

MASS 2 → HOUSE

1. 2010/2011 2.MI.

(8 bodova sklop = MOSFETOM)



$$R_1 = 4 \text{ k}\Omega$$

$$R_2 = 1 \text{ k}\Omega$$

$$R_{D1} - R_{D2} = 95 \text{ k}\Omega$$

$$R_D = 5 \text{ k}\Omega$$

$$R_T = 10 \text{ k}\Omega$$

$$R_g = 500 \Omega$$

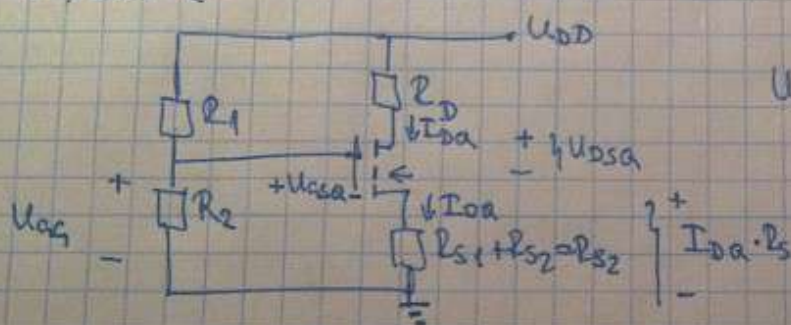
$$U_{DD} = 12 \text{ V}$$

$$U_{GSP} = 1 \text{ V}$$

$$k = 5 \text{ mA/V}^2$$

$$\lambda = 0.008 \text{ V}^{-1}$$

3. bodu
a) SRT (I)



$$U_{G9} = U_{DD} \cdot \frac{R_2}{R_1 + R_2} = 2.4 \text{ V}$$

$$U_{GSA} = U_G - U_S = U_{G9} - I_{DA} \cdot R_S \quad (1)$$

$$I_{DA} = \frac{k}{2} (U_{GSA} - U_{GSP})^2 \quad (2)$$

$$(2) \rightarrow (1) \dots ax^2 + bx + c = 0 \Rightarrow U_{GSA} = \begin{matrix} 1.57 \text{ V} \\ 0.025 \text{ V} \end{matrix} > U_{GSP} = 1 \text{ V} \quad \checkmark \text{ (nMOS)} \quad \times$$

$$U_{GSA}^2 + U_{GSA} \left(\frac{2}{kR_S} - 2U_{GSP} \right) - \frac{2}{kR_S} U_{G9} + U_{GSP}^2 = 0$$

$$I_{DA} = \frac{U_{G9} - U_{GSA}}{R_S} = 0.83 \text{ mA}$$

$$U_{DSA} = U_{DD} - I_{DA}(R_D + R_S) = 7 \text{ V}$$

b) parametri tranzistora

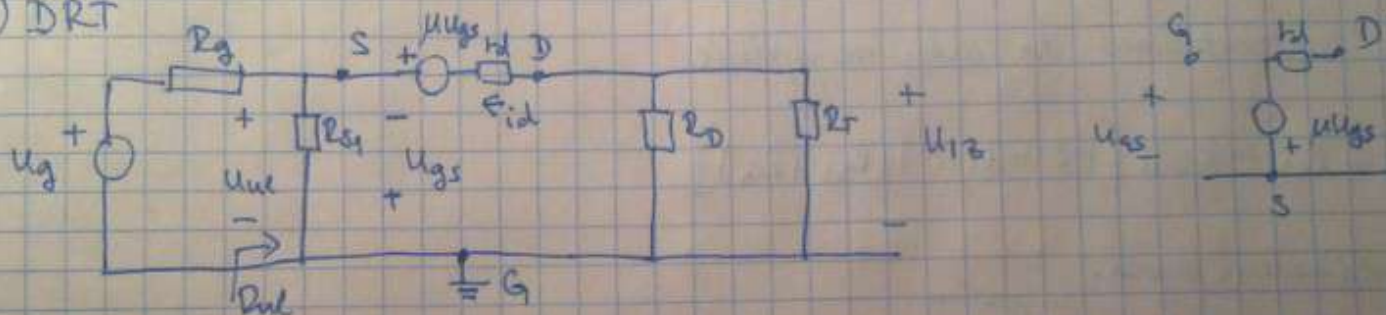
$$i_D = \frac{k}{2} (u_{GS} - u_{GS0})^2 (1 + \lambda u_{DS})$$

