

# IMAGE PROCESSING

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ASSIGNMENT-1

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Q.1] Explain the process of Histogram equalization for a given image having gray levels between  $[0, 9]$  perform Histogram Equalization.

Ans Histogram Equalization is an approach to enhance a given image. The idea is to design a transformation  $T(\cdot)$  such that the gray values in the output are uniformly distributed in  $[0, 1]$ .

Step1: For image with distinct gray values compute:

$$P_{in}(r_k) = \frac{n_k}{n} \quad 0 \leq r_k \leq L-1 \quad 0 \leq k \leq L-1$$

$L$  = Total no. of gray levels

$n_k$  = No. of pixels with gray value  $r_k$

$n$  = total no. of pixels.

Step2: Based on CDF compute the discrete version:

$$S_k = T(r_k) = (L-1) \sum_{j=0}^k P_{in}(r_j) \quad 0 \leq k \leq L-1$$

Input :

2	3	3	2
4	2	4	3
3	2	3	5
2	4	2	4

Gray Level	0	1	2	3	4	5	6	7	8
No. of pixels	0	0	6	5	4	1	0	0	0

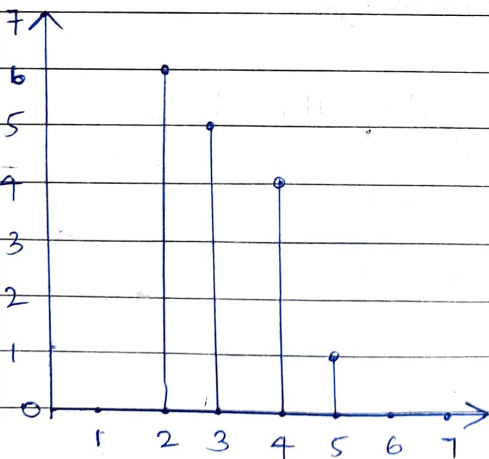
$k$	$r_k$	$n_k$	$P(r_k) = \frac{n_k}{n}$	$S_k = (L-1) \sum_{j=0}^k P(r_j)$	$S_k$
0	0	0	0	$0 \times 7 = 0$	0
1	1/8	0	0	$0 \times 7 = 0$	0
2	2/8	6	0.37	$0.37 \times 7 = 2.59$	3
3	3/8	5	0.31	$0.68 \times 7 = 4.76$	5
4	4/8	4	0.25	$0.93 \times 7 = 6.51$	7
5	5/8	1	0.062	$0.993 \times 7 = 6.94$	7
6	6/8	0	0	$0.992 \times 7 = 6.94$	7
7	7/8	0	0	$0.992 \times 7 = 6.94$	7
8	1	0	0	$0.992 \times 7 = 6.94$	7

 $n=16$ 

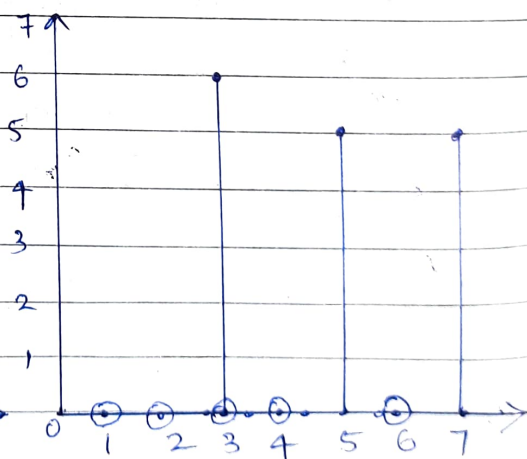
Gray level	0	3	5	7
No. of pixels	0	6	5	5

→ Histogram of Input & Output images

Input:



Output:



Output Image:

3	5	5	3
7	3	7	5
5	3	5	7
3	7	3	7

Q.2] Explain Smoothing & Sharpening filters in spatial domain

Ans. Smoothing Spatial filters are used for blurring and noise reduction.

- Blurring is used as a pre processing step for removal of small details from an image prior to object extraction. Noise reduction can be accomplished by blurring.

→ Types of Smoothing filters:-

① Linear filter:-

It is simply the average of the pixels contained in the neighbourhood of the filter mask. Eg: Average & weighted Avg. filter.

