INTRODUCTION

7 INTELLIGENT AGENTS

function TABLE-DRIVEN-AGENT(percept) returns an action

persistent: percepts, a sequence, initially empty

table, a table of actions, indexed by percept sequences, initially fully specified

append percept to the end of percepts $action \leftarrow LOOKUP(percepts, table)$

return action

Figure 2.3 The TABLE-DRIVEN-AGENT program is invoked for each new percept and returns an action each time. It retains the complete percept sequence in memory.

 $\textbf{function} \ \text{Reflex-Vacuum-Agent}([\textit{location}, \textit{status}]) \ \textbf{returns} \ \text{an action}$

if status = Dirty then return Suck else if location = A then return Forward else if location = B then return Backward

Figure 2.4 The agent program for a simple reflex agent in the two-location vacuum environment. This program implements the agent function tabulated in Figure ??.

```
\textbf{function} \ \textbf{SIMPLE-Reflex-Agent} (\textit{percept}) \ \textbf{returns} \ \textbf{an action}
```

persistent: rules, a set of condition–action rules

 $state \leftarrow \text{Interpret-Input}(percept)$ $rule \leftarrow \text{Rule-Match}(state, rules)$ $action \leftarrow rule. \text{Action}$

return action

Figure 2.6 A simple reflex agent. It acts according to a rule whose condition matches the current state, as defined by the percept.

```
\textbf{function} \ \ \textbf{Model-Based-Reflex-Agent} (\textit{percept}) \ \textbf{returns} \ \text{an action}
```

persistent: state, the agent's current conception of the world state

 $transition_model$, a description of how the next state depends on

the current state and action

 $sensor_model$, a description of how the current world state is reflected

in the agent's percepts

rules, a set of condition-action rules

action, the most recent action, initially none

 $state \leftarrow \texttt{UPDATE-STATE}(state, action, percept, transition_model, sensor_model)$

 $rule \leftarrow \text{RULE-MATCH}(state, rules)$

 $action \leftarrow rule. \textbf{ACTION}$

return action

Figure 2.8 A model-based reflex agent. It keeps track of the current state of the world, using an internal model. It then chooses an action in the same way as the reflex agent.

3 SOLVING PROBLEMS BY SEARCHING

```
function BEST-FIRST-SEARCH(problem, f) returns a solution node or failure
   node \leftarrow Node(problem.INITIAL)
  frontier \leftarrow a priority queue ordered by f, with node as an element
  reached \leftarrow a lookup table, with one entry with key problem.INITIAL and value node
  while not EMPTY?(frontier) do
     node \leftarrow Pop(frontier)
     if problem.Is-Goal(node.State) then return node
     for child in Expand(problem, node) do
        s \leftarrow child.\mathsf{STATE}
        if s is not in reached or child.PATH-COST < reached[s].PATH-COST then
           reached[s] \leftarrow child
           add child to frontier
  return failure
function EXPAND(problem, node) returns a list of successor nodes
  s \leftarrow node.State
  for action in problem. ACTIONS(s) do
     s' \leftarrow problem.RESULT(s, action)
      cost \leftarrow node.PATH-COST + problem.ACTION-COST(s, action, s')
     \textbf{yield} \ \mathsf{NODE}(\mathsf{STATE} = s', \mathsf{PARENT} = node, \mathsf{ACTION} = action, \mathsf{PATH}\text{-}\mathsf{COST} = cost)
```

Figure 3.7 The best-first search algorithm, and the function for expanding a node. The data structures used here are described in Section ??.

```
function BREADTH-FIRST-SEARCH(problem) returns a solution node, or failure node \leftarrow \text{NODE}(problem.\text{INITIAL})

if problem.\text{IS-GOAL}(node.\text{STATE}) then return node

frontier ← a FIFO queue, with node as an element reached \leftarrow \{problem.\text{INITIAL}\}

while not IS-EMPTY(frontier) do

node ← POP(frontier)

for child in EXPAND(problem, node) do

s \leftarrow child.\text{STATE}

if problem.\text{IS-GOAL}(s) then return child

if s is not in reached then

add s to reached

add child to frontier

return failure
```

Figure 3.8 Breadth-first search algorithm.

```
function ITERATIVE-DEEPENING-SEARCH(problem) returns a solution node, or failure
  for depth = 0 to \infty do
     result \leftarrow \text{DEPTH-LIMITED-SEARCH}(problem, depth)
     if result \neq cutoff then return result
function DEPTH-LIMITED-SEARCH(problem, \ell) returns a node or failure or cutoff
  frontier \leftarrow a LIFO queue (stack) with a node for the initial state
  result \leftarrow failure
  while not EMPTY?(frontier) do
     node \leftarrow Pop(frontier)
     if problem.IS-GOAL(node.STATE) then
       return node
     else if Depth(node) > \ell then
       result \leftarrow cutoff
     else if not IS-CYCLE(node) do
       for child in Expand(problem, node) do
          add child to frontier
  return result
```

Figure 3.12 Iterative deepening and depth-limited tree-like search. Iterative deepening repeatedly applies depth-limited search with increasing limits. It returns one of three different types of values: either a solution node, or *failure* when it has exhausted all nodes and proved there is no solution at any depth, or *cutoff* to mean there might be a solution at a deeper depth than *limit*. This is a tree-like search algorithm that does not keep track of *reached* states, and thus uses much less memory than best-first search, but runs the risk of visiting the same state multiple times on different paths. Also, if the IS-CYCLE check does not check *all* cycles, then the algorithm may get caught in a loop.

```
function BIBF-SEARCH(problem_F, f_F, problem_B, f_B) returns a solution node, or failure
   node_F \leftarrow Node(problem_F.INITIAL)
   node_B \leftarrow Node(problem_B.INITIAL)
   frontier_F \leftarrow a priority queue ordered by f_F, with node_F as an element
   frontier_B \leftarrow a priority queue ordered by f_B, with node_B as an element
   reached_F \leftarrow a lookup table, with one key node_F. STATE and value node_F
   reached_B \leftarrow a lookup table, with one key node_B. STATE and value node_B
   solution \leftarrow \text{failure}
   while not TERMINATED(solution, frontier<sub>F</sub>, frontier<sub>B</sub>) do
      if f_F(\text{TOP}(frontier_F)) < f_B(\text{TOP}(frontier_B)) then
         solution \leftarrow \mathsf{PROCEED}(F, problem_F frontier_F, reached_F, reached_B, solution)
      else
         solution \leftarrow PROCEED(B, problem_B, frontier_B, reached_B, reached_F, solution)
  return solution
\textbf{function} \ \mathsf{PROCEED}(\mathit{dir}, \mathit{problem}, \mathit{frontier}, \mathit{reached}, \mathit{reached}_2 \ \mathit{solution}) \ \textbf{returns} \ a \ \mathsf{solution}
   /* Expand node on frontier; check against the other frontier in reached<sub>2</sub>. */
   node \leftarrow Pop(frontier)
  for child in Expand(problem, node) do
      s \leftarrow child.\mathsf{STATE}
      if s not in reached or g(child) < g(reached[s]) then
         reached[s] \leftarrow child
        add child to frontier
        if s is in reached_2 then
            solution2 \leftarrow Join-Nodes(dir, child, reached2[s]))
            if g(solution2) < g(solution) then
               solution \leftarrow solution 2
   return solution
```

Figure 3.14 Bidirectional best-first search keeps two frontiers and two tables of reached states. When a path in one frontier intersects a path that was *reached* in the other half of the search, the two paths are joined (by the function JOIN-NODES) to form a potential solution. The first solution we get may not be the best; the function TERMINATED determines when to stop looking for new solutions.

```
function RECURSIVE-BEST-FIRST-SEARCH(problem) returns a solution, or failure return RBFS(problem, Node(problem.INITIAL), ∞)  

function RBFS(problem, node, f_limit) returns a solution or failure, and a new f-cost limit if problem.Is-GOAL(node.STATE) then return node successors ← EXPAND(node) if successors is empty then return failure, ∞ for s in successors do /* update f with value from previous search */ s.f ← max(s.g + s.h, node.f))  

loop do best ← the lowest f-value node in successors if best.f > f_limit then return failure, best.f alternative ← the second-lowest f-value among successors result, best.f ← RBFS(problem, best, min(f_limit, alternative)) if result ≠ failure then return result, best.f
```

Figure 3.21 The algorithm for recursive best-first search.

