

# 703650 VO Parallel Systems WS2020/2021 13 Dwarfs of HPC

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#### Overview

- ▶ 13 Dwarfs of HPC
  - abstract application categories
- "Tales from the Proseminar"
  - Daniel's Weird int Problem
  - ▶ g++ vs. gcc when compiling C code

#### Motivation

- MPI API or concepts such as "load imbalance" or "task-parallelism" are still pretty low-level characteristics of parallel programs
- we need to be able to recognize higher-level classes of applications and discuss them

- ▶ this lecture presents the most prominent classes of HPC applications
  - many new applications you encounter will fit into these categories

# How and Why are Dwarfs Defined?

- group applications by similarity in computation and data structures
  - first published by Asanovic et al in *The Landscape of Parallel Computing Research: A View from Berkeley*
  - https://www2.eecs.berkeley.edu/Pubs/TechRpts/2006/EECS-2006-183.pdf
- purely algorithmic, implementation-independent
  - enables cross-platform reasoning and cross-application resource sharing (e.g. libraries)
- serve as small, abstract, high-level benchmarks for studying new
  - programming models
  - communication patterns
  - hardware architectures, topologies
  - ..
- used to kick off innovation in all of these aspects



# 7 Original Dwarfs of HPC

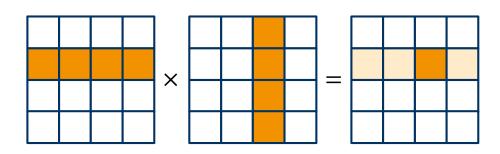
- What are we going do discuss?
  - 1. Dense Linear Algebra
  - 2. Sparse Linear Algebra
  - 3. Spectral Methods
  - ▶ 4. N-body Methods
  - ▶ 5. Structured Grids
  - ▶ 6. Unstructured Grids
  - > 7. Monte Carlo Methods

- What have you already heard?
  - matrix mul (first MPI lecture)

- particle-in-cell
- heat stencil
- Monte Carlo π

### Dense Linear Algebra

- data is stored in densely-populated matrices (or vectors)
  - data is stored uncompressed ("as is")
  - data access via strides, often unit stride
- e.g. matrix multiplication, LU decomposition, Gauss-Seidel, ...
- rarely done manually, there are a TON of libraries out there



### Dense Linear Algebra: Characteristics

- naïve implementations often memory bound
  - remember: memory wall!
  - caches and prefetching helps
- simple but significant data structure
  - stride often enables/prevents vectorization (SIMD)
  - column- vs. row-major access (often transposed) affects cache efficiency
- still the default measure for performance in HPC
  - e.g. TOP500 uses HPL, a high performance LINPACK benchmark
  - but nowadays not the only one (e.g. HPCG)

```
for (int i = 0; i < N; ++i) {
  for (int j = 0; j < N; ++j) {
    double tmp = 0.0;
  for (int k = 0; k < N; ++k) {
    tmp += A[i][k] * B[k][j];
  }
  result[i][j] = tmp;
}</pre>
```

```
vgatherqpd ymm0{k2}, [rax+ymm5*1]
vmulpd ymm0, ymm0, YMMWORD PTR [rdx+rdi]
...
```

