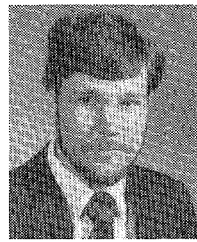




**Leon McCaughan** received the M.S. degree in physics in 1971 and the Ph.D. degree in biophysics in 1979, both from the University of Michigan, Ann Arbor.

From 1979 to 1980 he held a joint postdoctoral appointment with Brookhaven National Laboratory, Upton, NY, and the University of Michigan. His thesis and postdoctoral work investigated X-ray and neutron diffraction from membranes. In June 1980 he joined Bell Laboratories, Allentown, PA, where he has been engaged in the research and development of electrooptic devices.



**Edmond J. Murphy** was born in Cambridge, MA, on January 3, 1955. He received the B.S. degree in chemistry from Boston College, Boston, MA, in 1976 and the Ph.D. degree in chemical physics from the Massachusetts Institute of Technology, Cambridge, MA, in 1980.

He joined Bell Laboratories, Allentown, PA, in 1980 where he has been involved in research and development on optical guided wave device and fabrication technology.

Dr. Murphy is a member of the Optical Society of America.

# Transmission Characteristics of Dielectric-Coated Metallic Waveguide for Infrared Transmission: Slab Waveguide Model

MITSUNOBU MIYAGI, AKIHITO HONGO, AND SHOJIRO KAWAKAMI, MEMBER, IEEE

**Abstract**—A metallic hollow waveguide with inner dielectric multilayers is proposed for the transmission of infrared light and its basic transmission characteristics are fully analyzed by using a two-dimensional slab waveguide model. The power loss in the waveguide is shown to be extremely reduced by coating dielectric layers properly. Simple loss formulas are also presented which consider absorptions of dielectric materials, and minimum possible losses are theoretically estimated. Finally, relations to bending losses in the waveguide are discussed.

## I. INTRODUCTION

DEVELOPMENT of low-loss flexible waveguides is of great concern for high-powered  $\text{CO}_2$  lasers in various applications such as welding, cutting, heat-treating, and laser surgery [1]. There are two types of waveguides which have been proposed or fabricated so far to transmit infrared light. One is a solid-core waveguide, i.e., so-called fiber. Since the first paper appeared which shows that polycrystalline KRS-5 fibers can be fabricated by the extrusion technique with transmission losses of around 0.5 dB/m at  $10.6 \mu\text{m}$  [2], there has been increasing interest in infrared transmissive fibers [3]–[13]. Another is a hollow-core waveguide such as leaky waveguides [14], [15] or metallic (or lossy dielectric) hollow waveguides [16]–[26] whose basic properties were analyzed by Marcatili and Schmeltzer [27]. From the viewpoint of the transmission of a high-powered  $\text{CO}_2$  laser, metallic or lossy dielectric waveguides seem to be the most likely candidates among waveguides thus far proposed.

Manuscript received June 24, 1982; revised September 10, 1982.

The authors are with the Research Institute of Electrical Communication, Tohoku University, Sendai, Japan.

In this paper, we propose a metallic hollow waveguide with inner dielectric multilayers to obtain sufficiently low transmission losses. As far as a metallic waveguide with a single inner dielectric layer is concerned, transmission characteristics have been analyzed for the millimeter or submillimeter wavelengths in the late 1950's and more recently [28]–[32] for the transmission of  $\text{TE}_{0m}$  modes. Basic analyses must be done for the infrared because metals are properly characterized by a complex refractive index in the infrared rather than by a large conductivity. Furthermore, we are interested in the transmission of  $\text{HE}_{1m}$  modes not  $\text{TE}_{0m}$  modes in a circular waveguide and their basic transmission properties are able to be understood by analyzing those of modes in two-dimensional slab waveguides. On the other hand, Yeh *et al.* [33], [34] have done extensive analyses on a hollow-core waveguide with periodic dielectric layers which is called Bragg fiber. However, to realize low-loss waveguides with a finite number of dielectric layers, metallic waveguides seem to be preferable because large reflection is expected at the surface of a metal.

In Section II, we present a general theory for attenuation constants of the TE and TM modes in a two-dimensional slab waveguide by use of the idea of a surface impedance or admittance.

In Section III, transmission losses in a waveguide with a single inner dielectric layer are discussed for various kinds of metals. It is shown that the attenuation constant of the TM mode can be reduced significantly for suitable choice of the width of the dielectric layer. In order to reduce the attenuation constant of the TE or TM mode drastically, we propose a waveguide with inner dielectric multilayers in Section IV.

The effect of the absorption losses of dielectric materials are fully discussed and simple loss formulas are also presented.

## II. GENERAL EXPRESSION FOR ATTENUATION CONSTANT IN 2-D HOLLOW WAVEGUIDE

Consider a two-dimensional symmetric slab waveguide uniform along the  $y$  and  $z$  axes with a hollow-core width  $2T$ . The electric field  $E_y$  of the  $TE_p$  mode propagating along the  $z$  axis is expressed by

$$E_y = \cos\left(\frac{u}{T}x - \frac{p\pi}{2}\right)e^{-j\beta z} \quad (1)$$

in  $|x| < T$ .  $\beta$  and  $u/T$  are the axial and transverse phase constants related via

$$\beta^2 + \left(\frac{u}{T}\right)^2 = (n_0 k_0)^2 \quad (2)$$

where  $n_0$  ( $\simeq 1$ ) is a refractive index in  $|x| < T$ .

Introducing the normalized surface impedance  $z_{TE}$  defined by

$$\left(\frac{E_y}{H_z}\right)_{x=T} = \frac{\omega\mu_0}{n_0 k_0} z_{TE} \quad (3)$$

one obtains the characteristic equation to determine  $u$  as

$$u \tan\left(u - \frac{p\pi}{2}\right) = j \frac{n_0 k_0 T}{z_{TE}}. \quad (4)$$

By dividing  $u$  into real and imaginary parts as

$$u = u_0 + ju_i \quad (5)$$

and assuming that  $u_i$  is much smaller than  $u_0$ , one obtains from (4)

$$u_0 \tan\left(u_0 - \frac{p\pi}{2}\right) = -\text{Im}\left(\frac{n_0 k_0 T}{z_{TE}}\right) + \text{Re}\left(\frac{n_0 k_0 T}{z_{TE}}\right) \cdot u_i \tan\left(u_0 - \frac{p\pi}{2}\right), \quad (6)$$

$$u_i \left[ u_0 + \tan\left(u_0 - \frac{p\pi}{2}\right) \right] = \text{Re}\left(\frac{n_0 k_0 T}{z_{TE}}\right) + \text{Im}\left(\frac{n_0 k_0 T}{z_{TE}}\right) \cdot u_i \tan\left(u_0 - \frac{p\pi}{2}\right) \quad (7)$$

where higher order terms than  $u_i^2$  are neglected.

By eliminating  $\tan(u_0 - p\pi/2)$  in (6) and (7) and neglecting small terms of  $u_i^2$ , one obtains

$$u_i = \frac{z_0 \text{Re}(z_{TE})}{|z_{TE}|^2 + [1 + \text{Im}(z_{TE})/n_0 k_0 T] z_0^2} \quad (8)$$

where

$$z_0 = \frac{n_0 k_0 T}{u_0} \quad (9)$$

and the unknown quantity  $u_0$  is determined by the following transcendental equation:

$$\left[ \left| \frac{z_{TE}}{n_0 k_0 T} \right|^2 + \text{Im}\left(\frac{z_{TE}}{n_0 k_0 T}\right) \right] \tan^2\left(u_0 - \frac{p\pi}{2}\right) + u_0 \left[ \left| \frac{z_{TE}}{n_0 k_0 T} \right|^2 - \frac{1}{u_0^2} \text{Im}\left(\frac{z_{TE}}{n_0 k_0 T}\right) - \frac{1}{u_0^2} \right] \cdot \tan\left(u_0 - \frac{p\pi}{2}\right) - \text{Im}\left(\frac{z_{TE}}{n_0 k_0 T}\right) = 0 \quad (10)$$

which is obtained from (6) and (7) by elimination of  $u_i$ .

