Learning Objectives - Bayes' Rule

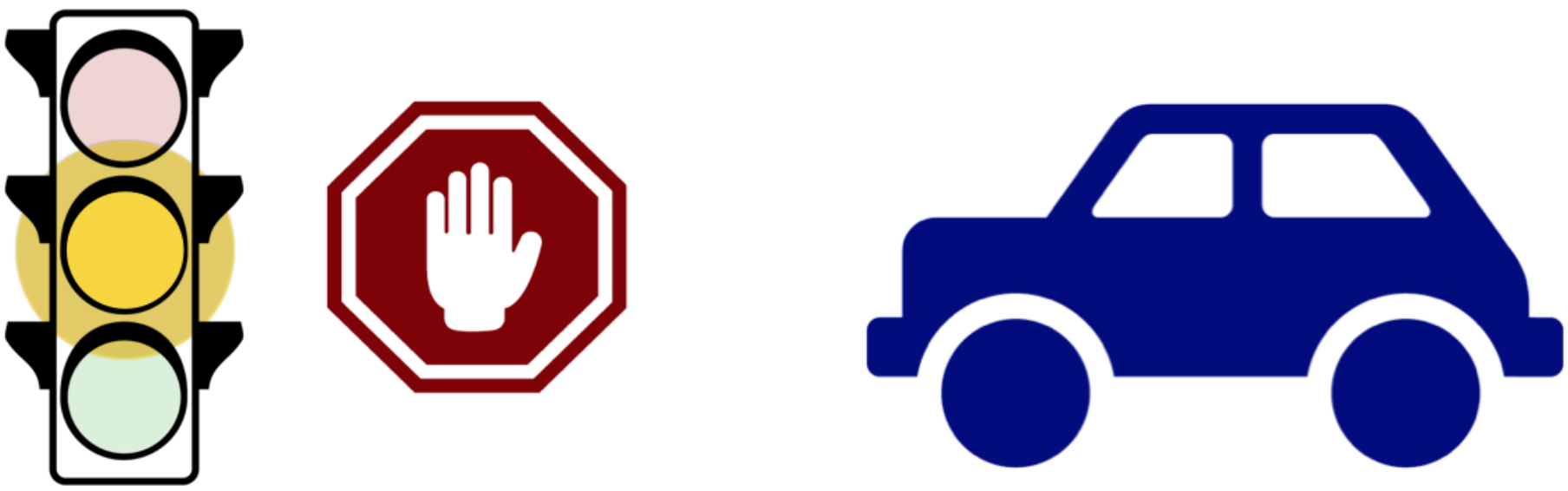
The following questions will help you review what you learned in the Bayes' Rule lesson.

Prior knowledge

For questions 1-3, assume you already have the following knowledge:

You're interested in finding out the probability of a car stopping if it sees a *yellow* traffic light.

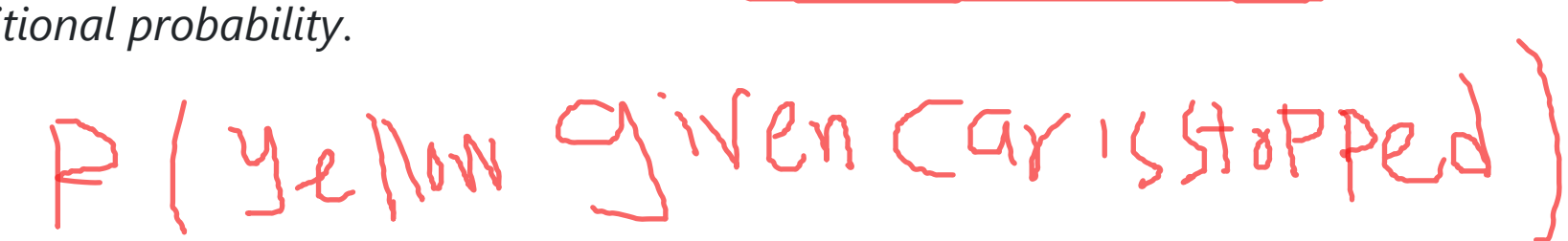
- Past data tells you that the probability of a car stopping at a traffic light intersection is $P(S) = 0.40$.
- You also know that the past probability of a traffic light being yellow (as opposed to red or green) is $P(Y) = 0.10$.



