# Probability Introduction

Week 02 - Day 01

# **Probability**

Probability = chance of an event (coin flip, result of a match, etc.)

# P(head) = 0.5 = 50% (1=100%)

P(tail) = 0.5 = 50% (1=100%)

# Axioms

# **Axiom 1: non negativity**

The probability of an event is greater or equal to zero

$$P(A) >= 0$$

P(Head) = -0.7 ???

#### **Axiom 2: unit measure**

The probability of all the possible events is 1

$$P(head) + P(tail) = 1$$

# **Axiom 2: additivity**

P(Head or Tail) = P(head) + P(Tails)

(disjoints events = "non overlapping" = mutually exclusive)

# Properties

### 1 - Probability of No Event

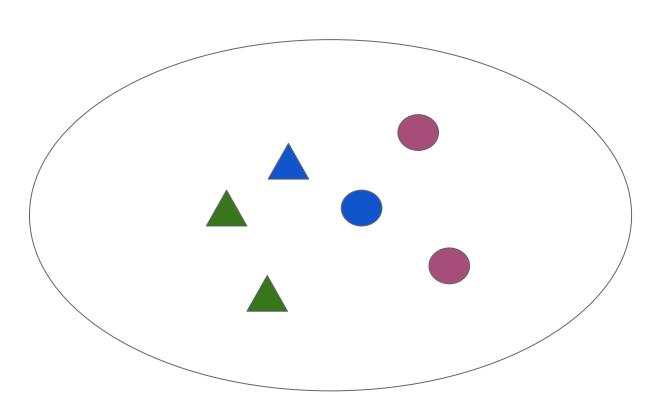
is zero!... (it's either tail or head)

# 2 - Probability of A or B (union)

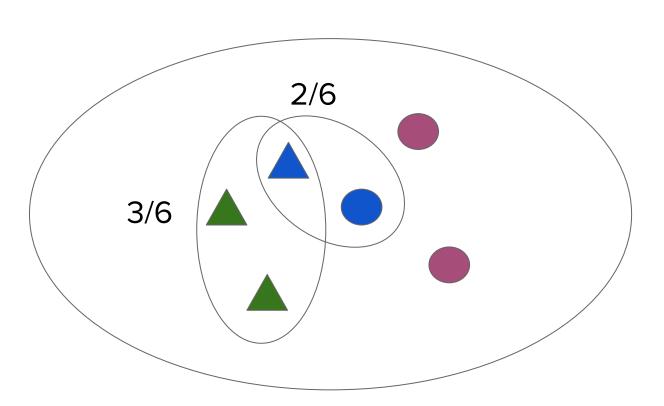
$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

If no overlapping -> just P(a) + P(B)

## P(triangle U blue) = ?



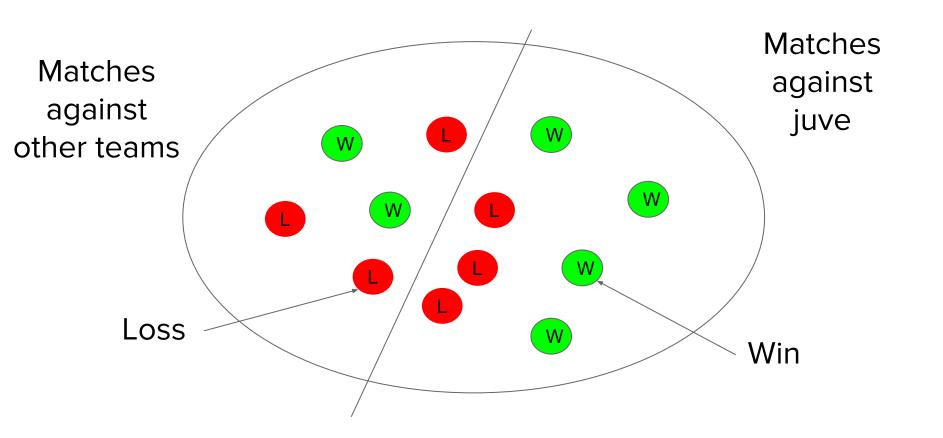
## P(triangle U blue) = ?