### Dense Linear Algebra: Optimizations

#### loop blocking or tiling

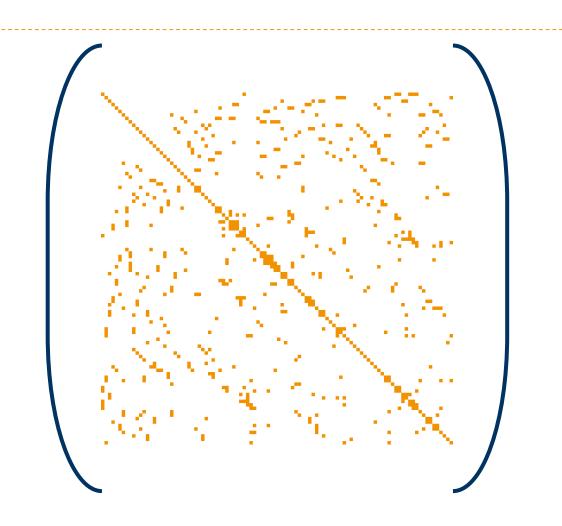
- do not work on single elements but smaller blocks (e.g. 2x2 or 32x32)
- exploits locality and cache
- also, lots of other HOTs (<u>H</u>igher <u>O</u>rder <u>T</u>ransformations)
- vectorization (SIMD, e.g. SSE/AVX)
  - might entail modifications, e.g. transposing matrix A or B in matrix mul
- hardware-specific instructions
  - e.g. fused multiply-add (FMA)

```
for (int ii = 0; ii < N; ii += ib) {
 for (int jj = 0; jj < N; jj += jb) {
  for (int k = 0; k < N; ++k) {
   for (int i = ii; i < ii+ib; ++i) {
    for (int j = jj; j < jj+jb; ++j) {
      // ... process single tile
```

# Sparse Linear Algebra

- data is stored in sparsely-populated matrices (or vectors)
  - vast majority of data is zero
  - data is stored in compressed format
  - data often accessed indirectly via indices

e.g. conjugate gradient, Google's PageRank, data mining



### Sparse Linear Algebra: Characteristics

- computationally or memory limited
  - depends on sparsity of data, data structure representation and algorithm
- different data structures available
  - e.g. coordinate scheme (COO) or "triplet format" or similar:  $(i, j, a_{ij})$
  - array of structs vs. struct of arrays
  - not necessarily sorted!

```
typedef struct sparseElement {
    int i; int j; double value;
} sparseElement;
sparseElement sparseMatrix[SIZE];
sparseMatrix[0].i = 0;
typedef struct sparseMatrixT {
   int i[SIZE]; int j[SIZE];
    double values[SIZE];
} sparseMatrixT;
sparseMatrixT sparseMatrix;
sparseMatrix.i[0] = 0;
```

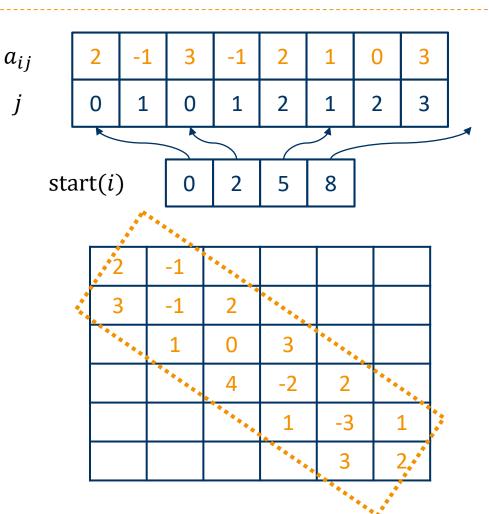
### Sparse Linear Algebra: Optimizations

#### compressed row storage (CRS)

- two arrays of size N
- one holds  $a_{ij}$ , the other j
- third array points to start of row i in j
- smaller memory footprint than COO
  - $\triangleright 2N + (m+1) \text{ vs. } 3N$

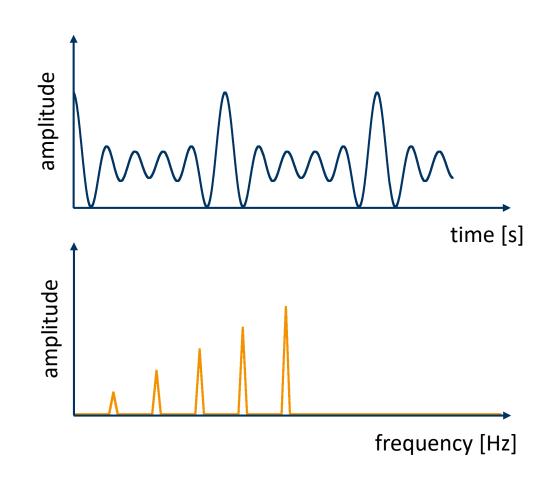
#### variants

- column-major variant (CCS)
- store small blocks (2x2 or 4x4) instead of single elements, improves SIMDness
- compressed diagonal storage (CDS)
  - ▶ remember: use domain-specific knowledge!



