating it to the time-series properties of the amenity of interest, x. We do this using a series of intuitive graphs and discussing the mathematical difference between the estimate of marginal willingness to pay recovered from the static model (equation [4]) and the estimate of marginal willingness to pay from the forward-looking model (equation [9]).

The transition properties of the amenity of interest will determine both the sign and size of the bias and therefore will determine when the estimation of the dynamic model is most warranted. When considering the time trend of the amenity, it is sufficient to address two key features: (a) What is the overall trend over the next T years, that is, is the expected average amenity level higher or lower than the current amenity level? and (b) Is the amenity level mean reverting or mean diverging? In the remainder of this section, we walk through the various potential paths of housing amenities and discuss their impacts on willingness-to-pay estimates.

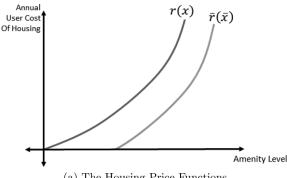
## A. The Amenity Is Simply Rising or Falling through Time

We first consider the case where the amenity of interest, x, is either simply rising or falling through time in a manner that preserves the variance in x across locations. In other words, the relationship between  $x_{it}$  and  $\bar{x}_{it}$  may be expressed as

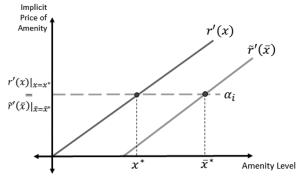
$$\bar{x}(x_{i,t}) = \phi + x_{i,t},\tag{10}$$

 $^{12}$  This highlights the fact that our framework focuses on the mapping of implicit prices into preference parameters; if households are forward looking, using equation (4) to recover  $\alpha_i$  (instead of equation [9]) would be a case of model misspecification. In other words, we abstract from the issues associated with inconsistent estimates of implicit prices (which would affect either modeling framework). For a discussion of these issues, see Chay and Greenstone (2005) and Bajari et al. (2012), both with hedonics-related applications, and Kane and Staiger (2008) more generally.

FIGURE 2.—THE AMENITY RISING THROUGH TIME



(a) The Housing Price Functions



(b) The Implicit Price Functions and Household i's MWTP

where  $\phi$  can be either positive or negative and with no restrictions on its magnitude. When  $\phi > 0$ , the amenity is rising over the T-year horizon and the average future amenity level,  $\bar{x}_{i,t}$ , will be higher than the current amenity level,  $x_{i,t}$ . This would be the case if the amenity were local expenditures on public schools and all schools received the same dollar increase in budget. Alternatively, when  $\phi < 0$ , the amenity is falling through time. In either case, this relationship ensures that a change in current  $x_{i,t}$  produces a one-for-one change in average future amenity consumption,  $\bar{x}$ , that is, for any two choices of current x, denoted  $x_a$  and  $x_b$ :  $|\bar{x}(x_a) - \bar{x}(x_b)| = |x_a - x_b|$ .

Graphically, a uniform increase in x ( $\phi > 0$ ) is represented in figure 2. In figure 2a, one can see that the increase in x results in a forward-looking price function that lies (in a parallel manner) to the right of the static price function. In other words, for any given level of housing expenditure, the associated average amenity level,  $\bar{x}_{i,t}$ , is higher than the current amenity level,  $x_{i,t}$ . Correspondingly, the forward-looking implicit price function, which is depicted in figure 2b, lies (in a parallel manner) to the right of the static implicit price function. In other words, the implicit price of the amenity is lower than the static model would imply.

As noted in figure 2b, the quantity effect (using  $\bar{x}$  instead of x) and the price effect (using  $\tilde{r}'(\cdot)$  instead of  $r'(\cdot)$ ) work in opposite directions and exactly offset one another; there is no bias associated with the static modeling framework, even for an amenity with potentially large time trends.

This holds true for the analogous case of a uniform decrease in x:  $\phi < 0$ . In this case, the decrease in x will result in a forward-looking price function that lies (in a parallel manner) to the left of the static price function and an implicit price function that lies (in a parallel manner) to the left of the static implicit price function. The negative quantity effect will be perfectly offset by the positive price effect, and there will be no bias.

