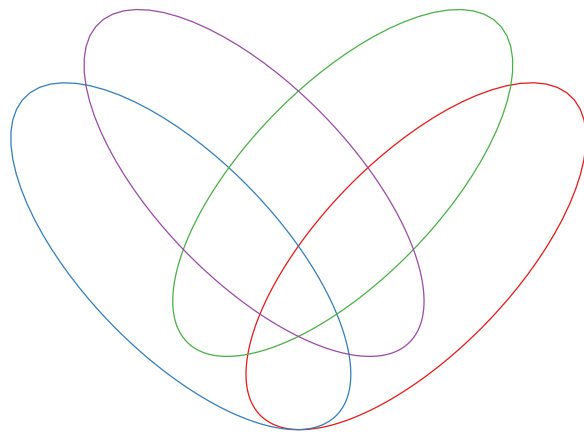


Venn diagrams in R with the Vennerable package

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Contents

1	Overview	3
2	Some loose definitions	6
3	Computation and Annotation	7
3.1	Computing Venn drawings	7
3.2	Annotation parameters	8
3.3	Graphical parameters	8
4	Unweighted Venn diagrams	10
4.1	Unweighted 2-set Venn diagrams	10
4.2	Unweighted 3-set Venn diagrams	11
4.3	Unweighted 4-set Venn diagrams	12
4.4	Unweighted Venn diagrams on more than four sets	14
5	Weighted Venn diagrams	16
5.1	Weighted 2-set Venn diagrams for 2 Sets	16
5.1.1	Circles	16
5.1.2	Squares	16
5.2	Weighted 3-set Venn diagrams	18
5.2.1	Circles	18
5.2.2	Squares	19
5.2.3	Triangles	21
5.3	Chow-Ruskey diagrams for 3 or more sets	22
6	Euler diagrams	24
6.1	2-set Euler diagrams	24
6.1.1	Circles	24
6.1.2	Squares	25
6.2	3-set Euler diagrams	27
6.2.1	Circles	27
6.2.2	Triangles	29
6.3	4-set Euler diagrams	31
6.3.1	Chow-Ruskey diagrams	31
7	This document	31

1 Overview

The Vennerable package provides routines to compute and plot Venn diagrams, including the classic two- and three-circle diagrams but also a variety of others with different properties and for up to seven sets. In addition it can plot diagrams in which the area of each region is proportional to the corresponding number of set items or other weights. This includes Euler diagrams, which can be thought of as Venn diagrams where regions corresponding to empty intersections have been removed.

Figure 5 shows a three-circle Venn diagram of the sort commonly found. To draw it, we use as an example the *StemCell* data of Boyer et al.[1] which lists the gene names associated with each of four transcription factors

```
> library(Vennerable)
> data(StemCell)
> str(StemCell)
```

List of 4

```
$ OCT4 : chr [1:623] "AASDH" "ABTB2" "ACCN4" "ACD" ...
$ SOX2 : chr [1:1279] "182-FIP" "AASDH" "ABCA5" "ABCB10" ...
$ NANOG: chr [1:1687] "13CDNA73" "AASDH" "ABCA5" "ABCB10" ...
$ E2F4 : chr [1:1273] "76P" "7h3" "AAMP" "AATF" ...
```

First we construct an object of class Venn:

```
> Vstem <- Venn(StemCell)
> Vstem
```

A Venn object on 4 sets named

OCT4,SOX2,NANOG,E2F4

```
0000 1000 0100 1100 0010 1010 0110 1110 0001 1001 0101 1101 0011 1011 0111 1111
  0   109  305   45  644   64  354  287  821   30   78   6  118  16  138  66
```

Although Vennerable can cope with 4-set Venn diagrams, for now we reduce to a three-set object

A Venn object on 3 sets named

OCT4,SOX2,NANOG

```
000 100 010 110 001 101 011 111
821 139 383  51 762  80 492 353
```

Note how the weights were appropriately updated.

Now a call to plot produces the diagram in Figure 5 showing how many genes are common to each transcription factor.

```
> plot(Vstem3, doWeights = FALSE)
```

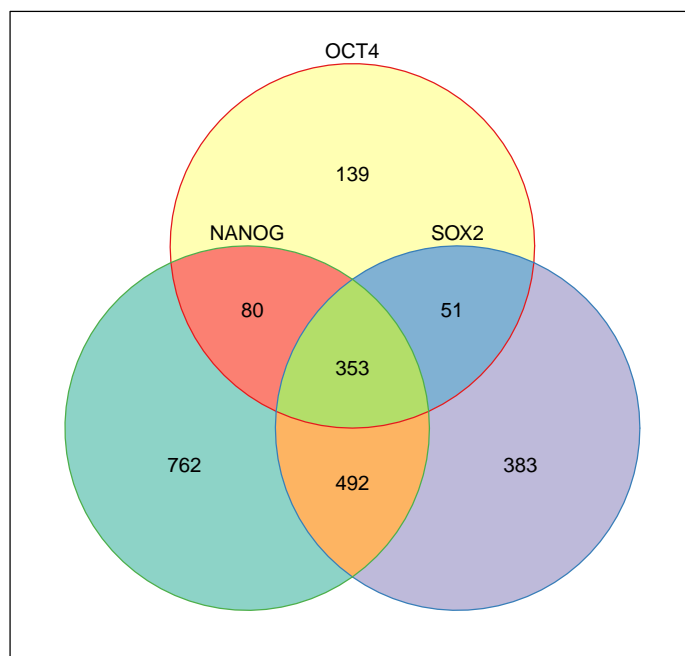


Figure 1: A three-circle Venn diagram

Quite commonly, we may have sets whose intersections we only know by the number of elements. These can be created as Venn objects by supplying a named vector of `Weights`:

```
> Vdemo2 <- Venn(SetNames = c("foo", "bar"), Weight = c(`01` = 7,
+               `11` = 8, `10` = 12))
```

Either way, we can plot Venn diagrams in which the area of each intersection is proportional to those weights as in Figure 2.

```
> plot(Vdemo2, doWeights = TRUE, type = "circles")
```