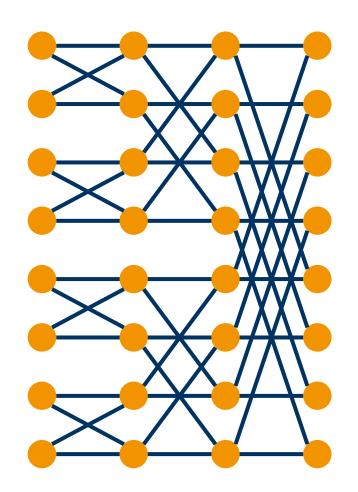
### Spectral Methods

- data in frequency domain, not time or space
  - can include multiple stages of computations alternating between local and global communication
- e.g. fast Fourier transform (FFT), audio and video signal processing
  - e.g. "focus hunting" in contrast-based autofocus of photo/video cameras



# Spectral Methods: Characteristics

- usually implemented using butterfly patterns
  - multiple stages of multiply-add
  - often latency limited due to global communication patterns (e.g. all-to-all)
- often resemble structured or unstructured grid methods after transformation to frequency domain



### Spectral Methods: Optimizations

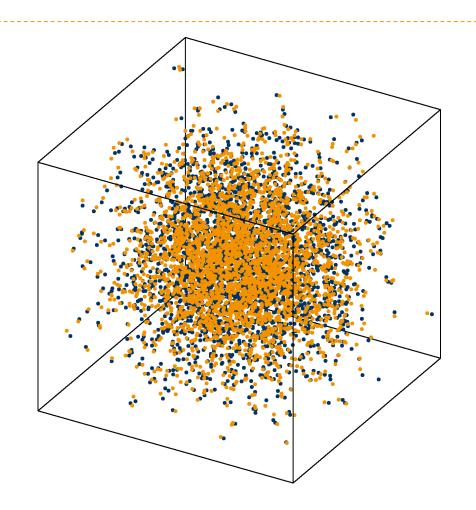
- requires optimization of the transformation to frequency domain
  - relies on transposing data efficiently
- afterwards, consider similar optimizations as for (un)structured grids

- severely restricted scalability to larger HPC systems
  - ongoing research
  - lot's of it in math

# N-body Methods

- models interactions between discrete, moving points
  - often requires dynamic data structures
  - varying spatial locality
  - movement affects load balance and data access costs

• e.g. galaxy collision simulations, molecular dynamics, protein folding



### N-body Methods: Characteristics

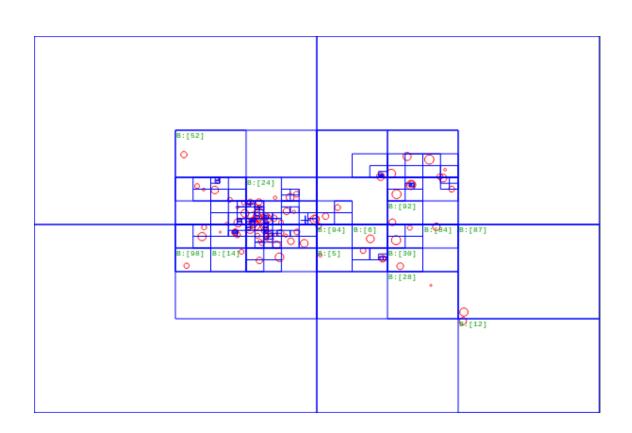
- computational effort is an issue
  - $\mathcal{O}(N^2)$  for N particles
  - but also global communication
- lots of hierarchical optimization studies
  - domain decomposition!
  - e.g. Barnes-Hut or fast multipole optimization

- alternative approaches rely on domain-specific knowledge, e.g.
  - ignore long-distance particle interactions
  - store particles in Cartesian topology & only consider particles in neighboring grid cells

