

Gate SmashersUninformed search
(blind / brute force)

- Search without info
- No knowledge
- Time consuming
- More complexity (time, space)
- Eg - DFS, BFS, Uniform cost search

Informed search

- Search with info
- Use knowledge to find steps to soln
- Quick soln
- Less complexity (time, space)
- Eg - Best first search
A*
Heuristic DFS

→ The process of looking for a sequence of actions that reaches the goal is called SEARCH.

→ A problem can be defined formally by 5 components.

1) initial state

2) actions

3) Transition model

4) goal test

5) path cost

state space - set of all states
reachable from initial state
by any sequence of actions.

→ An action sequence that leads from the initial state to goal state is called the SOLUTION.

→ OPTIMAL SOLN - has lowest path cost among all solutions.

→ Process of removing detail from representation is called ABSTRACTION.

→ Definition of a problem -

Initial state - s^0

Actions - $\{a_1, a_2, a_3, \dots\}$

Result $(s, a) = s'$

Goal test $(s) = \text{True/False}$

Path cost $(s_1 \xrightarrow{a_1} s_{i+1} \xrightarrow{a_2} s_{i+2}) \rightarrow \text{cost value}(n)$
where $i = 0, 1, \dots$
 $j = 1, 2, \dots$

Step cost $(s, a, s') \rightarrow n$

→ Uniformed search have no additional info about state beyond that provided in the problem definition, so they can only proceed by generating successors until they find a goal state

→ Root - initial state

branches - action

nodes - states

leaf node - node with no children

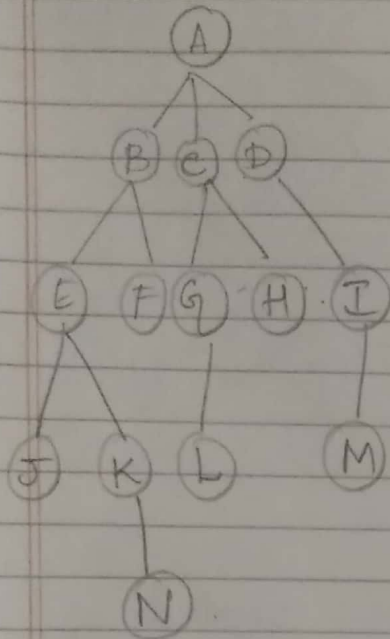
frontier - set of all leaf nodes available for expansion at any given point.

→ In graph-search, the frontier separates the state-space graph into explored & unexplored region, so that every path from initial state to an unexplored state has to pass through a state in the frontier

Uninformed

BFS - Breadthwise search / level search

- Uninformed search - no info about goal / cost / etc..
- FIFO (Queue)
- Optimal & complete (shortest & gives answer for sure)

