

ZADATK 1

$$T = 300 \text{ K}$$

$$n = 10^{15} \text{ cm}^{-3}$$

$$p = ?$$

$$T = 550 \text{ K}$$

$$n, p = ?$$

izvod:

$$np = n_i^2$$

$$n + N_A = p + N_D$$

$$p = n - N_D$$

$$n(n - N_D) = n_i^2$$

$$n^2 - N_D n - n_i^2 = 0$$

$$n_{2,2} = \frac{N_D \pm \sqrt{N_D^2 + 4n_i^2}}{2}$$

$$n = \frac{N_D + \sqrt{N_D^2 + 4n_i^2}}{2}$$

$$n = 1,9 \cdot 10^{15} \text{ cm}^{-3}$$

ZADATK 2.

$$N_A = 1,5 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_D = 10^{15} \text{ cm}^{-3}$$

$$T_1 = 300 \text{ K}$$

$$T_2 = 473 \text{ K}$$

nakon prvog:

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$N_A \gg n_i \Rightarrow p = 1,5 \cdot 10^{15}$$

$$n = 138240$$

nakon drugog

$$N_{\text{neto}} = N_A - N_D = 5 \cdot 10^{14} \text{ cm}^{-3}$$

$$N_{\text{neto}} \gg n_i$$

$$p = N_{\text{neto}} = 5 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = 414720 \text{ cm}^{-3}$$

$$n_i = C_1 T^{\frac{3}{2}} \exp\left(-\frac{E_{\text{go}}}{2kT}\right)$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$np = n_i^2 \Rightarrow p = 209675 \text{ cm}^{-3}$$

$$n \gg n_i$$

$$N_D = 10^{15}$$

$$n_i = 1,32 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_D = 10^{15}$$

$$np = n_i^2$$

$$p = 9,12 \cdot 10^{14} \text{ cm}^{-3}$$

$$n_i = 1,35 \cdot 10^{14} \text{ cm}^{-3}$$

$$N_A \gg n_i$$

$$p = N_A = 1,5 \cdot 10^{15} \text{ cm}^{-3}$$

$$n = 1,21 \cdot 10^{15} \text{ cm}^{-3}$$

$$p = \frac{N_{\text{neto}} + \sqrt{N_{\text{neto}}^2 + 4n_i^2}}{2}$$

$$p = 5,34 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = 3,41 \cdot 10^{15} \text{ cm}^{-3}$$

$$n_i = 4.96 \cdot 10^{11} \text{ cm}^{-3}$$

$$n = 2.46 \cdot 10^{17} \text{ cm}^{-3}$$

$$N_D = 2.46 \cdot 10^{17} \text{ cm}^{-3}$$

$$n_i = 1.71 \cdot 10^{14}$$

$$N_D \gg n_i$$

$$n = 2.46 \cdot 10^{17} \text{ cm}^{-3}$$

$$p = 1.19 \cdot 10^{11}$$

ZADATK 4.

$$N_A = 1.5 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_D = 2 \cdot 10^{15} \text{ cm}^{-3}$$

$$n_i = 1.44 \cdot 10^{10} \text{ cm}^{-3}$$

$$T = 300 \text{ K}$$

nakon prvog

$$N_A \gg n_i$$

$$p = N_A = 1.5 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_V = 3.67 \cdot 10^{19}$$

$$p_0 = N_V \exp\left(\frac{E_V - E_F}{E_T}\right)$$

$$\ln \frac{p_0}{N_V} = \frac{E_V - E_F}{E_T}$$

$$E_V - E_F = -0.261$$

$$E_F = E_V + 0.261 \text{ eV}$$

nakon drugog

$$N_{\text{neto}} = N_D - N_A$$

$$N_{\text{neto}} = 5 \cdot 10^{14}$$

$$N_{\text{neto}} \gg n_i$$

$$n = 5 \cdot 10^{14}$$

$$N_C = 3.67 \cdot 10^{19}$$

$$n_0 = N_C \exp\left(\frac{E_F - E_C}{E_T}\right)$$

$$E_F - E_C = -0.289$$

$$E_F = E_C - 0.289$$

$$E_F - E_C = -0,2$$

$$n_0 = N_C \exp\left(\frac{E_F - E_C}{kT}\right)$$

$$n_0 = 3,67 \cdot 10^{15} \exp\left(\frac{-0,2}{kT}\right)$$

$$n_0 = 1,6 \cdot 10^{16} \text{ cm}^{-3} \quad n\text{-tip}$$

$$n \gg n_i \quad N_D = n = 1,6 \cdot 10^{16} \text{ cm}^{-3}$$

a) prema rnu odzivnog

$$E_F - E_C = -0,1$$

$$n_0 = 7,63 \cdot 10^{17} \text{ cm}^{-3}$$

$$N_{D2} = n - N_{D1} = 7,52 \cdot 10^{17}$$

b) prema rnu valenlog

$$E_F - E_C = -0,3$$

$$n_0 = 3,36 \cdot 10^{14} \text{ cm}^{-3}$$

$$n_0 \gg n_i$$

$$N_{A1} - n_{02} = N_{A2}$$

$$N_A = 1,566 \cdot 10^{16} \text{ cm}^{-3}$$

ZADATAK 6.

$$T = 300 \text{ K}$$

$$n = 10^{15} \text{ cm}^{-3}$$

$$\sigma = ? \quad T = 300 \text{ K} \quad T = 530 \text{ K}$$

$$\mu_n = 900 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 350 \text{ cm}^2/\text{Vs}$$

$$\mu_{n2} = 0,8 \cdot 900 = 720 \text{ cm}^2/\text{Vs}$$

$$\mu_{p2} = 0,8 \cdot 350 = 280 \text{ cm}^2/\text{Vs}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$p = 2,07360$$

$$N_D = n$$

$$G = q(\mu_n \cdot n + \mu_p \cdot p)$$

$$G = 0,144 \text{ S/cm}$$

$$n_i = 7,74 \cdot 10^{14} \text{ cm}^{-3}$$

$$N_D = 10^{15} \text{ cm}^{-3}$$

$$n = \frac{N_D + \sqrt{N_D^2 + 4n_i^2}}{2}$$

$$n = 1,42 \cdot 10^{15} \text{ cm}^{-3}$$

$$p = 4,2 \cdot 10^{14} \text{ cm}^{-3}$$

$$G = q(\mu_n \cdot n + \mu_p \cdot p)$$

$$G = 0,182 \text{ S/cm}$$

$$N_{x2} = 2 \cdot 10^{15} \text{ cm}^{-3}$$

$$T = 300 \text{ K}$$

$$N_n = 900 \text{ cm}^2/\text{Vs}$$

$$N_p = 350 \text{ cm}^2/\text{Vs}$$

$$a) N_{x1} = N_{D1}$$

$$N_{x2} = N_{D2}$$

$$G = q \cdot \underbrace{(N_{D1} + N_{D2})}_{\approx n} \cdot N_n$$

$$G = 0,504 \text{ S/cm}$$

$$b) N_{x1} = N_D$$

$$N_{x2} = N_A$$

$$N_{\text{Aneto}} = 3 \cdot 10^{14}$$

$$G = q \cdot p \cdot \mu_p$$

$$G = 0,028 \text{ S/cm}$$

$$N_{\text{Aneto}} \approx p$$

$$n = \frac{n_i^2}{p} = 414720$$

ZADATK 8.