### N-body Methods: Optimizations

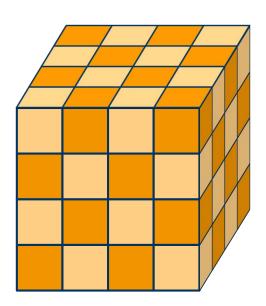
#### ▶ Barnes-Hut optimization:

- decompose domain into quadtree (for 2D)
- aggregate particle effect (e.g. gravitation from mass) for each cell into a single (hypothetical) particle at the center of gravity per cell
- reduces complexity from  $O(N^2)$  to  $O(N \cdot \log N)$



#### Structured Grids

- model interactions between discrete, fixed points
  - grid structure described by pattern
  - topological information easily derived
  - usually high spatial locality
  - may be subdivided into finer grid ("adaptive")
- e.g. heat transfer (stencil), computational fluid dynamics (CFD), octrees



#### Structured Grids: Characteristics

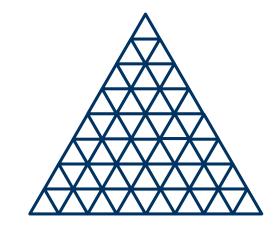
#### structured nature is a key aspect

- similar characteristics compared to dense linear algebra (e.g. row-major vs. columnmajor)
- memory addresses often predictable, facilitates e.g. prefetching
- adaptive grids possible

#### typically memory bound

- e.g. 7-point stencil in 3D: load 7 data points for computing a single new one
- local communication only (ghost cell exchange with direct neighbor)

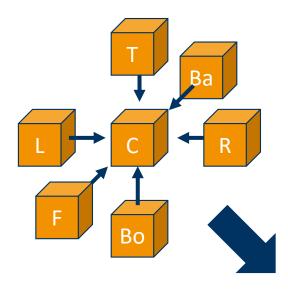
structured grid does not imply rectangular!





### Structured Grids: Optimizations

- decomposition, decomposition, decomposition
  - remember in 3D: slabs, poles, cubes
  - highly dependent on type of grid and specific use case
- structured nature of the problem makes analytic prediction possible
  - performance models and simulators for simple stencil kernels (e.g. Kerncraft)

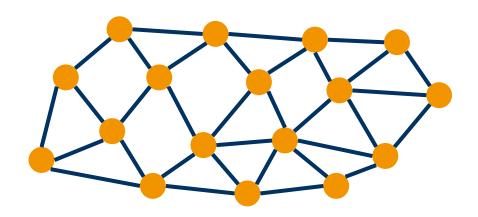


L1 misses: # L2 misses: # L3 misses: # ...

### **Unstructured Grids**

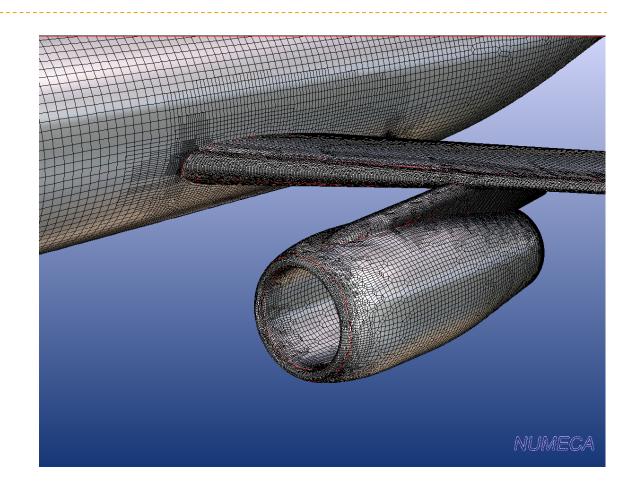
- model interactions between discrete, fixed points
  - grid pattern described explicitly by individual connections
  - irregular geometry and topology
  - usually involves multiple levels of indirection when accessing data

• e.g. computational fluid dynamics (CFD)