Therefore, the attenuation constant  $\alpha^{TE}$  of the mode, which is obtained from (2) as

$$\alpha^{TE} = \frac{u_0 u_i}{n_0 k_0 T^2} \quad (11)$$

is expressed by

$$\alpha^{TE} = \frac{1}{T} \frac{\text{Re}(z_{TE})}{|z_{TE}|^2 + [1 + \text{Im}(z_{TE})/n_0 k_0 T] z_0^2} \quad (12)$$

where it is assumed that  $n_0 k_0 T \gg 1$  and, therefore,  $\text{Re}(\beta) \simeq n_0 k_0$  in (11).

For the TM modes, introducing the normalized surface admittance  $y_{TM}$  defined by

$$\left(\frac{H_y}{E_z}\right)_{x=T} = -\frac{n_0 k_0}{\omega\mu_0} y_{TM} \quad (13)$$

one can similarly express the attenuation constant  $\alpha^{TM}$  as follows:

$$\alpha^{TM} = \frac{1}{T} \frac{\text{Re}(y_{TM})}{|y_{TM}|^2 + [1 + \text{Im}(y_{TM})/n_0 k_0 T] y_0^2} \quad (14)$$

$$y_0 = \frac{n_0 k_0 T}{u_0} \quad (15)$$

where  $u_0$  is determined by (10) where  $z_{TE}$  is replaced by  $y_{TM}$ . One should note that (12) and (14) take an alternative form for low-loss waveguides of

$$\alpha^{TE} \left\{ \begin{array}{l} = \frac{u_0}{4n_0 k_0 T^2} \frac{1-R}{1 + \sin(2u_0 - p\pi)/2u_0} \\ \alpha^{TM} \end{array} \right. \quad (16)$$

where  $R$  is defined by

$$R = \begin{cases} \left| \frac{z_{TE} - z_0}{z_{TE} + z_0} \right|^2; & \text{TE modes} \\ \left| \frac{y_{TM} - y_0}{y_{TM} + y_0} \right|^2; & \text{TM modes.} \end{cases} \quad (17)$$

Equation (16) is able to be directly deduced from (4) for TE modes and from the corresponding equation for TM modes; details will be mentioned elsewhere [35]. It is seen that low-loss waveguides can be realized either when  $|z_{TE}|/z_0$  ( $|y_{TM}|/y_0$ ) is much larger or smaller than unity.

When  $|z_{TE}|/z_0$  or  $|y_{TM}|/y_0$  is sufficiently small, one easily obtains

$$u_0 \simeq \frac{p+1}{2} \pi \quad (p=0, 1, 2, \dots) \quad (18)$$

and then

$$\begin{Bmatrix} \alpha^{\text{TE}} \\ \alpha^{\text{TM}} \end{Bmatrix} = n_0 k_0 \frac{u_0^2}{(n_0 k_0 T)^3} \text{Re} \left\{ \begin{Bmatrix} z_{\text{TE}} \\ y_{\text{TM}} \end{Bmatrix} \right\}. \quad (19)$$

The attenuation constant of the  $\text{TE}_p$  or  $\text{TM}_p$  mode is proportional to  $(p+1)^2$  if no media exist in  $|x| > T$  with the refractive index  $n_0$ .

On the other hand, when  $|z_{\text{TE}}|/z_0$  or  $|y_{\text{TM}}|/y_0$  is sufficiently large, one has

$$u_0 \simeq \frac{p\pi}{2} \quad (p = 0, 1, 2, \dots) \quad (20)$$

and then

$$\begin{Bmatrix} \alpha^{\text{TE}} \\ \alpha^{\text{TM}} \end{Bmatrix} = \left( 1 - \frac{1}{2} \delta_{p0} \right) \frac{1}{T} \text{Re} \left\{ \begin{Bmatrix} z_{\text{TE}}^{-1} \\ y_{\text{TM}}^{-1} \end{Bmatrix} \right\} \quad (21)$$

which shows that the attenuation constants of all modes do not depend on the mode number  $p$  except for that of the  $\text{TE}_0$  or  $\text{TM}_0$  mode.

### III. ATTENUATION CONSTANT IN 2-D METALLIC HOLLOW WAVEGUIDE WITH SINGLE INNER DIELECTRIC LAYER

In order to understand basic properties of a metallic hollow waveguide with inner dielectric multilayers, we first consider

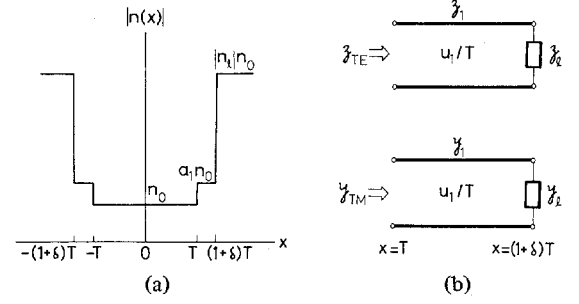


Fig. 1 (a) Refractive index profile of a metallic hollow waveguide with a single dielectric layer in the two-dimensional slab waveguide. (b) Transverse transmission line model corresponding to the waveguide where  $u_1/T$  and  $z_1(y_1)$  are transverse phase constant and normalized impedance (admittance) in  $T < X < (1+\delta)T$ , respectively, and  $z_l(y_l)$  is the normalized impedance (admittance) of the metal.

$$z_1 = \frac{n_0 k_0 T}{u_1} \simeq (a_1^2 - 1)^{-1/2}, \quad (24)$$

$$z_l \simeq (n_l^2 - 1)^{-1/2}, \quad (25)$$

$$y_1 = a_1^2 \frac{n_0 k_0 T}{u_1} \simeq a_1^2 (a_1^2 - 1)^{-1/2}, \quad (26)$$

$$y_l \simeq n_l^2 (n_l^2 - 1)^{-1/2}. \quad (27)$$

Therefore, one can express  $z_{\text{TE}}$  and  $y_{\text{TM}}$  as follows:

$$\begin{aligned} z_{\text{TE}} &= z_1 \frac{z_l + jz_1 \tan(\delta u_1)}{z_1 + jz_l \tan(\delta u_1)} \\ &= (a_1^2 - 1)^{-1/2} \frac{(n_l^2 - 1)^{-1/2} + j(a_1^2 - 1)^{-1/2} \tan[\delta(a_1^2 - 1)^{1/2} n_0 k_0 T]}{(a_1^2 - 1)^{-1/2} + j(n_l^2 - 1)^{-1/2} \tan[\delta(a_1^2 - 1)^{1/2} n_0 k_0 T]}, \end{aligned} \quad (28)$$

$$\begin{aligned} y_{\text{TM}} &= y_1 \frac{y_l + jy_1 \tan(\delta u_1)}{y_1 + jy_l \tan(\delta u_1)} \\ &= a_1^2 (a_1^2 - 1)^{-1/2} \frac{n_l^2 (n_l^2 - 1)^{-1/2} + ja_1^2 (a_1^2 - 1)^{-1/2} \tan[\delta(a_1^2 - 1)^{1/2} n_0 k_0 T]}{a_1^2 (a_1^2 - 1)^{-1/2} + jn_l^2 (n_l^2 - 1)^{-1/2} \tan[\delta(a_1^2 - 1)^{1/2} n_0 k_0 T]}. \end{aligned} \quad (29)$$

a metallic waveguide with a single dielectric layer whose refractive index profile  $n(x)$  is expressed by

$$n(x) = \begin{cases} n_0; & |x| < T \\ a_1 n_0; & T < |x| < (1+\delta)T \\ n_l n_0 = (n - j\kappa) n_0; & |x| > (1+\delta)T. \end{cases} \quad (22)$$

For the determination of  $z_{\text{TE}}$  or  $y_{\text{TM}}$ , one can use the transverse transmission line model [14], [36] schematically shown in Fig. 1 corresponding to the refractive index profile  $n(x)$ , where the transverse phase constant  $u_1/T$  in  $T < |x| < (1+\delta)T$  is approximated by use of the assumption  $n_0 k_0 T \gg u_0$  as

$$\frac{u_1}{T} \simeq (a_1^2 - 1)^{1/2} n_0 k_0 \quad (23)$$

and normalized impedance  $z_1$ ,  $z_l$  and admittance  $y_1$ ,  $y_l$  are given by

Values of the normalized impedance or admittance are listed in Tables I and II for various metals and transparent dielectrics at  $10.6 \mu\text{m}$ . Generally speaking, the normalized impedance of most metals is very small, whereas the normalized admittance is large in magnitude. For infrared waveguides, we have always  $n_0 k_0 T \gg 1$  and, therefore,  $|z_l| \ll n_0 k_0 T$ . However,  $|y_l|$  is not far from  $n_0 k_0 T$  in magnitude although it is less than  $n_0 k_0 T$ . One should notice that in microwave regions  $|y_l| \gg n_0 k_0 T$  is satisfied because  $\kappa$  is extremely large.