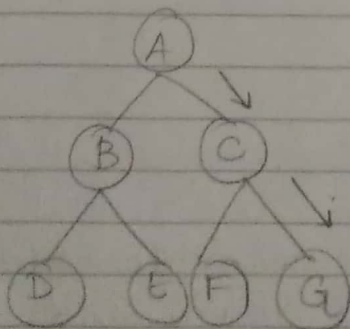


← queue ←

A
B C D
E F
G H
I
J K
L
M
N
=

3) DFS - Depthfirst Search

- Uninformed
- LIFO (Stack)
- non optimal & incomplete



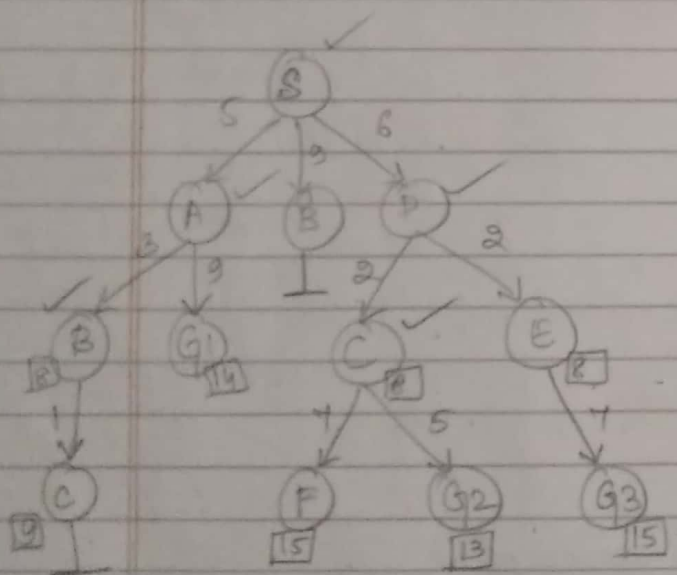
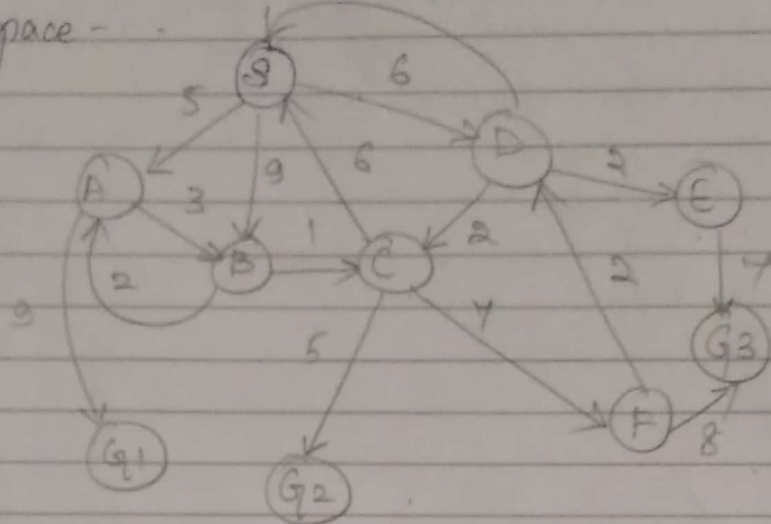
Stack

A B B B B
E D D

ACGFBED

- 3) Uniform cost search - move from start state to one of the goal state with minimal total cost on the path.
- cheapest path
 - uninformed search ..

Search space -



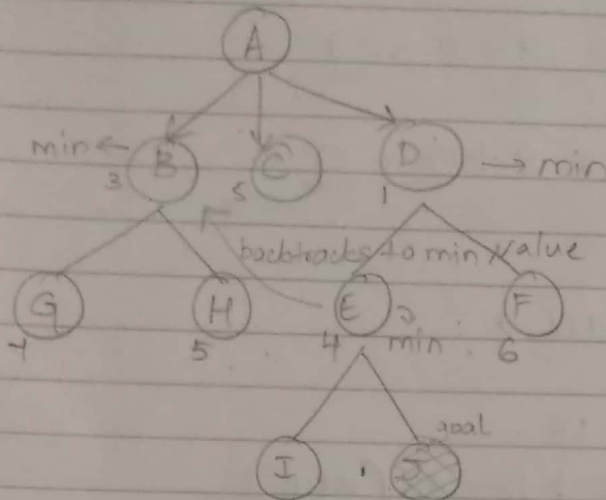
visited
S, A, D, B, C, E

Smallest E_f
check if it's goal
If it is then stop, else gotta expand

→ Informed search/heuristic search have additional info about search states, so they can guide the search by ranking successors acc to some fitness score. until they find a goal state.

Informed -

- 1) Best first search - depends on heuristic value
- Greedy search
 - priority queue is used
 - ↳ closed - already explored/visited
 - ↳ open - not visited



open - A, B, C, D, G, F
G, H

closed - A, B, D, E

Goal
A → D → E → J

- 2) A* Search - avoids expanding paths that are already expensive, but expands most promising paths first.

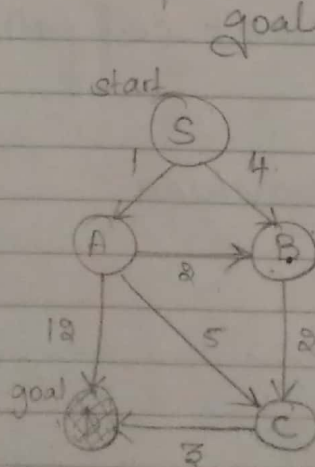
$$f(n) = g(n) + h(n) \rightarrow \text{heuristic value}$$

estimated total
path to reach
goal

cost to reach
the node

$$f(n) = g(n) + h(n)$$

$$S \rightarrow f(A) = 0 + 7 = 7$$



(str-line dist)
heuristic value

| | |
|---|---|
| S | 4 |
| A | 6 |
| B | 2 |
| C | 1 |
| D | 0 |

$$S \rightarrow A \quad f(n) = 1 + 6 = 7$$

$$S \rightarrow B \quad f(n) = 4 + 2 = 6 \text{ (min)}$$

$$\text{So, } S \rightarrow B \rightarrow C \quad f(n) = 6 + 1 = 7$$

$$B \rightarrow A \rightarrow B = 3 + 2 = 5 \text{ (min)}$$

$$B \rightarrow A \rightarrow C = 6 + 1 = 7$$

$$B \rightarrow A \rightarrow D = 13 + 0 = 13$$

paths - S → A (use this) now (used)