In addition to a graphical representation, we can analytically derive an expression for the difference between the static and forward-looking estimates and show that this adjustment factor will equal 0 when the amenity is simply rising or falling through time. Using the definition that appears in equation (6), that  $\tilde{r}(\bar{x}(x_{i,t})) = r(x_{i,t})$ , and differentiating with respect to  $x_{i,t}$  yields:

$$\tilde{r}'(\bar{x}_{i,t})\frac{\partial \bar{x}_{i,t}}{\partial x_{i,t}} = r'(x_{i,t}),\tag{11}$$

implying that

$$\underbrace{\tilde{r}'(\bar{x})}_{\left|\bar{x}=\bar{x}_{i,t}^*\right|} = \frac{1}{\frac{\partial \bar{x}_{i,t}}{\partial x_{i,t}}} \underbrace{r'(x)}_{\left|x=x_{i,t}^*\right|} .$$
(12)

First, it can be easily seen in equation (12) that a simple adjustment factor captures the difference between the MWTP estimate from the static model: and that from the forward-looking model. Second, it can be seen that when  $\bar{x}(x_{i,t}) = \phi + x_{i,t}, \ \partial \bar{x}_{i,t} / \partial x_{i,t} = 1 \text{ and the MWTP derived}$ using the static model will be identical to that derived using the forward-looking one.

The derivative,  $\partial \bar{x}_{i,t}/\partial x_{i,t}$  presents a simple and practical adjustment to estimates from the static model: one could recover this adjustment factor in a separate first stage and divide  $\hat{\alpha}_{i}^{s}$  by  $\partial \bar{x}_{i,t}/\partial x_{i,t}$ . This adjustment factor approach will be used in our empirical applications to convert estimates from the static model of MWTP into ones that would have obtained using the forward-looking model.

Finally, we note that this analysis also applies to the multivariate case where x is simply treated as a vector of amenities.13

#### B. The Amenity Is Mean Reverting or Mean Diverging

We now consider changes in the amenity of interest that are not uniform across the locations of the choice set. In other words, we consider cases where amenity levels are either mean reverting or mean diverging over the T-year horizon. The simplest case of mean reversion would arise if shocks to amenity levels arrive through time and these shocks decay. More complicated cases of mean reversion would be the

<sup>&</sup>lt;sup>13</sup> Some minor notational adjustments would be required. Let  $\alpha_i$ ,  $r'(x_{i,t})$ , and  $\tilde{r}'(\bar{x}_{i,t})$  be row vectors and x be a column vector. The adjustment factor would be a (Jacobian) matrix, and equation (12) would read:  $\tilde{r}'(\bar{x}_{it}^*) =$  $r'(x_{i,t}^*)[\partial \bar{x}_{i,t}/\partial x_{i,t}]^{-1}$ .

result of targeted policy. For example, in the case of school quality, resources may be diverted to districts with the lowest performance in the prior period. An example of mean diversion would be tipping points. For example, in the case of neighborhood racial composition, neighborhoods with minority levels above some tipping point may experience more in-migration of minorities. For our purposes, however, we do not distinguish between the underlying causes of mean reversion or mean divergence.

We now consider a relationship between  $x_{it}$  and  $\bar{x}_{it}$ , which may be expressed as

$$\bar{x}(x_{i,t}) = \phi + \gamma x_{i,t}. \tag{13}$$

With  $\gamma < 1$ , the amenity will be mean-reverting: for any two choices of x, denoted  $x_a$  and  $x_b$ ,  $|\bar{x}(x_a) - \bar{x}(x_b)| < |x_a - x_b|$ . With  $\gamma > 1$ , the amenity will be mean-diverging:  $|\bar{x}(x_a) - \bar{x}(x_b)| > |x_a - x_b|$ .

Given this setup, the necessary adjustment factor to the willingness to pay from the static model is given by

$$\partial \bar{x}_{i,t}/\partial x_{i,t} = \gamma, \tag{14}$$

implying that

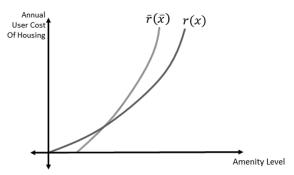
$$\tilde{r}'(\bar{x})\Big|_{\bar{x}=\bar{x}_{i,t}^*} = \frac{1}{\gamma}r'(x)\Big|_{x=x_{i,t}^*}$$
 (15)

or that the estimate derived by the static model is biased by the factor  $\gamma$ . Note that this holds for any level of the trend term,  $\phi$ , which is consistent with the discussion in section IIIA. Finally, the linearity specified in equation (13) is done solely for expositional purposes; the adjustment factor can easily be allowed to depend on  $x_{i,t}$ .