4 SEARCH IN COMPLEX ENVIRONMENTS

```
\begin{array}{l} \textbf{function} \ \text{Hill-Climbing}(\textit{problem}) \ \textbf{returns} \ \text{a state that is a local maximum} \\ \textit{current} \leftarrow \textit{problem}. \\ \textbf{Initial} \\ \textbf{loop do} \\ \textit{neighbor} \leftarrow \text{a highest-valued successor state of } \textit{current} \\ \textbf{if } \text{Value}(\textit{neighbor}) \leq \text{Value}(\textit{current}) \ \textbf{then return} \ \textit{current} \\ \textit{current} \leftarrow \textit{neighbor} \end{array}
```

Figure 4.2 The hill-climbing search algorithm, which is the most basic local search technique. At each step the current node is replaced by the best neighbor.

```
function Simulated-Annealing(problem, schedule) returns a solution state  \begin{array}{l} \textit{current} \leftarrow problem. \\ \textit{Initial} \\ \textbf{for} \ t = 1 \ \textbf{to} \propto \textbf{do} \\ T \leftarrow schedule(t) \\ \textbf{if} \ T = 0 \ \textbf{then return} \ current \\ next \leftarrow \\ \textit{a} \ \text{randomly selected successor of} \ current \\ \Delta E \leftarrow \\ \textit{Value}(next) - \\ \textit{Value}(current) \\ \textbf{if} \ \Delta E > 0 \ \textbf{then} \ current \leftarrow next \\ \textbf{else} \ current \leftarrow next \ \text{only with probability} \ e^{\Delta E/T} \\ \end{array}
```

Figure 4.4 The simulated annealing algorithm, a version of stochastic hill climbing where some downhill moves are allowed. The schedule input determines the value of the "temperature" T as a function of time.

```
function GENETIC-ALGORITHM(population, fitness) returns an individual
  repeat
      weights \leftarrow Weighted - By(population, fitness)
      population2 \leftarrow empty list
      for i = 1 to Size(population) do
          parent1, parent2 \leftarrow WEIGHTED-RANDOM-CHOICES(population, weights, 2)
          child \leftarrow Reproduce(parent1, parent2)
          if (small random probability) then child \leftarrow MUTATE(child)
          add child to population2
      population \leftarrow population 2
  until some individual is fit enough, or enough time has elapsed
  return the best individual in population, according to fitness
function REPRODUCE(parent1, parent2) returns an individual
  n \leftarrow \text{LENGTH}(parent1)
  c \leftarrow random number from 1 to n
  return APPEND(SUBSTRING(parent1, 1, c), SUBSTRING(parent2, c + 1, n))
```

Figure 4.7 A genetic algorithm. Within the function, *population* is an ordered list of individuals, *weights* is a list of corresponding fitness values for each individual, and *fitness* is a function to compute these values.

```
function And-Or-Search(problem) returns a conditional plan, or failure return Or-Search(problem, problem.Initial, [])

function Or-Search(problem, state, path) returns a conditional plan, or failure if problem.Is-Goal(state) then return the empty plan if Is-Cycle(path) then return failure for action in problem.Actions(state) do plan \leftarrow \text{And-Search}(problem, \text{Results}(state, action), [state] + path]) if plan \neq failure then return [action] + plan] return failure

function And-Search(problem, states, path) returns a conditional plan, or failure for s_i in states do plan_i \leftarrow \text{Or-Search}(problem, s_i, path) if plan_i = failure then return failure return [action] = failure then return failure return [action] = failure then [action] = failure return [action] = failure then [action] = failure then [action] = failure return [action] = failure then [action] = failure then [action] = failure then [action] = failure then [action] = failure return [action] = failure then [action] = fa
```

Figure 4.10 An algorithm for searching AND–OR graphs generated by nondeterministic environments. A solution is a conditional plan that considers every nondeterministic outcome and makes a plan for each one.

```
function ONLINE-DFS-AGENT(problem, s') returns an action
  persistent: result, a table mapping (s, a) to s', initially empty
               untried, a table mapping s to a list of untried actions
               unbacktracked, a table mapping s to a list of states never backtracked to
               s, a, the previous state and action, initially null
  if problem.IS-GOAL(s') then return stop
  if s' is a new state (not in untried) then untried [s'] \leftarrow problem. ACTIONS(s')
  if s is not null then
      result[s, a] \leftarrow s'
      add s to the front of unbacktracked[s']
  if untried[s'] is empty then
      if unbacktracked[s'] is empty then return stop
      else a \leftarrow an action b such that result[s', b] = POP(unbacktracked[s'])
  else a \leftarrow Pop(untried[s'])
  s \leftarrow s'
  return a
```

Figure 4.20 An online search agent that uses depth-first exploration. The agent can safely explore only in state spaces in which every action can be "undone" by some other action.

```
function LRTA*-AGENT(problem, s', h) returns an action
  persistent: result, a table mapping (s, a) to s', initially empty
                H, a table mapping s to a cost estimate, initially empty
                s, a, the previous state and action, initially null
  if Is-GOAL(s') then return stop
  if s' is a new state (not in H) then H[s'] \leftarrow h(s')
  if s is not null then
       result[s, a] \leftarrow s'
       H[s] \leftarrow \min_{b \in \mathsf{ACTIONS}(s)} \mathsf{LRTA*\text{-}COST}(s,b,\mathit{result}[s,b],H)
   a \leftarrow \text{argmin LRTA*-Cost}(problem, s', b, result[s', b], H)
       b \in ACTIONS(s)
   s \leftarrow s'
  return a
function LRTA*-Cost(problem, s, a, s', H) returns a cost estimate
  if s' is undefined then return h(s)
  else return problem. ACTION-COST(s, a, s') + H[s']
```

Figure 4.23 LRTA*-AGENT selects an action according to the values of neighboring states, which are updated as the agent moves about the state space.

5 ADVERSARIAL SEARCH AND GAMES

```
function MINIMAX-SEARCH(game, state) returns an action
  player \leftarrow game.To-Move(state)
  value, move \leftarrow MAX-VALUE(game, state)
  return move
function MAX-VALUE(game, state) returns a (utility, move) pair
  if game.Is-Terminal(state) then return game.Utility(state, player), null
  for a in game. ACTIONS(state) do
     v2, a2 \leftarrow Min-Value(game, game.Result(state, a))
     if v2 > v then
       v, move \leftarrow v2, a
  return v, move
function MIN-VALUE(game, state) returns a (utility, move) pair
  if game.Is-Terminal(state) then return game.Utility(state, player), null
  v \leftarrow +\infty
  for a in game.ACTIONS(state) do
     \textit{v2}, \textit{a2} \leftarrow \texttt{Max-Value}(\textit{game}, \textit{game}. \texttt{Result}(\textit{state}, \textit{a}))
     if v2 < v then
       v, move \leftarrow v2, a
  return v, move
```

Figure 5.3 An algorithm for calculating the optimal move using minimax—the move that leads to a terminal state with maximum utility, under the assumption that the opponent plays to minimize utility. The functions MAX-VALUE and MIN-VALUE go through the whole game tree, all the way to the leaves, to determine the backed-up value of a state and the move to get there.

```
function ALPHA-BETA-SEARCH(game, state) returns an action
   player \leftarrow game.To-Move(state)
   value, move \leftarrow \text{Max-Value}(game, state, -\infty, +\infty)
  return move
function MAX-VALUE(game, state, \alpha, \beta) returns a (utility, move) pair
  if game.Is-Terminal(state) then return game.Utility(state, player), null
   v \leftarrow -\infty
  for a in game. ACTIONS(state) do
      v2, a2 \leftarrow \text{Min-Value}(game, game. \text{Result}(state, a), \alpha, \beta)
     if v2 > v then
        v, move \leftarrow v2, a
        \alpha \leftarrow \text{MAX}(\alpha, v)
     if v \geq \beta then return v, move
  return v, move
function MIN-VALUE(game, state, \alpha, \beta) returns a (utility, move) pair
  if game.Is-Terminal(state) then return game.Utility(state, player), null
   v \leftarrow +\infty
  for a in game. ACTIONS (state) do
      v2,\,a2 \leftarrow \texttt{Max-Value}(game,\,game.\texttt{Result}(state,\,a),\alpha,\beta)
     if v2 < v then
        v, move \leftarrow v2, a
        \beta \leftarrow \text{Min}(\beta, v)
     if v \leq \alpha then return v, move
   return v, move
```

Figure 5.7 The alpha–beta search algorithm. Notice that these functions are the same as the MINIMAX-SEARCH functions in Figure 5.3, except that we maintain bounds in the variables α and β , and use them to cut off search when a value is outside the bounds.

```
function Monte-Carlo-Tree-Search(state) returns an action tree \leftarrow \text{Node}(state)
while Time-Remaining() do leaf \leftarrow \text{Select}(tree)
child \leftarrow \text{Expand}(leaf)
result \leftarrow \text{Simulate}(child)
Backpropagate(result, child)
return the move in Actions(state) whose node has highest number of playouts
```

Figure 5.11 The Monte Carlo tree search algorithm. A game tree, *tree*, is initialized, and then we repeat a cycle of SELECT / EXPAND / SIMULATE / BACKPROPAGATE until we run out of time, and return the move that led to the node with the highest number of playouts.