② Order static filter:-

They are non linear spatial filters. It is based on ordering the pixels contained in the image area encompassed by the filter. Eg: Median, min, max filter.

- Sharpening spatial filters: They are used to highlight fine details in an image or to enhance details that has been blurred either in error or as a natural effect of any method of acquisition.

→ Foundation of sharpening filter.

$$1-D: \frac{\partial f}{\partial x} = f(x+1) - f(x)$$

$$2^{nd} \text{ order of } 1-D: \frac{\partial^2 f}{\partial x^2} = f(x+1) + f(x-1) - 2f(x)$$

$$\text{Gradient operator: } \nabla f = \frac{\partial f(x,y)}{\partial x \partial y} = \frac{\partial f(x,y)}{\partial x} + \frac{\partial f(x,y)}{\partial y}$$



Laplacian Operator:  $\nabla^2 f = \frac{\partial^2 f(x,y)}{\partial x^2} + \frac{\partial^2 f(x,y)}{\partial y^2}$

$$\frac{\partial^2 f}{\partial x^2} = f(x+1, y) + f(x-1, y) - 2f(x, y)$$

$$\frac{\partial^2 f}{\partial y^2} = f(x, y+1) + f(x, y-1) - 2f(x, y)$$

$$\nabla^2 f = [f(x+1, y) + f(x-1, y) + f(x, y+1) + f(x, y-1) - 4f(x, y)]$$

Q.3] Explain how arithmetic & logical operations are helpful in image enhancement.

Ans • Addition, subtraction, multiplication, division comprise arithmetic operations while AND, OR, NOT makeup logical operations.

- They are often applied as preprocessing steps in image analysis in order to combine images in various ways.
- Addition - Used to create double exposures  

$$g(x, y) = f_1(x, y) + f_2(x, y)$$
- Subtraction - Used for finding changes in two images or to detect motion.  

$$g(x, y) = f_1(x, y) - f_2(x, y)$$
- Multiplication - Used to adjust brightness of an image.  

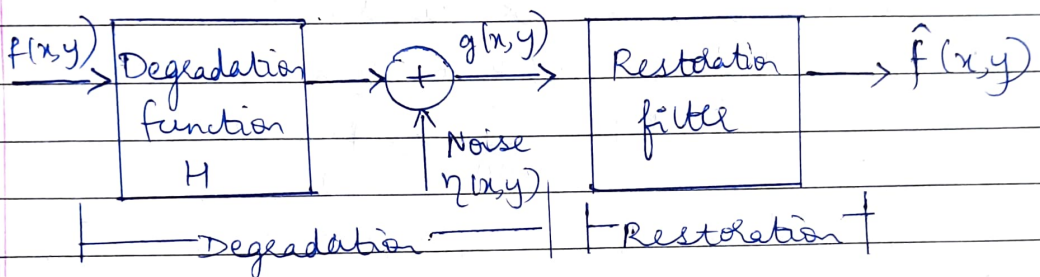
$$g(x, y) = f_1(x, y) \cdot f_2(x, y)$$
- Division - Used to adjust brightness of an image.  

$$g(x, y) = f_1(x, y) / f_2(x, y)$$

Q.4] What is image restoration? Explain the degradation model.

Ans. Image restoration attempts to restore images that have been degraded.

- It identifies the degradation process and attempt to reverse it.



- Degradation function along with some additive noise operates on  $f(x,y)$  to produce degraded image  $g(x,y)$
- Given  $g(x,y)$  & some prior knowledge about the degradation function  $H$  & additive noise  $\eta(x,y)$  objective of restoration is to obtain estimate  $\hat{f}(x,y)$  of the original image.
- If  $H$  is linear position invariant process then degraded image in spatial domain is given by,  $g(x,y) = h(x,y) * f(x,y) + \eta(x,y)$   

$\downarrow$  Spatial rep. of  $H$        $\downarrow$  Indicates convolution
- Since convolution in spatial domain is multiplication in frequency domain

$$G(u,v) = H(u,v) \cdot F(u,v) + \eta(u,v)$$

$\downarrow$   
 Identity  
 Operator.