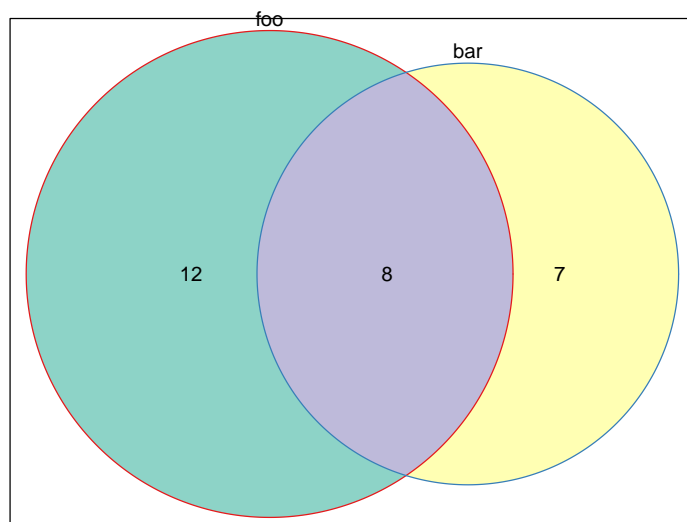


Figure 2: A two-set weighted Venn diagram

For these basic plots, use of the `Vennerable` package is perhaps overkill, but in more complex situations it has useful abilities. First it allows the use of a variety of other shapes for the set boundaries, and up to nine different sets. Secondly it implements a number of published or novel algorithms for generating diagrams in which the area of each region is proportional to, for example, the number of corresponding set elements. Finally it adds a number of graphical control abilities, including the ability to colour individual regions separately.

2 Some loose definitions

Figure 5 illustrates membership of three sets, in order OCT4, SOX2 , NANOG. Genes which are members of the SOX2 set but not the OCT4 or NANOG sets are members of an *intersection subset* with *indicator string* or *signature* 010.

Given n sets of elements drawn from a universe, there are 2^n intersection subsets. Each of these is a subset of the universe and there is one corresponding to each of the binary strings of length n . If one of these indicator strings has a 1 in the i -th position, all of members of the corresponding intersection subset must be members of the i -th set. Depending on the application, the universe of elements from which members of the sets are drawn may be important. Elements in intersection set 00 . . . , which are in the universe but not in any known set, are called (by me) *dark matter*, and we tend to display these differently.

A diagram which produces a visualisation of each of the sets as a connected curve in the plane whose regions of intersection are connected and correspond to each of the 2^n intersection subsets is an *unweighted Venn diagram*. Weights can be assigned to each of the intersections, most naturally being proportional to the number of elements each one contains. *Weighted Venn diagrams* have the same topology as unweighted ones, but (attempt to) make the area of each region proportional to the weights. This may not be possible, if any of the weights are zero for example, or because of the geometric constraints of the diagram. Venn diagrams based on 3 circles are unable in general to represent even nonzero weights exactly, and cannot be constructed at all for $n > 3$.

Diagrams in which only those intersections with non-zero weight appear are *Euler diagrams*, and diagrams which go further and make the area of every intersection proportional to its weight are weighted Euler diagrams. For more details and rather more rigour see first the online review of Ruskey and Weston[7] and then the references it contains.

3 Computation and Annotation

For a running example, we use sets named after months, whose elements are the letters of their names.

```
> setList <- strsplit(month.name, split = "")
> names(setList) <- month.name
> Vmonth3 <- VennFromSets(setList[1:3])
> Vmonth2 <- Vmonth3[, c("January", "February"), ]
```

3.1 Computing Venn drawings

The calls to `plot` are really convenience wrappers for two separate functions which compute the geometry of the drawing first, returning an object of class `VennDrawing` and then renders that object. For example

```
> plot(Vmonth3, doWeights = TRUE)
```

is equivalent to

```
> C3 <- compute.Venn(Vstem3, doWeights = TRUE)
> grid.newpage()
> plot(C3)
```

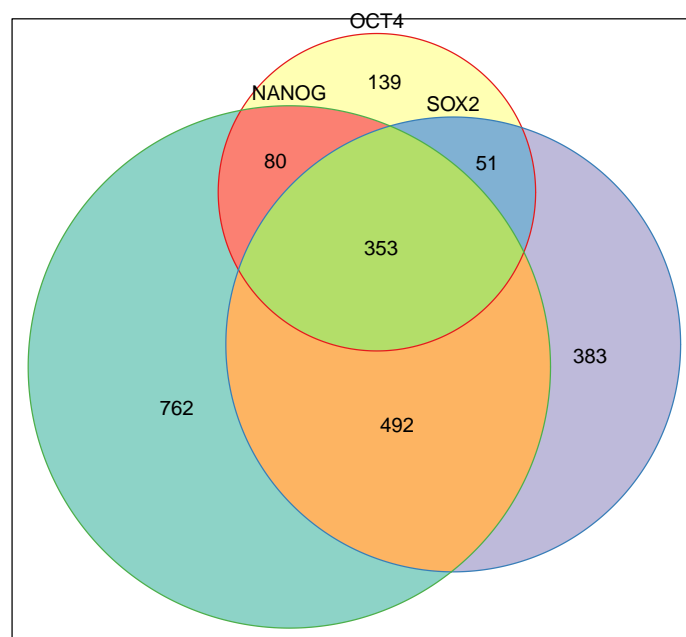


Figure 3: A weighted three-circle Venn diagram

Note the use of a function from the `grid` graphics library package. All of the renderings use `grid` objects for more powerful subsequent processing. The `compute.Venn` function can take a variety of arguments such as `doWeights` controlling the geometry and topology of the drawing, while the `plot` method has a number of arguments controlling annotation and display.

3.2 Annotation parameters

The text displayed in each face is controlled by the `FaceText` element of the `show` parameter list to `plot`. Other elements of the parameter control whether eg set names are displayed or faces are individually coloured

```
> plot(C3, show = list(FaceText = "signature", SetLabels = FALSE,
+                      Faces = FALSE))
```



Figure 4: The same Venn diagram with different `show` parameters

3.3 Graphical parameters

The package makes its own decisions about how to colour lines and faces depending on the complexity of the diagram. This can be overridden with the `gpList` argument to `plot`. The default choices are equivalent to

```
> gp <- DefaultgpStyles(C3)
> plot(C3, gpList = gp)
```


The only available high-level modification is that `DefaultgpStyles` can take the `ColourAlgorithm` style - see the man page for more details. Low-level modifications can be made by modifying the `gp` argument itself. That must be a named list, with elements that can include `Face`, `FaceText`, `Set`, and `SetText`. Each of those elements is itself a named list named by either the name of the set or the signature of the face. The elements of these lists in turn are graphical parameters in the sense of the `grid` package, essentially lists of parameter-value pairs in the sense of the `grid` package.

```
> gp <- DefaultgpStyles(C3, colourAlgorithm = "binary")
> plot(C3, gpList = gp, show = list(FaceText = "sets", SetLabels = FALSE,
+   Faces = TRUE))
```