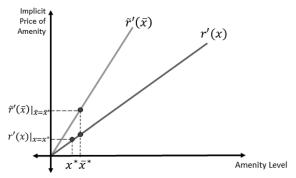
In figure 3a, we show the price functions for mean reversion of the amenity. It may be seen that the forward-looking housing price function is everywhere steeper than the one from the static model;  $\tilde{r}(\bar{x})$  is increasing at a faster rate than r(x), as each additional dollar spent on housing buys the household a smaller increase in  $\bar{x}$  than it does in x. <sup>14</sup> Correspondingly,  $\tilde{r}'(\bar{x})$  lies always above r'(x), as shown in figures 3b and 3c. In other words, the implicit price of the amenity is higher in the forward-looking model.

The bias is unambiguously toward 0 in the case of mean reversion. This is despite the fact that quantity and price effects work in opposite directions for some households in the market. Households that purchase a below-mean level of  $x_{i,t}$  will experience a level of  $\bar{x}_{i,t}$  that is greater than  $x_{i,t}$  and both the quantity and the price effects will be positive. This is shown in figure 3b. Households that purchase an above-mean level of  $x_{i,t}$  will experience a level of  $\bar{x}_{i,t}$  that is lower than  $x_{i,t}$ ; while the price effect will be positive, the

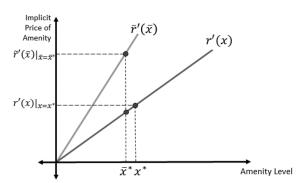
FIGURE 3.—THE AMENITY IS MEAN REVERTING THROUGH TIME



(a) The Housing Price Functions



(b) The Implicit Price Functions and Household i's MWTP Below-Mean Choice of  $x^*$ 



(c) The Implicit Price Functions and Household i's MWTP Above-Mean Choice of  $x^*$ 

quantity effect will be negative. This is shown in figure 3c.<sup>15</sup> However, the overall effect is unambiguous; as can be seen analytically in equation (15), their true willingness to pay is higher.

Analogously, when the amenity is mean diverging, the willingness to pay derived by the static model will be unambiguously biased away from 0 by the adjustment factor  $\gamma$  (as  $\gamma > 1$ ). Mean divergence results in a forward-looking price function that is everywhere flatter and a forward-looking implicit price function that is everywhere lower than in the static model.

 $<sup>^{14}</sup>$  In other words, when comparing two houses, the user-cost difference is fixed, but the user-cost difference reflects a smaller change in  $\bar{x}$  than x. Thus, the slope of  $\tilde{r}(\bar{x})$  must be larger than r(x) as the horizontal difference is smaller for the same vertical difference.

 $<sup>^{15}</sup>$  In figures 3b and 3c, we have illustrated the case where the mean of x is equal to the mean of  $\bar{x}$ . More generally, if the amenity is trending through time, mean reversion will imply that low-amenity houses will improve at a faster rate than high-amenity houses.

## C. Nonlinear Utility

In the appendix, we derive the nonlinear case in greater detail, including an empirical specification where utility is a function of  $\log(x)$ . The two key insights are as follows. First, the effects of a simply rising or falling amenity discussed in section IIIA still hold, broadly speaking: the price and quantity effects still work in opposite directions, yet they no longer exactly cancel one another out due to the nonlinearity of the utility function. (With concave utility, the static model will underestimate [overestimate] willingness to pay when the amenity is increasing [decreasing] over time.) Second, the effects of a mean-reverting or mean-diverging amenity discussed in section IIIB, still hold, broadly speaking: the static model will underestimate (overestimate) willingness to pay when the amenity is mean reverting (mean diverging) over time.

## IV. Empirical Applications

We now demonstrate the intuition laid out in sections II and III in two empirical settings. In the first application, of recovering the marginal willingness to pay to avoid violent crime, we highlight a setting with large heterogeneity in the adjustment factor. In the second application, of recovering the willingness to pay to avoid air pollution, we revisit the analysis of a major U.S. policy: the 1970 Clean Air Act Amendments.