(used) S → B, S → B → C

(used) S → A → B, S → A → C, S → A → D

(used) S → A → B → C

S → A → B → C → D (2 = 8)

use these P.T.O (used)

$$S \rightarrow A \rightarrow B \rightarrow C = 5 + 1 = \underline{6} \text{ (min)}$$

$$S \rightarrow A \rightarrow B \rightarrow C \rightarrow D = 8 + 0 = \underline{8}$$

hence
↓

$$(S \rightarrow B \rightarrow C) \rightarrow D = 9 + 0 = \underline{9}$$

$$(S \rightarrow A \rightarrow C) \rightarrow D = 9 + 0 = \underline{9}$$

Now,
total goal paths are →

$$S \rightarrow A \rightarrow D = 13$$

$$S \rightarrow A \rightarrow B \rightarrow C \rightarrow D = 8 \text{ (min)}$$

$$S \rightarrow B \rightarrow C \rightarrow D = 9$$

$$S \rightarrow A \rightarrow C \rightarrow D = 9$$

∴ Goal path ↓

$$\underline{S \rightarrow A \rightarrow B \rightarrow C \rightarrow D} \quad \underline{\text{cost} = 8}$$

→ Will A* always find the lowest cost path?
Depends on h value.

→ Condns for problem solving by searching

- 1) fully observable
- 2) known
- 3) discrete
- 4) Deterministic
- 5) Static

Heuristic search - Guides the search process in the most profitable path among all that are available

informed

| | | |
|---|---|---|
| 7 | 2 | 4 |
| 5 | - | 6 |
| 8 | 3 | 1 |

start state

| | | |
|---|---|---|
| - | 1 | 2 |
| 3 | 4 | 5 |
| 6 | 7 | 8 |

goal state

h_1 - spaces filled - 8

h_2 - sum of shortest distances to reach goal state
2's shortest dist

$$\underline{3} + \underline{1} + \underline{2} + 2 + 2 + 3 + 3 + 2 = 18$$

1's shortest dist 3's shortest dist

optimal soln - $h_1 + h_2 = 8 + 18 = \underline{26}$ moves max needed to solve problem

8 puzzle problem - (without heuristic)