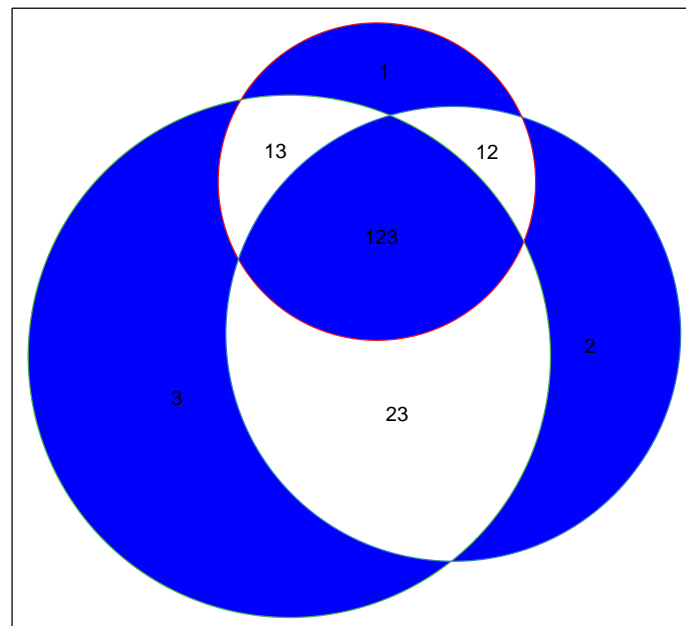
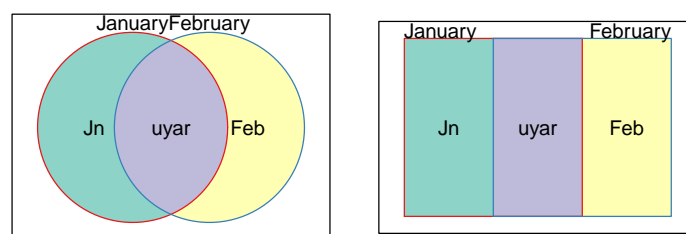


Figure 5: The effect of a different `ColourAlgorithm`

4 Unweighted Venn diagrams

4.1 Unweighted 2-set Venn diagrams

For two sets, a diagram can be drawn using either circles or squares, as controlled by the `type` argument. This is shown in Figure 6 where the `show` and `doWeights` parameters are not shown.¹



`plot(V,type=circles,...)`

`plot(V,type=squares,...)`

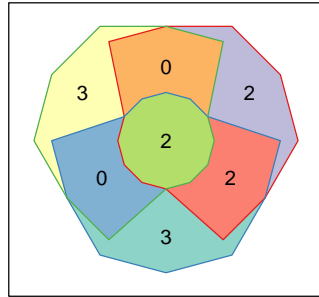
Figure 6: Unweighted 2-set Venn diagrams with `type=circles` or `type=squares`

¹Here and in the rest of this vignette, much of the code to plot the Figures, which is mainly devoted to layout, is not shown. However it can always be found by inspecting the source code of the vignette at `PACKAGETREE/Vennerable/doc/Venn.Rnw` where `PACKAGETREE` is directory where the package was installed.

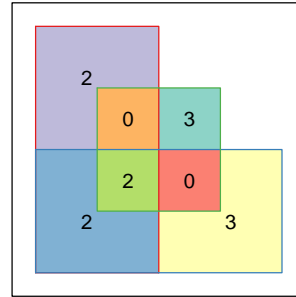
4.2 Unweighted 3-set Venn diagrams

For three sets, the type argument can be circles, squares, ChowRuskey, triangles or AWFE. We have already seen the circles plot. The AWFE plot is an implementation of the elegant ideas of [6]. The Chow-Ruskey plot is from [4], and is a redrawing of the AWFE plot in such a way that there is an algorithm which will allow all of the faces to be adjusted in area without disrupting the topology of the diagram. The triangles plot is fairly obvious, for example to reference[5], but I have not seen it implemented elsewhere.

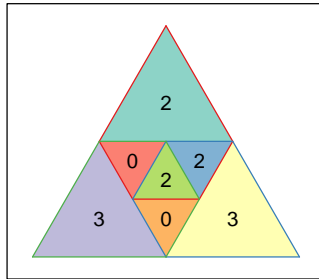
This example of the squares plot is *notsimple*, in the sense of [7], because the set boundaries don't cross transversally. Topologically, there is only one simple Venn diagram of order 3 (in a way that [7] makes precise).



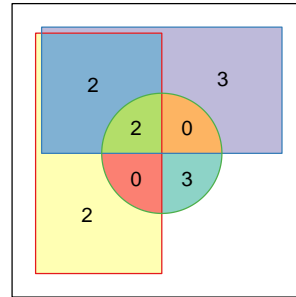
`plot(Vmonth3,type="ChowRuskey",...)`



`plot(Vmonth3,type="squares",...)`



`plot(Vmonth3,type="triangles",...)`



`plot(Vmonth3,type="AWFE",...)`

4.3 Unweighted 4-set Venn diagrams

For four sets, the type argument can be `ChowRuskey`, `AWFE`, `squares` or `ellipses`.

The squares plot is said by Edwards [6] to have been introduced by Lewis Carroll [2]. The ellipse plot was suggested by Venn [8].

Note how the package makes an attempt to identify a point within each face where the annotation can be plotted, but doesn't make a very good choice for very non-concave or elongated faces.

```
> V4 <- Venn(n = 4)
```

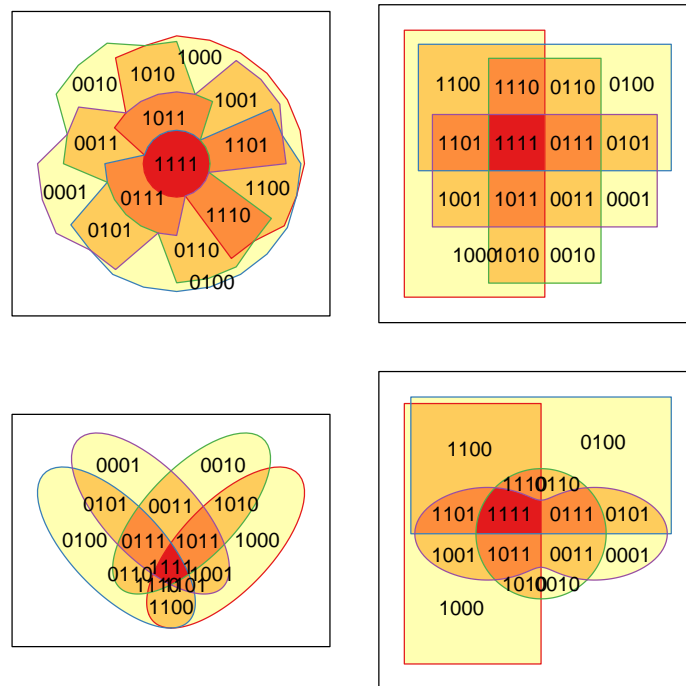


Figure 7: Venn diagrams on four sets drawn with the `type` argument set to `ChowRuskey`, `squares`, `ellipses`, and `AWFE`.