Car stopping at a yellow light

Traffic Light q1

When a car is stopped at an intersection, data shows that 12% of the time the light is yellow. So if we know a car is stopped, there's a 12% chance the light is yellow. This is called a *conditional probability*.



Given P(S) and P(Y) above, how would you represent this conditional probability in notation?

- P(S|Y) = 0.12
- P(S) = 0.12
- P(Y|S) = 0.12
- P(Y,S) = 0.12

$P(y|s) = P(y)\ \frac{P(s|y)}{P(s)} =$

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Traffic Light q2

Using what you know from question 1, answer the following: if the traffic light is yellow, what is the chance that the car will stop?

- 0.04
- 0.33
- 0.40
- 0.48
- 0.50
- 0.52

$P(\text{stop given yellow})$

$P(s|y) = \frac{0.4}{0.1} \times 0.12 = 0.48$

Traffic Light q3

Knowing that a car stopping at an intersection and the presence of a yellow traffic light are related events, what are P(S) and P(Y) known as?

- Posterior probabilities
- Past probabilities
- Prior probabilities
- Total probabilities

Questions 4 and 5 are different scenarios.

Prior knowledge for question 4:

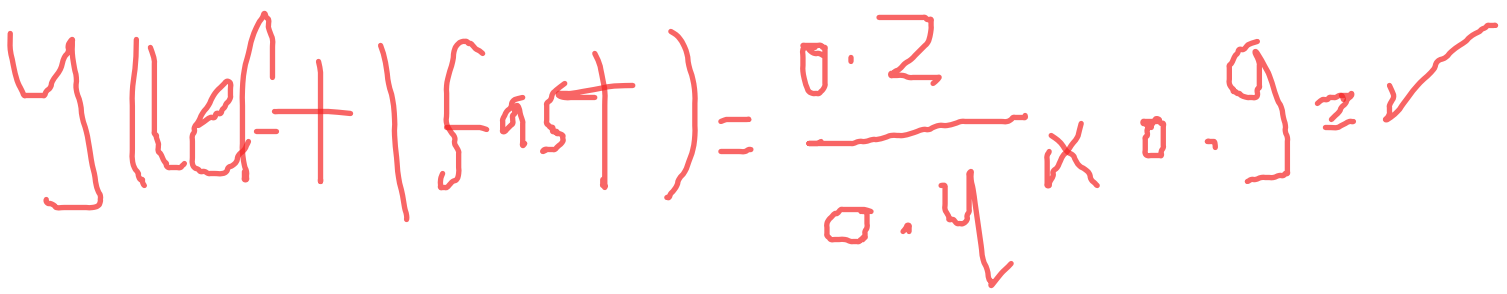
On a four-lane highway, cars are either going fast or not fast. Faster cars should go in the leftmost lanes.

- At any given time, 20% of cars are in the left-most lane.
- Overall, 40% of cars on the highway are classified as going fast.
- Out of all the cars in the leftmost lane, 90% are going fast.

Bayes q2

Given the above information, if a car is going fast, what is the probability that it will be in the leftmost lane?

- ○ 0.125
- ○ 0.25
- ○ 0.45
- ○ 0.55



Bayes' rule is not only used to incorporate sensor data into an estimate; it's also often used to incorporate test data into a medical diagnosis.

Prior knowledge for question 5:

- 1% of all people have cancer.
- 90% of people who have cancer test positive when given a cancer-detecting blood test, meaning the test detects cancer 90% of the time.
- 5% of people will have false positives, meaning that 5% of the time, this test will produce a positive result when people *do not* have cancer.

Bayes q3

Given the above data, what is the probability that a person has cancer if they have a positive cancer-test result? (Note: answers are rounded to the nearest 4th decimal place).

- ○ 0.1125
- ○ 0.1538
- ○ 0.2687
- ○ 0.8924

Next Concept