

know the consequences of being in NP and NP-complete

NP = non-deterministic polynomial

- it allows a choice of next-step
- uses yes/no problems



accepts

time complexity = polynomial
 n = input size
 k = constant (like 2) $O(n^2)$ / $O(n^k)$

if F is satisfiable, there exists a way for this algorithm to reach an accepting state

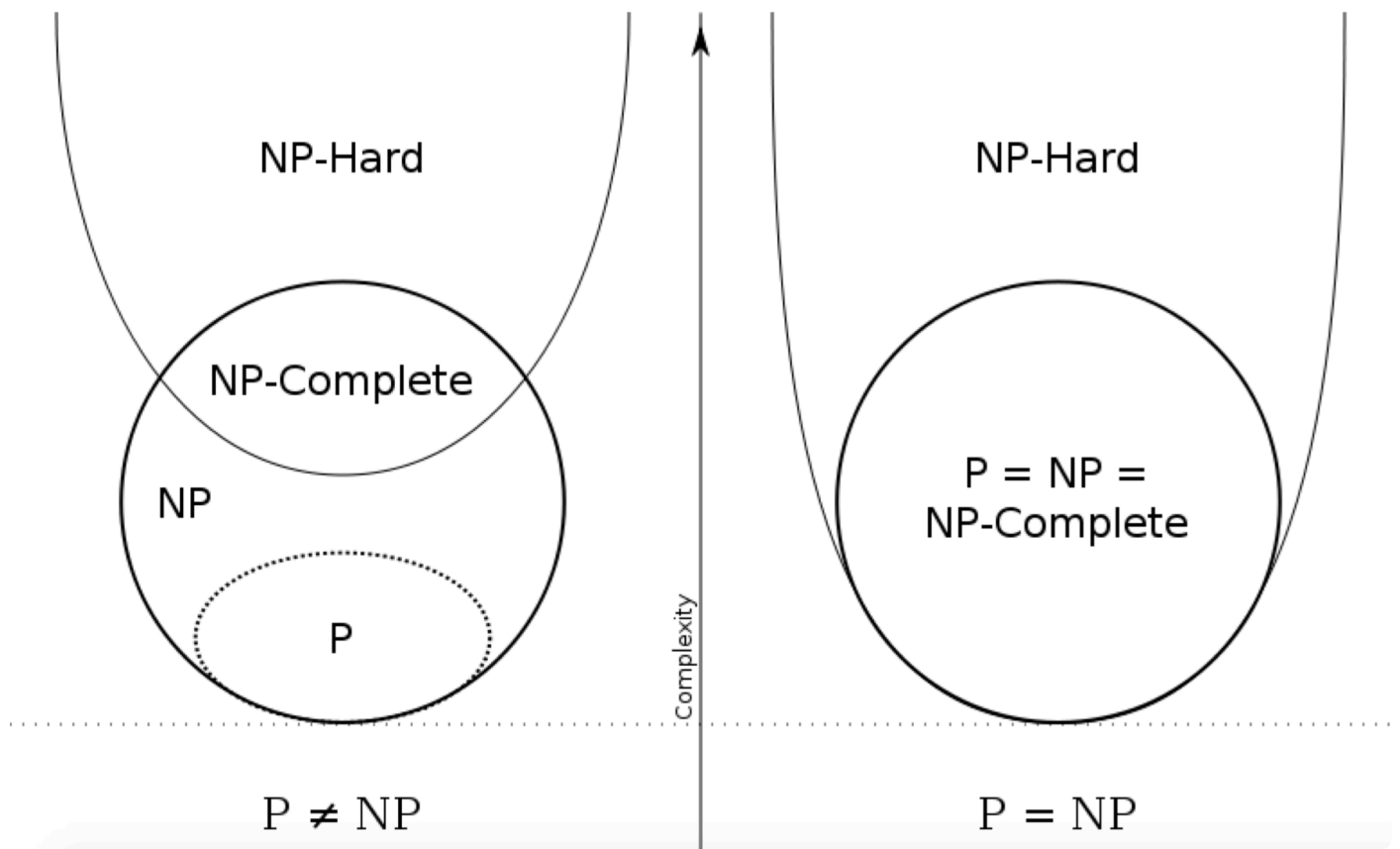
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nondeterministic algorithm
for i = 1 to n
    set  $x[i] = 0$  or  $1$  (nondet step)

if  $F[x[1], \dots, x[n]$  is true
    then ACCEPT
    else REJECT
```

NP-Complete: If one NP-complete problem can be solved in poly-time, then all of NP can be solved in poly-time



no one knows if this is possible
but if you prove one, you
prove it all.



QUESTIONS:

1) If a single NP -complete problem is shown to have a polynomial time (deterministic) algo, then it can be concluded that $P = NP$

TRUE. If you prove one, you prove all.

2) Whether any NP -complete problem is P **OPEN.**

3) If a single NP-complete problem is shown to require exponential time, then it can be concluded that $P=NP$.

FALSE

4) Every problem that can be solved in polynomial time non-deterministically can be solved by a polynomial time deterministic algo. OPEN

5) There is an NP-complete problem with a poly-time algo. OPEN

6) If one NP-complete problem is proved to require exponential time, then $P=NP$. FALSE

7) If one NP-complete problem is proved to require exponential time, then $P \neq NP$. TRUE