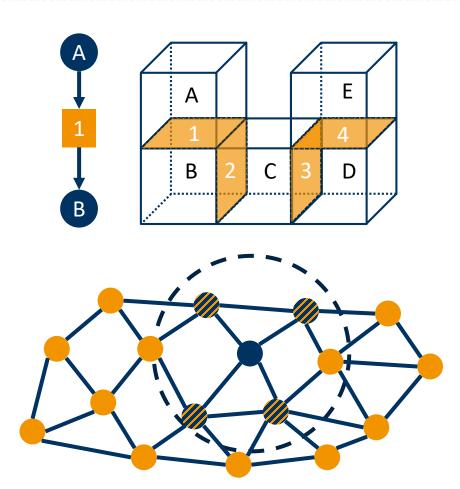
#### Unstructured Grids: Characteristics

- usually heavily latency bound due to indirect access
  - ... = cells[neighbors[i]]
  - ... = cell.getNeighbor(i)
  - also known as "pointer chasing"
- similar problems compared to structured grids, e.g.
  - domain decomposition / adaptivity
  - topological information
  - ghost cell exchange
  - but hardly analytically predictable



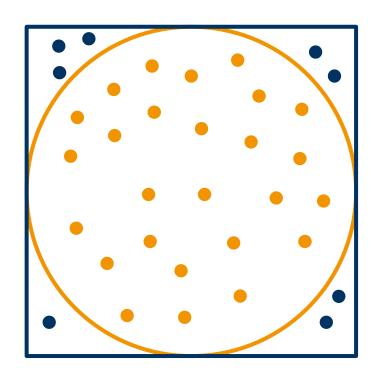
### Unstructured Grids: Optimizations

- problem space discretization and topology
  - which types of grid elements?
  - which types of connections?
  - cells, faces, vertices, edges, ...
  - should be efficient to load/store, navigate, and compute
- decomposition, decomposition, decomposition
  - efficient ghost cell exchange required
  - efficient grid navigation e.g. to access neighbors



### Monte Carlo Methods

- also known as map-reduce
  - process data independently and merge the results
- models statistical evaluation of repeated random trials
  - communication usually insignificant
  - embarrassingly parallel, multiple copies of sequential method
- e.g. numerical integration, quantum many-body problems, ray tracing



### Monte Carlo Methods: Characteristics

- parallelization almost a no-factor
  - similar to multiple sequential programs sharing some resources (e.g. L3 cache, random number generator)
  - relatively inexpensive reduction
- depends heavily on sequential optimizations

### Monte Carlo Methods: Optimizations

- not much to do beyond sequential optimization
  - **ILP**
  - prefetching
  - vectorization
  - resource contention (read: fast random number generation)

- consider different hardware
  - **GPUs**
  - FPGAs
  - ...
- try to decrease cost of evaluating a sample
  - increase number of samples if required

# Additional Dwarfs

#### Additional Dwarfs

- ▶ 8. Combinational Logic
- 9. Graph Traversal
- ▶ 10. Dynamic Programming
- ▶ 11. Backtrack & Branch+Bound
- ▶ 12. Graphical Models
- ▶ 13. Finite State Machine

- slightly different focus compared to first 7 dwarfs
  - more (but not exclusively) on integerheavy applications and machine learning
  - less on physical processes

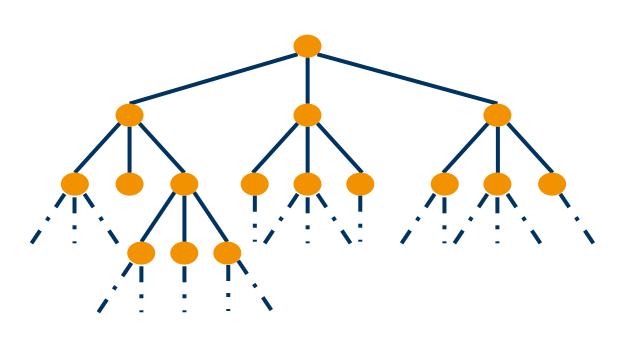
### Combinational Logic

- generally involves performing simple operations on large amounts of integer data
  - e.g. computing cyclic redundancy codes (CRC)
- often parallelizable on multiple levels
  - bit-level parallelism
  - block-level parallelism

```
uint8_t compute(uint8_t const msg[], int n) {
    uint8 t rem = 0;
    for (int byte = 0; byte < n; ++byte) {
        rem ^= (msg[byte] << (WIDTH - 8));</pre>
        for (uint8_t bit = 8; bit > 0; --bit) {
            if (rem & TOPBIT) {
                 rem = (rem << 1) ^ POLYNOMIAL;</pre>
             } else {
                 rem = (rem << 1);
    return (rem);
```