uninformed

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 8 | - |
| 7 | 6 | 5 |

start state

| | | |
|---|---|---|
| 1 | 2 | 3 |
| 4 | 5 | 6 |
| 7 | 8 | - |

goal state

$\{(123), (480), (765)\} \rightarrow$ Initial state

$\{(123), (485), (760)\}$

$\{(123), (486), (706)\}$

$\{(123), (405), (786)\}$

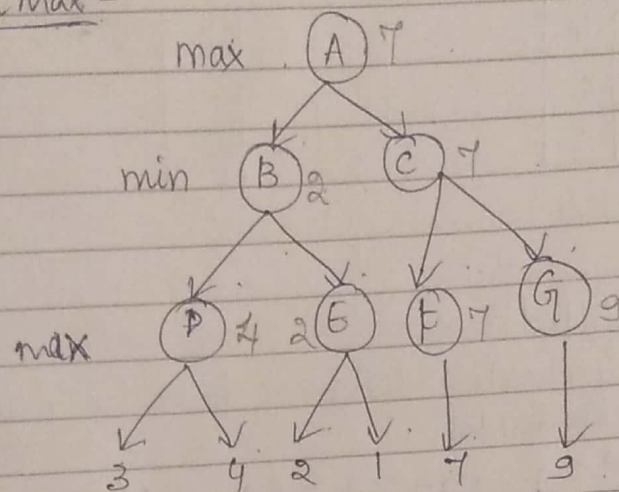
$\{(123), (450), (786)\}$

$\{(123), (456), (780)\}$

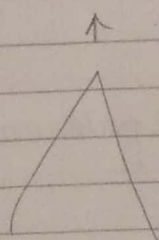
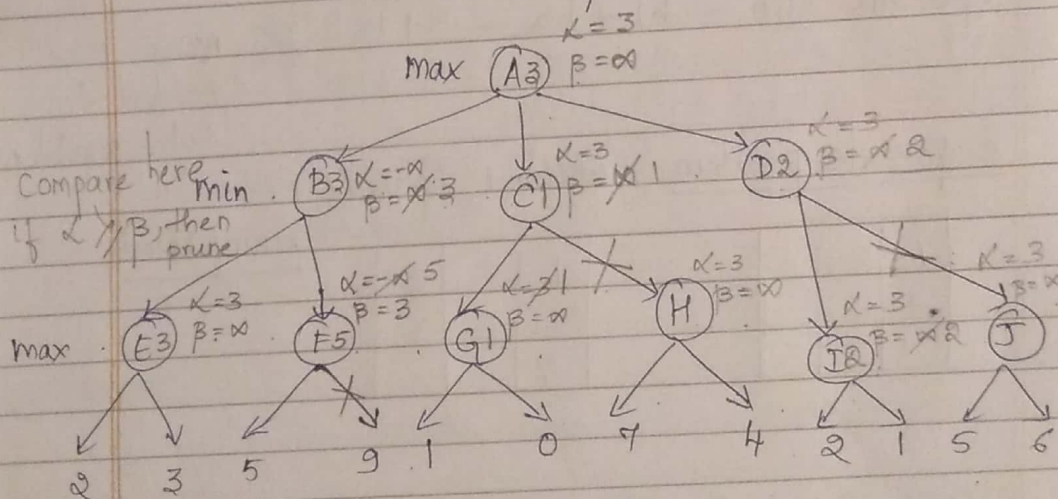
Total path cost = 5

Game tree \rightarrow MinMax
 \rightarrow α - β pruning

Min Max -



α - β pruning - α β $\alpha = -\infty$ (max)
 $\beta = \infty$ (min)



No. of α cutoffs - 1
 No. of β cutoffs - 2

Hidden Markov Model - used in speech recognition

| <u>Hidden</u> | <u>observed</u> |
|----------------|-----------------|
| B - Basketball | S - Sunny |
| F - Football | C - Cloudy |
| G - Games | R - Rainy |

State transition table 1

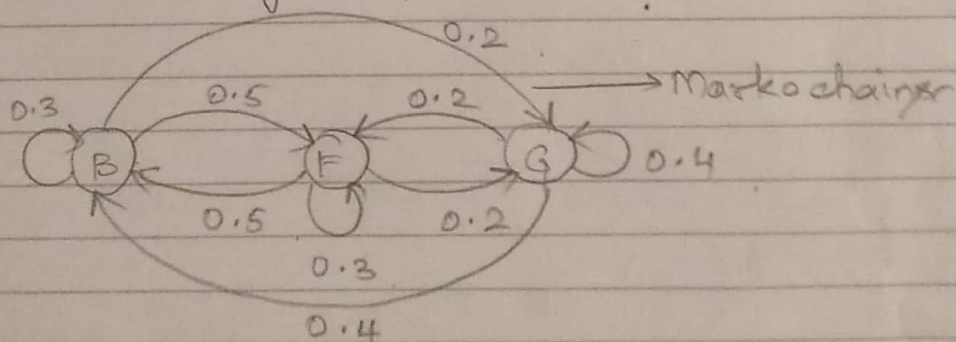
| Start/End | B | F | G | Sum |
|-----------|-----|-----|-----|-----|
| B | 0.3 | 0.5 | 0.2 | 1 |
| F | 0.5 | 0.3 | 0.2 | 1 |
| G | 0.4 | 0.2 | 0.4 | 1 |

↓
own values but sum should be equal to 1

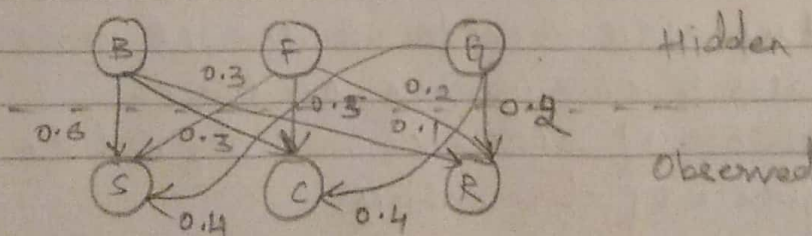
State transition table 2

| Start/End | S | C | R | Sum |
|-----------|-----|-----|-----|-----|
| B | 0.6 | 0.3 | 0.1 | 1 |
| F | 0.3 | 0.5 | 0.2 | 1 |
| G | 0.4 | 0.4 | 0.2 | 1 |