$$r = R = \frac{1}{\sigma} \cdot \frac{l}{S}$$

$$l = 10 \mu\text{m} = 10^{-3} \text{ cm}$$

$$S = 0,1 \text{ mm}^2 = 10^{-3} \text{ cm}^2$$

$$N_A = 10^{15} \text{ cm}^{-3}$$

$$N_D = 9 \cdot 10^{14} \text{ cm}^{-3}$$

$$N_n = 900$$

$$N_p = 350 \text{ cm}^2/\text{Vs}$$

$$T_1 = 300 \text{ K}$$

$$T_2 = 450 \text{ K}$$

$$\frac{T_1}{T_2} \quad N_{\text{Aneto}} = 10^{14} \text{ cm}^{-3}$$

$$N_A \gg n_i$$

$$N_A \approx p$$

$$n = 2 \cdot 10^6 \text{ cm}^{-3}$$

$$G = q \cdot \mu_p \cdot p$$

$$= 5,6 \cdot 10^{-3} \text{ S/cm}$$

$$R = \frac{1}{G} \cdot \frac{l}{S}$$

$$R = 179 \Omega$$

$$\frac{T_2}{T_1} \quad n_i = 5,91 \cdot 10^{13}$$

$$p = \frac{N_A + \sqrt{N_A^2 + 4n_i^2}}{2}$$

$$p = 1,27 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = 2,74 \cdot 10^{13} \text{ cm}^{-3}$$

$$G = q \cdot (N_p \cdot p + \mu_n \cdot n)$$

$$= 0,011$$

$$R = 90,4 \Omega$$

drift na struja

$$p = q \cdot p \cdot N_p \cdot S \cdot F = 5 \cdot S \cdot F$$

$$= 18,48 \text{ mA}$$

ZADATAK 10

$$J(x=0)$$

$$P_0 = 10^{15} \text{ cm}^{-3}$$

$$P_A = 5 \cdot 10^{15} \text{ cm}^{-3}$$

$$a = 10 \text{ nm}$$

$$N_p = 330 \text{ cm}^{-3} \text{ Vs}$$

$$T = 300 \text{ K}$$

$$D_p = N_p \cdot U_T$$

$$= 9,82 \text{ cm}^2/\text{s}$$

$$p(x) = p_0 + (p_A - p_0) \cdot e^{-\frac{x}{a}}$$

$$J_{DP} = -q \cdot D_p \cdot \frac{dp(x)}{dx}$$

$$= -q \cdot D_p \cdot \left(-\frac{1}{a} (p_A - p_0) \right) \cdot e^{-\frac{x}{a}}$$

$$= q \cdot D_p \cdot \frac{(p_A - p_0)}{a} \cdot e^{-\frac{x}{a}}$$

$$p_A \gg p_0$$

$$= q \cdot D_p \cdot \frac{P_A}{a} \cdot e^{-\frac{x}{a}}$$

$$= 7,86 \cdot 10^{-3} \text{ A/cm}^2$$

$$J_{DP}(x) = J_{DP}(0) \cdot e^{-\frac{x}{a}}$$

$$0,1 J_{DP}(0) = J_{DP}(0) \cdot e^{-\frac{x}{a}}$$

$$x = 2,3 \cdot 10^{-3} \text{ cm}$$

VJ. 1. $T = 300 \text{ K}$

$$p = 5 \cdot 10^{15} \text{ cm}^{-3}$$

$$n(300) = \frac{n_i(300)^2}{p}$$

$$n = 44472 \text{ cm}^{-3}$$

$$p \approx N_A = 5 \cdot 10^{15} \text{ cm}^{-3}$$

$$T = 550 \text{ K}$$

$$n_i = 1,32 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_A = 5 \cdot 10^{15} \text{ cm}^{-3}$$

$$p = \frac{N_A + \sqrt{N_A^2 + 4n_i^2}}{2}$$

$$p = 5,33 \cdot 10^{15} \text{ cm}^{-3}$$

$$n = 3,27 \cdot 10^{14} \text{ cm}^{-3}$$

VJ. 2.

$$T = 350 \text{ K}$$

$$p = 10^{17} \text{ cm}^{-3}$$

$$n_i = 4,96 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = 2,46 \cdot 10^{16} \text{ cm}^{-3}$$

$$N_D \approx 2,46 \cdot 10^{16} \text{ cm}^{-3}$$

$$T = 550$$

$$n_i = 1,32 \cdot 10^{15} \text{ cm}^{-3}$$

$$n = \frac{N_D + \sqrt{N_D^2 + 4n_i^2}}{2}$$

$$n = 1,36 \cdot 10^{16} \text{ cm}^{-3}$$

$$p = 10^{15} \text{ cm}^{-3}$$

$$n_i = 3,44 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = 1,05 \cdot 10^{14} \text{ cm}^{-3}$$

$$n + N_A = p + N_D$$

$$N_{\text{Aneto}} = p - n$$

$$= 3,95 \cdot 10^{14}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$N_A \approx p \approx 8,95 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = 2,32 \cdot 10^5 \text{ cm}^{-3}$$

V J. 4.

$$T = 450 \text{ K}$$

$$n = 10^{12} \text{ cm}^{-3}$$

$$n_i = 5,92 \cdot 10^{13} \text{ cm}^{-3}$$

$$p = 3,5 \cdot 10^{15}$$

$$N_A \approx p$$

$$T = 300 \text{ K}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$p \approx 3,5 \cdot 10^{15} \text{ cm}^{-3}$$

$$n = 5,92 \cdot 10^4 \text{ cm}^{-3}$$

V J. 5.

$$T = 450 \text{ K}$$

$$n = 10^{11} \text{ cm}^{-3}$$

$$n_i = 5,92 \cdot 10^{13} \text{ cm}^{-3}$$

$$p = 3,5 \cdot 10^{16} \text{ cm}^{-3}$$

$$N_A \approx 3,5 \cdot 10^{16} \text{ cm}^{-3}$$

V J. 6.

$$T = 350 \text{ K}$$

$$n = 10^{14} \text{ cm}^{-3}$$

$$n_i = 4,96 \cdot 10^{11} \text{ cm}^{-3}$$

$$p = 2,46 \cdot 10^6 \text{ cm}^{-3}$$

$$N_D \approx 10^{17} \text{ cm}^{-3}$$

V J. 7.

$$T = 200 \text{ K}$$

$$p = 10^{13} \text{ cm}^{-3}$$

$$n_i = 7,5 \cdot 10^4 \text{ cm}^{-3}$$

$$p \gg n_i$$

$$n = 10^{13} \text{ cm}^{-3}$$

V.J. 8.

$$N_A = 10^{15} \text{ cm}^{-3}$$

$$N_D = 1,35 \cdot 10^{15} \text{ cm}^{-3}$$

$$T = 300 \text{ K}$$

$$N_{\text{neto}} = 2,5 \cdot 10^{14} \text{ cm}^{-3}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$n \approx N_D \gg n_i$$

$$n = 2,5 \cdot 10^{14} \text{ cm}^{-3}$$

$$p = 3,29 \cdot 10^5 \text{ cm}^{-3}$$

$$T = 473 \text{ K}$$

$$n_i = 1,35 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = \frac{N_{\text{neto}} + \sqrt{N_{\text{neto}}^2 + 4n_i^2}}{2}$$

$$n = 3,03 \cdot 10^{14} \text{ cm}^{-3}$$

$$p = 5,89 \cdot 10^{13} \text{ cm}^{-3}$$

V.J. 9.

$$N_A = 1,5 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_D = 10^{15} \text{ cm}^{-3}$$

$$T = 300 \text{ K}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$N_{\text{neto}} = 5 \cdot 10^{14} \text{ cm}^{-3} \gg n_i$$

$$p = 5 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = 4,15 \cdot 10^5 \text{ cm}^{-3}$$

$$T = 450 \text{ K}$$

$$n_i = 5,92 \cdot 10^{13} \text{ cm}^{-3}$$

$$p = \frac{N_{\text{neto}} + \sqrt{N_{\text{neto}}^2 + 4n_i^2}}{2}$$

$$p = 5,07 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = 6,91 \cdot 10^{13} \text{ cm}^{-3}$$

V.J. 10.

$$T = 300 \text{ K}$$

$$n = 5 \cdot 10^7 \text{ cm}^{-3}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$p = 4,15 \cdot 10^{14} \text{ cm}^{-3}$$

$$N_{A1} \approx 4,15 \cdot 10^{14} \text{ cm}^{-3}$$

$$T = 450 \text{ K}$$

$$n_i = 5,92 \cdot 10^{13} \text{ cm}^{-3}$$

$$n = 5 \cdot 10^7 \text{ cm}^{-3}$$

$$p = 7 \cdot 10^{19}$$

$$N_{A2} \approx 7 \cdot 10^{19}$$

$$N_{Au} = N_{A2} - N_{A1} \approx N_{A2}$$

$$= 7 \cdot 10^{19} \text{ cm}^{-3}$$

V.J. 11.