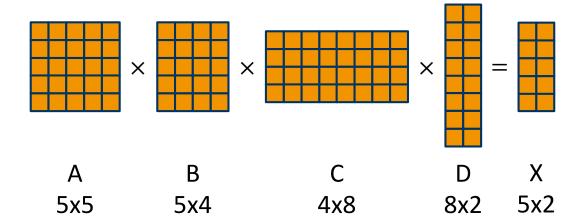
# **Graph Traversal**

- traverse a number of objects in a graph and examine characteristics
  - e.g. searching, sorting, collision detection, decision trees, ...
  - usually heavy on data reads and lookups,
     very little computation and output
- parallelizable over different paths in the graph
  - but indirect accesses are heavily latency-bound (c.f. unstructured grids)



# Dynamic Programming

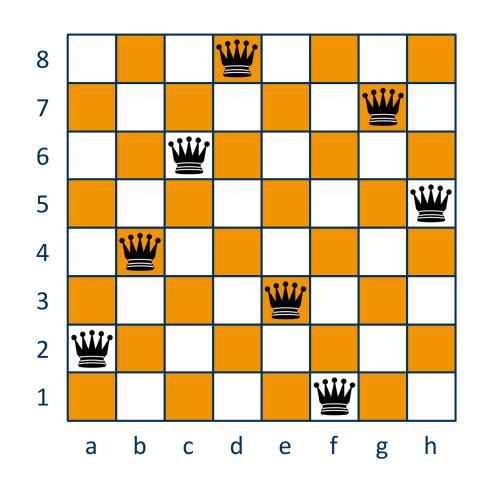
- method of computing solutions by solving simpler, overlapping sub-problems
  - applicable to problems where optimal result is composed of optimal results of sub-problems
  - e.g. matrix-chain-multiplication
- usually based on memoization
  - solve each sub-problem exactly once
  - store and re-use the result



$$A \times (B \times (C \times D)) = X$$
 154 ops  
 $(A \times B) \times (C \times D) = X$  204 ops  
 $((A \times B) \times C) \times D = X$  340 ops

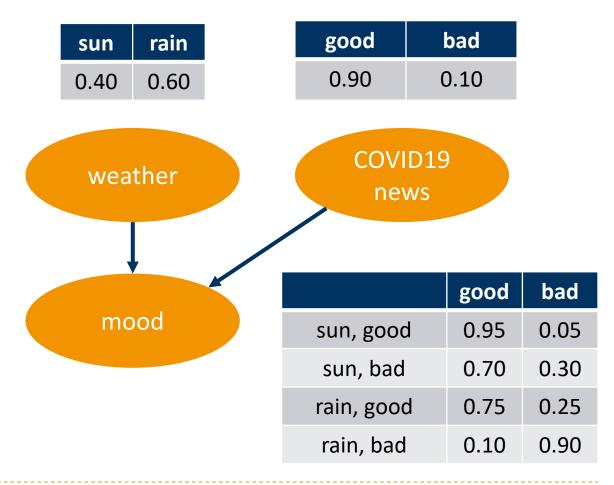
### Backtrack & Branch+Bound

- search and optimization problems for very large problem spaces
  - incrementally build solution but discard if determined unsuitable
  - e.g. n-queens problem
- use divide & conquer strategy:
  - break down complex problem into smaller sub-problems until they become solvable
  - solve sub-problems in parallel