A number of variants on the `squares` type are implemented. Currently they can only be accessed by passing the parameters `s` or `likesquares` to the low level creation function `compute.S4` directly, which is what is done in Figure 8. Also, for display purposes it can be easier to make sense of if the set boundaries differ in line thickness as shown here.

For more details on this see the help pages.

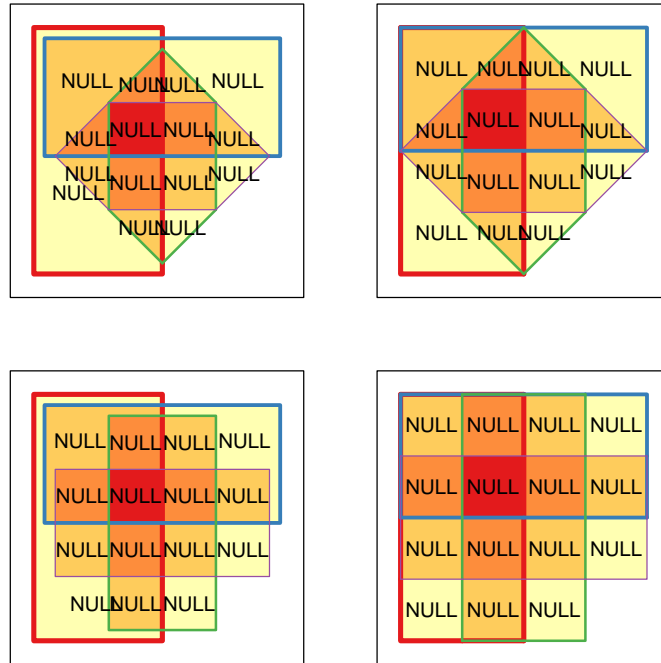


Figure 8: Four variants on the four-squares

4.4 Unweighted Venn diagrams on more than four sets

The package implements a variant of the Edwards construction[6], which can in principle generate Venn diagrams on an arbitrary number of sets n . The currently implemented algorithm only computes up to 8 sets for the classic construction.

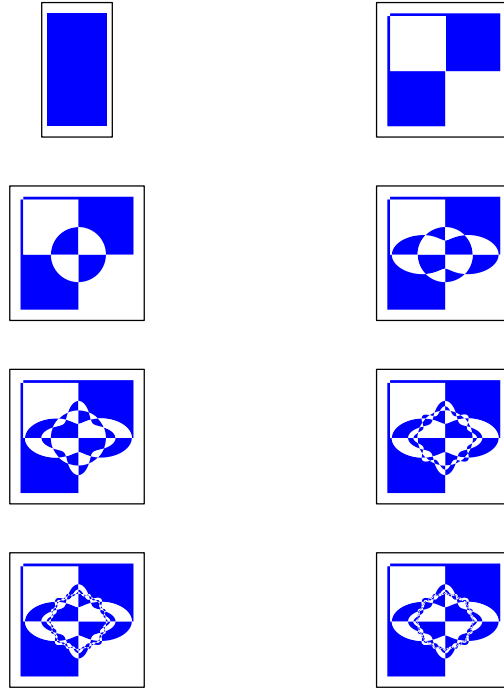


Figure 9: Edwards constructions for five to eight sets

A variant on the Edwards construction I developed as both quicker to compute with, because it is based on straight lines, and slightly easier to visualise high-order intersections in, is shown in Figure 10. It can be drawn by using `type="battle"` for up to 9 sets.

```
> plot(Venn(n = 9), type = "battle", show = list(SetLabels = FALSE,
+         FaceText = ""))
```

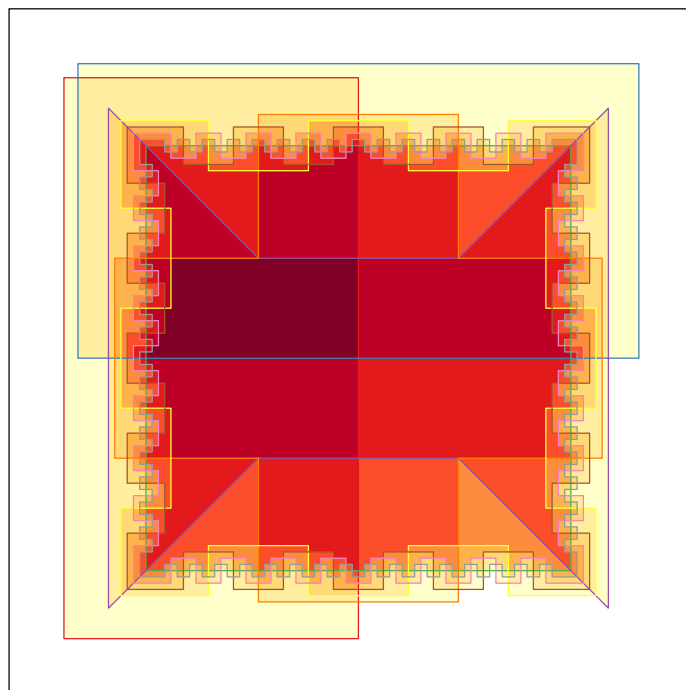


Figure 10: The battlement variant of the Edwards construction on 9 sets with the `type=battle` argument

5 Weighted Venn diagrams

There are repeated requests to generate Venn diagrams in which the areas of the faces themselves are meant to carry information, mainly by being proportional to the intersection weights. Even when these diagrams can be drawn, they are not often a success in clearly displaying information. But we shall try any way. In general, these will be produced with the `doWeights=TRUE` argument.

First of all we consider the case when all the visible intersection weights are nonzero.

5.1 Weighted 2-set Venn diagrams for 2 Sets

5.1.1 Circles

It is always possible to get an exactly area-weighted solution for two circles as shown in Figure 11.