$$g_m = \left. \frac{\partial i_D}{\partial u_{GS}} \right|_Q = k (u_{GSQ} - u_{GS0}) (1 + \lambda u_{DSQ}) = \dots = \boxed{3 \text{ mA/V}}$$

$$r_d = \frac{1}{g_d} = \frac{1}{\left. \frac{\partial i_D}{\partial u_{DS}} \right|_Q} = \frac{1}{\frac{k}{2} (u_{GSQ} - u_{GS0})^2 \cdot \lambda} = \dots = \frac{1}{I_{DQ} \cdot \lambda} = \boxed{150 \text{ k}\Omega}$$

$$\mu = g_m r_d = 450$$

c) DRT



(ako su \$S\$ i \$D\$ na \$\equiv\$ onda stupiti izvor + \$i_d\$ u \$\parallel\$)

$$i_d \cdot (R_D \parallel R_T) + i_d \cdot r_d - \mu \cdot u_{GS} - u_{GS} = 0$$

$$i_d (R_D \parallel R_T + r_d) = (1 + \mu) u_{GS} = - (1 + \mu) u_{ue}$$

$$u_{GS} = -u_{ue} \quad \uparrow$$

$$i_d = \frac{-(1 + \mu) u_{ue}}{R_D \parallel R_T + r_d} \quad (1)$$

$$u_{iz} = -i_d (R_D \parallel R_T) = \frac{(1 + \mu) u_{ue}}{R_D \parallel R_T + r_d} (R_D \parallel R_T) \quad | : u_{ue}$$

$$\frac{u_{iz}}{u_{ue}} = A_v = \frac{(1 + \mu) (R_D \parallel R_T)}{r_d + R_D \parallel R_T} = \dots = \boxed{g_{m,p}} \quad (\text{mogućnost } \lambda = 0 \text{ u } 200 \cdot G_s)$$

$$\Leftrightarrow \sim g_m (R_D \parallel R_T)$$

$$R_{ue}' = \frac{u'}{i'} \quad , \quad u' = u_{ue}$$

$$i' = -i_d$$

$$R_{ue}' = - \frac{u_{ue}}{i_d} \Rightarrow (1) \Rightarrow \frac{R_D \parallel R_T + r_d}{1 + \mu}$$

$$R_{ue} = R_{S1} \parallel R_{ue}' = R_{S1} \parallel \frac{R_D \parallel R_T + r_d}{1 + \mu}$$

R_{iz} : odspojiti R_T i u_{gs} , umjesto R_T neki izvor

$$R_{iz} = \frac{u}{i}$$

pretpostavimo da μu_{gs} ne djeluje

$$R_{iz} = R_D \parallel [r_d + (1 + \mu)(R_{S1} \parallel R_G)]$$

preslikavanje otpora:

otpor iz (S) $\xrightarrow{\text{se preslikava}} (D) \quad (1 + \mu) \times \text{veći}$

(D) \rightarrow (S) $(1 + \mu) \times \text{manji} \quad \left(\frac{1}{1 + \mu} \right)$

2. npn sićij (8b)