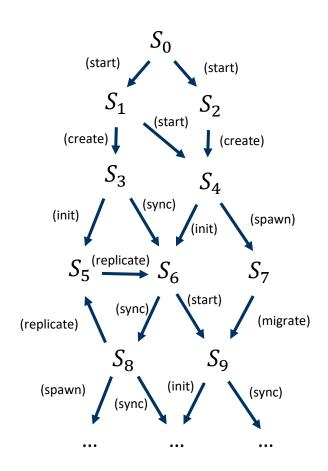
### Graphical Models

- also known as probabilistic models
- represent graphs consisting of random variables as nodes and dependencies as edges
  - e.g. Bayesian networks, Hidden Markov models
- ongoing research in math and computer science regarding parallelization and optimization



#### Finite State Machines

- represent interconnected set of states to be moved among
  - e.g. parsers
- can sometimes be decomposed into multiple state machines that act in parallel
  - ongoing research



### Literature Material

- ▶ White Paper by Berkeley University: "The Landscape of Parallel Computing Research: A View from Berkeley" from 2006:
  - https://www2.eecs.berkeley.edu/Pubs/TechRpts/2006/EECS-2006-183.pdf
- ▶ Holds more detailed descriptions and related aspects

### Note the Focus on Scientific Problems

- MPI can also be used to implement
  - distributed-memory runtime systems
  - emulate shared memory runtime systems on distributed memory (e.g. PGAS)
  - provide the connecting parallelism layer for shared-memory or sequential systems
    - ▶ e.g. use multiple accelerators in separate compute nodes (Celerity project @ UIBK)
    - extend shared memory parallelism to distributed memory (MPI+X)
    - **...**
- still, the majority of codes is of scientific computing nature

Tales from the Proseminar

- sequential 2D heat stencil
  - ▶ 100x100 problem size
  - -O0 (also with –O2) on LCC2
  - gcc 4.8.5 (but also 9.2 and MSVC 2019)
  - switching from long long loop iterators to int halves execution time

```
$ /usr/bin/time –f %E ./stencil_long 100 100
0:04.60
$ /usr/bin/time –f %E ./stencil_int 100 100
0:02.31
```

What the heck is going on?

profiled with gprof to find "hot spots", left is int, right is long long

% c	umulative	selt	f
time	seconds	second	ds name
32.92	0.76	0.76	int.c:93
20.06	1.22	0.46	int.c:78
<b>14.8</b> 3	1.56	0.34	int.c:79
10.47	1.80	0.24	<pre>int.c:87</pre>
9.59	2.02	0.22	int.c:86

% C	umulative	self	
time	seconds	second	ls name
36.84	1.69	1.69	long.c 79
31.61	3.15	1.45	long.c 78
16.35	3.90	0.75	long.c 93
5.34	4.15	0.25	long.c:86
3.27	4.30	0.15	long.c:87

```
// get temperature at current position
75
     value_t tc = A[i];
76
     // get temperatures of adjacent cells
     value_t txl = (i % Nx != 0) ? A[i - 1] : tc;
78
     value_t txr = (i % Nx != Nx - 1) ? A[i + 1] : tc;
     // ..... snip .....
     if (Ny > 1)
90
       B[i] = tc + 0.165 * (txl + txr + tyl + tyr + tzl + tzr + (-6 * tc));
91
92
     else
       B[i] = tc + 0.2 * (txl + txr + tzl + tzr + (-4 * tc));
93
     // if ((int)B[i] < (int)A[i])</pre>
```