In order to realize low-loss infrared waveguides with a single dielectric layer, we have to design the waveguide such that

$$|z_{\text{TE}}| \ll z_0 \quad (30)$$

or

$$|y_{\text{TM}}| \ll y_0 \quad (31)$$

by suitable choice of a width of the dielectric layer. In these cases, by substituting (28) and (29) into (19) and making some

TABLE I  
COMPLEX REFRACTIVE INDEXES OF VARIOUS MATERIALS AT  
 $\lambda = 10.6 \mu\text{m}$  DEDUCED FROM THE DATA [37] BY INTERPOLATION.  
NORMALIZED IMPEDANCE AND ADMITTANCE ARE ALSO SUMMARIZED

Material	$n = n - j\kappa$		Normalized impedance $\frac{1}{(n^2 - 1)^{1/2}}$	Normalized admittance $\frac{n^2}{(n^2 - 1)^{1/2}}$
	n	$\kappa$		
Al	20.5	58.6	$5.32 \times 10^{-3} + j1.52 \times 10^{-2}$	20.5-j58.6
Ag	13.4	75.2	$2.30 \times 10^{-3} + j1.29 \times 10^{-2}$	13.4-j75.2
Au	17.1	56.0	$4.99 \times 10^{-3} + j1.63 \times 10^{-2}$	17.1-j56.0
Cu	14.1	64.5	$3.23 \times 10^{-3} + j1.48 \times 10^{-2}$	14.1-j64.5
Sn	17.4	43.5	$7.92 \times 10^{-3} + j1.98 \times 10^{-2}$	17.4-j43.5
Zn	15.6	48.5	$6.01 \times 10^{-3} + j1.87 \times 10^{-2}$	15.6-j48.5

TABLE II  
FIGURES OF MERIT FOR VARIOUS DIELECTRIC-COATED METALLIC WAVEGUIDES  
AT  $\lambda = 10.6 \mu\text{m}$ . THE PARAMETER  $A$  IS ALSO SHOWN FOR METALS  
DESCRIBING THE WAVELENGTH DEPENDENCE OF THE FIGURE OF MERIT  $F$

Dielectrics	Mode	Normalized impedance or admittance	Metal			
			Al	Ag	Au	Cu
Ge ( $a_1 = 4.0$ )	TE	.258	$3.89 \times 10^{-5}$	$2.57 \times 10^{-3}$	$4.38 \times 10^{-3}$	$3.44 \times 10^{-3}$
	TM	4.131	$2.26 \times 10^2$	$3.42 \times 10^2$	$2.01 \times 10^2$	$2.55 \times 10^2$
ZnSe ( $a_1 = 2.4$ )	TE	.458	$1.24 \times 10^{-3}$	$8.16 \times 10^{-4}$	$1.39 \times 10^{-3}$	$1.09 \times 10^{-3}$
	TM	2.640	$5.53 \times 10^2$	$8.37 \times 10^2$	$4.92 \times 10^2$	$6.25 \times 10^2$
KCl ( $a_1 = 1.47$ )	TE	.928	$3.01 \times 10^{-4}$	$1.99 \times 10^{-4}$	$3.39 \times 10^{-4}$	$2.66 \times 10^{-4}$
	TM	2.006	$9.58 \times 10^2$	$1.45 \times 10^3$	$8.52 \times 10^2$	$1.08 \times 10^3$
KRS-5 ( $a_1 = 2.37$ )	TE	.465	$1.20 \times 10^{-3}$	$7.91 \times 10^{-4}$	$1.35 \times 10^{-3}$	$1.06 \times 10^{-3}$
	TM	2.614	$5.64 \times 10^2$	$8.54 \times 10^2$	$5.02 \times 10^2$	$6.38 \times 10^2$
Parameter A of Eq. (41)			0.09	0.12	0.17	0.16

simplification by use of the condition  $n^2 + \kappa^2 \gg a_1^2$  and  $\kappa \gg$  and  $\alpha_{\text{metal}}^{\text{TE}}$  and  $\alpha_{\text{metal}}^{\text{TM}}$  are attenuation constants of the TE and  $n$ , we finally express  $\alpha^{\text{TE}}$  and  $\alpha^{\text{TM}}$  as follows:

$$\alpha^{\text{TE}} = \frac{2}{1 + \frac{a_1^2 - 1}{n^2 + \kappa^2}} \cdot \frac{\alpha_{\text{metal}}^{\text{TE}}}{1 - \left[ 1 - \frac{4(a_1^2 - 1)n^2}{(n^2 + \kappa^2)^2} \right]^{1/2} \sin [2\delta(a_1^2 - 1)^{1/2} n_0 k_0 T - \psi_{\text{TE}}]} \quad (32)$$

$$\alpha^{\text{TM}} = \frac{2}{1 + \frac{a_1^2 - 1}{a_1^4} (n^2 + \kappa^2)} \cdot \frac{\alpha_{\text{metal}}^{\text{TM}}}{1 + \left[ 1 - \frac{4a_1^4}{a_1^2 - 1} \frac{n^2}{(n^2 + \kappa^2)^2} \right]^{1/2} \sin [2\delta(a_1^2 - 1)^{1/2} n_0 k_0 T - \psi_{\text{TM}}]} \quad (33)$$

where  $\psi_{\text{TE}}$  and  $\psi_{\text{TM}}$  are defined by

$$\psi_{\text{TE}} = \tan^{-1} \left[ \frac{n^2 + \kappa^2}{2(a_1^2 - 1)^{1/2} \kappa} \right] \approx \frac{\pi}{2} \quad (34)$$

$$\psi_{\text{TM}} = \tan^{-1} \left[ \frac{(a_1^2 - 1)^{1/2} n^2 + \kappa^2}{2a_1^2 \kappa} \right] \approx \frac{\pi}{2} \quad (35)$$

TM modes in the metallic waveguides without a dielectric layer expressed by

$$\left. \begin{array}{l} \alpha_{\text{metal}}^{\text{TE}} \\ \alpha_{\text{metal}}^{\text{TM}} \end{array} \right\} = n_0 k_0 \frac{u_0^2}{(n_0 k_0 T)^3} \times \left\{ \frac{n}{n^2 + \kappa^2}, \frac{n}{n} \right\} \quad (36)$$

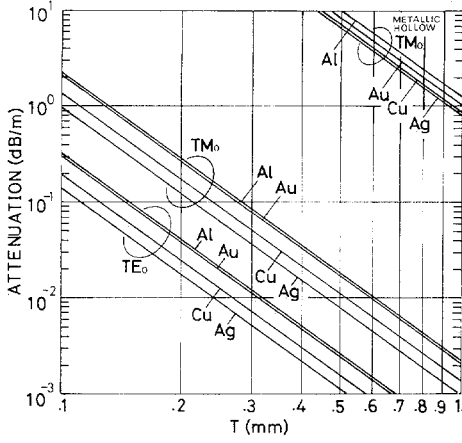


Fig. 2. Minimum power losses of the TE<sub>0</sub> and TM<sub>0</sub> modes in various waveguides with an inner zinc selenide ( $a_1 = 2.4$ ) layer at  $\lambda = 10.6 \mu\text{m}$ . Power losses of the TE<sub>0</sub> and TM<sub>0</sub> modes in the waveguides without a dielectric layer are also shown, where power losses of the TE<sub>0</sub> mode cannot be distinguished from those in the dielectric-coated metallic waveguides in the figure.