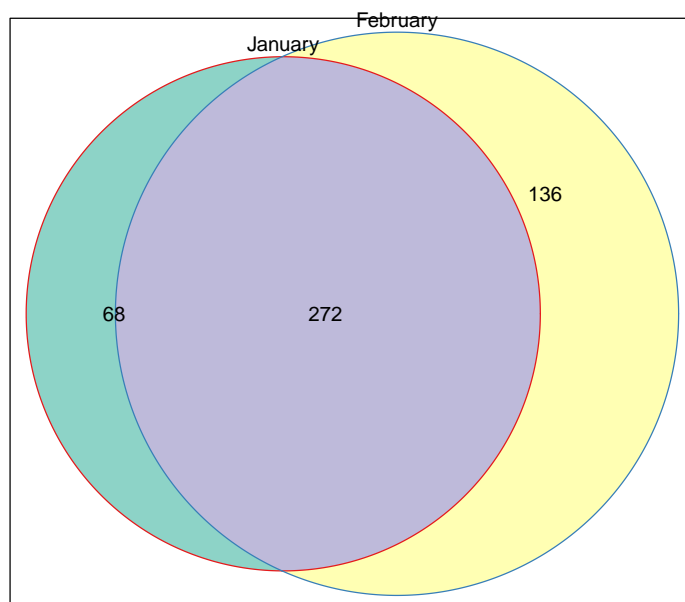


Figure 11: Weighted 2d Venn

5.1.2 Squares

As for circles, square weight-proportional diagrams can be simply constructed.

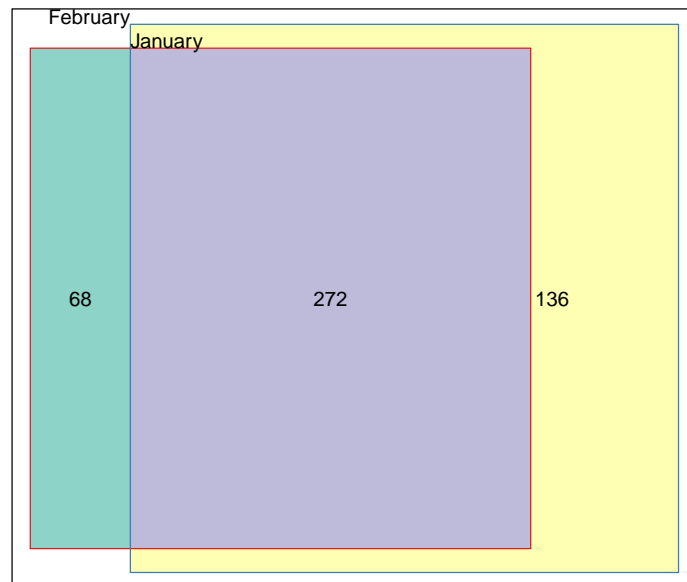


Figure 12: Weighted 2d Venn squares

5.2 Weighted 3-set Venn diagrams

5.2.1 Circles

There is no general way of creating area-proportional 3-circle diagrams. While these attempts at these diagrams are quite commonly seen, they must almost always be inexact.

The package makes an attempt to produce approximate ones.

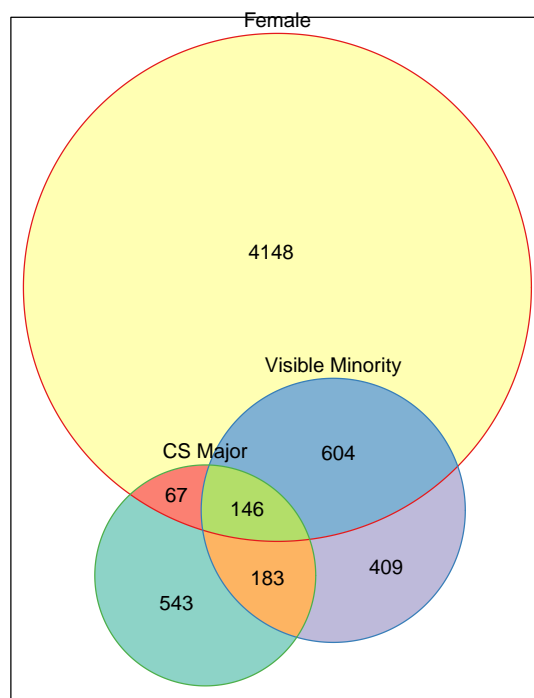


Figure 13: 3D Venn diagram

The algorithm used is to compute the individual circles to have the exact area necessary for proportionality, and then compute each of the three pairwise distances between centres necessary for the correct pairwise areas. If these distances do not satisfy the triangle inequality the largest is reduced until they do. Then the circles are arranged with their centres separated by these (possibly modified) distances.

5.2.2 Squares

There is a number of possible algorithms to generate exact Venn diagrams based on polygons. With `type=squares` the package uses an algorithm almost identical to that suggested by [3], which tries to generate rectangles as the set boundaries if possible

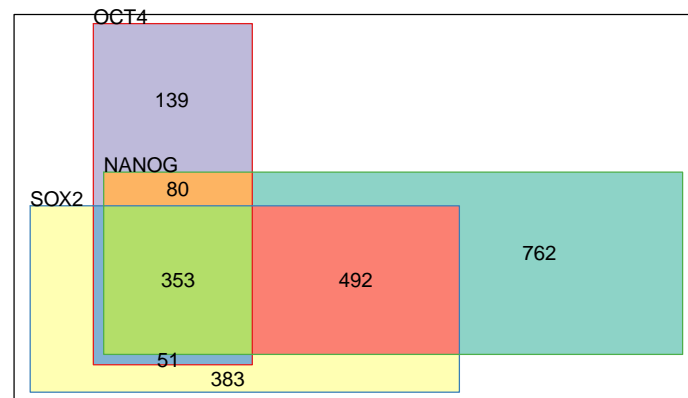


Figure 14: Weighted 3-set Venn diagram based on the algorithm of [3]

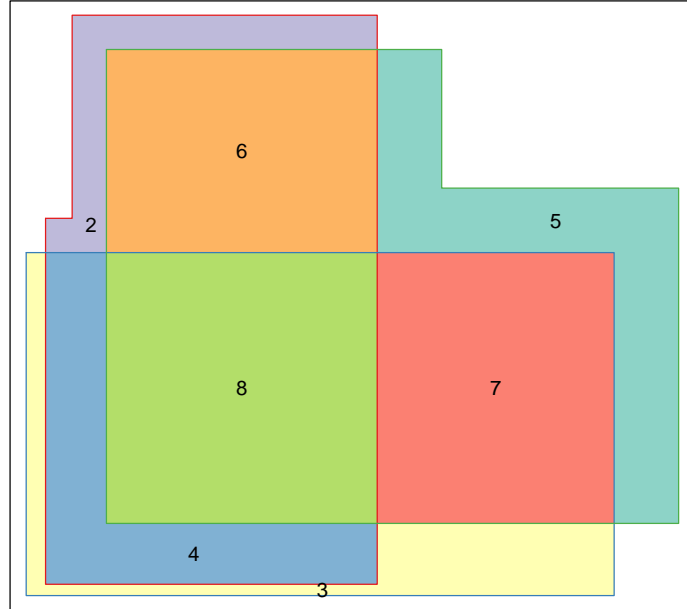


Figure 15: Weighted 3-set Venn diagram based on the algorithm of [3]. This time the algorithm fails to find rectangles.