far-fetched idea, but maybe branch (miss-)predictions? compared with perf stat:

```
2328.650634 task-clock:u (msec) #
                                      0.996 CPUs
            0 context-switches:u #
                                      0.000 K/sec
            0 cpu-migrations:u
                                     0.000 K/sec
          186 page-faults:u
                                      0.080 K/sec
5,739,935,525 cycles:u
                                      2.465 GHz
10,671,532,880 instructions:u
                                      1.86 IPC
1,196,623,336 branches:u
                                  # 513.870 M/sec
    1,030,678 branch-misses:u
                                      0.09%
  2.338387625 seconds time elapsed
```

```
4639.728721 task-clock:u (msec) #
                                     0.998 CPUs
            0 context-switches:u #
                                     0.000 K/sec
            0 cpu-migrations:u
                                 # 0.000 K/sec
          186 page-faults:u
                                     0.040 K/sec
11,444,184,736 cycles:u
                                     2.467 GHz
10,972,976,005 instructions:u
                                     0.96 IPC
                                 # 257.984 M/sec
1,196,977,569 branches:u
    1,030,347 branch-misses:u
                                     0.09%
  4.650327844 seconds time elapsed
```

```
value_t txl = ( i % Nx != 0 ) ? A[i-1] : tc;
      eax, DWORD PTR [rbp-20]
                                              rax, 3
                                       sal
mov
                                             rdx, [rax 8]
cdq
                                       lea
      DWORD PTR [rbp-24]
idiv
                                             rax, QWORD PTR [rbp-32]
                                       mov
      eax, edx
                                       add
                                             rax, rdx
mov
                                       movsd xmm0, QWORD PTR [rax]
test
      eax, eax
je
                                       jmp .L3
      .L2
      eax, DWORD PTR [rbp-20]
mov
cdqe
```

- ► Found instruction information on Agner Fog's blog for Intel Skylake architecture:
  - https://www.agner.org/optimize/instruction tables.pdf

inst.	operands	µорs	latency
idiv	r32	10	26
idiv	r64	57	42-95

if you want to study compiler output: <a href="https://godbolt.org/">https://godbolt.org/</a>

- root cause of the issues: single loop for multi-dimensional problem space
  - requires % operator to get boundaries (which are strided in linearized space)
  - replace with loop nest and comparison operators (>, <, ==, !=)</p>
- potentially premature optimization and violates step 1 of "Four Steps to Creating an Optimized Parallel Program"

### Tales from the Proseminar: g++ vs. gcc for C Code

```
void foo() {
                             for(int i = 0; i < 10; ++i) { }; return;
        g++
                                                                                                gcc
       push
               rbp
                                                               push
                                                                       rbp
               rbp, rsp
                                                                       rbp, rsp
       mov
                                                               mov
               DWORD PTR [rbp-4], 0
                                                                       DWORD PTR [rbp-4], 0
       mov
                                                               mov
.L3:
                                                                       .L2
                                                               jmp
               DWORD PTR [rbp-4], 9
                                                        .L3:
       cmp
               .L2
                                                                       DWORD PTR [rbp-4], 1
       jg
                                                               add
       add
               DWORD PTR [rbp-4], 1
                                                        .L2:
       jmp
               .L3
                                                                       DWORD PTR [rbp-4], 9
                                                                cmp
                                                               jle
.L2:
       nop
                                                               nop
               rbp
                                                                       rbp
       pop
                                                               pop
       ret
                                                               ret
```

### Summary

#### ▶ 13 Dwarfs of HPC

- abstract application categories
- facilitate cross-platform reasoning and cross-application component reuse
- 7 older ones, most well-studied physics problems
- ▶ 6 newer ones, partially of theoretical nature, subject to ongoing research
- give a broad perspective on HPC potential and limitations

#### "Tales from the Proseminar"

- Daniel's Weird int Problem: Don't consider all int instructions to be cheap!
- ▶ g++ vs. gcc when compiling C code

### Image Sources

- Dwarfs: <a href="http://pngimg.com/download/47261">http://pngimg.com/download/47261</a>, <a href="http://pngimg.com/download/47261">http://pngimg.com/moonshae-isles-campaign</a>.
- ▶ CRC: <a href="https://barrgroup.com/Embedded-Systems/How-To/CRC-Calculation-C-Code">https://barrgroup.com/Embedded-Systems/How-To/CRC-Calculation-C-Code</a>
- ▶ Barnes-Hut: <a href="https://en.wikipedia.org/wiki/Barnes%E2%80%93Hut\_simulation">https://en.wikipedia.org/wiki/Barnes%E2%80%93Hut\_simulation</a>
- ▶ Unstructured Mesh: <a href="https://resourcearea.cpu-24-7.com/en/numeca-welcome">https://resourcearea.cpu-24-7.com/en/numeca-welcome</a>