6 CONSTRAINT SATISFACTION PROBLEMS

```
function AC-3(csp) returns false if an inconsistency is found and true otherwise
  inputs: csp, a binary CSP with components (X, D, C)
  local variables: queue, a queue of arcs, initially all the arcs in csp
  while queue is not empty do
     (X_i, X_j) \leftarrow Pop(queue)
     if REVISE(csp, X_i, X_j) then
       if size of D_i = 0 then return false
       for X_k in X_i.Neighbors - \{X_j\} do add (X_k,\ X_i) to \mathit{queue}
  \mathbf{return}\ true
function REVISE(csp, X_i, X_j) returns true iff we revise the domain of X_i
  revised \leftarrow false
  for x in D_i do
     if no value y in D_j allows (x,y) to satisfy the constraint between X_i and X_j then
       delete x from D_i
        revised \leftarrow true
  return revised
```

Figure 6.3 The arc-consistency algorithm AC-3. After applying AC-3, either every arc is arc-consistent, or some variable has an empty domain, indicating that the CSP cannot be solved. The name "AC-3" was used by the algorithm's inventor (?) because it was the third version developed in the paper.

```
function BACKTRACKING-SEARCH(csp) returns a solution, or failure
  return BACKTRACK(csp, { })
function BACKTRACK(csp, assignment) returns a solution, or failure
  if assignment is complete then return assignment
  var \leftarrow Select-Unassigned-Variable(csp, assignment)
  for value in Order-Domain-Values(csp, var, assignment) do
      if value is consistent with assignment then
         add \{var = value\} to assignment
         inferences \leftarrow Inference(csp, var, assignment)
         if inferences \neq failure then
            add inferences to assignment
            result \leftarrow BACKTRACK(csp, assignment)
           if result \neq failure then
              return result
      remove \{var = value\} and inferences from assignment
  return failure
```

Figure 6.5 A simple backtracking algorithm for constraint satisfaction problems. The algorithm is modeled on the recursive depth-first search of Chapter 3. By varying the functions SELECT-UNASSIGNED-VARIABLE and ORDER-DOMAIN-VALUES, we can implement the general-purpose heuristics discussed in the text. The function INFERENCE can optionally be used to impose arc-, path-, or *k*-consistency, as desired. If a value choice leads to failure (noticed either by INFERENCE or by BACKTRACK), then value assignments (including those made by INFERENCE) are removed from the current assignment and a new value is tried.

```
function MIN-CONFLICTS(csp, max\_steps) returns a solution or failure inputs: csp, a constraint satisfaction problem max\_steps, the number of steps allowed before giving up current \leftarrow \text{an initial complete assignment for } csp for i=1 to max\_steps do
    if current is a solution for csp then return current var \leftarrow a randomly chosen conflicted variable from csp. Variables value \leftarrow the value v for var that minimizes Conflicts(csp, var, v, current) set var = value in current return failure
```

Figure 6.9 The MIN-CONFLICTS local search algorithm for CSPs. The initial state may be chosen randomly or by a greedy assignment process that chooses a minimal-conflict value for each variable in turn. The CONFLICTS function counts the number of constraints violated by a particular value, given the rest of the current assignment.

```
inputs: csp, a CSP with components X, D, C

n \leftarrow \text{number of variables in } X

assignment \leftarrow \text{an empty assignment}

root \leftarrow \text{any variable in } X

X \leftarrow \text{TOPOLOGICALSORT}(X, root)

for j = n down to 2 do

MAKE-ARC-CONSISTENT(PARENT(X_j), X_j)

if it cannot be made consistent then return failure

for i = 1 to n do

assignment[X_i] \leftarrow \text{any consistent value from } D_i
```

if there is no consistent value then return failure

 ${\bf return} \ assignment$

function TREE-CSP-SOLVER(csp) **returns** a solution, or failure

Figure 6.11 The TREE-CSP-SOLVER algorithm for solving tree-structured CSPs. If the CSP has a solution, we will find it in linear time; if not, we will detect a contradiction.

LOGICAL AGENTS

function KB-AGENT(percept) **returns** an action **persistent**: KB, a knowledge base t, a counter, initially 0, indicating time $\text{TELL}(KB, \text{MAKE-PERCEPT-SENTENCE}(percept, t)) \\ action \leftarrow \text{Ask}(KB, \text{MAKE-ACTION-QUERY}(t)) \\ \text{TELL}(KB, \text{MAKE-ACTION-SENTENCE}(action, t)) \\ t \leftarrow t + 1 \\ \textbf{return} \ action$

Figure 7.1 A generic knowledge-based agent. Given a percept, the agent adds the percept to its knowledge base, asks the knowledge base for the best action, and tells the knowledge base that it has in fact taken that action.

```
function TT-ENTAILS?(KB, α) returns true or false
inputs: KB, the knowledge base, a sentence in propositional logic
   α, the query, a sentence in propositional logic

symbols ← a list of the proposition symbols in KB and α

return TT-CHECK-ALL(KB, α, symbols, { } })

function TT-CHECK-ALL(KB, α, symbols, model) returns true or false
if EMPTY?(symbols) then
   if PL-TRUE?(KB, model) then return PL-TRUE?(α, model)
   else return true || when KB is false, always return true
else do
   P ← FIRST(symbols)
   rest ← REST(symbols)
   return (TT-CHECK-ALL(KB, α, rest, model ∪ {P = true}))
   and
   TT-CHECK-ALL(KB, α, rest, model ∪ {P = false})))
```

Figure 7.8 A truth-table enumeration algorithm for deciding propositional entailment. (TT stands for truth table.) PL-TRUE? returns *true* if a sentence holds within a model. The variable *model* represents a partial model—an assignment to some of the symbols. The keyword "and" is used here as a logical operation on its two arguments, returning *true* or *false*.

```
 \begin{array}{l} \textbf{function} \ \text{PL-RESOLUTION}(KB,\alpha) \ \textbf{returns} \ true \ \text{or} \ false \\ \textbf{inputs}: \ KB, \ \text{the knowledge base, a sentence in propositional logic} \\ \alpha, \ \text{the query, a sentence in propositional logic} \\ clauses \leftarrow \text{the set of clauses in the CNF representation of} \ KB \land \neg \alpha \\ new \leftarrow \{ \} \\ \textbf{loop do} \\ \textbf{for pair of clauses} \ C_i, \ C_j \ \textbf{in} \ clauses \ \textbf{do} \\ resolvents \leftarrow \text{PL-RESOLVE}(C_i, C_j) \\ \textbf{if} \ resolvents \ \text{contains the empty clause} \ \textbf{then return} \ true \\ new \leftarrow new \cup resolvents \\ \textbf{if} \ new \subseteq clauses \ \textbf{then return} \ false \\ clauses \leftarrow clauses \cup new \\ \end{array}
```

Figure 7.9 A simple resolution algorithm for propositional logic. The function PL-RESOLVE returns the set of all possible clauses obtained by resolving its two inputs.

```
function PL-FC-ENTAILS?(KB,q) returns true or false
inputs: KB, the knowledge base, a set of propositional definite clauses q, the query, a proposition symbol count \leftarrow a table, where count[c] is the number of symbols in c's premise inferred \leftarrow a table, where inferred[s] is initially false for all symbols agenda \leftarrow a queue of symbols, initially symbols known to be true in KB

while agenda is not empty do
p \leftarrow Pop(agenda)
if p = q then return true
if inferred[p] = false then
inferred[p] \leftarrow true
for clause c in k where p is in c.PREMISE do
decrement <math>count[c]
if count[c] = 0 then add c.CONCLUSION to agenda
return false
```

Figure 7.12 The forward-chaining algorithm for propositional logic. The agenda keeps track of symbols known to be true but not yet "processed." The count table keeps track of how many premises of each implication are as yet unknown. Whenever a new symbol p from the agenda is processed, the count is reduced by one for each implication in whose premise p appears (easily identified in constant time with appropriate indexing.) If a count reaches zero, all the premises of the implication are known, so its conclusion can be added to the agenda. Finally, we need to keep track of which symbols have been processed; a symbol that is already in the set of inferred symbols need not be added to the agenda again. This avoids redundant work and prevents loops caused by implications such as $P \Rightarrow Q$ and $Q \Rightarrow P$.

```
function DPLL-SATISFIABLE?(s) returns true or false inputs: s, a sentence in propositional logic clauses \leftarrow \text{the set of clauses in the CNF representation of } s symbols \leftarrow \text{a list of the proposition symbols in } s return \text{ DPLL}(clauses, symbols, f) function \text{ DPLL}(clauses, symbols, model) \text{ returns } true \text{ or } false if every clause in clauses is true in model then return true if some clause in clauses is false in model then return false P, value \leftarrow \text{FIND-Pure-Symbol}(symbols, clauses, model) if P is non-null then return DPLL(clauses, symbols − P, model \cup \{P=value\}\}) P, value \leftarrow \text{FIND-UNIT-CLAUSE}(clauses, model) if P is non-null then return DPLL(clauses, symbols − P, model \cup \{P=value\}\}) P \leftarrow \text{FIRST}(symbols); rest \leftarrow \text{REST}(symbols) return DPLL(clauses, rest, model \cup \{P=true\}\}) or \text{DPLL}(clauses, rest, model \cup \{P=false\}\})
```

Figure 7.14 The DPLL algorithm for checking satisfiability of a sentence in propositional logic. The ideas behind FIND-PURE-SYMBOL and FIND-UNIT-CLAUSE are described in the text; each returns a symbol (or null) and the truth value to assign to that symbol. Like TT-ENTAILS?, DPLL operates over partial models.

```
function WALKSAT(clauses, p, max\_flips) returns a satisfying model or failure

inputs: clauses, a set of clauses in propositional logic

p, the probability of choosing to do a "random walk" move, typically around 0.5

max\_flips, number of flips allowed before giving up

model \leftarrow a random assignment of true/false to the symbols in clauses

for i=1 to max\_flips do

if model satisfies clauses then return model

clause \leftarrow a randomly selected clause from clauses that is false in model

with probability p flip the value in model of a randomly selected symbol from clause

else flip whichever symbol in clause maximizes the number of satisfied clauses

return failure
```