5.2.3 Triangles

The triangular Venn diagram on 3-sets lends itself nicely to an area-proportional drawing under some constraints on the weights (detailed elsewhere).

```
> C3t <- compute.Venn(V3a, type = "triangles")
> gp <- DefaultgpStyles(C3t)
> gp[["Set"]] <- lapply(gp[["Set"]], function(gps) {
+   gps$lwd <- 3
+   gps
+ })
> plot(C3t, gp = gp, show = list(SetLabels = FALSE))
```

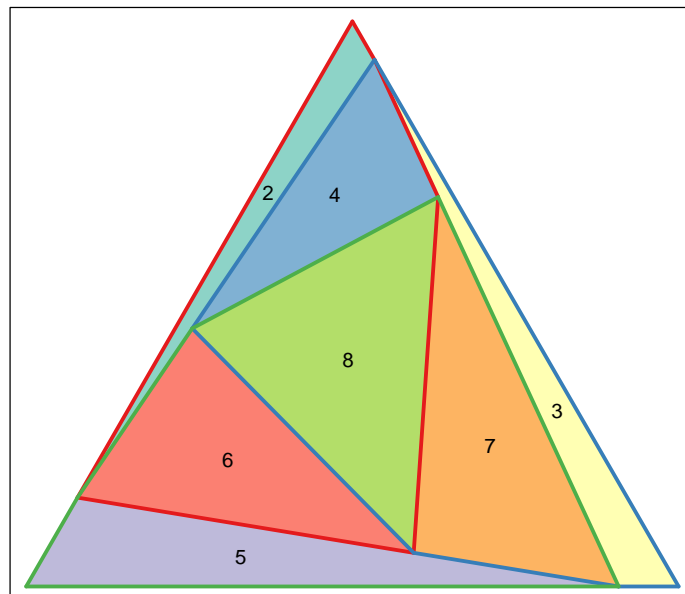


Figure 16: Triangular Venn with external universe

5.3 Chow-Ruskey diagrams for 3 or more sets

The general Chow-Ruskey algorithm [4] for area-proportional faces can be implemented in principle for an arbitrary number of sets provided the weight of the common intersection is nonzero. In practice the package is limited (to $n = 9$) by the size of the largest AWFE diagram it can compute.

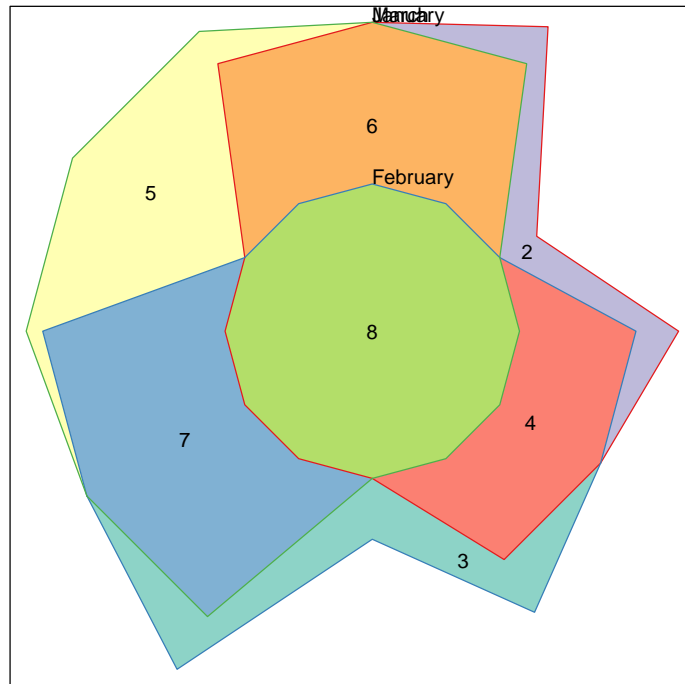


Figure 17: Chow-Ruskey weighted 3-set diagram

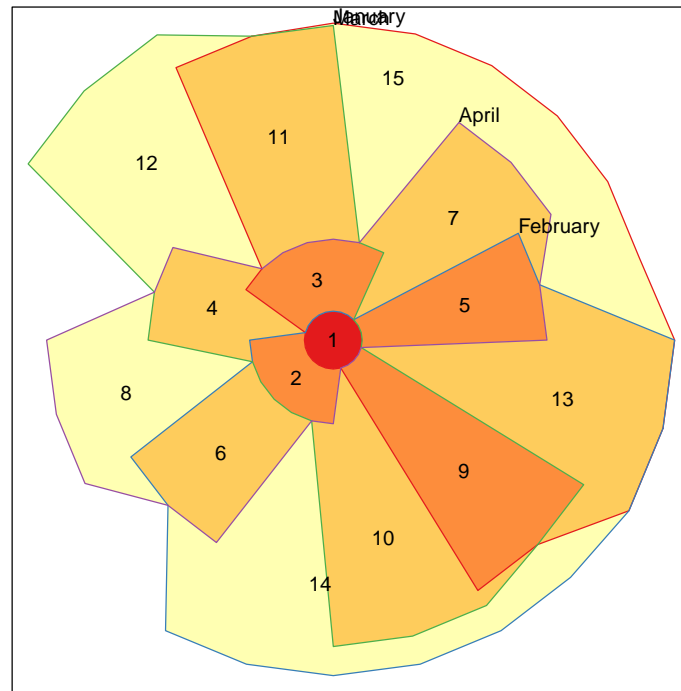


Figure 18: Chow-Ruskey weighted 4-set diagram

6 Euler diagrams

A *Euler diagram* is one in which regions of zero-weight are not displayed at all (but those which are displayed are not necessarily area-proportional). This can be achieved, for some geometries, by use of the `doEuler=TRUE` argument.

As we have seen, for some geometries it is not possible to enforce exact area-proportionality when requested by the `doWeight=TRUE` argument, and an attempt is made to produce an approximately area-proportional diagram. In particular, regions whose weight is zero may appear with nonzero areas. These two flags can interact in weird and uncomfortable ways depending on exactly which intersection weights are zero.

