

□ WRITTEN

HOMEWORK #1

1.) Use Boolean Algebra to prove that

$$(\bar{A} * B * \bar{C}) + (\bar{A} * B * C) + (A * \bar{B} * C) + (A * B * \bar{C}) + (A * B * C) = (A+B) * (B+C)$$

$$B(\bar{A}\bar{C} + \bar{A}C + A\bar{C} + AC) + (A\bar{B}C) = (A+B)(B+C)$$

$$B + (A\bar{B}C) = (A+B)(B+C)$$

$$B + \bar{B}(AC) = B + AC$$

$$B + AC = B + AC$$

$$\text{LHS} = \text{RHS} \checkmark$$

\therefore equivalent

2.) Prove that $A \text{ XOR } B = A * \bar{B} + \bar{A} * B$

→ Truth Table

A	B	\bar{A}	\bar{B}	$A * \bar{B}$	$\bar{A} * B$	$A * \bar{B} + \bar{A} * B$	$A \oplus B$
0	0	1	1	0	0	0	0
0	1	1	0	0	1	1	1
1	0	0	1	1	0	1	1
1	1	0	0	0	0	0	0

↑ tautology \approx equivalent

XOR (\oplus) = cannot be same

i.e. $0 \oplus 0 = 0$ $1 \oplus 0 = 1$

$0 \oplus 1 = 1$ $1 \oplus 1 = 0$

$\therefore A \text{ XOR } B = A * \bar{B} + \bar{A} * B$

via truth table ✓

3.) Write function that represents following circuit. Do not simplify

$$(AB\bar{C}) + [(\bar{D}(AB\bar{C})) + ((AB\bar{C})' D)] * (\bar{A}D) + (\bar{D} + B) \text{ (simplified)}$$

$$f(x) = (AB\bar{C}) \oplus D * (\bar{A}D) + (\bar{D} + B) = F$$

$$AB\bar{C} \text{ XNOR } D * \text{NOT}(AD) + (\bar{D} + B) = F$$

4.) Given the following truth table.

4.1) Write function in SOP form. Do not simplify.

SOP = sum of products, minterms

• want all 1's output

$$= m_0 + m_1 + m_2 + m_5 + m_6$$

where: $m_0 = (\bar{A}\bar{B}\bar{C})$ $m_5 = (A\bar{B}C)$

$m_1 = (\bar{A}\bar{B}C)$ $m_6 = (AB\bar{C})$

$m_2 = (\bar{A}B\bar{C})$

so:

$$f(x) = (\bar{A}\bar{B}\bar{C}) + (\bar{A}\bar{B}C) + (\bar{A}B\bar{C}) + (A\bar{B}C) + (AB\bar{C})$$

4.2) Write function in POS form. Do not simplify.

POS = product of sums, maxterms

• want all 0's output

$$= M_3 + M_4 + M_7$$

where: $M_3 = (A + \bar{B} + \bar{C})$

$M_4 = (\bar{A} + B + C)$

$M_7 = (\bar{A} + \bar{B} + \bar{C})$

so:

$$f(x) = (A + \bar{B} + \bar{C}) * (\bar{A} + B + C) * (\bar{A} + \bar{B} + \bar{C})$$

5.) most simplified SOP & POS form for ea. of the functions.

5.1) $m_0 + m_1 + m_2$

$x_0 \backslash x_1$	0	1
0	1 ₀	1 ₂
1	1 ₁	0 ₃

$$\underline{\text{SOP}} = (\bar{x}_1 * \bar{x}_0)$$

$$\underline{\text{POS}} = (\bar{x}_1 + \bar{x}_0)$$

5.2) $M_0 * M_3 * M_4 * M_7$

$x_0 \backslash x_1$	00	01	11	10
0	0 ₀	1 ₂	1 ₆	0 ₄
1	1 ₁	0 ₃	0 ₇	1 ₅

$$\underline{\text{SOP}} = (x_1 * \bar{x}_0) + (\bar{x}_1 * x_0)$$

$$\underline{\text{POS}} = (x_1 + x_0) * (\bar{x}_1 + \bar{x}_0)$$

5.3) $m_4 + m_5 + m_7 + m_{12} + m_{13} + m_{15}$

$2^4 = 16$

$x_3 \backslash x_2$ $x_1 x_0$	00	01	11	10
00	0	1 ₄	1 ₂	0 ₈
01	0	1 ₅	1 ₃	0 ₉
11	0	1 ₇	1 ₁₅	0 ₁₁
10	0	0 ₆	0 ₁₄	0 ₁₀

SOP = $(x_0 * x_2) + (\bar{x}_1 * x_2)$

POS = $x_2 * (\bar{x}_1 + x_0)$

- POS is SOP essentially but,
product of sums w/
 x_2 factored out

5.4) $m_0 + m_3 + m_4 + m_8 + D_2 + D_5 + D_7 + D_{10} + D_{13} + D_{15}$

$x_3 \backslash x_2$ $x_1 x_0$	00	01	11	10
00	1 ₀	1 ₄	0 ₁₂	1 ₈
01	0 ₁	DC ₅	DC ₁₃	0 ₉
11	1 ₃	DC ₇	DC ₁₅	0 ₁₁
10	DC ₂	0 ₆	0 ₁₄	DC ₁₀

SOP = $(\bar{x}_0 * \bar{x}_2) + (\bar{x}_3 * \bar{x}_1 * \bar{x}_0) +$
 $(\bar{x}_3 * \bar{x}_2 * x_1)$

POS = $(\bar{x}_2 + \bar{x}_3) * (\bar{x}_0 + x_1) *$
 $(\bar{x}_3 + \bar{x}_0) * (\bar{x}_2 + \bar{x}_1)$

5.5) $m_1 + m_3 + m_7 + m_9 + m_{11} + m_{15} + m_{17} + m_{19} + m_{25} + m_{27} + D_4 + D_6 +$
 $D_{12} + D_{14} + D_{16} + D_{18} + D_{20} + D_{22} + D_{24} + D_{26} + D_{28} + D_{30}$

$x_3 \backslash x_2$ $x_1 x_0$	00	01	11	10
00	0 ₀	DC ₄	DC ₁₂	0 ₈
01	1 ₁	0 ₅	0 ₁₃	1 ₉
11	1 ₃	1 ₇	1 ₁₅	1 ₁₁
10	0 ₂	DC ₆	DC ₁₄	0 ₁₀
00	DC ₁₆	DC ₂₀	DC ₂₈	DC ₂₄
01	1 ₁₇	0 ₂₁	0 ₂₉	1 ₂₅
11	1 ₁₉	0 ₂₃	0 ₃₁	1 ₂₇
10	DC ₁₈	DC ₂₂	DC ₃₀	DC ₂₆

SOP = $(x_0 * \bar{x}_2) + (x_2)$

POS = $(\bar{x}_2 + x_1) * (x_2 + \bar{x}_1)$
 $* (\bar{x}_2 + \bar{x}_0)$