

Find time complexity T(n) for the following code snippet:

```
a = 1;
b = 1;
while(b < n)
{
    a += 1;
    b += a;
    cout<<"Hi";
}
```

Solution:

<u>a</u>	<u>b</u>
1	1
2	1+1=2
3	2+2
4	2+2+3
.	.
.	.
.	.
.	.
\mathbb{Z}	2+2+3... \mathbb{Z}

$$b = \frac{z(z+1)}{2}$$

$$b < n$$

$$b \geq n \rightarrow \frac{z(z+1)}{2} \geq n$$

$$\rightarrow z^2 \geq n$$

$$\rightarrow z = \sqrt{n}$$

$$\text{Time complexity} = O(\sqrt{n})$$