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## Part-C

Q.2]

X	1	2	2	3	4	5
Y	1	1	3	2	3	5

Step 1: Choosing cluster centres,  
 $v_1 = (2, 1)$  and  $v_2 = (2, 3)$

Data Point	Distance from $v_1$	Distance from $v_2$	Allocated
$a_1(1, 1)$	1	2.24	$v_1$
$a_2(2, 1)$	0	2	$v_1$
$a_3(2, 3)$	2	0	$v_2$
$a_4(3, 2)$	1.41	1.41	$v_1$
$a_5(4, 3)$	2.83	2	$v_2$
$a_6(5, 5)$	5	3.61	$v_2$

\* Distance is calculated by euclidean measure  
 $(x_1, x_2) \& (y_1, y_2)$ ,  $d = \sqrt{(x_1 - y_1)^2 + (x_2 - y_2)^2}$

$$\therefore a_1(1, 1) :- d = \sqrt{(1-2)^2 + (1-1)^2} = 0$$

Step 3: Cluster 1 of  $v_1 = \{a_1, a_2, a_4\}$   
 Cluster 2 of  $v_2 = \{a_3, a_5, a_6\}$

Step 4: Recalculate cluster centres:

$$v_1 = \frac{1}{3} [(1, 1) + (2, 1) + (3, 2)] = (2, 1.33)$$

$$v_2 = \frac{1}{3} [(2, 3) + (4, 3) + (5, 5)] = \frac{1}{3} [(11, 11)]$$

$$= (3.67, 3.67)$$

Repeating step 2 until we get same elements

Data Point	Distance from $V_1$	Distance from $V_2$	Allocated
$a_1$	1.05	3.78	$V_1$
$a_2$	0.33	3.15	$V_1$
$a_3$	1.67	1.8	$V_1$
$a_4$	1.204	1.8	$V_1$
$a_5$	2.605	0.75	$V_2$
$a_6$	4.711	1.88	$V_2$

→ Cluster 1 of  $V_1 = \{a_1, a_2, a_3, a_4\}$   
 Cluster 2 of  $V_2 = \{a_5, a_6\}$

Step 6: Recalculating centres,

$$V_1 = \frac{1}{4} [a_1 + a_2 + a_3 + a_4] = \frac{1}{4} [(1,1) + (2,1) + (2,3) + (3,2)]$$

$$= (2, 1.75)$$

$$V_2 = \frac{1}{2} [a_5 + a_6] = \frac{1}{2} [(4,3) + (5,5)]$$

$$= (4.5, 4)$$

Step 7: Repeating step 2 again as centres not same.

Data Point	Distance from $V_1$	Distance from $V_2$	Allocated
$a_1$	1.25	4.61	$V_1$
$a_2$	0.75	3.9	$V_1$
$a_3$	1.25	2.69	$V_1$
$a_4$	1.03	2.5	$V_1$
$a_5$	2.36	1.12	$V_2$
$a_6$	4.42	1.12	$V_2$

→ Cluster 1 of  $v_1 = \{a_1, a_2, a_3, a_4\}$   
Cluster 2 of  $v_2 = \{a_5, a_6\}$

\* Clusters are the same as previous iteration hence we can stop.

⇒ The final clusters are

Cluster 1:  $\{(1,1), (2,1), (2,3), (3,2)\}$

Cluster 2:  $\{(4,3), (5,5)\}$