# A. The Willingness to Pay to Avoid Crime

For this application, we begin with a data set describing housing transactions and violent crime rates for five counties located in the Bay Area of California (Alameda, Contra Costa, Marin, San Mateo, and Santa Clara) over the period 1990 to 2008. The housing transactions data were purchased from DataQuick and contain dates of sale, prices, geographical coordinates, property age, square footage, lot size, and number of rooms (in addition to a number of other variables). These transaction data are much richer than required for illustrating the concepts discussed in this paper, as they allow econometricians to follow households through time (note that this richness would be needed for the fully dynamic model). The crime statistics come from the FBI Uniform Crime Reporting Program and were accessed via the RAND California database. These data are organized by city and are measured as incidents per 100,000 residents. The data describe annual violent crime rates for 75 cities within the San Francisco metropolitan area.<sup>17</sup> In this data set, violent crime is defined as "crimes against people, including homicide, forcible rape, robbery, and aggravated assault." Crime rates are imputed for each house in our data set using an inverse-distance weighted average of the city-level crime rates using the great circle calculation.<sup>18</sup> The final sample contains 541,415 transactions used to estimate the housing price function separately by county. We then calculate household-specific estimates of MWTP for each of the 372,334 households in the sample.<sup>19</sup> Respectively, the panels in figure 4 illustrate the county-specific distributions and time series of the violent crime rate.

Employing these data to recover the parameters of the housing price function, we adopt the familiar log-linear specification, which we estimate separately for each county, k:<sup>20</sup>

$$log(r_{j,k,t}) = \theta_{0,k} + \theta_{1,k} x_{j,k,t} + \theta_{2,k} x_{j,k,t}^2 + H'_{j,k,t} \theta_{3,k} + \epsilon_{j,k,t}.$$
(16)

We follow the literature and multiply observed sales prices by 0.075 to convert to annual user costs of housing. The vector of housing attributes,  $H_{j,k,t}$ , includes property age, square footage, lot size, number of rooms, a set of dummies for year of sale, and a set of Census tract fixed effects to control for any tract-level, time-invariant unobservables that may be correlated with our measure of violent crime.<sup>21</sup> The results are as expected: housing price is decreasing at a decreasing rate in violent crimes for all five counties.<sup>22</sup>

As laid out in section III, the ratio of static and forward-looking estimates of marginal willingness to pay is solely determined by the transition process of the amenity of interest. In this application, we assume that households have rational expectations and specify the transition of violent crime as following an AR(1) process. We estimate the following equation,<sup>23</sup>

$$x_{j,k,t} = \rho_{0,k} + \rho_{1,k} x_{j,k,t-1} + \rho_{2,k} t + \varepsilon_{j,k,t}, \tag{17}$$

where k denotes county, j denotes the house and t denotes the year of sale. With this simple transition process,  $\bar{x}$  may

<sup>&</sup>lt;sup>16</sup> A well-known limitation of the linear-utility model is that the degree of uncertainty over future amenity values does not affect the current optimal choice, and, as such, risk aversion plays no role in decision making.

<sup>&</sup>lt;sup>17</sup> Figure A.1 in the appendix illustrates the location of these city centroids.

 $<sup>^{\</sup>rm 18}\,\rm This$  algorithm finds the shortest distance between any two points on the surface of a sphere.

<sup>&</sup>lt;sup>19</sup>The process of cleaning these data involves a number of cuts. In the appendix, we discuss these cuts and present summary statistics for both the housing transactions data set and the household data set in tables A.2 and A.3, respectively.

<sup>&</sup>lt;sup>20</sup> While the choice of functional form for this price function is important for correctly recovering households' MWTP, the ratio of static willingness to pay and forward-looking willingness to pay estimates is invariant to this choice, as discussed in section III. For a complete discussion of the choice of functional form in hedonic regressions, see Cropper, Deck, and McConnell (1988).

<sup>&</sup>lt;sup>21</sup> According to the Census Bureau, Census tracts are small, relatively permanent statistical subdivisions of 1,200 to 8,000 residents. See Kuminoff, Parmeter, and Pope (2010), who use Monte Carlo evidence to suggest that including spatial fixed effects is the most appropriate way to deal with omitted-variable bias from neighborhood-level unobservables.

<sup>&</sup>lt;sup>22</sup> The price-function estimates (and standard errors) for each of the five counties are reported in table A.6 in the appendix. These price functions (and associated implicit price functions) are also presented in figure A.2 in the appendix

<sup>&</sup>lt;sup>23</sup> Our results are effectively unchanged when we consider alternative specifications for the formation of expectations. Results from both an adaptive-expectations framework and an AR(2) framework, as well as a specification with an additional control amenity, are presented in table A.7 in the appendix.