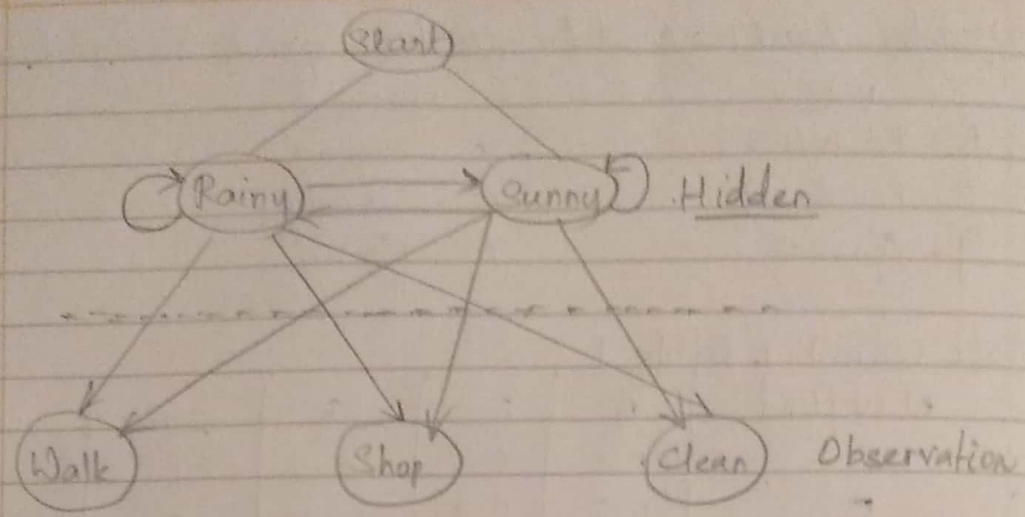
State transition diagram for table (1)



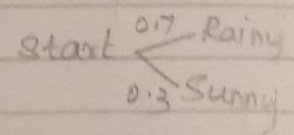
State transition table diagram for table (2)



20)



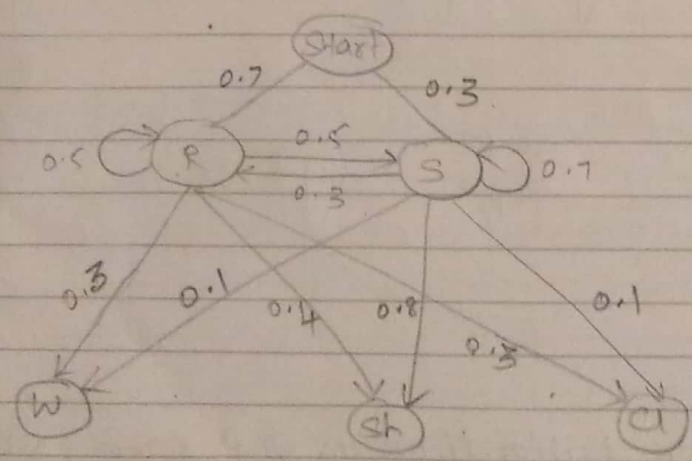
Draw transition tables



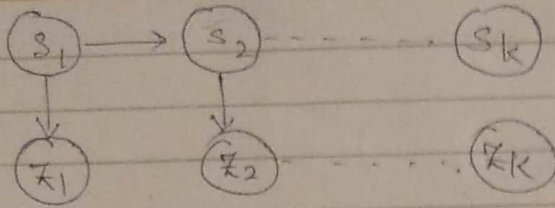
Random values
which sum upto
1

| Start/End | Rainy | Sunny | Sum |
|-----------|-------|-------|-----|
| Rainy | 0.5 | 0.5 | 1 |
| Sunny | 0.4 | 0.3 | 1 |

| Start/End | W | Sh | cl | Sum |
|------------------------|-----|-----|-----|-----|
| Rainy Rainy | 0.3 | 0.4 | 0.2 | 1 |
| Sunny Sunny | 0.1 | 0.8 | 1 | 1 |
| Clean | 0.8 | 0.2 | | |

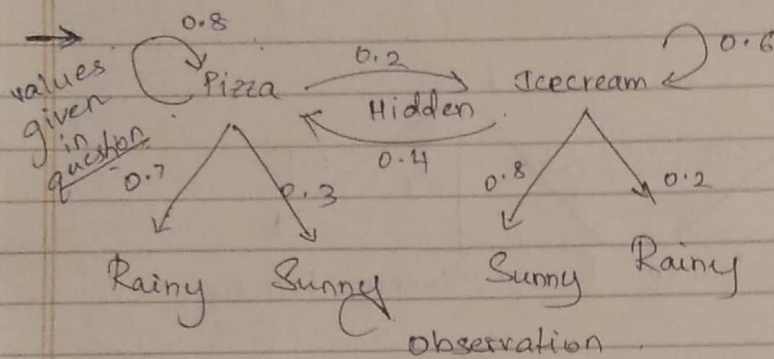


- Future state depends on current state
- States & observations are known
- sequence of states is not defined to get particular sequence of observations