$$T = 300 \text{ K}$$

$$p = 10^{15} \text{ cm}^{-3}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$n = 207360$$

$$N_A \approx 10^{15}$$

$$T = 550$$

$$n_i = 1,32 \cdot 10^{15} \text{ cm}^{-3}$$

$$p = 10^{15}$$

$$n = 1,74 \cdot 10^{15}$$

$$n + N_A = p + N_D$$

$$N_D = 1,74 \cdot 10^{15} \text{ cm}^{-3}$$

$$E_F - E_C = -0.18 \text{ eV}$$

$$N_C = CT^{\frac{3}{2}} = 3,67 \cdot 10^{19}$$

$$n = N_C \exp\left(\frac{E_F - E_C}{E_T}\right)$$

$$n = 3,49 \cdot 10^{16} \text{ cm}^{-3}$$

$$p = 5941$$

$$N_D = 3,49 \cdot 10^{16} \text{ cm}^{-3}$$

$$0,18 + E_V = E_F$$

$$E_V - E_F = -0,18$$

$$p = 3,49 \cdot 10^{16} \text{ cm}^{-3}$$

$$N_A = 3,49 \cdot 10^{16} \text{ cm}^{-3}$$

$$N_{AV} = N_A + N_D = 6,98 \cdot 10^{16} \text{ cm}^{-3}$$

VJ. 13.

$$T = 300 \text{ K}$$

$$n = 10^{15} \text{ cm}^{-3}$$

$$n \gg p$$

$$N_D = 10^{15}$$

$$N_n = 450 \text{ cm}^2/\text{Vs}$$

$$N_p = 220 \text{ cm}^2/\text{Vs}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$T = 523 \text{ K}$$

$$n_i = 7,31 \cdot 10^{14} \text{ cm}^{-3}$$

$$n = \frac{N_D + \sqrt{N_D^2 + 4n_i^2}}{2}$$

$$n = 1,39 \cdot 10^{15} \text{ cm}^{-3}$$

$$p = 3,84 \cdot 10^{14}$$

$$\sigma = q(N_n \cdot n + N_p \cdot p)$$

$$= 0,114 \text{ S/cm}$$

VJ. 14

$$T = 300 \text{ K}$$

$$n = 10^{14} \text{ cm}^{-3}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$p = 2,07 \cdot 10^{16} \text{ cm}^{-3}$$

$$N_A = 2,07 \cdot 10^{16} \text{ cm}^{-3}$$

$$T = 400 \text{ K}$$

$$\mu_n = 800 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 520 \text{ cm}^2/\text{Vs}$$

$$n_i = 7,23 \cdot 10^{12} \text{ cm}^{-3}$$

$$p = N_A = 2,07 \cdot 10^{16}$$

$$n = 2,52 \cdot 10^9$$

$$\sigma = q \cdot \mu_p \cdot p$$

$$\sigma = 1,06 \text{ S/cm}$$

$$n = 10 \cdot p$$

$$n_i = 6,75 \cdot 10^{14} \text{ cm}^{-3}$$

$$n \cdot p = n_i^2$$

$$10 p^2 = n_i^2$$

$$p = 2,13 \cdot 10^{14}$$

$$n = 2,13 \cdot 10^{15}$$

$$p + N_D = n + N_A$$

$$N_D - N_A = 1,917 \cdot 10^{15} \text{ cm}^{-3} \text{ Noheta}$$

$$VJ. 16. \quad T = 400 \text{ K}$$

$$p = n \cdot 10^5$$

$$n_i = 2,23 \cdot 10^{10} \text{ cm}^{-3}$$

$$n^2 \cdot 10^5 = n_i^2$$

$$n = 2,23 \cdot 10^{10} \text{ cm}^{-3}$$

$$p = 2,23 \cdot 10^{15} \text{ cm}^{-3} \gg n$$

$$N_A = 2,23 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_n = 300 \text{ cm}^{-1} \text{Vs}$$

$$N_p = 350 \text{ cm}^{-1} \text{Vs}$$

$$n = 1,917 \cdot 10^{15}$$

$$\sigma = q \cdot n \cdot N_n$$

$$\sigma = 0,276 \text{ S/cm}$$

$$T = 300 \text{ K}$$

$$N_n = 300 \text{ cm}^{-1} \text{Vs}$$

$$N_p = 350 \text{ cm}^{-1} \text{Vs}$$

$$p = 2,23 \cdot 10^{15} \text{ cm}^{-3}$$

$$\sigma = q \cdot p \cdot N_p$$

$$\sigma = 0,128 \text{ S/cm}$$

$$y = ?$$

$$y = \frac{1}{\sigma} = 7,83 \text{ } \Omega \cdot \text{cm}$$

$$VJ. 17 \quad T = 550$$

$$\sigma = 0,28 \text{ S/cm}$$

$$\sigma = q \cdot (N_n \cdot n + N_p \cdot p)$$

$$n_i = 1,32 \cdot 10^{15} \text{ cm}^{-3}$$

$$\frac{\sigma}{q} = N_n \cdot n + N_p \cdot \frac{n_i^2}{n} \cdot \frac{1}{n}$$

$$\frac{\sigma}{q} \cdot n = N_n \cdot n^2 + N_p \cdot n_i^2$$

$$300 n^2 - 1,75 \cdot 10^{13} n + 6,0934 \cdot 10^{32} = 0$$

$$\rightarrow n_1 = 1,49 \cdot 10^{15} \text{ cm}^{-3}$$

$$n_2 = 4,55 \cdot 10^{14} \text{ cm}^{-3}$$

$$\rightarrow p_1 = 1,47 \cdot 10^{15} \text{ cm}^{-3}$$

$$p_2 = 3,83 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_A = 2,13 \cdot 10^{14}$$

$$T = 300$$

$$\sigma = 0,28 \text{ S/cm}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$300 n^2 - 1,75 \cdot 10^{13} n + 725 \cdot 10^{22} = 0$$

$$n_1 = 1,94 \cdot 10^{15}$$

$$n_2 = 4,42 \cdot 10^{14}$$

$$N_D = 1,34 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_n = 300 \text{ cm}^{-1} \text{Vs}$$

$$N_p = 350 \text{ cm}^{-1} \text{Vs}$$

$$N_{D2} = N_D - N_{\text{Donato}} = 1,62 \cdot 10^{15}$$

$$N_A = 10^{14} \text{ cm}^{-3}$$

$$T_i = 300$$

$$T_d = 450 \text{ K}$$

$$N_B = 1.1 \cdot 10^{13} \text{ cm}^{-3}$$

$$N_P = 330 \text{ cm}^2/\text{Vs} \quad N_P = 297.5 \text{ cm}^2/\text{Vs}$$

$$N_n = 900 \text{ cm}^2/\text{Vs} \quad N_n = 765 \text{ cm}^2/\text{Vs}$$

$$N_{Dnefo} = 10^{14} \text{ cm}^{-3}$$

$$n_i = 1.44 \cdot 10^{10} \text{ cm}^{-3}$$

$$n_i = 3.92 \cdot 10^{13} \text{ cm}^{-3}$$

$$n = N_{Dnefo}$$

$$n = \frac{N_{Dnefo} + \sqrt{N_{Dnefo}^2 + 4 \cdot n_i^2}}{2}$$

$$G = q \cdot n \cdot N_n$$

$$n = 1.27 \cdot 10^{14} \text{ cm}^{-3}$$

$$G = 0.0144 \text{ S/cm}$$

$$p = 2.75 \cdot 10^{13}$$

$$G = 0.0169 \text{ S/cm}$$

VJ. 19

$$N_{x1} = 5 \cdot 10^{16} \text{ cm}^{-3}$$

$$N_{x2} = 10^{17}$$

$$G = ? \quad \gamma = ?$$

$$N_n = 900 \text{ cm}^2/\text{Vs}$$

$$N_p = 350 \text{ cm}^2/\text{Vs}$$

a) naj veći $\Rightarrow G_{\min} \quad n_i = 1.44 \cdot 10^{10} \text{ cm}^{-3}$

$$N_{x1} = N_{D1}$$

$$N_{x2} = N_A$$

$$N_{Anefo} = 5 \cdot 10^{16}$$

$$p = 5 \cdot 10^{16}$$

$$G = 2.8 \text{ S/cm}$$

$$\gamma = 0.357 \text{ } \Omega\text{cm}$$

b) naj manji $\rightarrow G_{\max}$

$$N_{x1} = N_{D1}$$

$$N_{x2} = N_{D2}$$

$$N_D = 1.5 \cdot 10^{17} \text{ cm}^{-3}$$

$$G = 21.6 \text{ S/cm}$$

$$\gamma = 0.0463 \text{ } \Omega\text{cm}$$

VJ 20.