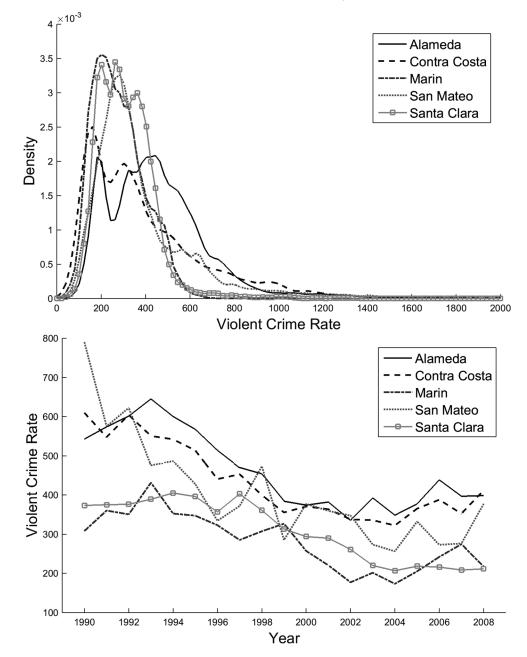


FIGURE 4.—VARIATION IN VIOLENT CRIMES PER 100,000 RESIDENTS

then be expressed as  $\bar{x}_{j,k,t} = \phi_{k,t} + \gamma_k x_{j,k,t}$  where  $\gamma_k$  is given by the weighted average,

$$\gamma_k = \frac{\sum_{s=1}^T \beta^{s-1} \rho_{1,k}^{s-1}}{\sum_{s=1}^T \beta^{s-1}},\tag{18}$$

where we set  $\beta$  to the commonly used discount factor of 0.95 and set T to seven years, which is approximately the median household tenure in the United States over our sample period. Our results are robust to each of these choices, with the obvious caveat that a very large decrease in either T or  $\beta$  would violate the intuition laid out in sections II and III, as either T = 1 or  $\beta = 0$  collapse the model into the static

framework.<sup>24</sup> To calculate standard errors, we implemented a bootstrap procedure with 1,000 draws. Standard errors for  $\hat{\gamma}$  could also be obtained using the delta method.<sup>25</sup>

Calculated according to equation (18), the county-specific estimates of the adjustment factors,  $\gamma_k$ , which determine both the size and sign of the bias, are presented in table 1.26 All

 $^{24}$  Results for  $T \in \{5,9\}$  and  $\beta \in \{0.90, 1.00\}$  are presented in table A.7 in the appendix.

<sup>25</sup> Using the delta method, the standard errors of  $\hat{\gamma}$  can be constructed as  $\partial \gamma / \partial \rho_1$  times the standard error of  $\rho_1$ , where  $\partial \gamma / \partial \rho_1 = (\sum_{s=1}^T \beta^{s-1})^{-1} \sum_{s=1}^T \beta^{s-1} (s-1) \rho_1^{s-2}$ .

 $^{26}$  The county-specific transition probability parameters for violent crime (i.e.,  $\rho_{0,k},\,\rho_{1,k}$ ), and  $\rho_{2,k}$ , are reported in table A.4 in the appendix.

TABLE 1.—COUNTY-SPECIFIC ESTIMATES OF γ

	Alameda	Contra Costa	Marin	San Mateo	Santa Clara
$\gamma_k$	0.8751	0.8313	0.5091	0.5077	0.7465
	(0.0003)	(0.0002)	(0.0009)	(0.0005)	(0.0004)

Standard errors are given in parentheses

TABLE 2.—AVERAGE ANNUAL MARGINAL WILLINGNESS TO PAY BY COUNTY

	Alameda	Contra Costa	Marin Marin	San Mateo	Santa Clara
Static	-5.60 (0.26)	-16.54 (0.19)	-16.00 (1.47)	-4.24 (0.30)	-11.61 (0.43)
Forward looking Implied bias	-6.40 (0.30) -12.49% (0.03)	-19.90 (0.22) -16.97% (0.02)	-31.42 (2.88) -49.09% (0.09)	-8.35 (0.60) -49.23% (0.05)	-15.55 (0.58) -25.35% (0.04)

Standard errors are given in parentheses.

values of  $\gamma_k$  are strictly less than 1, indicating that violent crime is mean reverting in each of the five counties.<sup>27</sup>

Using the estimates from the price function alone, we recover the static model's estimate of annual MWTP according to equation (4), that is,  $\hat{\alpha}_i^s$ , is equal to the estimated implicit price of violent crime at each household's observed level of violent crime exposure.<sup>28</sup> The sample mean of the distribution of these estimates is -\$10.66 (in year 2000 dollars) with a standard error of \$0.19. In other words, the static model implies that the average household dislikes violent crime and is willing to pay \$10.66 per year to avoid one additional crime per 100,000 local residents. This translates to an average willingness to pay of \$37.41 per year to reduce the violent crime rate by 1% at the mean level of violent crime (350.92 incidents per 100,000 residents).