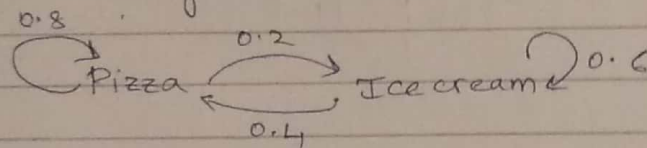
s_{1-k} - States

x_{1-k} - observations

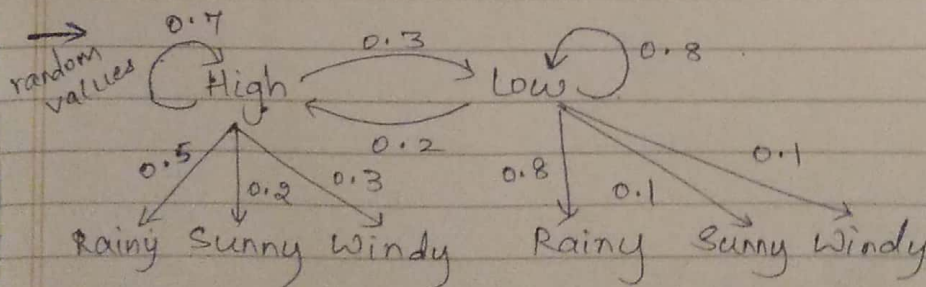
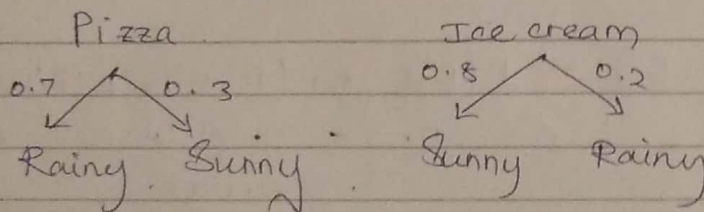


Draw Transition & emission probabilities -

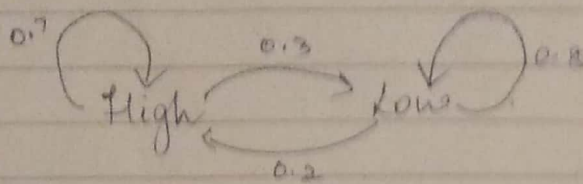
Transition probabilities -



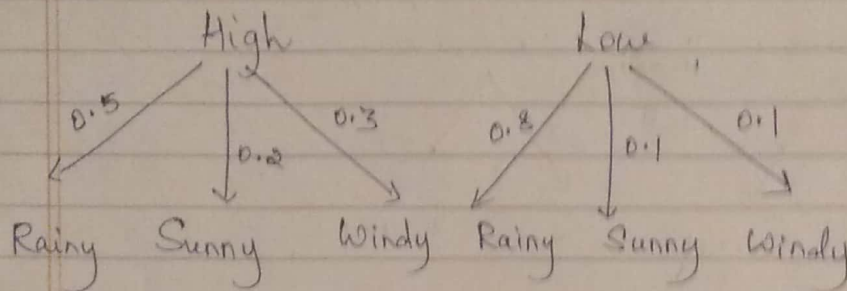
Emission probabilities -



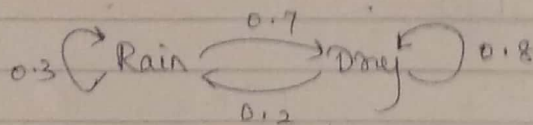
Transition probabilities-



Emission probabilities-



→



$$P(D|D) = 0.8$$

$$P(R|R) = 0.3$$

$$P(R|D) = 0.7$$

$$P(D|R) = 0.2$$

$$\begin{aligned}
 P(D, D, R, R) &= P(R|R) * P(R|D) * P(D|D) * P(D|R) \\
 &= 0.3 * 0.7 * 0.8 * 0.2 \\
 &= \underline{\underline{0.0336}}
 \end{aligned}$$