$$l = 10 \text{ } \mu\text{m} = 10^{-3} \text{ cm}$$

$$S = 1 \text{ } \mu\text{m}^2 = 10^{-3} \text{ cm}^2$$

$$G = 100 \text{ S/cm}$$

$$U = 1.8 \text{ V}$$

$$R = \frac{U}{I}$$

$$I = \frac{U}{R} = 1.8 \cdot 10^{-3} \text{ A}$$

$$R = \gamma \cdot \frac{l}{S} = \frac{1}{G} \cdot \frac{l}{S}$$

$$R = 1000 \text{ } \Omega$$

ZADATAK 1.

$$T = 300 \text{ K}$$

$$d_B = ?$$

$$U = 0 \text{ V}$$

$$N_A = 10^{17} \text{ cm}^{-3}$$

$$N_D = 10^{16} \text{ cm}^{-3}$$

$$C_B = ?$$

$$S = 5 \text{ mm}$$

$$n_i = 1,44 \cdot 10^{10} \text{ cm}^{-3}$$

$$P_{op} \approx N_A = 10^{17} \text{ cm}^{-3}$$

$$N_{on} = N_D = 10^{16} \text{ cm}^{-3}$$

$$U_k = U_T \cdot \ln\left(\frac{n_{on} \cdot P_{op}}{n_i^2}\right) = 0,755 \text{ V}$$

$$d_B = \sqrt{\frac{2 \cdot \epsilon_0 \cdot \epsilon_r}{L} \cdot \left(\frac{1}{N_A} + \frac{1}{N_D}\right) (U_k - U)} = 0,328 \text{ } \mu\text{m}$$

$$C_B = \epsilon_0 \cdot \epsilon_r \cdot \frac{S}{d_B} = 1,58 \text{ nF}$$

ZADATAK 2.

$$N_D = 10^{17} \text{ cm}^{-3}$$

$$N_A = 10^{15} \text{ cm}^{-3}$$

$$N_n = 900 \text{ cm}^2/\text{Vs}$$

$$N_p = 300 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 1 \text{ ns}$$

$$\tau_p = 0,5 \text{ ns}$$

$$S = 1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$I_s = ?$$

$$W_n \gg L_n$$

$$W_p \gg L_p$$

$$I_s = q \cdot S \left(D_n \frac{n_{op}}{L_n} + D_p \frac{p_{op}}{L_p} \right)$$

$$n_{op} = \frac{n_i^2}{N_A} = 207360 \text{ cm}^{-3}$$

$$p_{op} = \frac{n_i^2}{N_D} = 2073,6 \text{ cm}^{-3}$$

$$D_n = N_n \cdot U_T = 23,28 \text{ cm}^2/\text{s}$$

$$D_p = N_p \cdot U_T = 7,76 \text{ cm}^2/\text{s}$$

$$L_n = \sqrt{D_n \tau_n} = 48,25 \text{ } \mu\text{m}$$

$$L_p = \sqrt{D_p \tau_p} = 19,7 \text{ } \mu\text{m}$$

$$I_s = 1,63 \cdot 10^{-12} \text{ A}$$

$$I = I_s \left(\exp\left(\frac{U}{U_T}\right) - 1 \right)$$

$$I = 0,41 \text{ mA}$$

$$N_D = 10^{15} \text{ cm}^{-3}$$

$$N_A = 10^{12} \text{ cm}^{-3}$$

$$\mu_n = 700 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 350 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 0,5 \text{ ns}$$

$$\tau_p = 1 \text{ ns}$$

$$S = 1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$V = 0,5 \text{ V}$$

$$m = 1$$

$$L_p \gg W_n = 1 \mu\text{m}$$

$$L_n \gg W_p = 2 \mu\text{m}$$

$$I_s = q \cdot S \cdot \left(D_n \frac{n_{op}}{W_p} + D_p \frac{p_{on}}{W_n} \right)$$

$$n_{op} = 2073,6 \text{ cm}^{-3}$$

$$p_{on} = 207360 \text{ cm}^{-3}$$

$$D_n = 18,1 \text{ cm}^2/\text{s}$$

$$D_p = 9,05 \text{ cm}^2/\text{s}$$

$$I_s = 3,03 \cdot 10^{-11} \text{ A}$$

$$I = I_s \left(\exp \frac{V}{m V_T} - 1 \right)$$

$$= 7,55 \cdot 10^{-3} \text{ A}$$

ZADATAK 4.

$$N_D = 10^{17} \text{ cm}^{-3}$$

$$N_A = 10^{15} \text{ cm}^{-3}$$

$$\mu_n = 900 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 300 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 1 \text{ ns}$$

$$\tau_p = 0,5 \text{ ns}$$

$$S = 1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$I_s = ?$$

$$V = 0,5 \text{ V}$$

$$m = 1$$

$$L_p \gg W_n = 1 \mu\text{m}$$

$$L_n < W_p$$

$$L_n = \sqrt{D_n \cdot \tau_n} = 4,82 \cdot 10^{-3} \text{ cm}$$

$$n_{op} = 207360 \text{ cm}^{-3}$$

$$p_{on} = 2073,6 \text{ cm}^{-3}$$

$$D_n = 23,28 \text{ cm}^2/\text{s}$$

$$D_p = 7,76 \text{ cm}^2/\text{s}$$

$$I_s = q \cdot S \cdot \left(D_n \frac{n_{op}}{L_n} + D_p \frac{p_{on}}{W_n} \right)$$

$$= 1,86 \cdot 10^{-13} \text{ A}$$

$$I = I_s \cdot \left(\exp \left(\frac{V}{m V_T} \right) - 1 \right)$$

$$= 4,63 \cdot 10^{-4} \text{ A}$$

ZADATAK 5.

$$N_D = 10^{19} \text{ cm}^{-3}$$

$$N_A = 10^{17} \text{ cm}^{-3}$$

$$\mu_n = 700 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 350 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 0.15 \text{ ns}$$

$$\tau_p = 1 \text{ ns}$$

$$S = 1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$\xi = ?$$

$$U = 0.5 \text{ V}$$

$$L_p \ll W_n$$

$$L_n \gg W_p = 1 \mu\text{m}$$

$$I_s = q \cdot S \left(D_n \frac{n_{op}}{W_p} + D_p \frac{p_{on}}{L_p} \right)$$

$$n_{op} = \frac{n_i^2}{N_A} = 2073 \text{ cm}^{-3}$$

$$p_{on} = \frac{n_i^2}{N_D} = 207360 \text{ cm}^{-3}$$

$$D_n = 18.1 \text{ cm}^2/\text{s}$$

$$D_p = 9.05 \text{ cm}^2/\text{s}$$

$$L_p = \sqrt{D_p \cdot \tau_p} = 3 \cdot 10^3 \text{ cm}$$

$$I_s = 1.6 \cdot 10^{-12} \text{ A}$$

$$I = I_s \left(\exp \frac{U}{m U_T} - 1 \right)$$

$$= 3.98 \cdot 10^{-4} \text{ A}$$

ZADATAK 6.

$$N_D = 10^{19} \text{ cm}^{-3}$$

$$N_A = 5 \cdot 10^{19} \text{ cm}^{-3}$$

$$\mu_n = 350 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 300 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 1.2 \text{ ns}$$

$$\tau_p = 9.8 \text{ ns}$$

$$S = 1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$\xi = ?$$

$$U = 0.5 \text{ V} \rightarrow \text{napr. } U$$

$$U = 50 \text{ mV}$$

$$L_p \gg W_n = 1 \mu\text{m}$$

$$L_n \gg W_p = 2 \mu\text{m}$$

$$I_s = q \cdot S \left(D_n \frac{n_{op}}{W_p} + D_p \frac{p_{on}}{W_n} \right)$$

$$n_{op} = 41472 \text{ cm}^{-3}$$

$$p_{on} = 2073 \text{ cm}^{-3}$$

$$I_s = 7.65 \cdot 10^{-10} \text{ A}$$

$$I = I_s \left(\exp \frac{U}{U_T} - 1 \right)$$

$$D_n = 21.93 \text{ cm}^2/\text{s}$$

$$D_p = 7.76 \text{ cm}^2/\text{s}$$

$$I_1 = 1.9 \cdot 10^{-3} \text{ A}$$

$$I_2 = 4.52 \cdot 10^{-4} \text{ A}$$

$$\xi = 50$$

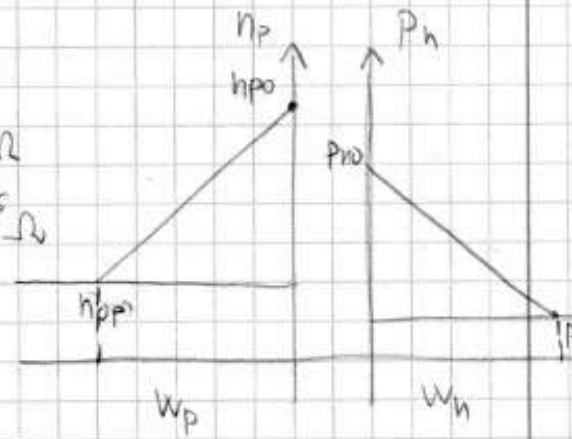
$$r_d = \frac{U_T}{I_s}$$

$$r_{d1} = 13.61 \Omega$$

$$r_{d2} = 439 \cdot 10^6 \Omega$$

$$n_{po} = 1.03 \cdot 10^{13} \text{ cm}^{-3}$$

$$p_{no} = 5.16 \cdot 10^{11} \text{ cm}^{-3}$$



ZADATOK 7.