Figure 7.15 The WALKSAT algorithm for checking satisfiability by randomly flipping the values of variables. Many versions of the algorithm exist.

```
function Hybrid-Wumpus-Agent(percept) returns an action
  inputs: percept, a list, [stench,breeze,glitter,bump,scream]
  persistent: KB, a knowledge base, initially the atemporal "wumpus physics"
                t, a counter, initially 0, indicating time
               plan, an action sequence, initially empty
  Tell(KB, Make-Percept-Sentence(percept, t))
  TELL the KB the temporal "physics" sentences for time t
   safe \leftarrow \{[x, y] : ASK(KB, OK_{x,y}^t) = true\}
  if Ask(KB, Glitter^t) = true then
     plan \leftarrow [Grab] + PLAN-ROUTE(current, \{[1,1]\}, safe) + [Climb]
  if plan is empty then
     unvisited \leftarrow \{[x, y] : ASK(KB, L_{x,y}^{t'}) = false \text{ for all } t' \leq t\}
     plan \leftarrow PLAN-ROUTE(current, unvisited \cap safe, safe)
  if plan is empty and Ask(KB, HaveArrow^t) = true then
     possible\_wumpus \leftarrow \{[x, y] : Ask(KB, \neg W_{x,y}) = false\}
     plan \leftarrow PLAN-SHOT(current, possible\_wumpus, safe)
  if plan is empty then // no choice but to take a risk
     \textit{not\_unsafe} \leftarrow \{[x,y] \; : \; \mathsf{ASK}(\mathit{KB}, \neg \; \mathit{OK}^t_{x,y}) = \mathit{false}\}
     plan \leftarrow Plan-Route(current, unvisited \cap not\_unsafe, safe)
  if plan is empty then
     plan \leftarrow PLAN-ROUTE(current, \{[1, 1]\}, safe) + [Climb]
   action \leftarrow Pop(plan)
  Tell(KB, Make-Action-Sentence(action, t))
   t \leftarrow t + 1
  return action
\textbf{function} \ \text{PLAN-ROUTE}(current, goals, allowed) \ \textbf{returns} \ \text{an action sequence}
  inputs: current, the agent's current position
           goals, a set of squares; try to plan a route to one of them
           allowed, a set of squares that can form part of the route
  problem \leftarrow ROUTE-PROBLEM(current, goals, allowed)
  return A*-GRAPH-SEARCH(problem)
```

Figure 7.17 A hybrid agent program for the wumpus world. It uses a propositional knowledge base to infer the state of the world, and a combination of problem-solving search and domain-specific code to decide what actions to take.

Figure 7.19 The SATPLAN algorithm. The planning problem is translated into a CNF sentence in which the goal is asserted to hold at a fixed time step t and axioms are included for each time step up to t. If the satisfiability algorithm finds a model, then a plan is extracted by looking at those proposition symbols that refer to actions and are assigned true in the model. If no model exists, then the process is repeated with the goal moved one step later.

FIRST-ORDER LOGIC

9 INFERENCE IN FIRST-ORDER LOGIC

```
function UNIFY(x, y, \theta) returns a substitution to make x and y identical
  inputs: x, a variable, constant, list, or compound expression
           y, a variable, constant, list, or compound expression
          \theta, the substitution built up so far (optional, defaults to empty)
  if \theta = failure then return failure
  else if x = y then return \theta
  else if Variable?(x) then return Unify-Var(x, y, \theta)
  else if Variable?(y) then return Unify-Var(y, x, \theta)
  else if COMPOUND?(x) and COMPOUND?(y) then
      return UNIFY(x.ARGS, y.ARGS, UNIFY(x.OP, y.OP, \theta))
  else if LIST?(x) and LIST?(y) then
      return UNIFY(x.REST, y.REST, UNIFY(x.FIRST, y.FIRST, \theta))
  else return failure
function UNIFY-VAR(var, x, \theta) returns a substitution
  if \{var/val\} \in \theta then return UNIFY(val, x, \theta)
  else if \{x/val\} \in \theta then return UNIFY(var, val, \theta)
  else if OCCUR-CHECK?(var, x) then return failure
  else return add \{var/x\} to \theta
```

Figure 9.1 The unification algorithm. The algorithm works by comparing the structures of the inputs, element by element. The substitution θ that is the argument to UNIFY is built up along the way and is used to make sure that later comparisons are consistent with bindings that were established earlier. In a compound expression such as F(A,B), the OP field picks out the function symbol F and the ARGS field picks out the argument list (A,B).

```
function FOL-FC-ASK(KB, \alpha) returns a substitution or false
  inputs: KB, the knowledge base, a set of first-order definite clauses
             \alpha, the query, an atomic sentence
  local variables: new, the new sentences inferred on each iteration
   repeat until new is empty
        new \leftarrow \{ \}
        for rule in KB do
            (p_1 \wedge \ldots \wedge p_n \Rightarrow q) \leftarrow \text{STANDARDIZE-VARIABLES}(rule)
            for \theta such that SUBST(\theta, p_1 \land \ldots \land p_n) = \text{SUBST}(\theta, p'_1 \land \ldots \land p'_n)
                          for some p'_1, \ldots, p'_n in KB
                q' \leftarrow \text{SUBST}(\theta, q)
                if q' does not unify with some sentence already in KB or new then
                     add q' to new
                     \phi \leftarrow \text{UNIFY}(q', \alpha)
                     if \phi is not fail then return \phi
        add new to KB
  return false
```

Figure 9.3 A conceptually straightforward, but inefficient, forward-chaining algorithm. On each iteration, it adds to KB all the atomic sentences that can be inferred in one step from the implication sentences and the atomic sentences already in KB. The function STANDARDIZE-VARIABLES replaces all variables in its arguments with new ones that have not been used before.

```
function FOL-BC-ASK(KB, query) returns a generator of substitutions return FOL-BC-OR(KB, query, \{\})

generator FOL-BC-OR(KB, goal, \theta) yields a substitution for rule (lhs \Rightarrow rhs) in FETCH-RULES-FOR-GOAL(KB, goal) do (lhs, rhs) \leftarrow STANDARDIZE-VARIABLES((lhs, rhs)) for \theta' in FOL-BC-AND(KB, lhs, UNIFY(rhs, goal, \theta)) do yield \theta'

generator FOL-BC-AND(KB, goals, \theta) yields a substitution if \theta = failure then return else if LENGTH(goals) = 0 then yield \theta else do

first, rest \leftarrow FIRST(goals), REST(goals)
for \theta' in FOL-BC-OR(KB, SUBST(\theta, first), \theta) do
for \theta'' in FOL-BC-AND(KB, rest, \theta') do
yield \theta''
```

Figure 9.6 A simple backward-chaining algorithm for first-order knowledge bases.

```
procedure APPEND(ax, y, az, continuation)

trail \leftarrow \text{Global-Trail-Pointer}()

if ax = [] and \text{Unify}(y, az) then \text{Call}(continuation)

RESET-Trail(trail)

a, x, z \leftarrow \text{New-Variable}(), \text{New-Variable}(), \text{New-Variable}()

if \text{Unify}(ax, [a \mid x]) and \text{Unify}(az, [a \mid z]) then \text{Append}(x, y, z, continuation)
```

Figure 9.8 Pseudocode representing the result of compiling the Append predicate. The function NEW-VARIABLE returns a new variable, distinct from all other variables used so far. The procedure Call(continuation) continues execution with the specified continuation.

10 KNOWLEDGE REPRESENTATION

AUTOMATED PLANNING

```
Init(At(C_1, SFO) \wedge At(C_2, JFK) \wedge At(P_1, SFO) \wedge At(P_2, JFK) \\ \wedge Cargo(C_1) \wedge Cargo(C_2) \wedge Plane(P_1) \wedge Plane(P_2) \\ \wedge Airport(JFK) \wedge Airport(SFO)) \\ Goal(At(C_1, JFK) \wedge At(C_2, SFO)) \\ Action(Load(c, p, a), \\ PRECOND: At(c, a) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a) \\ Effect: \neg At(c, a) \wedge In(c, p)) \\ Action(Unload(c, p, a), \\ PRECOND: In(c, p) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a) \\ Effect: At(c, a) \wedge \neg In(c, p)) \\ Action(Fly(p, from, to), \\ PRECOND: At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to) \\ Effect: \neg At(p, from) \wedge At(p, to))
```

Figure 11.1 A PDDL description of an air cargo transportation planning problem.

```
Init(Tire(Flat) \land Tire(Spare) \land At(Flat, Axle) \land At(Spare, Trunk))
Goal(At(Spare, Axle))
Action(Remove(obj, loc),
PRECOND: At(obj, loc) \land At(obj, Ground))
Action(PutOn(t, Axle),
PRECOND: Tire(t) \land At(t, Ground) \land \neg At(Flat, Axle) \land \neg At(Spare, Axle)
Effect: \neg At(t, Ground) \land At(t, Axle))
Action(LeaveOvernight,
PRECOND:
Effect: \neg At(Spare, Ground) \land \neg At(Spare, Axle) \land \neg At(Spare, Trunk)
\land \neg At(Flat, Ground) \land \neg At(Flat, Axle) \land \neg At(Flat, Trunk))
```