$$N_{DE} = 2 \cdot 10^{18} \text{ cm}^{-3}$$

$$N_{AB} = 3 \cdot 10^{16} \text{ cm}^{-3}$$

$$\mu_{pE} = 270 \text{ cm}^2/\text{Vs}$$

$$\mu_{nB} = 540 \text{ cm}^2/\text{Vs}$$

$$I_E = 10 \mu\text{A}$$

$$W_B = 1,1 \mu\text{m} = 1,1 \cdot 10^{-4} \text{ cm}$$

$$W_E = 1,7 \mu\text{m} = 1,7 \cdot 10^{-4} \text{ cm}$$

$$S = 1 \text{ mm}^2 = 10^{-2} \text{ cm}^2$$

$$U_{BE} = 0,55 \text{ V}$$

$$U_{CB} = 5 \text{ V}$$

$$U_T = 25 \text{ mV}$$

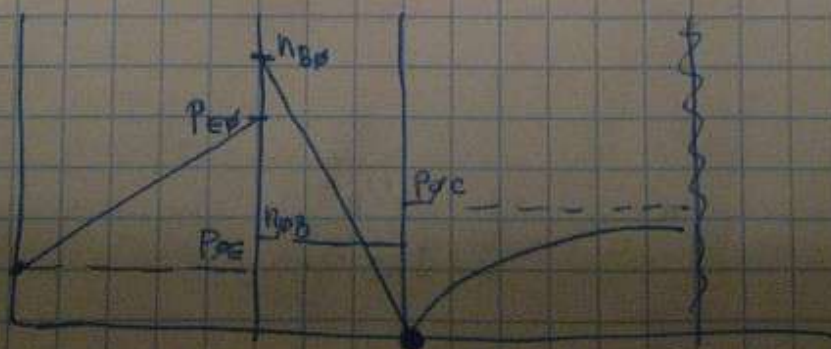
$$I_{CB\phi} \approx 0 \text{ A}$$

$$N_{DE} = n_{\phi E} \Rightarrow p_{\phi E} = \frac{n_i^2}{n_{\phi E}} = 1,05 \cdot 10^2 \text{ cm}^{-3}$$

$$N_{AB} = p_{\phi B} \Rightarrow n_{\phi B} = \frac{n_i^2}{p_{\phi B}} = 7,1 \cdot 10^3 \text{ cm}^{-3}$$

$$N_{DE} > N_{AB} > N_{DC}$$

$$p_{\phi E} < n_{\phi B} < p_{\phi C}$$



$$p_{E0} = p_{0E} \exp\left(\frac{U_{BE}}{U_T}\right) = 3,76 \cdot 10^{11} \text{ cm}^{-3}$$

$$n_{B0} = n_{0B} \exp\left(\frac{U_{BE}}{U_T}\right) = 2,51 \cdot 10^{13} \text{ cm}^{-3}$$

$$I_{pE} = q \cdot S \cdot D_{pE} \cdot \frac{dp(x)}{dx} = q \cdot S \cdot \cancel{D_p} \cdot U_T \cdot \frac{p_{E0}}{w_E} = 23,9 \mu\text{A}$$

$$I_{nE} = q \cdot S \cdot D_{nE} \cdot \frac{n_{B0}}{w_B} = 4,929 \mu\text{A}$$

$$I_E = I_{nE} - I_{nE} \Rightarrow I_{nE} = I_{nE} - I_E = \boxed{4,919 \mu\text{A}}$$

$$I_E = -(I_{nE} + I_{pE}) = \boxed{-4,953 \mu\text{A}}$$

$$I_C = I_{nE} = \boxed{4,919 \mu\text{A}}$$

$$I_B + I_E + I_C = 0$$

$$I_B = -I_E - I_C = \boxed{34 \mu\text{A}}$$

$$\alpha = \frac{I_C}{-I_E} = \frac{4,919 \mu\text{A}}{4,953 \mu\text{A}} = 0,9931$$

$$\beta = \frac{I_C}{I_B} = 146$$

$$\beta^* = \frac{I_{nC}}{I_{nE}} = 0,9980$$

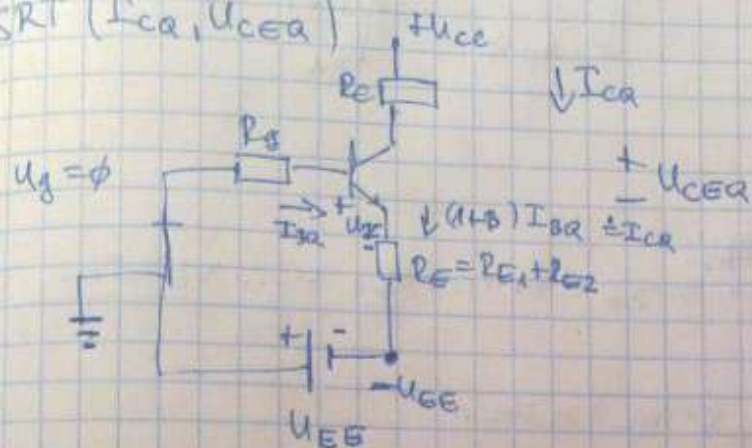
$$\beta^* = 1 - \frac{1}{2} \left(\frac{w_B}{L_{nB}} \right)^2$$