6.1 2-set Euler diagrams

6.1.1 Circles

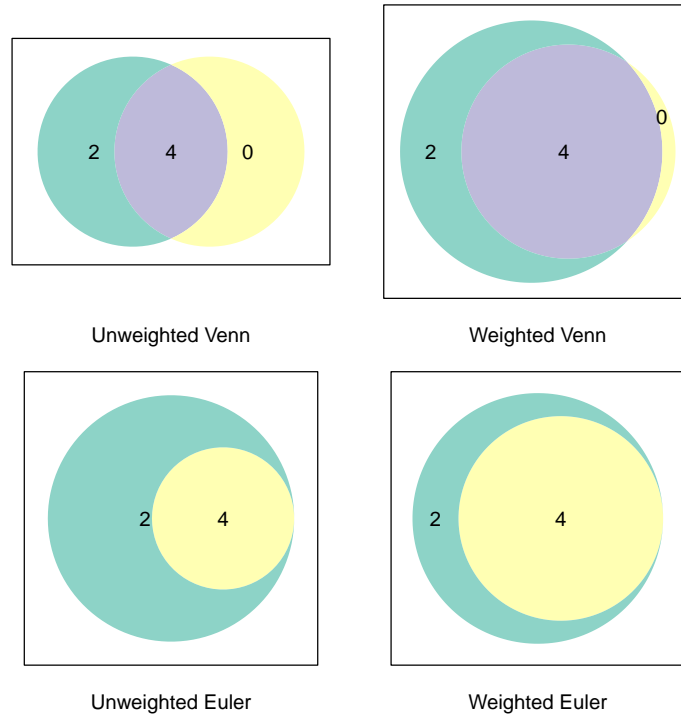


Figure 19: Effect of the Euler and `doWeights` flags.

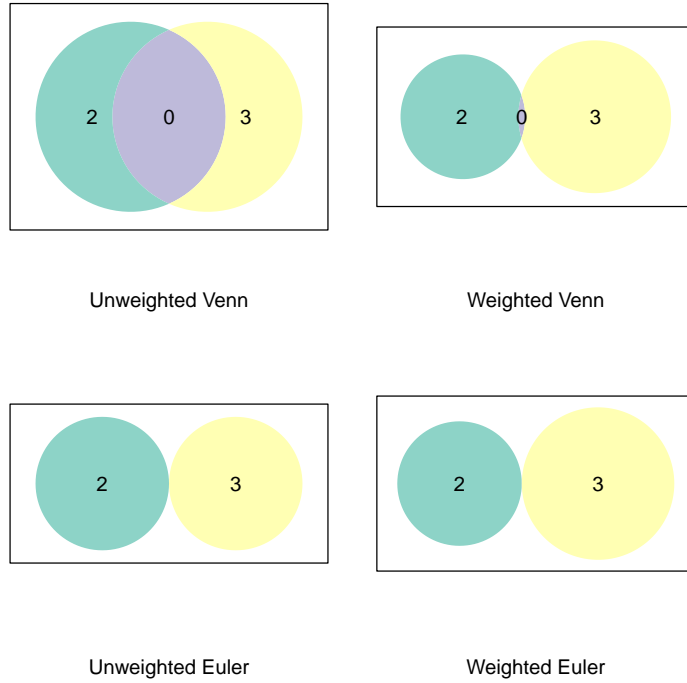
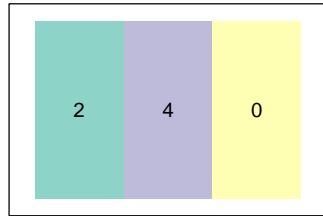


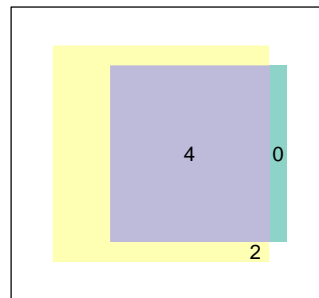
Figure 20: As before for a set of weights with different zeroes

6.1.2 Squares

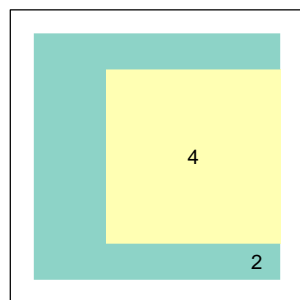
As for circles, the idea of a weighted Venn diagram when some of the weights are zero doesn't make much sense in theory but might be useful for making visual points.



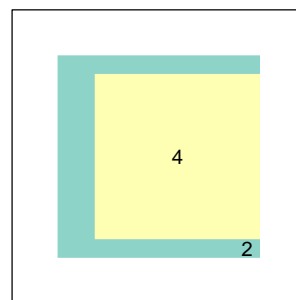
Unweighted Venn



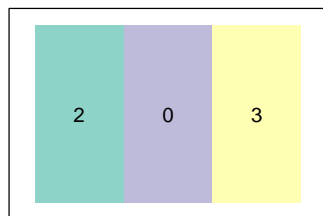
Weighted Venn



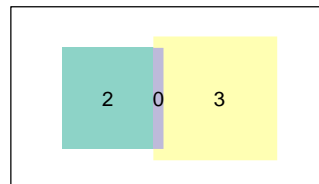
Unweighted Euler



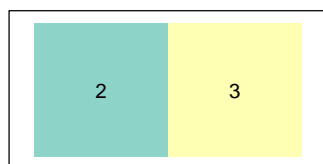
Weighted Euler



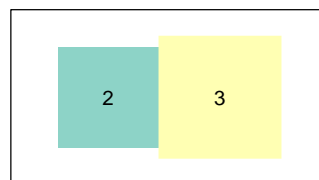
Unweighted Venn



Weighted Venn



Unweighted Euler



Weighted Euler

6.2 3-set Euler diagrams

6.2.1 Circles

There is currently no effect of setting `doEuler=TRUE` for three circles, but the `doWeights=TRUE` flag does an approximate job. There are about 40 distinct ways in which intersection regions can have zeroes can occur, and some of these expose bugs in the underlying polygon-polygon clipping code, but here are some examples.