$$T = 300 \text{ K}$$

$$I_s = 1 \cdot 10^{-12} \text{ A}$$

$$R_{th} = 10 \Omega$$

$$I = 1 \text{ mA}$$

$$U = ?$$

$$U = U_D + I \cdot R_{th}$$

$$I = I_s \left(e^{\frac{U_D}{U_T}} - 1 \right)$$

$$\frac{I}{I_s} + 1 = e^{\frac{U_D}{U_T}}$$

$$U_D = U_T \cdot \ln \left(\frac{I}{I_s} + 1 \right)$$

$$= 0,536 \text{ V}$$

$$U = 0,546 \text{ V}$$

ZADATOK 8.

$$I_s = 1 \text{ pA} = 10^{-12} \text{ A}$$

$$i_D = 1,5 [\text{mA}] + 0,25 \sin(\omega t) [\text{mA}]$$

$$U_T = 25 \text{ mV}$$

$$U = U_D + I \cdot R_{th} = 0,545 \text{ V}$$

$$U_D = U_T \ln \left(\frac{1}{I_s} + 1 \right)$$

$$= 0,53 \text{ V}$$

$$I \cdot R_{th} = 1,5 \cdot 10^{-3} \cdot 10$$

$$= 0,015$$

$$U_D = i_D r_D + i_D R_{th} = i_D (r_D + R_{th})$$

$$= 6,67 \text{ mV}$$

$$U_D = 0,545 [\text{V}] + 6,67 \sin(\omega t) [\text{mV}]$$

ZADATOK 9.

$$U = 60 \text{ mV}$$

$$U_1, U_2 = ?$$

$$I_s = 10 \text{ pA}$$

$$U_T = 25 \text{ mV}$$

$$m = 1$$

$$U = U_1 + U_2$$

$$U_1 = U - U_2$$

$$I_{D1} = I_s \left(\exp \left(\frac{U_1}{U_T} \right) - 1 \right)$$

$$I_{D2} = I_s \left(\exp \left(\frac{U_2}{U_T} \right) - 1 \right)$$

$$I_{D3} = I_s \left(\exp \left(\frac{-U_2}{U_T} \right) - 1 \right)$$

$$I_{D1} + I_{D3} = I_{D2}$$

$$\exp \frac{U_1}{U_T} + \exp \frac{-U_2}{U_T} - 1 = \exp \frac{U_2}{U_T}$$

$$\exp \frac{U}{U_T} = \frac{U_2}{U_1} + \exp \frac{-U_2}{U_T} - 1 = \exp \frac{U_2}{U_T}$$

$$\frac{\exp \frac{U}{U_T} + 1}{\exp \frac{U_2}{U_T} + 1} - 1 = \exp \frac{U_2}{U_T}$$

$$U_2 = 27,47 \text{ mV}$$

$$U_1 = 32,53 \text{ mV}$$

$$\frac{12,02}{x} - 1 = x \cdot x$$

$$12,02 - x = x^2$$

$$\frac{x \pm 3}{x^2 \mp 4}$$

VJ. 1.

$$\begin{aligned} d_B &= ? \\ T &= 300 \text{ K} \\ U &= 0 \text{ V} \\ S &= 25 \mu\text{m}^2 \\ C_B &= ? \end{aligned}$$

$$\begin{aligned} N_A &= 5 \cdot 10^{17} \text{ cm}^{-3} \\ N_D &= 10^{16} \text{ cm}^{-3} \\ n_i &= 1,44 \cdot 10^{10} \text{ cm}^{-3} \\ U_K &= 0,797 \text{ V} \\ d_B &= 3,24 \cdot 10^{-5} \text{ cm} \end{aligned}$$

$$\begin{aligned} C_B &= \epsilon \frac{S}{d_B} \\ &= 7,98 \cdot 10^{-15} \text{ F} \end{aligned}$$

VJ. 2

$$\begin{aligned} T &= 300 \text{ K} \\ U &= -3 \\ S &= 50 \mu\text{m}^2 \\ d_B, C_B &= ? \end{aligned}$$

$$\begin{aligned} N_A &= 5 \cdot 10^{16} \text{ cm}^{-3} \\ N_D &= 10^{15} \text{ cm}^{-3} \end{aligned}$$

$$\begin{aligned} U_K &= U_T \ln \left(\frac{N_A \cdot N_D}{n_i^2} \right) \\ &= 0,68 \text{ V} \end{aligned}$$

$$d_B = \sqrt{\frac{2 \cdot \epsilon_s \cdot \epsilon_0}{q} \left(\frac{1}{N_A} + \frac{1}{N_D} \right) (U_K - U)}$$

$$d_B = 2,2 \cdot 10^{-4} \text{ cm}$$

$$C_B = \epsilon \cdot \frac{S}{d_B} = 2,35 \cdot 10^{-15} \text{ F}$$

$$\epsilon = \epsilon_s \cdot \epsilon_0$$

VJ. 3

$$\begin{aligned} T &= 300 \text{ K} \\ U &= 0,3 \text{ V} \\ S &= 50 \mu\text{m}^2 \\ d_B, C_B &= ? \end{aligned}$$

$$\begin{aligned} N_A &= 5 \cdot 10^{16} \text{ cm}^{-3} \\ N_D &= 10^{15} \text{ cm}^{-3} \end{aligned}$$

$$\begin{aligned} U_K &= U_T \ln \left(\frac{N_A \cdot N_D}{n_i^2} \right) \\ &= 0,68 \text{ V} \end{aligned}$$

$$d_B = 7,08 \cdot 10^{-5} \text{ cm}$$

$$C_B = \epsilon \cdot \frac{S}{d_B} = 7,3 \cdot 10^{-15} \text{ F}$$

VJ. 4.

$$\begin{aligned} T &= 350 \text{ K} \\ U &= 0 \text{ V} \\ S &= 100 \mu\text{m}^2 \\ d_B, C_B &= ? \end{aligned}$$

$$\begin{aligned} N_A &= 5 \cdot 10^{17} \text{ cm}^{-3} \\ N_D &= 5 \cdot 10^{15} \text{ cm}^{-3} \end{aligned}$$

$$U_K = 0,695$$

$$d_B = 4,26 \cdot 10^{-5} \text{ cm}$$

$$C_B = 2,4 \cdot 10^{-14} \text{ F}$$

$$n_i = 4,96 \cdot 10^{11} \text{ cm}^{-3}$$

VJ. 5

$$\begin{aligned} T &= 350 \text{ K} \\ U &= -2 \text{ V} \\ S &= 100 \mu\text{m}^2 \end{aligned}$$

$$\begin{aligned} N_A &= 5 \cdot 10^{17} \text{ cm}^{-3} \\ N_D &= 5 \cdot 10^{15} \text{ cm}^{-3} \end{aligned}$$

$$U_K = 0,596$$

$$d_B = 3,24 \cdot 10^{-5} \text{ cm}$$

$$C_B = 1,26 \cdot 10^{-14} \text{ F}$$

$$d_B, C_B = ?$$

$$n_i = 4,96 \cdot 10^{11} \text{ cm}^{-3}$$

$$N_D = 5 \cdot 10^{17} \text{ cm}^{-3}$$

$$N_A = 10^{16} \text{ cm}^{-3}$$

$$W_n \gg L_p$$

$$W_p \gg L_n$$

$$\mu_n = 800 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 280 \text{ cm}^2/\text{Vs}$$