In the derivation of (32)–(36), we have assumed  $n^2 + \kappa^2 \gg a_1^2$ , which is almost satisfied for most of the metals and transparent dielectrics around  $10.6 \mu\text{m}$ .

As seen from (32) and (33), the attenuation constants of the modes have minimum when

$$\delta(a_1^2 - 1)^{1/2} n_0 k_0 T = \begin{cases} q\pi, & q = 0, 1, 2, \dots; \text{ TE modes} \\ (q + \frac{1}{2})\pi, & q = 0, 1, 2, \dots; \text{ TM modes} \end{cases} \quad (37)$$

and their minimum values  $\alpha_{\min}$  are approximated by

$$\alpha_{\min} = n_0 k_0 \frac{u_0^2}{(n_0 k_0 T)^3} \frac{n}{n^2 + \kappa^2} \times \begin{cases} \frac{1}{1 + \frac{a_1^2 - 1}{n^2 + \kappa^2}}; & \text{TE modes} \\ \frac{a_1^4}{a_1^2 - 1} \frac{1}{1 + \frac{a_1^4}{a_1^2 - 1} \frac{1}{n^2 + \kappa^2}}; & \text{TM modes.} \end{cases} \quad (38)$$

Fig. 2 shows minimum power losses of the TE<sub>0</sub> and TM<sub>0</sub> modes in various metal waveguides with a single dielectric (ZnSe) layer. The power losses in the waveguides without a dielectric layer are also shown. One can see that the power losses in the waveguides are reduced by two or three orders of magnitude for TM modes, whereas appreciable loss reduction cannot be expected for the TE mode by coating a single dielectric layer. This does not depend on the width of the dielectric layer as far as (37) is satisfied. However, the wavelength dependence of the power losses varies with the width and relatively thinner dielectric layer, i.e., smaller  $q$  in (37) is preferable to have broad wavelength dependence of the power losses as shown in Fig. 3.

In order to see the effect of coating in more detail, we introduce a figure of merit defined by

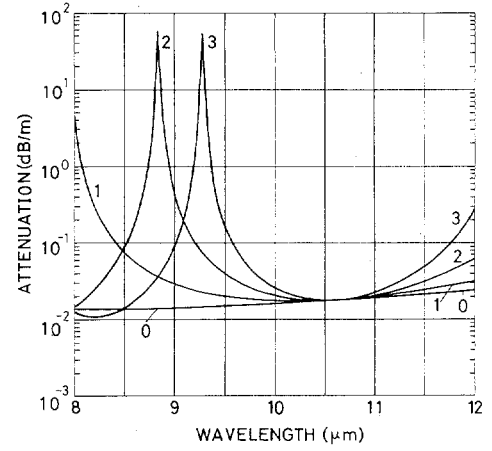


Fig. 3. Wavelength dependence of the power loss of the TM<sub>0</sub> mode in the aluminum waveguide with an inner zinc selenide layer, where  $T = 500 \mu\text{m}$  and it is assumed that  $n_1 = 20.5 - j58.6$  and  $a_1 = 2.4$  are constant over the wavelengths. The number on each curve represents  $q$  in (37).

$$\alpha_{\min} = \frac{\alpha_{\text{metal}}}{1 + F} \quad (39)$$

which leads to

$$F = \begin{cases} \frac{a_1^2 - 1}{n^2 + \kappa^2}; & \text{TE modes} \\ \frac{a_1^2 - 1}{a_1^4} (n^2 + \kappa^2); & \text{TM modes.} \end{cases} \quad (40)$$

One should note that the figure of merit does not depend on the core width, thickness of the dielectric layer, and the mode number  $p$ . Typical examples of the figures of merit at  $10.6 \mu\text{m}$  are summarized in Table II for various waveguides. One can see that large figures of merit are obtained for the TM modes. Especially, the optimum value of the refractive index  $a_1$  is  $2^{1/2}$  for the TM modes.

As the refractive indexes of most transparent dielectrics do not depend much on the wavelength, wavelength dependence of the figure of merit is mainly determined by  $n^2 + \kappa^2$  of metals. By using data deduced from [37], one can reasonably approximate  $F$  as

$$F/F_{10.6} = \begin{cases} [1 + A(\lambda - 10.6)]^{-1}; & \text{TE modes} \\ [1 + A(\lambda - 10.6)]; & \text{TM modes} \end{cases} \quad (41)$$

where  $F_{10.6}$  is the figure of merit at  $\lambda = 10.6 \mu\text{m}$  and  $A$  is around 0.1–0.2, as summarized in Table II, which shows that  $F$  is relatively insensitive to the wavelength.

We finally mention a metal as a waveguide constituent. Power losses of the TE or TM modes are approximately determined

by only one parameter  $n/(n^2 + \kappa^2)$  for metals as seen in (38). Although this parameter depends on a particular metal, the loss reduction rate of the TM modes is very large and it is not essential to select the metal as the waveguide constituent from the viewpoint of transmission characteristics.

#### IV. ATTENUATION CONSTANT IN 2-D HOLLOW WAVEGUIDE WITH MULTIPLE INNER DIELECTRIC LAYERS

In the analyses in Section III, we found that the transmission losses of the TE modes in the metallic hollow waveguide cannot be reduced significantly by coating a single inner dielectric layer. In this section, we shall consider a waveguide which reduces the attenuation constant of the TE or TM mode drastically. A basic idea to have low-loss waveguide is to reduce or increase  $|z_{TE}|/z_0$  or  $|y_{TM}|/y_0$  compared with unity as seen in (16) and (17). We propose a metallic hollow waveguide coated by two kinds of dielectrics as shown in Fig. 4, where the thickness of dielectric layers  $\delta_i T$  ( $i = 1, 2$ ) and that of dielectric layer  $\delta T$  adjacent to the metal are chosen such that

$$\delta_i T = \frac{\pi}{2} \frac{1}{(a_i^2 - 1)^{1/2} n_0 k_0} \quad (i = 1, 2) \quad (42)$$

$$\delta T = \frac{\pi}{2} \frac{1}{(a_1^2 - 1)^{1/2} n_0 k_0} \times \begin{cases} 2; & \text{TE modes} \\ 1; & \text{TM modes.} \end{cases} \quad (43)$$

The corresponding transverse transmission line model is shown in Fig. 5, where

$$u_i/T = (a_i^2 - 1)^{1/2} n_0 k_0 \quad (i = 1, 2) \quad (44)$$

$$z_i = (a_i^2 - 1)^{-1/2} \quad (i = 1, 2) \quad (45)$$

$$y_i = a_i^2 (a_i^2 - 1)^{-1/2} \quad (i = 1, 2). \quad (46)$$

We first assume that dielectric materials are free from absorptions, i.e.,  $a_i$  ( $i = 1, 2$ ) are real quantities. It is easily found that

$$\alpha_0^{\text{TE}} = \frac{n_0 k_0 u_0^2}{(n_0 k_0 T)^3} \frac{n}{n^2 + \kappa^2} \frac{C^m}{1 + \frac{\kappa}{(n^2 + \kappa^2) n_0 k_0 T} C^m + \frac{u_0^2}{(n^2 + \kappa^2) (n_0 k_0 T)^2} C^{2m}} \quad (51)$$