Figure 11.2 The simple spare tire problem.

```
Init(On(A, Table) \land On(B, Table) \land On(C, A) \\ \land Block(A) \land Block(B) \land Block(C) \land Clear(B) \land Clear(C) \land Clear(Table)) \\ Goal(On(A, B) \land On(B, C)) \\ Action(Move(b, x, y), \\ \text{PRECOND: } On(b, x) \land Clear(b) \land Clear(y) \land Block(b) \land Block(y) \land \\ (b \neq x) \land (b \neq y) \land (x \neq y), \\ \text{Effect: } On(b, y) \land Clear(x) \land \neg On(b, x) \land \neg Clear(y)) \\ Action(MoveToTable(b, x), \\ \text{PRECOND: } On(b, x) \land Clear(b) \land Block(b) \land Block(x), \\ \text{Effect: } On(b, Table) \land Clear(x) \land \neg On(b, x)) \\ \end{cases}
```

Figure 11.3 A planning problem in the blocks world: building a three-block tower. One solution is the sequence [MoveToTable(C, A), Move(B, Table, C), Move(A, Table, B)].

```
Refinement(Go(Home, SFO), \\ STEPS: [Drive(Home, SFOLongTermParking), \\ Shuttle(SFOLongTermParking, SFO)]) \\ Refinement(Go(Home, SFO), \\ STEPS: [Taxi(Home, SFO)]) \\ \hline \\ Refinement(Navigate([a, b], [x, y]), \\ PRECOND: a = x \land b = y \\ STEPS: []) \\ Refinement(Navigate([a, b], [x, y]), \\ PRECOND: Connected([a, b], [a - 1, b]) \\ STEPS: [Left, Navigate([a - 1, b], [x, y])]) \\ Refinement(Navigate([a, b], [x, y]), \\ PRECOND: Connected([a, b], [a + 1, b]) \\ STEPS: [Right, Navigate([a + 1, b], [x, y])]) \\ \cdots
```

Figure 11.7 Definitions of possible refinements for two high-level actions: going to San Francisco airport and navigating in the vacuum world. In the latter case, note the recursive nature of the refinements and the use of preconditions.

```
function HIERARCHICAL-SEARCH(problem, hierarchy) returns a solution, or failure frontier \leftarrow a FIFO queue with [Act] as the only element loop do

if EMPTY?(frontier) then return failure plan \leftarrow POP(frontier) /* chooses the shallowest plan in frontier */ hla \leftarrow the first HLA in plan, or null if none prefix,suffix \leftarrow the action subsequences before and after hla in plan outcome \leftarrow RESULT(problem.INITIAL, prefix)

if hla is null then /* so plan is primitive and outcome is its result */

if outcome satisfies problem.GOAL then return plan
else for each sequence in REFINEMENTS(hla, outcome, hierarchy) do
frontier \leftarrow Insert(APPEND(prefix, sequence, suffix), frontier)
```

Figure 11.8 A breadth-first implementation of hierarchical forward planning search. The initial plan supplied to the algorithm is [Act]. The REFINEMENTS function returns a set of action sequences, one for each refinement of the HLA whose preconditions are satisfied by the specified state, outcome.

```
function ANGELIC-SEARCH(problem, hierarchy, initialPlan) returns solution or fail
  frontier \leftarrow a FIFO queue with initialPlan as the only element
  loop do
      if Empty?( frontier) then return fail
       plan \leftarrow Pop(frontier) /* chooses the shallowest node in frontier */
       if REACH^+(problem.Initial, plan) intersects problem.GOAL then
          if plan is primitive then return plan /* REACH<sup>+</sup> is exact for primitive plans */
           guaranteed \leftarrow REACH^-(problem.INITIAL, plan) \cap problem.GOAL
           if guaranteed \neq \{\} and MAKING-PROGRESS(plan, initialPlan\}) then
               finalState \leftarrow any element of guaranteed
               \textbf{return} \ \mathsf{DECOMPOSE}(hierarchy, problem. \mathsf{INITIAL}, plan, final State)
           hla \leftarrow \text{some HLA in } plan
           prefix, suffix \leftarrow the action subsequences before and after hla in plan
          for sequence in REFINEMENTS(hla, outcome, hierarchy) do
               frontier \leftarrow Insert(APPEND(prefix, sequence, suffix), frontier)
function Decompose(hierarchy, s_0, plan, s_f) returns a solution
   solution \leftarrow an empty plan
  while plan is not empty do
     action \leftarrow Remove-Last(plan)
     s_i \leftarrow a state in REACH<sup>-</sup>(s_0, plan) such that s_f \in REACH^-(s_i, action)
     problem \leftarrow a problem with INITIAL = s_i and GOAL = s_f
     solution \leftarrow Append(Angelic-Search(problem, hierarchy, action), solution)
     s_f \leftarrow s_i
  return solution
```

Figure 11.11 A hierarchical planning algorithm that uses angelic semantics to identify and commit to high-level plans that work while avoiding high-level plans that don't. The predicate MAKING-PROGRESS checks to make sure that we aren't stuck in an infinite regression of refinements. At top level, call ANGELIC-SEARCH with [Act] as the initialPlan.

```
Jobs(\{AddEngine1 \prec AddWheels1 \prec Inspect1\},\\ \{AddEngine2 \prec AddWheels2 \prec Inspect2\})
Resources(EngineHoists(1), WheelStations(1), Inspectors(2), LugNuts(500))
Action(AddEngine1, Duration:30,\\ Use: EngineHoists(1))
Action(AddEngine2, Duration:60,\\ Use: EngineHoists(1))
Action(AddWheels1, Duration:30,\\ Consume: LugNuts(20), Use: WheelStations(1))
Action(AddWheels2, Duration:15,\\ Consume: LugNuts(20), Use: WheelStations(1))
Action(Inspect_i, Duration:10,\\ Use: Inspectors(1))
```

Figure 11.13 A job-shop scheduling problem for assembling two cars, with resource constraints. The notation $A \prec B$ means that action A must precede action B.

12 QUANTIFYING UNCERTAINTY

function DT-AGENT(percept) returns an action

persistent: belief_state, probabilistic beliefs about the current state of the world action, the agent's action

update belief_state based on action and percept calculate outcome probabilities for actions, given action descriptions and current belief_state select action with highest expected utility given probabilities of outcomes and utility information return action

Figure 12.1 A decision-theoretic agent that selects rational actions.

13 PROBABILISTIC REASONING

```
function ENUMERATION-ASK(X, \mathbf{e}, bn) returns a distribution over X
  inputs: X, the query variable
            e, observed values for variables E
            bn, a Bayes net with variables \{X\} \cup \mathbf{E} \cup \mathbf{Y} / \star \mathbf{Y} = hidden \ variables \star /
   \mathbf{Q}(X) \leftarrow a distribution over X, initially empty
   for value x_i of X do
       \mathbf{Q}(x_i) \leftarrow \text{ENUMERATE-ALL}(bn.\text{VARS}, \mathbf{e}_{x_i})
            where \mathbf{e}_{x_i} is \mathbf{e} extended with X = x_i
   return Normalize(\mathbf{Q}(X))
function ENUMERATE-ALL(vars, e) returns a real number
  if Empty?(vars) then return 1.0
   Y \leftarrow \mathsf{FIRST}(vars)
   if Y has value y in e
       then return P(y \mid parents(Y)) \times \text{Enumerate-All(Rest(}vars), \mathbf{e})
       else return \sum_y P(y \mid parents(Y)) \times \text{Enumerate-All(Rest(\it{vars}), e}_y)
            where \mathbf{e}_y is \mathbf{e} extended with Y = y
```

Figure 13.10 The enumeration algorithm for answering queries on Bayes nets.

```
function ELIMINATION-ASK(X, \mathbf{e}, bn) returns a distribution over X inputs: X, the query variable \mathbf{e}, observed values for variables \mathbf{E} bn, a Bayesian network specifying joint distribution \mathbf{P}(X_1, \dots, X_n) factors \leftarrow [] for var in ORDER(bn.VARS) do factors \leftarrow [MAKE-FACTOR(var, \mathbf{e})|factors] if var is a hidden variable then factors \leftarrow SUM-OUT(var, factors) return NORMALIZE(POINTWISE-PRODUCT(factors))
```

Figure 13.11 The variable elimination algorithm for inference in Bayes nets.

```
function PRIOR-SAMPLE(bn) returns an event sampled from the prior specified by bn inputs: bn, a Bayesian network specifying joint distribution \mathbf{P}(X_1,\ldots,X_n) \mathbf{x}\leftarrow an event with n elements for variable X_i in X_1,\ldots,X_n do \mathbf{x}[i]\leftarrow a random sample from \mathbf{P}(X_i\mid\ parents(X_i)) return \mathbf{x}
```

Figure 13.14 A sampling algorithm that generates events from a Bayesian network. Each variable is sampled according to the conditional distribution given the values already sampled for the variable's parents.

```
function REJECTION-SAMPLING(X, \mathbf{e}, bn, N) returns an estimate of \mathbf{P}(X \mid \mathbf{e}) inputs: X, the query variable \mathbf{e}, observed values for variables \mathbf{E} bn, a Bayesian network N, the total number of samples to be generated local variables: \mathbf{N}, a vector of counts for each value of X, initially zero for j=1 to N do \mathbf{x} \leftarrow \text{PRIOR-SAMPLE}(bn) if \mathbf{x} is consistent with \mathbf{e} then \mathbf{N}[x] \leftarrow \mathbf{N}[x] + 1 where x is the value of X in \mathbf{x} return \text{NORMALIZE}(\mathbf{N})
```