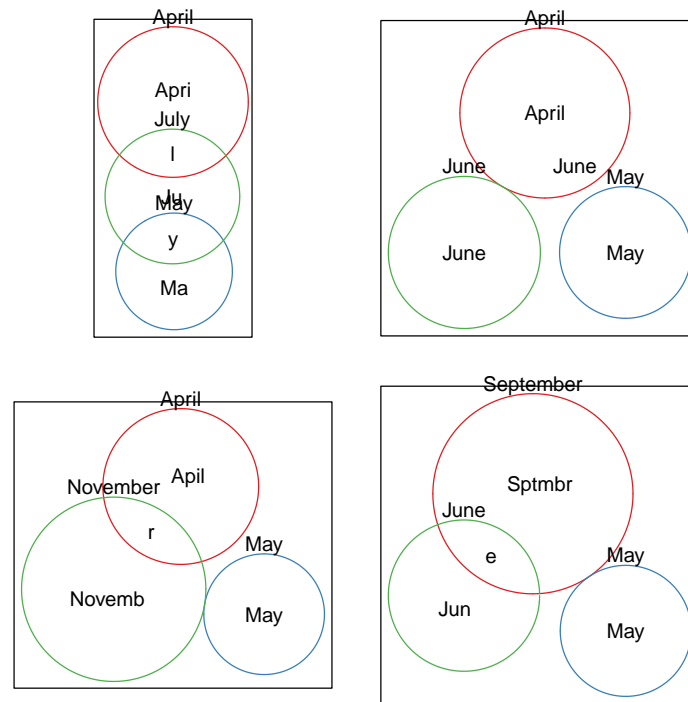


Figure 21: Weighted 3d Venn empty intersections. Note ghost face in top-right example. Rerunning this Figure with `Faces=TRUE` will reveal further problems.

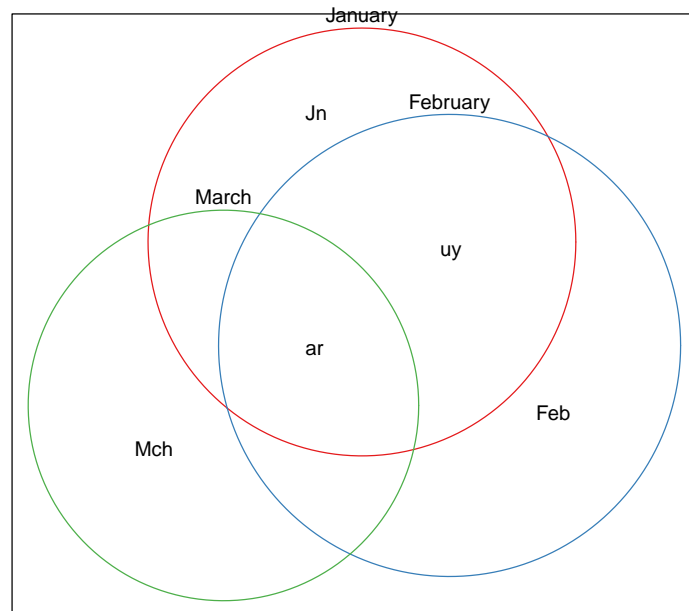
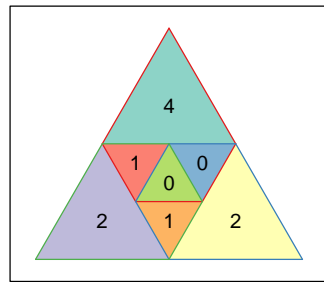


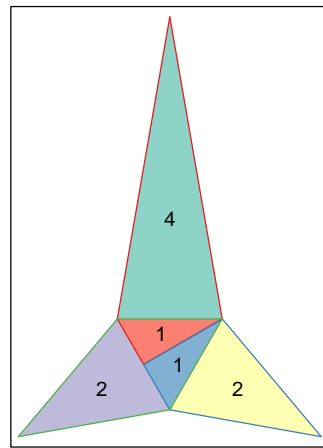
Figure 22: Approximate weighted 3d Venn showing element set membership

6.2.2 Triangles

The `doEuler` flag has no effect for triangles; all the weighted diagrams produced are Euler diagrams.

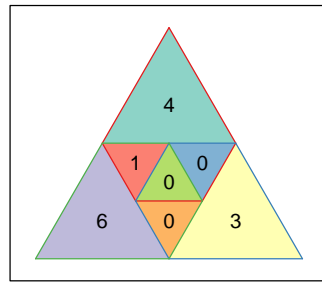


Unweighted Euler

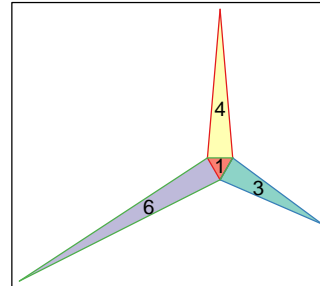


Weighted Euler

Figure 23: 3d Venn triangular with two zero weights plotted with the `doWeights` flag FALSE and TRUE



Unweighted Euler



Weighted Euler

Figure 24: 3d Venn triangular with three zero weights plotted with the `doWeights` flag FALSE and TRUE

6.3 4-set Euler diagrams

6.3.1 Chow-Ruskey diagrams

The `doEuler` flag has no effect for Chow-Ruskey because all the weighted diagrams produced are Euler diagrams.

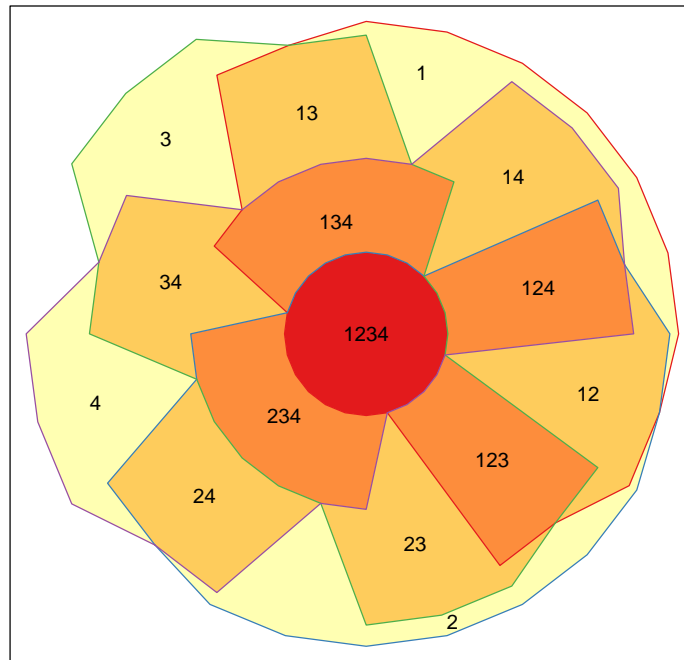


Figure 25: Chow-Ruskey diagram with some zero weights

7 This document

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CVS id of this document	Id: Venn.Rnw,v 1.26 2007/10/16 10:59:52 js229 Exp .
Generated on	9 th July, 2009
R version	R version 2.9.0 (2009-04-17)

References

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