$$\alpha_0^{\text{TM}} = \frac{a_1^4}{a_1^2 - 1} \frac{n_0 k_0 u_0^2}{(n_0 k_0 T)^3} \frac{n}{n^2 + \kappa^2} \frac{D^m}{1 + \frac{a_1^4}{a_1^2 - 1} \frac{\kappa}{(n^2 + \kappa^2) n_0 k_0 T} D^m + \frac{a_1^8}{(a_1^2 - 1)^2 (n^2 + \kappa^2) (n_0 k_0 T)^2} D^{2m}} \quad (52)$$

$$\begin{aligned} z_{TE} &= (n_1^2 - 1)^{-1/2} C^m \\ &\simeq \frac{n + j\kappa}{n^2 + \kappa^2} C^m \end{aligned} \quad (47)$$

$$\begin{aligned} y_{TM} &= \frac{a_1^4}{a_1^2 - 1} \frac{(n_1^2 - 1)^{1/2}}{n_1^2} D^m \\ &\simeq \frac{a_1^4}{a_1^2 - 1} \frac{n + j\kappa}{n^2 + \kappa^2} D^m \end{aligned} \quad (48)$$

where  $C$  and  $D$  are defined by

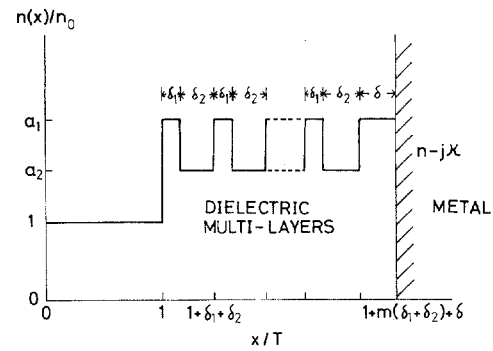


Fig. 4. Refractive index profile of a symmetric 2-D hollow waveguide with multiple inner dielectric layers. The thickness of the material with a refractive index of  $a_1 n_0$  or  $a_2 n_0$  is  $\delta_1 T$  or  $\delta_2 T$  defined by (42) except for the nearest layer to the metal with  $a_1 n_0$  of  $\delta T$  defined by (43).

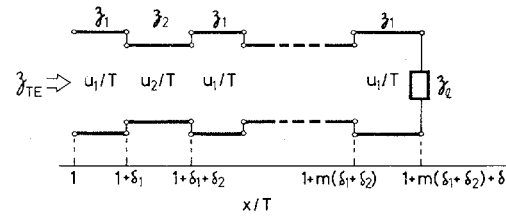


Fig. 5. Transverse transmission line model for the TE modes corresponding to the waveguide whose refractive index profile is shown in Fig. 4. For the TM modes, one simply replaces  $z$  by  $y$ .

$$C = \frac{a_2^2 - 1}{a_1^2 - 1} \quad (49)$$

$$D = \frac{a_1^4 a_2^2 - 1}{a_2^4 a_1^2 - 1}. \quad (50)$$

By substituting (47) and (48) into (12) and (14), one can express the attenuation constants of the TE and TM modes, designated by  $\alpha_0^{\text{TE}}$  and  $\alpha_0^{\text{TM}}$ , as follows:

It is clear that low-loss waveguides can be obtained either when  $C < 1$  ( $D < 1$ ) or  $C > 1$  ( $D > 1$ ). However, it is preferable to choose  $C < 1$  for TE modes and  $D < 1$  for TM modes. For, as  $n_0 k_0 T$  is large, considerable layers are required for the third terms in the denominators of (51) and (52) to predominate. Therefore, we hereafter consider the waveguides with  $C < 1$  for TE modes and  $D < 1$  for TM modes. In these cases, (51) and (52) are simplified as

$$\left. \begin{aligned} \alpha_0^{\text{TE}} \\ \alpha_0^{\text{TM}} \end{aligned} \right\} = \frac{n_0 k_0 u_0^2}{(n_0 k_0 T)^3} \frac{n}{n^2 + \kappa^2} \times \begin{cases} C^m \\ \frac{a_1^4}{a_1^2 - 1} D^m \end{cases} \quad (53)$$

for any  $m$ , where  $u_0$  is defined by (18). One should notice that a considerable amount of the loss reduction is expected by large number  $m$ . However, at the same time for larger  $m$ , one has to take absorptions of the dielectric materials into account.

Let the complex refractive indexes of dielectric materials be  $(a_i - ja'_i) n_0$  ( $i = 1, 2$ ). The corresponding transverse transmission line is simply obtained by replacing  $u_i/T$ ,  $z_i$ , and  $y_i$  by

$$\frac{u_i}{T} \rightarrow \frac{u_i}{T} \left( 1 - j \frac{a_i a'_i}{a_i^2 - 1} \right) \quad (54)$$

$$z_i \rightarrow z_i \left( 1 + j \frac{a_i a'_i}{a_i^2 - 1} \right) \quad (55)$$

$$y_i \rightarrow y_i \left( 1 - j \frac{a_i^2 - 2}{a_i^2 - 1} \frac{a'_i}{a_i} \right) \quad (56)$$

in (44)–(46).

By using the conditions of (42) and (43) and neglecting higher order terms of  $a_i'^2$  ( $i = 1, 2$ ) and  $(n^2 + \kappa^2)^{-2}$ , one can express  $z_{TE}$  and  $y_{TM}$  after rather complicated calculations as

$$z_{TE} = \frac{n + j\kappa}{n^2 + \kappa^2} C^m (1 + \epsilon_{TE}) \quad (57)$$

$$y_{TM} = \frac{a_1^4}{a_1^2 - 1} \frac{n + j\kappa}{n^2 + \kappa^2} D^m (1 + \epsilon_{TM}) \quad (58)$$

where  $\epsilon_{TE}$  and  $\epsilon_{TM}$  are defined by

$$\epsilon_{TE} = \frac{\pi}{2} (n - j\kappa) \left\{ \left[ \frac{a_1 a'_1}{(a_1^2 - 1)^{1/2}} + \frac{a_2 a'_2}{(a_2^2 - 1)^{1/2}} \right] \cdot \frac{1}{a_2^2 - 1} \frac{C^{-m} - 1}{C^{-1} - 1} + \frac{2a_1 a'_1}{(a_1^2 - 1)^{3/2}} \right\} \quad (59)$$

$$\epsilon_{TM} = \frac{\pi}{2} (n - j\kappa) \left\{ \left[ \frac{a'_1}{a_1(a_1^2 - 1)^{1/2}} + \frac{a'_2}{a_2(a_2^2 - 1)^{1/2}} \right] \cdot D^{-1} \frac{D^{-m} - 1}{D^{-1} - 1} + \frac{a'_1}{a_1(a_1^2 - 1)^{1/2}} \right\}. \quad (60)$$

Therefore, the attenuation constants  $\alpha^{TE}$  and  $\alpha^{TM}$  of the TE and TM modes are expressed by

$$\alpha^{TE}/\alpha_0^{TE} = 1 + \frac{n^2 + \kappa^2}{n} \frac{\pi}{2} \left\{ \left[ \frac{a_1 a'_1}{(a_1^2 - 1)^{1/2}} + \frac{a_2 a'_2}{(a_2^2 - 1)^{1/2}} \right] \cdot \frac{1}{a_2^2 - 1} \frac{C^{-m} - 1}{C^{-1} - 1} + \frac{2a_1 a'_1}{(a_1^2 - 1)^{3/2}} \right\} \quad (61)$$

$$\alpha^{TM}/\alpha_0^{TM} = 1 + \frac{n^2 + \kappa^2}{n} \frac{\pi}{2} \left\{ \left[ \frac{a'_1}{a_1(a_1^2 - 1)^{1/2}} + \frac{a'_2}{a_2(a_2^2 - 1)^{1/2}} \right] \cdot D^{-1} \frac{D^{-m} - 1}{D^{-1} - 1} + \frac{a'_1}{a_1(a_1^2 - 1)^{1/2}} \right\}. \quad (62)$$

Fig. 6 shows power losses in the hollow aluminum waveguide with multiple dielectric layers consisting of zinc selenide and germanium as a function of numbers of layer pairs. One can see that absorption-limited power losses of the waveguide are extremely small and possible numbers of layer pairs are  $m \approx 10$  in this particular case. In the figures results predicted by