The forward-looking model's estimate of annual marginal willingness to pay is recovered by adjusting each household's static estimate by the county-specific estimate of  $\gamma_k$ :  $\hat{\alpha}_i^f = \hat{\alpha}_i^s/\hat{\gamma}_k$ . This method is, by construction, equivalent to using equation (9) directly, following the discussion in section III. As all values of  $\gamma_k$  are estimated to be strictly less than 1, our forward-looking willingness-to-pay measures are larger than the static measures in absolute value. The sample mean of the distribution of these estimates is -\$14.28 with a standard error of \$0.28. That is, the average household is willing to pay \$14.28 per year to avoid one additional crime per 100,000 local residents.

This implies that the traditional static approach leads to estimates that are over 25% lower in absolute terms.<sup>29</sup>

Importantly, our county-level specification allows us to explore heterogeneity in the ratio of MWTP estimates. As can be seen in table 2, there are large differences across counties in the ratio of static to forward-looking estimates. For example, in Alameda and Contra Costa counties, the static and forward-looking models yield similar results; while crime is falling in both of those counties, there is only a small amount of mean reversion (which is the key factor driving the bias). There is, however, a substantial difference between the estimates of the static and forward-looking models in both Marin and San Mateo counties. While crime is also falling in these counties, there is a considerable amount of mean reversion in the violent crime rate.

Finally, as these are the same data used in Bishop and Murphy (2011), we are able to directly compare the results obtained using the simple adjustment factor approach derived here with the fully dynamic approach used there. As previously noted, the forward-looking model laid out in this paper is not fully dynamic, as households may not reoptimize within the T-period time horizon. The forward-looking model exogenously sets each household's probability of moving to 0 for T periods (and ends the process after that), while in the fully dynamic model, reoptimization probabilities are endogenously solved for in each period.<sup>30</sup> However, as the utility and transition-probability functions are the same in both papers, the estimates are directly comparable. Interestingly, the average forward-looking estimate of willingness to pay found here of -\$14.28 is reasonably close to the average fully dynamic estimate of willingness to pay found in Bishop and Murphy (2011) of -\$13.45.

# B. The Willingness to Pay to Avoid Air Pollution

In this application, we revisit the well-known work of Chay and Greenstone (2005) that analyzes the housing market impacts of the decrease in air pollution driven by the Clean Air Act (CAA) Amendments of 1970. The measure of air pollution is total suspended particulates (TSP), one of the primary targets of the 1970 amendments.<sup>31</sup> Using a novel instrumental-variable (IV) strategy to estimate the hedonic price function for TSP, Chay and Greenstone find a large increase in housing values over the 1970s due to the CAA-driven declines in TSP.

<sup>&</sup>lt;sup>27</sup> The corresponding values of  $\phi_{k,t}$  take the form  $\phi_{0,k} + \phi_{1,k}t$  and are shown in table A.5 in the appendix. These values imply that in each of our nineteen years of the sample, expected crime is falling over a seven-year horizon. However, as discussed in section III, this trend term will not affect how estimates from our forward-looking model will differ from those from the static model.

 $<sup>^{28}</sup>$  In less than 1% of cases,  $\theta_{1,k} + 2\theta_{2,k}x_{j,k,t} > 0$ , implying a positive value for that household's willingness to pay for crime exposure. We exclude these households from the calculation of utility parameters.

<sup>&</sup>lt;sup>29</sup> The FBI's reported violent crime rate is a commonly used statistic of high-profile crime in the United States. However, it is likely that households respond more to homicides than to the other subcomponents of the violent

crime rate. Therefore, using data describing county-level homicides for the five counties of our analysis over 1990 to 2008 (published by the California Department of Justice), we estimate an AR(1) process using the rate of homicide, which we calculate using county populations in the year 2000 (published by the U.S. Census Bureau). We find mean reversion in the homicide rate and recover an adjustment factor of  $\gamma=0.799$ , with a standard error of 0.089.

<sup>&</sup>lt;sup>30</sup> While the fully dynamic model is naturally a richer framework, solving for these endogenous reoptimization probabilities is exactly what increases the computational and data requirements.

<sup>&</sup>lt;sup>31</sup> TSP includes all particulate matter that is suspended in the air, including the more recently regulated PM10 (suspended particulates smaller than 10 microns in size) and the currently regulated PM2.5 (suspended particulates smaller than 2.5 microns in size).