$$n_{op} = 20736 \text{ cm}^{-3}$$

$$p_{op} = 414.72 \text{ cm}^{-3}$$

$$\tau_n = 0.8 \text{ ns}$$

$$\tau_p = 0.5 \text{ ns}$$

$$D_n = 20.69 \text{ cm}^2/\text{s}$$

$$D_p = 7.24 \text{ cm}^2/\text{s}$$

$$S = 1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$I_s = ?$$

$$U = 0.6 \text{ V}$$

$$I_D = ?$$

$$L_n = 4 \cdot 10^{-3} \text{ cm}$$

$$L_p = 1.9 \cdot 10^{-3} \text{ cm}$$

$$I_s = q \cdot S \left(D_n \frac{n_{op}}{L_n} + D_p \frac{p_{op}}{L_p} \right)$$

$$I_s = 1.74 \cdot 10^{-13} \text{ A}$$

$$I = I_s \left(\exp \frac{U}{U_T} - 1 \right)$$

$$I = 2.07 \cdot 10^{-3} \text{ A}$$

VL 7

$$N_D = 5 \cdot 10^{17} \text{ cm}^{-3}$$

$$N_A = 10^{16} \text{ cm}^{-3}$$

$$W_n \gg L_p$$

$$W_p \gg L_n$$

$$\mu_n = 800 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 280 \text{ cm}^2/\text{Vs}$$

$$n_{op} = 2.46 \cdot 10^{12} \text{ cm}^{-3}$$

$$p_{op} = 492.032$$

$$\tau_n = 0.8 \text{ ns}$$

$$\tau_p = 0.5 \text{ ns}$$

$$D_n = 24.14 \text{ cm}^2/\text{s}$$

$$D_p = 3.45 \text{ cm}^2/\text{s}$$

$$S = 1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$L_n = 4.39 \cdot 10^{-3} \text{ cm}$$

$$L_p = 2.06 \cdot 10^{-3} \text{ cm}$$

$$I_s = q \cdot S \left(D_n \frac{n_{op}}{L_n} + D_p \frac{p_{op}}{L_p} \right)$$

$$= 2.14 \cdot 10^{-10} \text{ A}$$

$$n_i = 4.96 \cdot 10^{11} \text{ cm}^{-3}$$

$$I = 0.095 \text{ A}$$

$$N_D = 5 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_A = 10^{17} \text{ cm}^{-3}$$

$$\mu_n = 700 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 320 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 0,5 \text{ ns}$$

$$\tau_p = 0,8 \text{ ns}$$

$$S = 0,1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$U = 0,5 \text{ V}$$

$$L_D \gg W_n = 1,5 \text{ } \mu\text{m}$$

$$L_n \gg W_p = 2 \text{ } \mu\text{m}$$

$$n_{op} = 2073 \text{ cm}^{-3}$$

$$p_{op} = 41472 \text{ cm}^{-3}$$

$$D_n = 18,1 \text{ cm}^2/\text{s}$$

$$D_p = 8,28 \text{ cm}^2/\text{s}$$

$$I_s = q \cdot S \cdot \left(D_n \frac{n_{op}}{W_p} + D_p \frac{p_{op}}{W_n} \right)$$

$$= 3,96 \cdot 10^{-13} \text{ A}$$

$$I = 9,87 \cdot 10^{-5} \text{ A}$$

V. 9.

$$N_D = 5 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_A = 10^{17} \text{ cm}^{-3}$$

$$\mu_n = 600 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 300 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 0,5 \text{ ns}$$

$$\tau_p = 0,8 \text{ ns}$$

$$S = 0,1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$U = 0,5 \text{ V}$$

$$n_i = 4,96 \cdot 10^{11} \text{ cm}^{-3}$$

$$L_D \gg W_n = 1,5 \text{ } \mu\text{m}$$

$$L_n \gg W_p = 2 \text{ } \mu\text{m}$$

$$n_{op} = 2460160 \text{ cm}^{-3}$$

$$p_{op} = 49203200 \text{ cm}^{-3}$$

$$D_n = 18,1 \text{ cm}^2/\text{s}$$

$$D_p = 9,05 \text{ cm}^2/\text{s}$$

$$I_s = q \cdot S \cdot \left(D_n \frac{n_{op}}{W_p} + D_p \frac{p_{op}}{W_n} \right)$$

$$I_s = 5,1 \cdot 10^{-10} \text{ A}$$

$$I = 8,03 \cdot 10^{-3} \text{ A}$$

V. 10.

$$N_D = 5 \cdot 10^{17} \text{ cm}^{-3}$$

$$N_A = 10^{16} \text{ cm}^{-3}$$

$$\mu_n = 300 \text{ cm}^2/\text{Vs}$$

$$\mu_p = 280 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 0,3 \text{ ns}$$

$$\tau_p = 0,4 \text{ ns}$$

$$S = 0,1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$U = 0,5 \text{ V}$$

$$L_D \gg W_n = 2 \text{ } \mu\text{m}$$

$$L_n \ll W_p$$

$$n_{op} = 20736 \text{ cm}^{-3}$$

$$p_{op} = 414 \text{ cm}^{-3}$$

$$D_n = 20,69 \text{ cm}^2/\text{s}$$

$$D_p = 7,24 \text{ cm}^2/\text{s}$$

$$L_n = 4,07 \cdot 10^{-3} \text{ cm}$$

$$I_s = q \cdot S \cdot \left(D_n \frac{n_{op}}{L_n} + D_p \frac{p_{op}}{W_n} \right)$$

$$= 1,98 \cdot 10^{-14} \text{ A}$$

$$I = 4,79 \cdot 10^{-6} \text{ A}$$

VJ. 11.

$$N_B = 10^{16} \text{ cm}^{-3}$$

$$N_A = 5 \cdot 10^{17} \text{ cm}^{-3}$$

$$N_n = 500 \text{ cm}^2/\text{Vs}$$

$$N_p = 350 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 0.4 \text{ ns}$$

$$\tau_p = 0.3 \text{ ns}$$

$$S = 0.1 \text{ mm}^2$$

$$I_s = ?$$

$$T = 300 \text{ K}$$

$$U = 0.5 \text{ V}$$

$$L_D \gg W_n = 2 \text{ mm}$$

$$L_n \ll W_p$$

$$n_{op} = 414$$

$$p_{op} = 20736$$

$$D_n = 12.93$$

$$D_p = 9.05$$

$$L_n = 2.27 \cdot 10^{-3} \text{ cm}$$

$$I_s = q \cdot S \cdot \left(D_n \frac{n_{op}}{L_n} + D_p \frac{p_{op}}{W_n} \right)$$

$$I_s = 1.49 \cdot 10^{-13} \text{ A}$$

$$I = I_s \left(e^{\frac{U}{U_T}} - 1 \right)$$

$$I = 3.73 \cdot 10^{-5} \text{ A}$$

VJ. 12.

$$N_B = 5 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_A = 5 \cdot 10^{17} \text{ cm}^{-3}$$

$$N_n = 500 \text{ cm}^2/\text{Vs}$$

$$N_p = 300 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 0.5 \text{ ns}$$

$$\tau_p = 1 \text{ ns}$$

$$U = 0.5 \text{ V}$$

$$L_p \ll W_n$$

$$L_n \gg W_p = 1 \text{ mm}$$

$$n_{op} = 414 \text{ cm}^{-3}$$

$$p_{op} = 41472 \text{ cm}^{-3}$$

$$D_n = 12.93 \text{ cm}^2/\text{s}$$

$$D_p = 7.76 \text{ cm}^2/\text{s}$$

$$L_p = 2.79 \cdot 10^{-3} \text{ cm}$$

$$I_s = q \cdot S \cdot \left(D_n \frac{n_{op}}{W_p} + D_p \frac{p_{op}}{L_p} \right)$$

$$= 2.14 \cdot 10^{-14} \text{ A}$$

$$I = I_s \left(e^{\frac{U}{U_T}} - 1 \right)$$

$$I = 5.32 \cdot 10^{-6} \text{ A}$$

VJ. 13

$$N_B = 5 \cdot 10^{15} \text{ cm}^{-3}$$

$$N_A = 5 \cdot 10^{17} \text{ cm}^{-3}$$

$$N_n = 400 \text{ cm}^2/\text{Vs}$$

$$N_p = 250 \text{ cm}^2/\text{Vs}$$

$$\tau_n = 0.5 \text{ ns}$$

$$\tau_p = 1 \text{ ns}$$

$$S = 0.1 \text{ mm}^2$$

$$T = 300 \text{ K}$$

$$n_i = 4.96 \cdot 10^{11} \text{ cm}^{-3}$$

$$L_D \ll W_n \quad L_n \gg W_p$$

$$n_{op} = 492.032 \text{ cm}^{-3}$$

$$p_{op} = 4.92 \cdot 10^7 \text{ cm}^{-3}$$

$$D_n = 12.06 \text{ cm}^2/\text{s}$$

$$D_p = 7.54 \text{ cm}^2/\text{s}$$

$$L_p = 2.74 \cdot 10^{-3} \text{ cm}$$

$$I_s = q \cdot S \cdot \left(D_n \frac{n_{op}}{W_p} + D_p \frac{p_{op}}{L_p} \right)$$

$$= 3.12 \cdot 10^{-11} \text{ A}$$

VJ. 14.