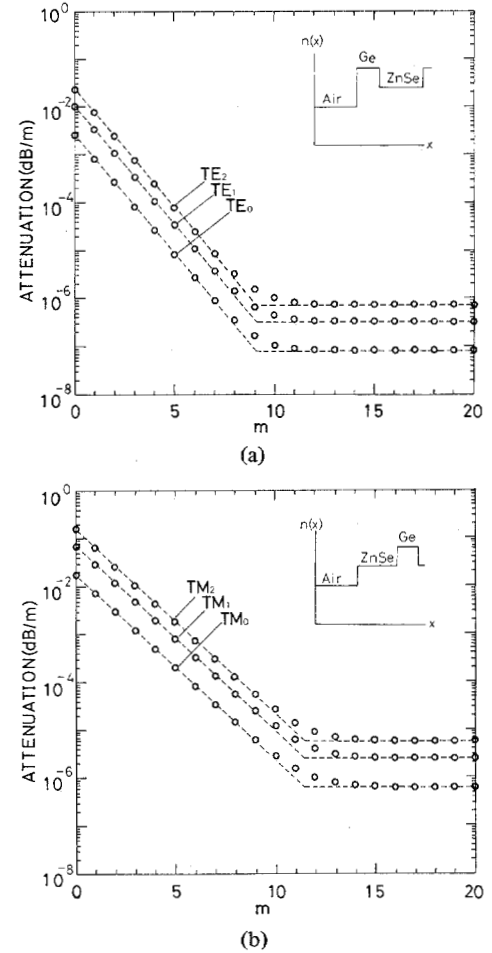


Fig. 6. Power losses of several (a) TE modes and (b) TM modes in the aluminum hollow waveguide with multiple inner dielectric layers composing of the zinc selenide whose complex refractive index is  $2.4 - j3.36 \times 10^{-8}$  and the germanium of  $4.0 - j10^{-6}$  as a function of  $m$  at  $\lambda = 10.6 \mu\text{m}$  and  $T = 500 \mu\text{m}$ . The nearest layer to the metal or hollow core is the germanium for TE modes and the zinc selenide for TM modes, respectively, as shown in insets. Dashed lines represent power losses predicted by (63) and (64).

the following very simple loss formulas, which are obtained by linear approximations of exact ones, are also shown in dashed lines as

$$\alpha^{TE} = \begin{cases} \frac{n_0 k_0 u_0^2}{(n_0 k_0 T)^3} \frac{n}{n^2 + \kappa^2} C^m; & m < m_s \\ \frac{n_0 k_0 u_0^2}{(n_0 k_0 T)^3} \frac{\pi}{2(a_1^2 - a_2^2)} \left[ \frac{a_1 a'_1}{(a_1^2 - 1)^{1/2}} + \frac{a_2 a'_2}{(a_2^2 - 1)^{1/2}} \right]; & m > m_s \end{cases} \quad (63)$$

$$\alpha^{TM} = \begin{cases} \frac{n_0 k_0 u_0^2}{(n_0 k_0 T)^3} \frac{n}{n^2 + \kappa^2} \frac{a_1^4}{a_1^2 - 1} D^m; & m < m_s \\ \frac{n_0 k_0 u_0^2}{(n_0 k_0 T)^3} \frac{\pi}{2} \frac{a_1^4}{a_1^2 - 1} (1 - D)^{-1} \left[ \frac{a'_1}{a_1(a_1^2 - 1)^{1/2}} + \frac{a'_2}{a_2(a_2^2 - 1)^{1/2}} \right]; & m > m_s. \end{cases} \quad (64)$$

$m_s$  represents the maximum number of efficient layer pairs for the power loss reduction over which no reduction is possible and it is defined by

$$m_s = \begin{cases} \log \left\{ \frac{n^2 + \kappa^2}{n} \frac{\pi}{2(a_1^2 - a_2^2)} \left[ \frac{a_1 a_1'}{(a_1^2 - 1)^{1/2}} + \frac{a_2 a_2'}{(a_2^2 - 1)^{1/2}} \right] \right\} / \log C; & \text{TE modes} \\ \log \left\{ \frac{n^2 + \kappa^2}{n} \frac{\pi}{2} (1 - D)^{-1} \left[ \frac{a_1'}{a_1(a_1^2 - 1)^{1/2}} + \frac{a_2'}{a_2(a_2^2 - 1)^{1/2}} \right] \right\} / \log D; & \text{TM modes.} \end{cases} \quad (65)$$

One should note that minimum attainable losses depend on mode number (or  $u_0$ ), core width, wavelength, and properties of dielectric materials and do not depend on the properties of metals used. This is because electromagnetic fields decay sufficiently at the metal surface. On the other hand, the maximum number of efficient pair layers  $m_s$  depends on  $(n^2 + \kappa^2)/n$  of metals. The larger  $(n^2 + \kappa^2)/n$  is, the smaller  $m_s$  becomes. In examples shown in Fig. 6, we have used the least absorptions for the zinc selenide and the germanium so far reported [38]. Actually, the minimum attainable losses are limited by the absorptions losses of the germanium. In order to see the effect of absorptions of dielectric materials in more detail, we consider the possible minimum losses and efficient number of layer pairs based on (63)–(65) by assuming  $a_1' = a_2'$  for simplicity.

Fig. 7 shows the minimum power losses and maximum number of the efficient pair layers for various combinations of transparent dielectric materials at  $10.6 \mu\text{m}$  as a function of  $a_1' (= a_2')$ . It is shown that waveguides with small power losses can be expected even for materials with high absorptions such as  $a_1' = a_2' = 10^{-4}$  in the two-dimensional slab waveguide.

In closing this section, we consider the bending loss in the dielectric-coated metallic waveguide. A previous analysis [39] shows that the attenuation constant  $\alpha$  in uniformly bent hollow slab waveguides characterized by small  $|z_{\text{TE}}|/z_0$  or  $|y_{\text{TM}}|/y_0$  is generally expressed by

$$\alpha/\alpha_\infty = \begin{cases} 1 - \frac{2}{3} \left( 1 - \frac{15}{4u_0^2} \right) \left( \frac{n_0 k_0 T}{u_0} \right)^4 \left( \frac{T}{R} \right)^2; & \text{large bending radius} \\ \left( \frac{n_0 k_0 T}{u_0} \right)^2 \frac{T}{R}; & \text{small bending radius} \end{cases} \quad (66)$$

where  $\alpha_\infty$  is the attenuation constant in straight waveguides,  $R$  is the bending radius, and  $u_0$  is defined by (18) for  $\text{TE}_p$  or  $\text{TM}_p$  modes. Equation (66) clearly shows that the waveguide with small  $\alpha_\infty$  such as the dielectric coated metallic waveguide has a small bending loss or it is bent with a small bending radius as well.

