

# 1 Semântica Operacional Small-Step Linguagem Funcional

## 1.1 Sintaxe

$$\begin{aligned} E ::= & n \mid v \mid b \mid E \text{ op } E \\ & \mid \text{If } E \text{ then } E \text{ else } E \\ & \mid E \ E \mid \text{Fun } x : T \Rightarrow E \\ & \mid \text{let } x : T = E \text{ in } E \end{aligned}$$
$$\begin{aligned} n &\in \mathbb{Z} \\ b &\in \{\text{true}, \text{false}\} \\ \text{op} &::= + \mid - \mid * \mid \dots \\ T &:: \text{Int} \mid \text{Bool} \mid T \rightarrow T \\ v &:: n \mid b \mid \text{Fun } x : T \Rightarrow E \end{aligned}$$

## 1.2 Semântica

(SOMA1)

$$\frac{E_1 \rightarrow E'_1}{E_1 + E_2 \rightarrow E'_1 + E_2}$$

(SOMA2)

$$\frac{E \rightarrow E'}{n + E \rightarrow n + E'}$$

(SOMA3)

$$\overline{n_1 + n_2 \rightarrow \text{sum}(n_1, n_2)}$$

(AP1)

$$\frac{E_1 \rightarrow E'_1}{E_1 \ E_2 \rightarrow E'_1 \ E_2}$$

(AP2)

$$\frac{E \rightarrow E'}{v \ E \rightarrow v \ E'}$$

(AP3)

$$\overline{(\text{Fun } x : T \Rightarrow E) \ v \rightarrow \{v/x\}E}$$

(Let1)

$$\frac{E_1 \rightarrow E'_1}{\text{let } x : T = E_1 \text{ in } E_2 \rightarrow \text{let } x : T = E'_1 \text{ in } E_2}$$

(Let2)

$$\overline{\text{let } x : T = v \text{ in } E \rightarrow \{v/x\}E}$$