Q.5) Explain image restoration in the presence of noise using spatial filtering.

Ans When there is noise present in an image then  $g(x,y) = f(x,y) + n(x,y)$ .

Spatial filtering can be done when only additive noise is present. The following techniques can be used:

(i) Mean filter: a) Arithmetic mean.

$$\hat{f}(x,y) = \frac{1}{mn} \sum_{(s,t) \in S_{xy}} g(s,t)$$

Results in smoothing effect of an image.

b) Geometric mean:

$$\hat{f}(x,y) = \left[ \prod_{(s,t) \in S_{xy}} g(s,t) \right]^{1/mn}$$

c) Harmonic mean:  $\hat{f}(x,y) = \frac{mn}{\sum_{(s,t) \in S_{xy}} 1/g(s,t)}$

d) Contra Harmonic mean:  $\hat{f}(x,y) = \frac{\sum_{(s,t)} g(s,t)^{q+1}}{\sum_{(s,t)} g(s,t)^q}$

(ii) Order Statistics filter:

a) Median filter:  $\hat{f}(x,y) = \text{median}_{(s,t) \in S_{xy}} \{g(s,t)\}$

b) Max/min filter:  $\hat{f}(x,y) = \max_{(s,t) \in S_{xy}} \{g(s,t)\}$   
 $\hat{f}(x,y) = \min_{(s,t)} \{g(s,t)\}$

c) Mid point filter:  $\hat{f}(x,y) = \frac{1}{2} [\max_{(s,t)} \{g(s,t)\} + \min_{(s,t)} \{g(s,t)\}]$

d) Alpha trimmed mean filter:

$$\hat{f}(x,y) = \frac{1}{mn-d} \sum_{(s,t) \in S_{xy}} g_{\alpha}(s,t)$$

middle pixels  
(mn-d)



[iii] Adaptive filters:

a] Adaptive local noise filter:

$$\hat{f}(x,y) = g(x,y) - \frac{\sigma_n^2}{\sigma_L^2} [g(x,y) - m_L]$$

b] Adaptive median filter:

Proposed for restoration of gray scale images that are corrupted by salt & pepper noise

Q.6] Describe periodic noise reduction using freq. domain filtering.

Ans. It is due to electromechanical interference & during image acquisition.

• It can be done on periodic noise to reduce it using the following filters:

i] Bandreject filters: Remove/alternate a band of frequency

$$H(u,v) = \begin{cases} 1 & \text{if } D(u,v) < D_0 - W/2 \\ 0 & \text{if } D_0 - W/2 \leq D(u,v) \leq D_0 + W/2 \\ 1 & \text{if } D(u,v) > D_0 + W/2 \end{cases}$$

a] Butterworth bandreject filter:

$$H(u,v) = \frac{1}{1 + \left[ \frac{D(u,v)W}{D^2(u,v) - D_0^2} \right]^{2n}}$$

b] Gaussian bandreject filter

$$H(u,v) = 1 - e^{-1/2 \left[ \frac{D^2(u,v) - D_0^2}{D(u,v)W} \right]^{2n}}$$

ii] Bandpass filters: The goal is to isolate the noise pattern from image which can help simplify analysis of noise.

$$H_{bp}(u,v) = 1 - H_{br}(u,v)$$



iii)

Notch filters: They reject frequencies of predefined neighbours about a centre frequency.

$$H(u,v) = \begin{cases} 0, & \text{if } D_1(u,v) \leq D_0 \text{ \& } D_2(u,v) \leq D_0 \\ 1, & \text{otherwise} \end{cases}$$

$$D_1(u,v) = [(u - M/2 - u_0)^2 + (v - N/2 - v_0)^2]^{1/2}$$

$$D_2(u,v) = [(u - M/2 + u_0)^2 + (v - N/2 + v_0)^2]^{1/2}$$

a) Butterworth notch filter:

$$H(u,v) = 1 / \left[ 1 + \left[ \frac{D_0^2}{D_1(u,v) D_2(u,v)} \right]^n \right]$$

b) Gaussian notch filter:

$$H(u,v) = 1 - e^{-\frac{1}{2} \left[ \frac{D_1(u,v) D_2(u,v)}{D_0^2} \right]}$$