Figure 13.15 The rejection-sampling algorithm for answering queries given evidence in a Bayesian network.

```
function LIKELIHOOD-WEIGHTING(X, \mathbf{e}, bn, N) returns an estimate of \mathbf{P}(X \mid \mathbf{e})
  inputs: X, the query variable
            e, observed values for variables E
            bn, a Bayesian network specifying joint distribution P(X_1, \dots, X_n)
            N, the total number of samples to be generated
  local variables: W, a vector of weighted counts for each value of X, initially zero
  for j = 1 to N do
       \mathbf{x}, w \leftarrow \text{Weighted-Sample}(bn, \mathbf{e})
       \mathbf{W}[x] \leftarrow \mathbf{W}[x] + w where x is the value of X in \mathbf{x}
  return NORMALIZE(W)
function WEIGHTED-SAMPLE(bn, \mathbf{e}) returns an event and a weight
  w \leftarrow 1; \mathbf{x} \leftarrow an event with n elements initialized from \mathbf{e}
  for variable X_i in X_1, \ldots, X_n do
       if X_i is an evidence variable with value x_i in e
            then w \leftarrow w \times P(X_i = x_i \mid parents(X_i))
            else \mathbf{x}[i] \leftarrow a random sample from \mathbf{P}(X_i \mid parents(X_i))
  return x, w
```

Figure 13.16 The likelihood-weighting algorithm for inference in Bayesian networks. In WEIGHTED-SAMPLE, each nonevidence variable is sampled according to the conditional distribution given the values already sampled for the variable's parents, while a weight is accumulated based on the likelihood for each evidence variable.

```
function GIBBS-ASK(X, \mathbf{e}, bn, N) returns an estimate of \mathbf{P}(X \mid \mathbf{e}) local variables: \mathbf{N}, a vector of counts for each value of X, initially zero \mathbf{Z}, the nonevidence variables in bn \mathbf{x}, the current state of the network, initially copied from \mathbf{e} initialize \mathbf{x} with random values for the variables in \mathbf{Z} for j=1 to N do choose any variable Z_i from \mathbf{Z} according to any distribution \rho(i) set the value of Z_i in \mathbf{x} by sampling from \mathbf{P}(Z_i \mid mb(Z_i)) \mathbf{N}[x] \leftarrow \mathbf{N}[x] + 1 where x is the value of X in \mathbf{x} return NORMALIZE(\mathbf{N})
```

Figure 13.18 The Gibbs sampling algorithm for approximate inference in Bayes nets; this version cycles through the variables, but choosing variables at random also works.

14 PROBABILISTIC REASONING OVER TIME

```
function FORWARD-BACKWARD(\mathbf{ev}, prior) returns a vector of probability distributions inputs: \mathbf{ev}, a vector of evidence values for steps 1, \dots, t prior, the prior distribution on the initial state, \mathbf{P}(\mathbf{X}_0) local variables: \mathbf{fv}, a vector of forward messages for steps 0, \dots, t \mathbf{b}, a representation of the backward message, initially all 1s \mathbf{sv}, a vector of smoothed estimates for steps 1, \dots, t \mathbf{fv}[0] \leftarrow prior \mathbf{for} \ i = 1 \ \mathbf{to} \ t \ \mathbf{do} \mathbf{fv}[i] \leftarrow \mathrm{FORWARD}(\mathbf{fv}[i-1], \mathbf{ev}[i]) \mathbf{for} \ i = t \ \mathbf{downto} \ 1 \ \mathbf{do} \mathbf{sv}[i] \leftarrow \mathrm{NORMALIZE}(\mathbf{fv}[i] \times \mathbf{b}) \mathbf{b} \leftarrow \mathrm{BACKWARD}(\mathbf{b}, \mathbf{ev}[i]) return \mathbf{sv}
```

Figure 14.4 The forward–backward algorithm for smoothing: computing posterior probabilities of a sequence of states given a sequence of observations. The FORWARD and BACKWARD operators are defined by Equations (??) and (??), respectively.

```
function FIXED-LAG-SMOOTHING(e_t, hmm, d) returns a distribution over \mathbf{X}_{t-d}
   inputs: e_t, the current evidence for time step t
             hmm, a hidden Markov model with S \times S transition matrix T
              d, the length of the lag for smoothing
   persistent: t, the current time, initially 1
                  f, the forward message P(X_t | e_{1:t}), initially hmm.PRIOR
                  B, the d-step backward transformation matrix, initially the identity matrix
                  e_{t-d:t}, double-ended list of evidence from t-d to t, initially empty
   local variables: O_{t-d}, O_t, diagonal matrices containing the sensor model information
   add e_t to the end of e_{t-d:t}
   \mathbf{O}_t \leftarrow \text{diagonal matrix containing } \mathbf{P}(e_t \mid X_t)
   if t > d then
       \mathbf{f} \leftarrow \text{FORWARD}(\mathbf{f}, e_{t-d})
       remove e_{t-d-1} from the beginning of e_{t-d:t}
        \mathbf{O}_{t-d} \leftarrow \text{diagonal matrix containing } \mathbf{P}(e_{t-d} \mid X_{t-d})
        \mathbf{B} \leftarrow \mathbf{O}_{t-d}^{-1} \mathbf{T}^{-1} \mathbf{B} \mathbf{T} \mathbf{O}_t
   else \mathbf{B} \leftarrow \mathbf{BTO}_t
   t \leftarrow t + 1
   if t > d+1 then return Normalize(\mathbf{f} \times \mathbf{B1}) else return null
```

Figure 14.6 An algorithm for smoothing with a fixed time lag of d steps, implemented as an online algorithm that outputs the new smoothed estimate given the observation for a new time step. Notice that the final output NORMALIZE($\mathbf{f} \times \mathbf{B1}$) is just $\alpha \mathbf{f} \times \mathbf{b}$, by Equation (??).

```
function Particle-Filtering(\mathbf{e}, N, dbn) returns a set of samples for the next time step inputs: \mathbf{e}, the new incoming evidence N, the number of samples to be maintained dbn, a DBN defined by \mathbf{P}(\mathbf{X}_0), \mathbf{P}(\mathbf{X}_1 \mid \mathbf{X}_0), and \mathbf{P}(\mathbf{E}_1 \mid \mathbf{X}_1) persistent: S, a vector of samples of size N, initially generated from \mathbf{P}(\mathbf{X}_0) local variables: W, a vector of weights of size N for i=1 to N do S[i] \leftarrow \text{sample from } \mathbf{P}(\mathbf{X}_1 \mid \mathbf{X}_0 = S[i]) \quad /* \text{ step } 1 */ \\ W[i] \leftarrow \mathbf{P}(\mathbf{e} \mid \mathbf{X}_1 = S[i]) \qquad /* \text{ step } 2 */ \\ S \leftarrow \text{WEIGHTED-SAMPLE-WITH-REPLACEMENT}(N, S, W) \qquad /* \text{ step } 3 */ \\ \mathbf{return} S
```

Figure 14.17 The particle filtering algorithm implemented as a recursive update operation with state (the set of samples). Each of the sampling operations involves sampling the relevant slice variables in topological order, much as in PRIOR-SAMPLE. The WEIGHTED-SAMPLE-WITH-REPLACEMENT operation can be implemented to run in O(N) expected time. The step numbers refer to the description in the text.

15 PROBABILISTIC PROGRAMMING

```
type Researcher, Paper, Citation
random String Name(Researcher)
random String Title(Paper)
random Paper PubCited(Citation)
random String Text(Citation)
random Boolean Prof(Researcher)
origin Researcher Author(Paper)
#Researcher \sim OM(3,1)
Name(r) \sim CensusDB\_NamePrior()
Prof(r) \sim Boolean(0.2)
#Paper(Author = r) \sim if Prof(r) then OM(1.5,0.5) else OM(1,0.5)
Title(p) \sim CSPaperDB\_TitlePrior()
CitedPaper(c) \sim UniformChoice(Paper p)
Text(c) \sim HMMGrammar(Name(Author(CitedPaper(c))), Title(CitedPaper(c)))
```

Figure 15.4 An OUPM for citation information extraction. For simplicity the model assumes one author per paper and omits details of the grammar and error models. OM(a,b) is a discrete log-normal, base 10, i.e., the order of magnitude is $10^{a\pm b}$.

```
\#Aircraft(Arrival=t) \sim Poisson(\lambda_a)
Exits(a,t) \sim \text{ if } InFlight(a,t) \text{ then } Boolean(\alpha_e)
InFlight(a,t) = (t=Arrival(a)) \vee (InFlight(a,t-1) \wedge \neg Exits(a,t-1))
X(a,t) \sim \text{ if } t = Arrival(a) \text{ then } InitX() \text{ else if } InFlight(a,t) \text{ then } N(\mathbf{F}X(a,t-1),\Sigma_x)
\#Blip(Source=a, Time=t) \sim \text{ if } InFlight(a,t) \text{ then } Bernoulli(DetectionProb}(X(a,t)))
\#Blip(Time=t) \sim Poisson(\lambda_f)
Z(b) \sim \text{ if } Source(b)=null \text{ then } UniformZ(R) \text{ else } \sim N(\mathbf{H}X(Source(b), Time(b)), \Sigma_b)
```