$$I_s = 10 \cdot 10^{-12} \text{ A}$$

$$R_s = 15 \text{ k}\Omega$$

$$T = 300 \text{ K}$$

$$I = 10 \text{ mA}$$

$$U = ?$$

$$I = I_s \left(e^{\frac{U}{U_T}} - 1 \right)$$

$$\frac{I}{I_s} + 1 = e^{\frac{U}{U_T}}$$

$$U_T \ln \left(\frac{I}{I_s} + 1 \right) = U$$

$$U_D = 9,536 \text{ V}$$

$$U' = R \cdot I$$

$$U' = 0,15 \text{ V}$$

$$U = U_D + U' = 9,686 \text{ V}$$

VJ. 15

$$I_s = 10^{-9}$$

$$T = 350 \text{ K}$$

$$R_s = 15 \text{ k}\Omega$$

$$I = 10 \text{ mA}$$

$$U' = R \cdot I$$

$$= 0,15 \text{ V}$$

$$U_D = U_T \ln \left(\frac{I}{I_s} + 1 \right)$$

$$U_D = 0,436$$

$$U = 0,586 \text{ V}$$

VJ. 16

$$I_s = 10 \cdot 10^{-12}$$

$$R = 15 \text{ k}\Omega$$

$$T = 300 \text{ K}$$

$$i_D = 1,5 + 0,25 \sin \omega t \text{ [mA]}$$

$$U_D = U_T \ln \left(\frac{I}{I_s} + 1 \right)$$

$$U_D = 9,487 \text{ V}$$

$$U = U_D + I \cdot R_D = 9,5095 \text{ V}$$

$$U_D = (9,509 + 8,06 \cdot 10^{-3})$$

$$r_d = \frac{U_T}{I} = 17,24 \text{ k}\Omega$$

$$u_d = I_f (r_d + R_s) = 3,02 \cdot 10^{-3}$$

VJ. 17.

$$I_s = 10 \text{ pA}$$

$$R_{s1} = 12 \text{ k}\Omega$$

$$i_D = (2,5 + 0,35 \sin \omega t) \text{ [mA]}$$

$$T = 300 \text{ K}$$

$$U_D = 0,5 \text{ V}$$

$$U_D = U_D + I \cdot R_{s1} = 0,53 \text{ V}$$

$$r_d = \frac{U_T}{I} = 10,34 \text{ k}\Omega$$

$$u_D = (0,53 + 7,8 \cdot 10^{-3} \sin \omega t) \text{ V}$$

$$u_d = (r_d + R_{s1}) \cdot i_d = 7,8 \cdot 10^{-3}$$

VJ. 18.

$$U = 65 \text{ mV}$$

$$I_{s1} = I_{s2} = 10 \text{ pA}$$

$$U_{s3} = 20 \text{ pA}$$

$$U_T = 25 \text{ mV}$$

$$U = U_T \ln \left(\frac{I}{I_s} + 1 \right)$$

$$I_{s1} \left(e^{\frac{U}{U_T}} - 1 \right) + I_{s2} \left(e^{\frac{U}{U_T}} - 1 \right) = I_{s3} \left(e^{\frac{U}{U_T}} - 1 \right) + I_3 = I_3$$

$$U_1 + U_2 = U$$

$$\frac{U_1}{U_T} + \frac{U_2}{U_T} = \frac{U}{U_T}$$

$$I_3 = 1,0376 \text{ V}$$

ZADATK 1.

$$R_T = 100 \Omega$$

$$C = 2,2 \text{ mF}$$

$$U_{pey} = 230 \text{ V}$$

$$f = 50 \text{ Hz}$$

$$n = 25$$

$$U_{sm} = \frac{\sqrt{2} U_{pey}}{n} = 13 \text{ V}$$

$$U_{2m} = U_{sm} = 13 \text{ V}$$

$$T = R_T \cdot C = 220 \text{ ms}$$

$$T = \frac{1}{f} = 20 \text{ ms}$$

$$U_{2vm} = U_{2m} \frac{T}{2T} = 591 \text{ mV}$$

$$U_{12} = U_{2m} - U_{2vm} = 12,43 \text{ V}$$

$$U_{12ey} = \frac{U_{2vm}}{\sqrt{3}} = 341 \text{ mV}$$

$$r = \frac{U_{12ey}}{U_{12}} = 0,0275$$

ZADATK 2.

$$U_{12} = ?$$

$$r = ?$$

$$R_T = 50 \Omega$$

$$C = 4,7 \text{ mF}$$

$$U_{pey} = 230 \text{ V}$$

$$f = 50 \text{ Hz}$$

$$n = 30$$

$$U_{sm} = \frac{\sqrt{2} U_{pey}}{n} = 10,84 \text{ V}$$

$$U_{2m} = U_{sm} = 10,84 \text{ V}$$

$$T = R_T \cdot C = 235 \text{ ms}$$

$$T = \frac{1}{f} = 20 \text{ ms}$$

$$U_{2vm} = U_{2m} \frac{T}{4T} = 230,7 \text{ mV}$$

$$U_{12} = U_{2m} - U_{2vm} = 10,61 \text{ V}$$

$$U_{12ey} = \frac{U_{2vm}}{\sqrt{3}} = 133 \text{ mV}$$

$$r = \frac{U_{12ey}}{U_{12}} = 0,0126$$

ZADATK 3.

$$r = 10^{-3}$$

$$R_T = 1 \text{ k}\Omega$$

$$U_{sm} = 250 \text{ V}$$

$$f = 50 \text{ Hz}$$

$$n = 10$$

$$U_{sm} = \frac{U_{pm}}{n} = 25 \text{ V}$$

$$U_{2m} = U_{sm} = 25 \text{ V}$$

$$U_{12ey} = \frac{U_{2m} \frac{T}{4CR_T f}}{\sqrt{3}}$$

$$= \frac{U_{2m}}{4\sqrt{3} CR_T f}$$

$$U_{12} = U_{2m} - U_{2vm} = U_{2m} - U_{2m} \frac{1}{4CR_T f} = U_{2m} \frac{4CR_T f - 1}{4CR_T f}$$

$$U_{12} = 24,96 \text{ V}$$

$$r = \frac{U_{12ey}}{U_{12}} = \frac{U_{2m} \cdot 4CR_T f}{4\sqrt{3} CR_T f \cdot U_{12m} (4CR_T f - 1)}$$

$$C = 2,89 \text{ mF}$$

$$R_T = 10 \text{ k}\Omega$$

$$V_d = 10 \text{ V}$$

$$t=0 \quad U_{C0} = 0 \text{ V}$$

$$U_C(0^+) = U_{C0} = 0 \text{ V}$$

$$U_{12}(0^+) = U_{120} = \frac{V_d}{R_T + R_g} (V_d - U_{C0}) = 0,833$$

$$U_C(t) = U_{C0} + (U_1 - U_{C0}) \cdot (1 - e^{-\frac{t}{\tau_1}})$$

$$\tau_1 = C \cdot (R_g + R_T) = 6 \mu\text{s}$$

VS. 1.

$$r = 10^{-3}$$

$$R_T = 1 \text{ k}\Omega$$

$$V_{pm} = 250 \text{ V}$$

$$f_m = 50 \text{ Hz}$$

$$n = 10$$

$$C = ?$$

$$U_{sm} = \frac{U_{pm}}{n} = 25 \text{ V}$$

$$U_{12M} = U_{sm} = 25 \text{ V}$$

$$U_{12VM} = U_{12M} \cdot \frac{T}{2T}$$

$$= \frac{1}{4000 \text{ C}}$$

$$U_{12VEF} = \frac{1}{4000 \sqrt{3} \text{ C}}$$

$$U_{12} = U_{12M} - U_{12VM}$$

$$= 25 - \frac{1}{4000 \text{ C}}$$

$$= \frac{100000 \text{ C} - 1}{4000 \text{ C}}$$

$$r = \frac{U_{12VEF}}{U_{12}} = 10^{-3}$$

$$\frac{1}{1000} = \frac{\frac{1}{4000 \sqrt{3} \text{ C}}}{\frac{100000 \text{ C} - 1}{4000 \text{ C}}}$$

$$100000 \text{ C} - 1 = \frac{1000}{\sqrt{3}}$$

$$C = 5,78 \text{ mF}$$

VS. 2.