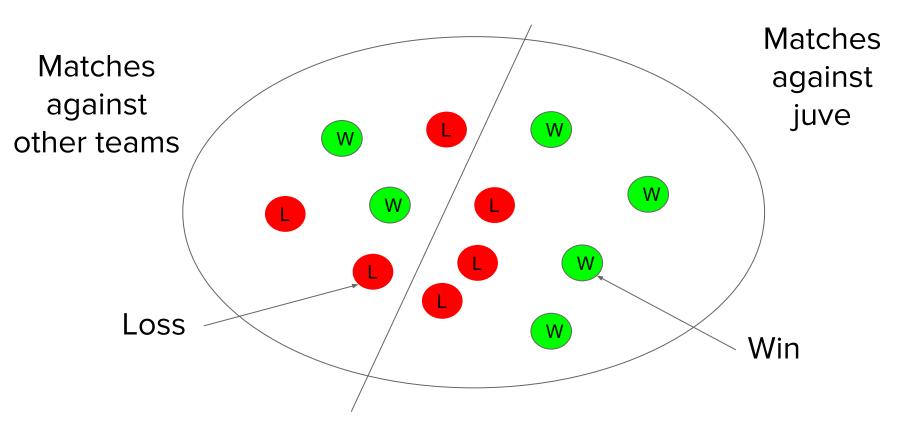
# 3 - Conditional Probability

$$P(A|B) = P(A \cap B) / P(B)$$

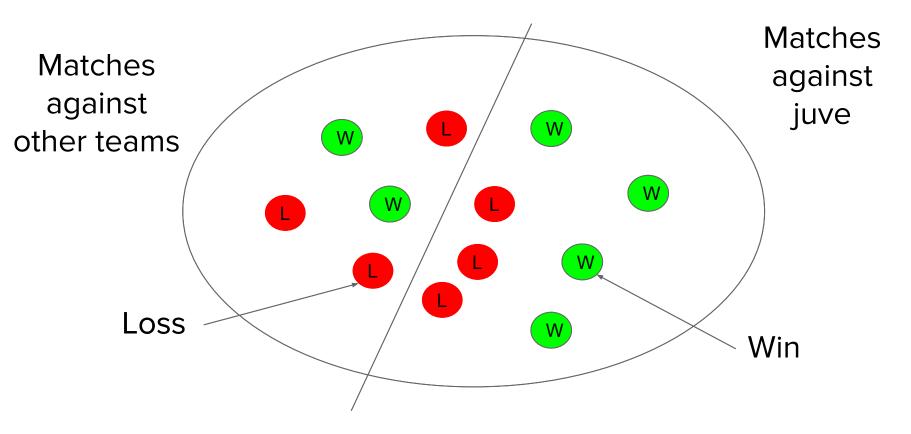
- 1) Useful for ML
- 2) Example: p(win | playing against juventus)



#### P(win | playing against juve) = ?



#### P(win | playing against juve) = 4/7



# 4 - Joint probability

 $P(A \cap B) = P(A|B) * P(B)$ 

Just play with the previous formula!

# 5 - Total probability

<u>video</u>

# Combinatorics

#### **Basic definition**

<u>Combinatorics</u> is the study of how sets can be enumerated

"How many strings of 5 letters can I build using only [a,b,e,n,o]."

# **Counting principle**

$$3 \text{ girls} = (a,b,c)$$

4 boys = 
$$(1,2,3,4)$$

How many possible couples like (girl,boy) can you have?

# **Counting principle**

a1,a2,a3,a4

b1,b2,b3,b4

c1,c2,c3,c4

 $4x3 = 12 \rightarrow double for loop! :)$ 

#### **Permutations**

<u>Video</u>

#### **Combinations**

<u>Video</u>

# With replacement (sampling)

The same element can be chosen more than one time

# **Birthday paradox**

https://en.wikipedia.org/wiki/Birthday\_problem

#### **Lesson material**

Skip:

Distinguishable vs. Indistinguishable ("balls and urns")