Figure 15.5 An OUPM for radar tracking of multiple targets. X(a,t) is the state of aircraft a at time t, while Z(b) is the observed position of blip b.

```
\#SeismicEvents \sim Poisson(T * \lambda_e)
Time(e) \sim UniformReal(0,T)
EarthQuake(e) \sim Boolean(0.999)
Location(e) \sim \text{if } Earthquake(e) \text{ then } SpatialPrior() \text{ else } UniformEarth()
Depth(e) \sim \text{if } Earthquake(e) \text{ then } UniformReal(0,700) \text{ else } Exactly(0)
Magnitude(e) \sim Exponential(log(10))
Detected(e, p, s) \sim Logistic(weights(s, p), Magnitude(e), Depth(e), Distance(e, s))
\#Detections(site = s) \sim Poisson(T * \lambda_f(s))
\#Detections(event=e, phase=p, station=s) = if Detected(e, p, s) then 1 else 0
OnsetTime(a, s) \sim \mathbf{if} \ (event(a) = null) \ \mathbf{then} \sim UniformReal}(0, T)
   else Time(event(a)) + GeoTT(Distance(event(a), s), Depth(event(a)), phase(a))
                   + Laplace(\mu_t(s), \sigma_t(s))
Amplitude(a, s) \sim \mathbf{if} (event(a) = null) \mathbf{then} \ NoiseAmpModel(s)
  \textbf{else} \ AmpModel(Magnitude(event(a)), Distance(event(a), s), Depth(event(a)), phase(a))\\
Azimuth(a, s) \sim \text{if } (event(a) = null) \text{ then } UniformReal(0, 360)
   else GeoAzimuth(Location(event(a)), Depth(event(a)), phase(a), Site(s))
                   + Laplace(0, \sigma_a(s))
Slowness(a, s) \sim if (event(a) = null) then UniformReal(0, 20)
   else = GeoSlowness(Location(event(a)), Depth(event(a)), phase(a), Site(s))
                   + Laplace(0, \sigma_s(s))
ObservedPhase(a,s) \ \sim \ CategoricalPhaseModel(phase(a))
```

Figure 15.6 A simplified version of the NET-VISA model (see text).

16 MAKING SIMPLE DECISIONS

```
\begin{array}{l} \text{integrate } percept \text{ into } D \\ j \leftarrow \text{the value that maximizes } VPI(E_j) \ / \ C(E_j) \\ \text{if } VPI(E_j) \ > \ C(E_j) \\ \text{return } \text{REQUEST}(E_j) \\ \text{else return the best action from } D \end{array}
```

Figure 16.9 Design of a simple, myopic information-gathering agent. The agent works by repeatedly selecting the observation with the highest information value, until the cost of the next observation is greater than its expected benefit.

17 MAKING COMPLEX DECISIONS

Figure 17.6 The value iteration algorithm for calculating utilities of states. The termination condition is from Equation (??).

```
function Policy-Iteration(mdp) returns a policy inputs: mdp, an MDP with states S, actions A(s), transition model P(s' \mid s, a) local variables: U, a vector of utilities for states in S, initially zero \pi, a policy vector indexed by state, initially random repeat U \leftarrow \text{Policy-Evaluation}(\pi, U, mdp) unchanged? \leftarrow \text{true} for state s in S do a^* \leftarrow \underset{a \in A(s)}{\operatorname{argmax}} \text{ Q-Value}(mdp, s, a, U) if \text{ Q-Value}(mdp, s, a^*, U) > \text{ Q-Value}(mdp, s, \pi[s], U) then do \pi[s] \leftarrow a^*; unchanged? \leftarrow \text{ false} until unchanged? return \pi
```

Figure 17.9 The policy iteration algorithm for calculating an optimal policy.

```
function POMDP-VALUE-ITERATION(pomdp, \epsilon) returns a utility function inputs: pomdp, a POMDP with states S, actions A(s), transition model P(s' \mid s, a), sensor model P(e \mid s), rewards R(s), discount \gamma \epsilon, the maximum error allowed in the utility of any state local variables: U, U', sets of plans p with associated utility vectors \alpha_p U' \leftarrow \text{a set containing just the empty plan } [], \text{ with } \alpha_{[]}(s) = R(s) repeat U \leftarrow U' U' \leftarrow \text{the set of all plans consisting of an action and, for each possible next percept, a plan in <math>U with utility vectors computed according to Equation (??) U' \leftarrow \text{REMOVE-DOMINATED-PLANS}(U') until MAX-DIFFERENCE(U, U') < \epsilon(1-\gamma)/\gamma return U
```

Figure 17.15 A high-level sketch of the value iteration algorithm for POMDPs. The REMOVE-DOMINATED-PLANS step and MAX-DIFFERENCE test are typically implemented as linear programs.

18 MAKING DECISIONS IN MULTIAGENT ENVIRONMENTS

```
 \begin{array}{l} Actors(A,B) \\ Init(At(A,LeftBaseline) \, \wedge \, At(B,RightNet) \, \wedge \\ \quad Approaching(Ball,RightBaseline)) \, \wedge \, Partner(A,B) \, \wedge \, Partner(B,A) \\ Goal(Returned(Ball) \, \wedge \, (At(a,RightNet) \, \vee \, At(a,LeftNet)) \\ Action(Hit(actor,Ball), \\ \quad \  \  \, \text{PRECOND:} Approaching(Ball,loc) \, \wedge \, At(actor,loc) \\ \quad \  \  \, \text{Effect:} Returned(Ball)) \\ Action(Go(actor,to), \\ \quad \  \  \, \text{PRECOND:} At(actor,loc) \, \wedge \, to \, \neq \, loc, \\ \quad \  \  \, \text{Effect:} At(actor,to) \, \wedge \, \neg \, At(actor,loc)) \\ \end{array}
```

Figure 18.1 The doubles tennis problem. Two actors *A* and *B* are playing together and can be in one of four locations: *LeftBaseline*, *RightBaseline*, *LeftNet*, and *RightNet*. The ball can be returned only if a player is in the right place. Note that each action must include the actor as an argument.

19 LEARNING FROM EXAMPLES

Figure 19.4 The decision-tree learning algorithm. The function IMPORTANCE is described in Section ??. The function PLURALITY-VALUE selects the most common output value among a set of examples, breaking ties randomly.

```
function Model-Selection(Learner, examples, k) returns a hypothesis

local variables: err, an array, indexed by size, storing validation-set error rates for size = 1 to \infty do

err[size] \leftarrow Cross-Validation(Learner, size, examples, k)

if err is starting to increase significantly then do

best\_size \leftarrow the value of size with minimum err[size]

return Learner(best\_size, examples)

function Cross-Validation(Learner, size, examples, k) returns error rate average training set error rate,

errs \leftarrow 0

for fold = 1 to k do

training\_set, validation\_set \leftarrow Partition(examples, fold, k)

h \leftarrow Learner(size, training\_set)

errs \leftarrow errs + Error-Rate(h, validation\_set)

return errs/k // average error rate on validation sets, across k-fold cross-validation
```

Figure 19.7 An algorithm to select the model that has the lowest error rate on validation data by building models of increasing complexity, and choosing the one with best empirical error rate, err, on the validation data set. Learner(size, examples) returns a hypothesis whose complexity is set by the parameter size, and which is trained on the examples. DATA-PARTITION(examples, fold, k) splits examples into two subsets: a validation set of size N/k and a training set with all the other examples. The split is different for each value of fold.

```
function DECISION-LIST-LEARNING(examples) returns a decision list, or failure 

if examples is empty then return the trivial decision list No
t \leftarrow a test that matches a nonempty subset examples_t of examples
such that the members of examples_t are all positive or all negative 

if there is no such t then return failure
if the examples in examples_t are positive then o \leftarrow Yes else o \leftarrow No
return a decision list with initial test t and outcome o and remaining tests given by DECISION-LIST-LEARNING(examples - examples_t)
```

Figure 19.10 An algorithm for learning decision lists.

```
function ADABOOST(examples, L, K) returns a weighted-majority hypothesis
  inputs: examples, set of N labeled examples (x_1, y_1), \ldots, (x_N, y_N)
             L, a learning algorithm
             K, the number of hypotheses in the ensemble
  local variables: w, a vector of N example weights, initially 1/N
                       h, a vector of K hypotheses
                       \mathbf{z}, a vector of K hypothesis weights
  for k = 1 to K do
       \mathbf{h}[k] \leftarrow L(examples, \mathbf{w})
        error \leftarrow 0
       for j = 1 to N do
            if \mathbf{h}[k](x_j) \neq y_j then error \leftarrow error + \mathbf{w}[j]
       for j = 1 to N do
            if \mathbf{h}[k](x_j) = y_j then \mathbf{w}[j] \leftarrow \mathbf{w}[j] \cdot error/(1 - error)
        \mathbf{w} \leftarrow \text{NORMALIZE}(\mathbf{w})
       \mathbf{z}[k] \leftarrow \log (1 - error) / error
  return WEIGHTED-MAJORITY(h, z)
```

Figure 19.25 The ADABOOST variant of the boosting method for ensemble learning. The algorithm generates hypotheses by successively reweighting the training examples. The function WEIGHTED-MAJORITY generates a hypothesis that returns the output value with the highest vote from the hypotheses in \mathbf{h} , with votes weighted by \mathbf{z} .