$$C, r = ?$$

$$U_{12} = 21 \text{ V}$$

$$R_T = 560 \text{ }\Omega$$

$$U_{pm} = 150 \text{ V}$$

$$f = 50 \text{ Hz}$$

$$n = 10$$

$$U_{sm} = \frac{U_{pm} \sqrt{2}}{n} = 21,21 \text{ V}$$

$$U_{12M} = 21,21 \text{ V}$$

$$U_{12VM} = U_{12M} \cdot \frac{T}{2T}$$

$$= \frac{303}{800000 \text{ C}}$$

$$U_{12VEF} = \frac{303}{800000 \sqrt{3} \text{ C}}$$

$$= 0,12 \text{ V}$$

$$U_{12} = U_{12M} - U_{12VM}$$

$$21 = 21,21 - \frac{303}{800000 \text{ C}}$$

$$C = 1,8 \cdot 10^{-3} \text{ F}$$

$$r = \frac{U_{12VEF}}{U_{12}} = 5,78 \cdot 10^{-3}$$

$$\begin{aligned}
 R_T &= 220 \Omega \\
 C &= 1 \text{ mF} \\
 U_{pm} &= 325 \\
 f &= 50 \text{ Hz} \\
 n &= 20
 \end{aligned}$$

$$\begin{aligned}
 U_{12M} &= 16,25 \text{ V} \\
 U_{12VM} &= U_{12M} \frac{T}{2\pi} \\
 &= 0,74 \text{ V} \\
 U_{12VEF} &= 9,43 \text{ V}
 \end{aligned}$$

$$\begin{aligned}
 &= 15,51 \text{ V} \\
 r &= \frac{U_{12EF}}{U_{12}} \\
 &= 0,028
 \end{aligned}$$

VJ. 4

$$C, U_{12} = ?$$

$$\begin{aligned}
 r &= 10^{-3} \\
 R_T &= 1 \text{ k}\Omega \\
 U_{pm} &= 250 \text{ V} \\
 f &= 50 \text{ Hz} \\
 n &= 10
 \end{aligned}$$

$$\begin{aligned}
 U_{sm} &= \frac{U_{pm}}{n} = 25 \text{ V} \\
 U_{12M} &= 25 \text{ V} \\
 U_{12VM} &= U_{12M} \frac{T}{4\pi} \\
 &= \frac{3000 \text{ C}}{1} \\
 U_{12VEF} &= 3000\sqrt{3} \text{ C}
 \end{aligned}$$

$$\begin{aligned}
 U_{12} &= U_{12M} - U_{12VM} \\
 &= 25 - \frac{1}{8000 \text{ C}} = 24,96 \text{ V}
 \end{aligned}$$

$$U_{12} = \frac{200000 \text{ C} - 1}{8000 \text{ C}}$$

$$r = \frac{U_{12VEF}}{U_{12}}$$

$$\frac{1}{1000} = \frac{3000\sqrt{3}}{(200000 \text{ C} - 1) \cdot 8000\sqrt{3} \text{ C}}$$

$$200000 \text{ C} - 1 = \frac{1000}{\sqrt{3}}$$

$$C = 2,89 \cdot 10^{-3} \text{ F}$$

VJ. 5

$$C, r = ?$$

$$\begin{aligned}
 U_{12} &= 21 \text{ V} \\
 R_T &= 560 \Omega \\
 U_{pey} &= 450 \text{ V} \\
 f &= 50 \text{ Hz} \\
 n &= 10
 \end{aligned}$$

$$\begin{aligned}
 U_{sm} &= \frac{U_{pey} \sqrt{2}}{n} = 21,21 \text{ V} \\
 U_{12M} &= 21,21 \text{ V} \\
 U_{12VM} &= U_{12M} \frac{T}{4\pi} \\
 &= \frac{303}{160000 \text{ C}} \\
 &= 0,21 \text{ V}
 \end{aligned}$$

$$\begin{aligned}
 U_{12} &= U_{12M} - U_{12VM} \\
 21 &= 21,21 - \frac{303}{160000 \text{ C}}
 \end{aligned}$$

$$C = 9 \cdot 10^{-3} \text{ F}$$

$$\begin{aligned}
 r &= \frac{U_{12EF}}{U_{12}} \\
 r &= 5,78 \cdot 10^{-3}
 \end{aligned}$$

$$U_{12VEF} = 0,12$$

VJ. 6

$$U_{12}, r = ?$$

$$\begin{aligned}
 R_T &= 220 \Omega \\
 C &= 1 \text{ mF} \\
 U_{pm} &= 325 \text{ V} \\
 f &= 50 \text{ Hz} \\
 n &= 20
 \end{aligned}$$

$$\begin{aligned}
 U_{sm} &= \frac{U_{pm}}{n} = 16,25 \text{ V} \\
 U_{12M} &= 16,25 \text{ V} \\
 U_{12VM} &= U_{12M} \frac{T}{4\pi} \\
 &= 0,37 \text{ V} \\
 U_{12VEF} &= 0,21 \text{ V}
 \end{aligned}$$

$$\begin{aligned}
 U_{12} &= U_{12M} - U_{12VM} \\
 &= 15,88 \text{ V}
 \end{aligned}$$

$$r = \frac{U_{12VEF}}{U_{12}}$$

$$r = 0,0132$$

$$r = 0,005$$

$$R_T = 330 \Omega$$

$$U_{pm} = 150 V$$

$$f = 50 Hz$$

$$n = 15$$

$$U_{sm} = \frac{U_{pm}}{n} = 10 V$$

$$U_{12M} = 10 V$$

$$U_{12VM} = U_{12M} \cdot \frac{T}{4T}$$

$$= \frac{1}{66000}$$

$$U_{12VER} = \frac{1}{66000 \sqrt{2}}$$

$$U_{12} = U_{12M} - U_{12VM}$$

$$U_{12} = 10 - \frac{1}{66000}$$

$$U_{12} = \frac{66000 - 1}{66000} = 9,91 V$$

$$r = \frac{U_{12VER}}{U_{12}} = \frac{\frac{1}{66000 \sqrt{2}}}{\frac{66000 - 1}{66000}} = \frac{1}{200}$$

$$66000 - 1 = \frac{200}{\sqrt{2}}$$

$$C = 1,76 \cdot 10^{-5} F$$

V.8

$r, r = ?$

$$U_{12} = 11 V$$

$$R_T = 300 \Omega$$

$$U_{pm} = 350 V$$

$$f = 50 Hz$$

$$n = 30$$

$$U_{sm} = \frac{U_{pm}}{n} = 11,67 V = \frac{35}{3} V$$

$$U_{12M} = 11,67 V$$

$$U_{12VM} = U_{12M} \cdot \frac{T}{4T}$$

$$= \frac{7}{360000}$$

$$U_{12VER} = \frac{7}{360000 \sqrt{2}}$$

$$= 0,386$$

$$U_{12} = U_{12M} - U_{12VM}$$

$$11 = \frac{35}{3} - \frac{7}{360000}$$

$$C = 2,91 \cdot 10^{-4} F$$

$$r = \frac{U_{12VER}}{U_{12}}$$

$$r = 0,0351$$

V.9.

$U_{12}, r = ?$

$$R_T = 500 \Omega$$

$$C = 4,7 \mu F$$

$$U_{pm} = 250 V$$

$$f = 50 Hz$$

$$n = 25$$

$$U_{sm} = \frac{U_{pm}}{n} = 10 V$$

$$U_{12M} = 10 V$$

$$U_{12VM} = U_{12M} \cdot \frac{T}{4T}$$

$$= 0,021$$

$$U_{12VER} = 0,012$$

$$U_{12} = U_{12M} - U_{12VM}$$

$$= 9,979 V$$

$$r = \frac{U_{12VER}}{U_{12}}$$

$$r = 1,2 \cdot 10^{-3}$$