This application is an ideal setting for us to revisit for two reasons. First, the approaches are quite complementary; Chay and Greenstone's (2005) key focus is to credibly estimate the price function, while our focus is to develop insights regarding the mapping of these price functions into MWTP estimates. Second, we use the quasi-experimental variation associated with Chay and Greenstone to highlight the impacts of our forward-looking framework. Chay and Greenstone's novel insight was to recognize that the CAA Amendments of 1970 generated exogenous variation in TSP concentrations that could be used to identify the price function; the 1970 Amendments subjected counties with threshold-exceeding TSP concentrations to increased regulation and deemed them to be in "nonattainment status." This designation forms the basis of Chay and Greenstone's IV: using an indicator for a county's status to instrument for its decline in TSP. Interestingly, this regulatory environment generates mean reversion in TSP concentrations, as the largest TSP declines would be seen in the counties with the highest initial concentrations.

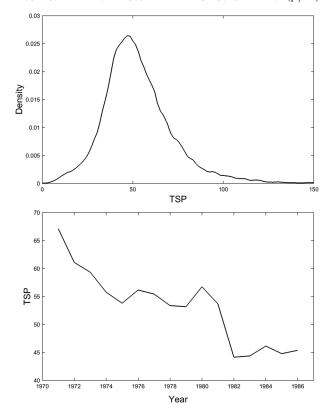
To implement our approach, we directly use the estimate of the average implicit price of TSP found in Chay and Greenstone (2005). This estimate, which describes the causal impact of TSP on the log of housing sales price, comes from an IV, first-difference approach that includes county-level controls. Chay and Greenstone find that a 1  $\mu/m^3$  (microgram per cubic meter of air) increase in TSP causes house prices to fall by 0.28% (i.e., the price of the average house falls by \$243 in 2001 dollars).

Following the discussion in section II, we convert this implicit price into one described by annual user costs of housing (versus sales prices) by multiplying it by 0.075, arriving at an annualized implicit price of -\$18.23. Thus, our static estimate of the average marginal willingness to pay is  $\hat{\alpha}^s = -\$18.23$  for a 1  $\mu/m^3$  increase in TSP.<sup>32</sup>

To estimate the transition probabilities required to form the forward-looking estimate, we use data describing county-by-year TSP concentrations from the EPA's Air Quality Monitoring System over the period 1957 to 2000. These are the same underlying EPA data from which the sample used to estimate the price function in Chay and Greenstone (2005) was created. These data are organized by air-quality monitor and report annual mean TSP concentrations for each monitor in the sample, which we aggregate to county level.<sup>33</sup>

While we have access to 44 years of data, we create a 16-year sample of 1971 to 1986. This period reflects the

FIGURE 5.—VARIATION IN COUNTY-LEVEL TSP CONCENTRATION ( $\mu/m^3$ )



post-CAA years over which TSP was the target of EPA regulation. The 1970 Amendments began implementation in 1971. Beginning in 1987, the EPA stopped using TSP as its preferred measure of particulates, and many monitors ceased to record TSP concentrations.<sup>34</sup> There is a significant downward trend in TSP concentrations over this time period. We show this time-series variation, along with the distribution of TSP, in figure 5.

We specify the transition of TSP as following an AR(1) process,

$$x_{k,t} = \rho_0 + \rho_1 x_{k,t-1} + \rho_2 t + \varepsilon_{k,t}, \tag{19}$$

where k denotes county and t denotes year.<sup>35</sup> As in our previous application, this simple transition process allows us to express  $\bar{x}$  as  $\bar{x}_{k,t} = \phi_t + \gamma x_{k,t}$ , where  $\gamma$  (the term that determines the bias) is given by the weighted average,

$$\gamma = \frac{\sum_{s=1}^{T} \beta^{s-1} \rho_1^{s-1}}{\sum_{s=1}^{T} \beta^{s-1}},\tag{20}$$

and, as before,  $\beta$  is set to 0.95 and T is set to seven years.

Our estimate of  $\gamma$  is 0.519 (with a standard error of 0.005).<sup>36</sup> This indicates a significant level of mean reversion,

 $<sup>^{32}</sup>$  By multiplying the implicit price by 0.05, Chay and Greenstone (2005) report a somewhat analogous number of 0.05  $\times$  \$243  $\approx$  \$12. Previewing the importance of calculating a forward-looking estimate, they state, "Of course, the valuation calculations for a one-unit reduction in TSPs will vary depending on the discount rate and individuals expectations on the future path of TSPs."