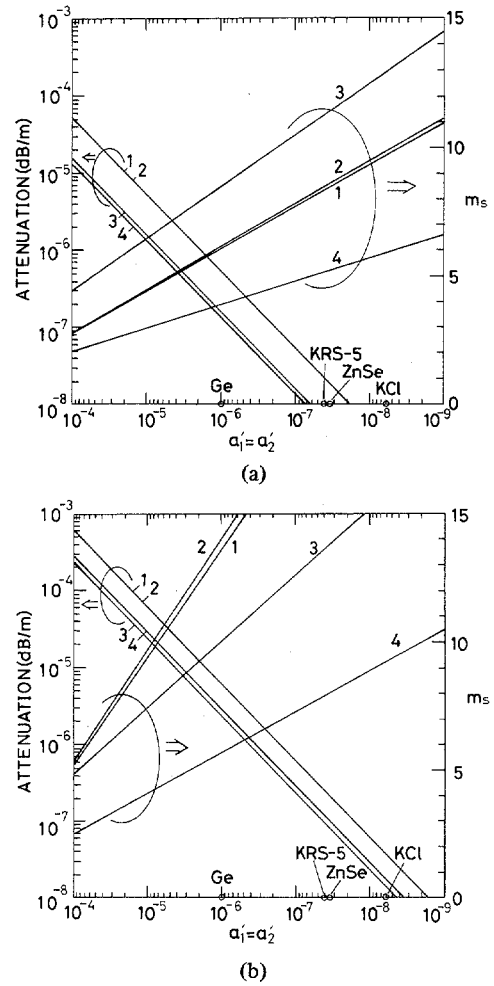


Fig. 7. Minimum power losses and maximum efficient numbers  $m_s$  of pair layers for (a) the  $\text{TE}_0$  mode and (b) the  $\text{TM}_0$  mode as a function of  $a_1' (= a_2')$  in the aluminum waveguide with  $T = 500 \mu\text{m}$  coated by various combinations of dielectric materials, where 1) ZnSe-KCl, 2) KRS-5-KCl, 3) Ge-ZnSe, 4) Ge-KCl. The smallest absorption coefficients ( $a_j'$ ) of actual materials so far reported [38] are also shown by small circles.

## V. CONCLUSION

A metallic hollow waveguide with inner dielectric multilayers is proposed for the transmission of infrared light and its basic transmission characteristics are fully analyzed by using a two-dimensional slab waveguide model. Waveguides with small power losses can be expected by coating even dielectric materials with relatively high absorptions in a straight waveguide structure. The waveguide is also shown to have a small bending loss.

A general theory for evaluating power losses in a circular waveguide structure will be reported in a subsequent paper and an optimum design theory of the dielectric-coated metallic waveguide will be discussed.

## REFERENCES

- [1] E. Garmire, T. McMahon, and M. Bass, "Propagation of infrared light in flexible hollow waveguides," *Appl. Opt.*, vol. 15, pp. 145–150, Jan. 1976.
- [2] D. A. Pinnow, A. L. Gentile, A. G. Standlee, A. J. Timper, and L. M. Hobrock, "Polycrystalline fiber optical waveguides for infrared transmission," *Appl. Phys. Lett.*, vol. 33, pp. 28–29, July 1978.



- [3] J. A. Harrington, "Crystalline infrared fibers," in *Proc. SPIE-International Society for Optical Engineering*, vol. 266, pp. 10-15, 1981.
- [4] J. A. Harrington and A. G. Standlee, "Optical attenuation in IR fibers," in *Dig. of Tech. Papers, IEEE/OSA Conf. Laser and Electrooptics*, Washington, DC, June 10-12, 1981, paper WC4.
- [5] J. H. Garfunkel, R. A. Skogman, and R. A. Walters, "Infrared transmitting fibers of polycrystalline silver halides," in *Dig. of Tech. Papers, IEEE/OSA Conf. Laser Eng. and Appl.*, Washington, DC, May 30-June 1, 1979, paper 8.1.
- [6] D. Chen, R. A. Skogman, E. G. Bernal, and H. Vora, "The performance of polycrystalline silver halide fibers at 10.6  $\mu\text{m}$ ," in *5th European Conf. Opt. Commun.*, Amsterdam, The Netherlands, Sept. 17-19, paper 19.7-1.
- [7] D. Chen, R. A. Skogman, E. G. Bernal, and C. Butter, "Fabrication of silver halide fibers by extrusion," in *Fiber Optics: Advances in Research and Development*, B. Bendow and S. S. Mitra, Eds. New York: Plenum, pp. 119-122, 1979.
- [8] S. Sakuragi, K. Imagawa, M. Saito, H. Kotani, T. Morikawa, and J. Shimada, "IR transmission capabilities of thallium halide and silver halide optical fibers," *Adv. Ceram.*, vol. 2, pp. 84-93, 1981.
- [9] S. Sakuragi, M. Saito, Y. Kubo, K. Imagawa, H. Kotani, T. Morikawa, and J. Shimada, "KRS-5 optical fibers capable of transmitting high-power CO<sub>2</sub> laser beam," *Opt. Lett.*, vol. 6, pp. 629-631, Dec. 1981.
- [10] Y. Okamura, Y. Mimura, Y. Komazawa, and C. Ota, "CsI crystalline fiber for infrared transmission," *Japan. J. Appl. Phys.*, vol. 19, pp. L649-L651, Oct. 1980.
- [11] Y. Mimura, Y. Okamura, Y. Komazawa, and C. Ota, "CsBr crystalline fiber for visible and infrared transmission," *Japan. J. Appl. Phys.*, vol. 20, pp. L17-L18, Jan. 1981.
- [12] T. J. Bridges, J. S. Hasiak, and A. R. Strnad, "Single-crystal AgBr infrared optical fibers," *Opt. Lett.*, vol. 5, pp. 85-86, Mar. 1980.
- [13] J. Y. Boniort, C. Brehm, Ph. Dupont, D. Guignot, and C. Le Sergeant, "Infrared glass optical fibers for 4 and 10 micron band," in *6th European Conf. Opt. Commun.*, Sept. 16-19, 1980, York, England, pp. 61-64.
- [14] M. Miyagi and S. Nishida, "Transmission characteristics of dielectric tube leaky waveguide," *IEEE Trans. Microwave Theory Tech.*, vol. MTT-28, pp. 536-541, June 1980.
- [15] M. Miyagi, "Bending losses in hollow and dielectric tube leaky waveguides," *Appl. Opt.*, vol. 20, pp. 1221-1229, Apr. 1981.
- [16] H. Nishihara, T. Inoue, and J. Koyama, "Low-loss parallel-plate waveguide at 10  $\mu\text{m}$ ," *Appl. Phys. Lett.*, vol. 25, pp. 391-393, Oct. 1974.
- [17] Y. Mizushima, T. Sugeta, T. Urisu, H. Nishihara, and J. Koyama, "Ultralow loss waveguide for long distance transmission," *Appl. Opt.*, vol. 19, pp. 3259-3260, Oct. 1980.
- [18] E. Garmire, T. McMahon, and M. Bass, "Flexible infrared-transmissive metal waveguides," *Appl. Phys. Lett.*, vol. 29, pp. 254-256, Aug. 1976.
- [19] —, "Propagation of IR light in flexible hollow waveguides: Further discussion," *Appl. Opt.*, vol. 15, pp. 3037-3039, Dec. 1976.
- [20] E. Garmire, "Low-loss optical transmission through bent hollow metal waveguides," *Appl. Phys. Lett.*, vol. 31, pp. 92-94, July 1977.
- [21] E. Garmire, T. McMahon, and M. Bass, "Low-loss propagation and polarization rotation in twisted infrared metal waveguides," *Appl. Phys. Lett.*, vol. 34, pp. 35-37, Jan. 1979.
- [22] —, "Flexible infrared waveguides for high-power transmission," *IEEE J. Quantum Electron.*, vol. QE-16, pp. 23-32, Jan. 1980.
- [23] U. Kubo, Y. Hashishin, and M. Nakatsuka, "Development of parallel metal plate hollow light guide for CO<sub>2</sub> laser," presented at the 4th Congress of Int. Soc. for Laser Surgery, Nov. 23-27, 1981, Tokyo, Japan.
- [24] T. Matsushima, I. Yamauchi, and T. Sueta, "Flexible infrared-transmission plastic waveguides coated with evaporated aluminum," *Japan. J. Appl. Phys.*, vol. 20, pp. 1345-1346, 1981.
- [25] T. Hidaka, T. Morikawa, and J. Shimada, "Oxide-glass cladding middle infrared optical waveguides," *Trans. IECE Japan*, vol. J64-C, pp. 590-596, Sept. 1981.
- [26] T. Hidaka, "Loss calculation of the hollow-core, oxide-glass-cladding, middle-infrared optical waveguides," *J. Appl. Phys.*, vol. 53, pp. 93-97, Jan. 1982.
- [27] E. A. J. Marcetili and R. A. Schmeltzer, "Hollow metallic and dielectric waveguides for long distance optical transmission and lasers," *Bell Syst. Tech. J.*, vol. 43, pp. 1783-1809, July 1964.
- [28] H. G. Unger, "Circular electric wave transmission in a dielectric-coated waveguide," *Bell Syst. Tech. J.*, vol. 36, pp. 1253-1278, Sept. 1957.
- [29] H. G. Unger, "Lined waveguide," *Bell Syst. Tech. J.*, vol. 41, pp. 745-768, Mar. 1962.
- [30] J. W. Carlin and P. D'Agostino, "Low-loss modes in dielectric lined waveguides," *Bell Syst. Tech. J.*, vol. 50, pp. 1631-1638, May-June 1971.
- [31] —, "Normal modes in overmoded dielectric-lined circular waveguide," *Bell Syst. Tech. J.*, vol. 52, pp. 453-486, Apr. 1973.
- [32] C. Dragone, "High-frequency behavior of waveguides with finite surface impedance," *Bell Syst. Tech. J.*, vol. 60, pp. 89-116, Jan. 1981.
- [33] P. Yeh, A. Yariv, and C. S. Hong, "Electromagnetic propagation in periodic stratified media. I. General theory," *J. Opt. Soc. Amer.*, vol. 67, pp. 423-438, 1977.
- [34] P. Yeh, A. Yariv, and E. Maron, "Theory of Bragg fiber," *J. Opt. Soc. Amer.*, vol. 68, pp. 1196-1201, 1978.
- [35] M. Miyagi and S. Kawakami, "Waveguide loss evaluation by ray-optics method," unpublished.
- [36] S. Kawakami, *Optical Waveguides* (in Japanese). Tokyo: Asakura Shoten, 1980, pp. 126-132.
- [37] K. Kudo, *(Tables of Properties of Fundamental Materials)* (in Japanese). Kiso Bussei Zuhyo Tokyo: Kyoritsu Shuppan, 1972.
- [38] T. Miyata, "Optically transparent materials supporting high powered technology" (in Japanese), *Science and Technol.*, vol. 22, pp. 36-43, Mar. 1981.
- [39] M. Miyagi and S. Kawakami, "Losses and phase constant changes caused by bends in the general class of hollow waveguides for the infrared," *Appl. Opt.*, vol. 20, pp. 4221-4226, Dec. 1981.



