

# **NEURAL NETWORKS AND FUZZY SYSTEMS**

## **A DYNAMICAL SYSTEMS APPROACH TO MACHINE INTELLIGENCE**

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