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Part-B

Q.1] Euler Totient Function:

The Euler totient function counts the positive integers upto which a given integer n . It is denoted by ' ϕ ' & also called Euler phi function.

- If n is a prime number

$$\phi(n) = n-1$$

- $\phi(a * b) = \phi(a) * \phi(b)$

if a & b are co-prime.

→ Given, $n=14$

- To calculate $\phi(14)$, we find two numbers such that they are co-prime.

- Let the two numbers be $a=2$ and $b=7$.

We know that $\gcd(2,7)=1$.

This implies that they are co-prime.

$\therefore 2, 7$ are co prime.

- Now we can write the function as

$$\phi(14) = \phi(2) * \phi(7)$$

Applying property $\phi(n) = n-1$ for n being prime

$$\begin{aligned}\phi(14) &= (2-1) \times (7-1) \\ &= 1 \times 6\end{aligned}$$

$$\therefore \phi(14) = 6$$