<sup>&</sup>lt;sup>33</sup> To arrive at this annual mean TSP concentration, the EPA takes a geometric mean of each monitor's daily TSP concentrations in a year. To aggregate to the county level, we follow Chay and Greenstone and take a weighted (arithmetic) mean over all monitors' annual means within each county. The numbers of each monitor's readings serve as weights.

<sup>&</sup>lt;sup>34</sup> See Kahn (1997) for a detailed discussion of the timeline.

<sup>&</sup>lt;sup>35</sup> We follow Chay and Greenstone (2005) and treat the United States as a national market.

 $<sup>^{36}</sup>$  This estimate is robust to alternative specifications of the formation of expectations. Specifying an AR(2) process yields an estimate of  $\gamma$  of

as would be expected given the CAA motivation. This also indicates that a large adjustment would need to be made to the static estimate of willingness to pay. In particular, we construct the forward-looking estimate of average MWTP for a 1  $\mu/m^3$  increase in TSP by dividing the static estimate of  $\hat{\alpha}^s = -\$18.23$  by  $\hat{\gamma} = 0.519$ . Thus, our forward-looking estimate of average marginal willingness to pay is  $\hat{\alpha}^f = -\$35.14$ , or almost double the static-model estimate.

To allow for the possibility that the CAA itself affected the expectation-formation process, we also estimate our model using the pre-CAA years of 1957 to 1970. Using this pre-CAA sample, the estimate of  $\gamma$  is 0.640 (with a standard error of 0.016). This estimate, which indicates a lower level of mean reversion prior to 1971, is to be expected. As carefully documented in Chay and Greenstone (2005), the CAA Amendments provided much stronger incentives for dirty counties to reduce their TSP concentrations, thus contributing to the higher levels of mean reversion post-CAA. This estimate of  $\gamma$  implies a forward-looking estimate of marginal willingness to pay of  $\hat{\alpha}^f = -\$28.48$ .

To conclude, Chay and Greenstone (2005) showed that by using credible, exogenous variation in TSP (driven by the CAA Amendments of 1970), the housing market impacts of air pollution were larger than previously thought, as existing studies recovered small and/or statistically insignificant impacts of TSP in the housing market.<sup>37</sup> We build on that conclusion by showing that due to the mean-reverting nature of the variation in TSP, the implications for household preferences would be even larger again.

# V. Conclusion

Researchers in a wide variety of applied fields have relied on Rosen's intuitive 1974 model to recover households' marginal willingness to pay for a myriad of implicitly traded goods and services. In the majority of these applications, researchers have applied the hedonic model to the housing market, recovering estimates of willingness to pay for house-and neighborhood-specific amenities. This housing market application, however, is also the one most at risk of substantially biased estimates, given the underlying assumption of free mobility in the Rosen framework. And despite many recent advances in the estimation of dynamic models, there continues to exist a substantial burden on econometricians in terms of both computation and data requirements for the estimation of a dynamic model.

In this paper, we seek to more fully describe the costs and benefits associated with estimating Rosen's familiar model. We illustrate the bias under the assumption that the true datagenerating model is forward looking using both a series of intuitive graphs and simple algebraic calculations. We then propose a systematic approach to diagnosing the sign and size of the potential bias for a given empirical application based on the time trend of the amenity of interest. We highlight the interesting result where, without reversion to (or divergence from) the average trend through time, there will be no bias (even with changing amenity levels and forwardlooking agents). Finally, we propose an adjustment factor that transforms the marginal willingness-to-pay estimate from the static model into one from the forward-looking model.

We highlight these concepts with two empirical applications. In the first, we recover households' willingness to pay to avoid violent crime in each of five counties in the Bay Area of California. We find considerable heterogeneity across counties in the rates of mean reversion of violent crime and therefore considerable heterogeneity in the bias associated with specifying the traditional, static model. In the second application, we recover households' willingness to pay to avoid air pollution. With significant mean reversion driven by the Clean Air Act Amendments of 1970, we find a large difference between the estimates of marginal willingness to pay from the static and forward-looking models. The results of both of these applications support our suggestion that it may be prudent for researchers to use a simple analysis of the time-series properties of an amenity to assess the potential benefits prior to adopting either a static or dynamic framework.

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<sup>&</sup>lt;sup>37</sup>Chay and Greenstone themselves present three conventional estimates of the housing market impacts of TSP reductions: estimates from a 1970 cross-sectional regression (small but significant results), estimates from a 1980 cross-sectional regression (counterintuitively signed but significant results), and estimates from a 1973–1980 first-difference regression with no IV (small and insignificant results).

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