Mitsunobu Miyagi was born in Hokkaido, Japan, on December 12, 1942. He graduated from Tohoku University, Sendai, Japan, in 1965, and received the M.E. and Ph.D. degrees in 1967 and 1970, respectively.

He was appointed a Research Associate at the Research Institute of Electrical Communication, Tohoku University, in 1970. From 1975 to 1977, while on leave of absence from Tohoku University, he joined McGill University, Montreal, P.Q., Canada, where he was engaged in the research on optical communications. Since 1978, he has been an Associate Professor at Tohoku University. His major interests are in optical communications, especially in developing IR waveguides for high-powered CO<sub>2</sub> lasers.

Dr. Miyagi is a member of the Institute of Electronics and Communication Engineers of Japan and the Optical Society of America.



Akihito Hongo was born in Fukushima, Japan, on February 2, 1959. He received the B.E. degree from Tohoku University, Sendai, Japan, in 1981.

He is currently working towards the M.E. degree at Tohoku University, studying in the field of IR optical waveguides.

Mr. Hongo is a member of the Institute of Electronics and Communication Engineers of Japan.



Shojiro Kawakami (S'60-M'65-M'69) was born in Gifu, Japan, on November 8, 1936. He received the B.E., M.E., and Ph.D. degrees from the University of Tokyo, Tokyo, Japan, in 1960, 1962, and 1965, respectively.

In 1965 he was appointed a Research Associate at Tohoku University, Sendai, Japan, and in 1966 he was made Assistant Professor. Since 1979 he has been a Professor. From 1960 to 1965, he was engaged in the research of millimeter wave detection systems and microwave

switching circuits. Since 1965 his main interest has been in the field of optical communication. In his early career in optical communication, he had much interest in near square-law fibers, and later also in *W*-type single-mode fibers. He has recently been interested in modal power dynamics in multimode fibers. He has also carried out some work in the electromagnetic theory and has been interested in experimental investigations of optical devices such as fiber Faraday rotators and metal-dielectric multilayer polarizers. He is the author of the book *Optical Waveguides*. In 1977 he was awarded the Ichimura Prize for his contribution to *W*-type fibers.

Prof. Kawakami is a member of the Institute of Electronics and Communication Engineers of Japan.

## Q-Switched Semiconductor Diode Lasers

DEAN Z. TSANG, MEMBER, IEEE, AND JAMES N. WALPOLE

(Invited Paper)

**Abstract**—Diode lasers with an intracavity electroabsorption modulator have been operated with full on/off modulation at rates of 3 GHz. In addition, modulation of the lasers has been shown up to a detector-limited frequency of 6 GHz. A new model of these devices, which includes amplified spontaneous emission and high gain is developed in this paper. A quasi-static gain approximation is introduced and the dynamics of the electron and photon population are modeled by three coupled nonlinear difference equations which can be numerically solved with very little computation time. The model predicts the possibility of a new mode of *Q*-switched operation with the capacity for repetition rates of tens of gigahertz and binary pulse position modulation at rates of the order of 10 Gbits/s.

### I. INTRODUCTION

**Q**-SWITCHED semiconductor diode lasers are of interest for applications in optical fiber communication systems or generally as a source of optical pulses when high peak power and large depth of modulation are required at high repetition rates. An actively *Q*-switched laser in which the intracavity loss can be electrically driven is desirable for these applications. In this paper we first briefly review previous work and then present theoretical and experimental results for a diode laser actively *Q*-switched by an intracavity p-n junction electroabsorption modulator [1]–[3]. The model is then applied to study digital modulation at rates of the order of 10 Gbits/s.

*Q*-switching lasers by rapidly switching the intracavity optical loss is a technique for producing optical pulses with high peak power [4] and high repetition rates [5], [6]. In early studies with diode lasers, large optical pulses were seen at the end of the diode excitation pulse. This phenomenon,

seen primarily in single heterostructure lasers, was called "*Q*-switching," but was not associated with variations of the optical loss [7]. Variations in the optical loss can be produced through passive means in which the loss is not directly modulated or active means in which the loss is directly modulated. Passive *Q*-switching due to saturable absorption has been observed in diode lasers with two nonuniformly pumped gain sections [8], [9]. Actively *Q*-switched lasers can be directly modulated, an advantage for many applications. The first proposals for actively *Q*-switched diode lasers included the use of electrooptically switched [10] and acoustooptically switched [11] distributed feedback gratings as a means of varying mirror reflectivities. The first actively *Q*-switched laser operation has been previously reported by the authors and co-workers [1]–[3] using diode lasers with an intracavity electroabsorption modulator at rates up to 2.5 GHz. Short pulses have also been produced at lower repetition rates in a diode laser with a dye-laser-pumped passive section in a combination of active *Q*-switching and active gain switching [12]. Electrical variation of the optical coupling to an adjacent guide [13] or the optical confinement [14] are two other recently proposed schemes to *Q*-switch diode lasers. In this paper we report full on/off modulation at 3 GHz as well as modulation of the lasers up to a detector-limited frequency of 6 GHz.

Previous theoretical treatments of actively *Q*-switched diode lasers have been modifications of the conventional rate equations in which the gain and loss are evenly distributed over the cavity [10], [11]. In order to include the effects of high gain and amplified spontaneous emission (ASE), a new treatment based on a rate equation approximation has been developed [3], [15] and will be described in detail in this paper for a laser with separate gain and loss sections.

This new treatment constitutes a major part of this paper. We show that a quasi-static gain approximation can be made which significantly reduces the amount of numerical compu-

Manuscript received August 31, 1982. This work was supported by the Departments of the Air Force and the Navy and the Defense Advanced Research Projects Agency.

The authors are with Lincoln Laboratory, Massachusetts Institute of Technology, Lexington, MA 02173.