20 DEEP LEARNING

```
function ADAM-OPTIMIZER(f, L, \theta, \rho, \alpha, \delta) returns updated \theta

/* Defaults: \rho_1 = 0.9; \rho_2 = 0.999; \alpha = 0.001; \delta = 10^{-8} */s \leftarrow 0
r \leftarrow 0
t \leftarrow 0

while \theta has not converged

x, y \leftarrow a minibatch of m examples from training set
g \leftarrow \frac{1}{m} \nabla_{\theta} \sum_{i} L(f(x^{(i)}; \theta), y^{(i)}) / * compute gradient */t \leftarrow t + 1
s \leftarrow \rho_1 s + (1 - \rho_1) g / * Update biased first moment estimate */r \leftarrow \rho_2 r + (1 - \rho_2) g \odot g / * Update biased second moment estimate */s \hat{s} \leftarrow \frac{s}{1 - \rho_1^{\cdot}} / * Correct bias in first moment */r \hat{\chi} \frac{r}{1 - \rho_2^{\chi}} / * Correct bias in second moment */\hat{\delta} \leftarrow \frac{s}{1 - \rho_1^{\chi}} / * Correct bias in second moment */r
\hat{\delta} \theta = - \leftarrow \frac{\starrow}{\sqrt{\chi} + \delta} / * Compute update (operations applied element-wise) */r
\hat{\theta} \leftarrow \theta + \Delta \theta / * Apply update */
```

Figure 20.6 The Adam (adaptive moments) optimizer. The function $f(x, \theta)$ describes the model and L describes the loss function. ρ_1 and ρ_2 are decay rates for estimates of the two moments, and α is the learning rate, while δ is a small constant used for numerical stabilization.

21 LEARNING PROBABILISTIC MODELS

22 REINFORCEMENT LEARNING

```
function PASSIVE-ADP-AGENT(percept) returns an action
  inputs: percept, a percept indicating the current state s' and reward signal r'
  persistent: \pi, a fixed policy
                mdp, an MDP with model P, rewards R, discount \gamma
                 U, a table of utilities, initially empty
                {\cal N}_{sa}, a table of frequencies for state–action pairs, initially zero
                N_{s'\,|\,sa}, a table of outcome frequencies given state-action pairs, initially zero
                s, a, the previous state and action, initially null
  if s' is new then U[s'] \leftarrow r'; R[s'] \leftarrow r'
  if s is not null then
       increment N_{sa}[s, a] and N_{s'|sa}[s', s, a]
       for t such that N_{s' \mid sa}[t, s, a] is nonzero do
           P(t \mid s, a) \leftarrow N_{s' \mid sa}[t, s, a] / N_{sa}[s, a]
   U \leftarrow \text{POLICY-EVALUATION}(\pi, U, mdp)
  if s'. TERMINAL? then s, a \leftarrow \text{null else } s, a \leftarrow s', \pi[s']
  return a
```

Figure 22.2 A passive reinforcement learning agent based on adaptive dynamic programming. The POLICY-EVALUATION function solves the fixed-policy Bellman equations, as described on page ??.

```
function PASSIVE-TD-AGENT(percept) returns an action inputs: percept, a percept indicating the current state s' and reward signal r' persistent: \pi, a fixed policy U, a table of utilities, initially empty N_s, a table of frequencies for states, initially zero s, a, r, the previous state, action, and reward, initially null if s' is new then U[s'] \leftarrow r' if s is not null then increment N_s[s] U[s] \leftarrow U[s] + \alpha(N_s[s])(r + \gamma U[s'] - U[s]) if s'.TERMINAL? then s, a, r \leftarrow null else s, a, r \leftarrow s', \pi[s'], r' return a
```

Figure 22.4 A passive reinforcement learning agent that learns utility estimates using temporal differences. The step-size function $\alpha(n)$ is chosen to ensure convergence, as described in the text.

```
function Q-LEARNING-AGENT(percept) returns an action inputs: percept, a percept indicating the current state s' and reward signal r' persistent: Q, a table of action values indexed by state and action, initially zero N_{sa}, a table of frequencies for state—action pairs, initially zero s, a, r, the previous state, action, and reward, initially null if TERMINAL?(s') then Q[s', None] \leftarrow r' if s is not null then increment N_{sa}[s, a] Q[s, a] \leftarrow Q[s, a] + \alpha(N_{sa}[s, a])(r + \gamma \max_{a'} Q[s', a'] - Q[s, a]) s, a, r \leftarrow s', \operatorname{argmax}_{a'} f(Q[s', a'], N_{sa}[s', a']), r' return a
```

Figure 22.8 An exploratory Q-learning agent. It is an active learner that learns the value Q(s,a) of each action in each situation. It uses the same exploration function f as the exploratory ADP agent, but avoids having to learn the transition model because the Q-value of a state can be related directly to those of its neighbors.

NATURAL LANGUAGE PROCESSING

```
function CYK-PARSE(words, grammar) returns a table of parse trees
  P \leftarrow a table, initially all 0 / * P[X, i, k] is probability of an X spanning words<sub>i:k</sub> */
  T \leftarrow a table / * T[X, i, k] is best X tree spanning words<sub>i:k</sub> */
  / ★ Insert lexical categories for each word. ★/
  for i = 1 to LEN(words) do
     for (X \rightarrow words_i [p]) in grammar.Lexicon do
        P[X, i, i] \leftarrow p
        T[X, i, i] \leftarrow \text{TREE}(X, words_i)
  /* Construct X_{i:k} from Y_{i:j} + Z_{j+1:k}, shortest spans first. */
  for (i, j, k) in Subspans(Len(words)) do
     for (X \rightarrow Y Z[p]) in grammar.RULES do
        PYZ \leftarrow P[\,Y,\ i,\ j] \ \times \ P[Z,\ j+1,\ k] \ \times \ p
        if PYZ > P[X, i, k] do
           P[X, i, k] \leftarrow PYZ
           T[X, i, k] \leftarrow \text{TREE}(X, T[Y, i, j], T[Z, j + 1, k])
  return T
function SUBSPANS(N) returns (i, j, k) tuples
  for length = 2 to N do
     for i = 1 to N + 1 - varlength do
        k \leftarrow i + length - 1
        for j = i to k - 1 do
           yield (i, j, k)
```

Figure 23.5 The CYK algorithm for parsing. Given a sequence of words, it finds the most probable parse tree for the whole sequence, and for each subsequence. It keeps a table of P[X,i,k] giving the probability of the most probable tree of category X spanning $words_{i:k}$. It returns a table, T, in which an entry T[X,i,k] is the most probable tree of category X spanning positions i to k inclusive. The function SUBSPANS returns all tuples (i,j,k) covering a span of $words_{i:k}$, with $i \leq j < k$, listing the tuples by increasing length of the i:k span, so that when we go to combine two shorter spans into a longer one, the shorter spans are already in the table.

```
[[S [NP-SBJ-2 Her eyes]
[VP were
[VP glazed
[NP *-2]
[SBAR-ADV as if
[S [NP-SBJ she]
[VP did n't
[VP [VP hear [NP *-1]]
or
[VP [ADVP even] see [NP *-1]]
[NP-1 him]]]]]]]]
```

Figure 23.6 Annotated tree for the sentence "Her eyes were glazed as if she didn't hear or even see him." from the Penn Treebank. Note that in this grammar there is a distinction between an object noun phrase (NP) and a subject noun phrase (NP-SBJ). Note also a grammatical phenomenon we have not covered yet: the movement of a phrase from one part of the tree to another. This tree analyzes the phrase "hear or even see him" as consisting of two constituent VPs, [VP hear [NP *-1]] and [VP [ADVP even] see [NP *-1]], both of which have a missing object, denoted *-1, which refers to the NP labeled elsewhere in the tree as [NP-1 him].

DEEP LEARNING FOR NATURAL LANGUAGE PROCESSING

25 PERCEPTION

26 ROBOTICS

```
function Monte-Carlo-Localization(a, z, N, P(X'|X, v, \omega), P(z|z^*), m) returns
a set of samples for the next time step
  inputs: a, robot velocities v and \omega
           z, range scan z_1, \ldots, z_M
           P(X'|X, v, \omega), motion model
           P(z|z^*), range sensor noise model
           m, 2D map of the environment
  persistent: S, a vector of samples of size N
  local variables: W, a vector of weights of size N
                     S', a temporary vector of particles of size N
                     W', a vector of weights of size N
   if S is empty then
                              /* initialization phase */
       \mathbf{for}\ i=1\ \mathrm{to}\ N\ \mathbf{do}
            S[i] \leftarrow \text{sample from } P(X_0)
       for i = 1 to N do /* update cycle */
           S'[i] \leftarrow \text{sample from } P(X'|X = S[i], v, \omega)
           W'[i] \leftarrow 1
           for j = 1 to M do
                z^* \leftarrow \text{RayCast}(j, X = S'[i], m)
                W'[i] \leftarrow W'[i] \cdot P(z_j | z^*)
       S \leftarrow \text{Weighted-Sample-With-Replacement}(N, S', W')
   return S
```

Figure 26.6 A Monte Carlo localization algorithm using a range-scan sensor model with independent noise.

PHILOSOPHY AND ETHICS OF AI

28 THE FUTURE OF AI

29 MATHEMATICAL BACKGROUND

30 NOTES ON LANGUAGES AND ALGORITHMS

```
generator POWERS-OF-2() yields ints i \leftarrow 1 while true do yield i i \leftarrow 2 \times i for p in POWERS-OF-2() do PRINT(p)

Figure 30.1 Example of a generator function and its invocation within a loop.
```