$$\hookrightarrow \sqrt{D_{nB} \cdot \tau_{nB}}$$

$$\Rightarrow \beta^* = 1 - \frac{1}{2} \frac{w_B^2}{D_{nB} \cdot \tau_{nB}}$$

3. zajednički emiter \Rightarrow negativno pojačanje (8b)

a) SRT (I_{CQ}, U_{CEQ})



BE-krug

$$I_{BQ} \cdot R_g + U_{BE} + (1+\beta) I_{BQ} \cdot R_E - U_{EE} = 0$$

$$I_{BQ} = \frac{U_{EE} - U_{BE}}{R_g + (1+\beta) R_E} = \frac{10 - 0,7}{0,5 + 101 \cdot 0,5} = 0,01083 \text{ mA} = \boxed{10,83 \mu\text{A}}$$

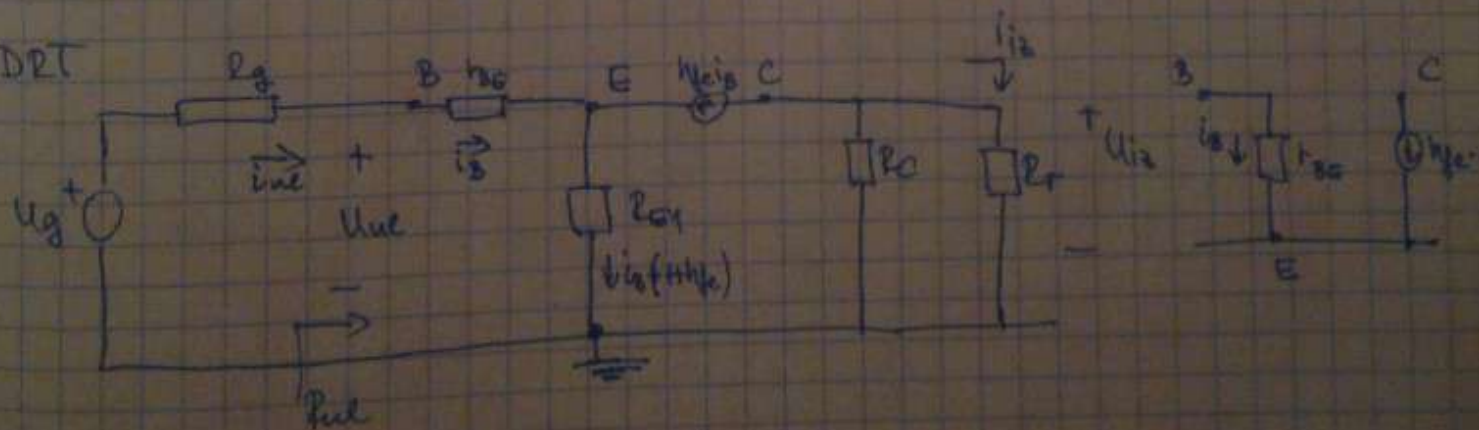
$$I_{CQ} = \beta \cdot I_{BQ} = 1,083 \text{ mA}$$

$$U_{CEQ} = U_{CC} - (-U_{EE}) - I_{CQ} (R_C + R_E) = 10 + 10 - 1,083 (0,5 + 0,5) = \boxed{4,3 \text{ V}}$$

$U_{CEQ} > U_{BEQ} = U_{BE} \rightarrow$ tranz. je u NAP-u

$$r_{be} = \frac{U_T}{I_{BQ}} = \boxed{2,3 \text{ k}\Omega}$$

b) DRT



$$A_V = \frac{U_{iz}}{U_{ul}} = \frac{-h_{fe} \cdot i_B \cdot R_C \parallel R_T}{i_B r_{BE} + (1+h_{fe}) i_B \cdot R_{E1}} = \dots = \boxed{-4,55}$$

$$\hookrightarrow A_V \approx - \frac{R_C \parallel R_T}{R_{E1}}$$

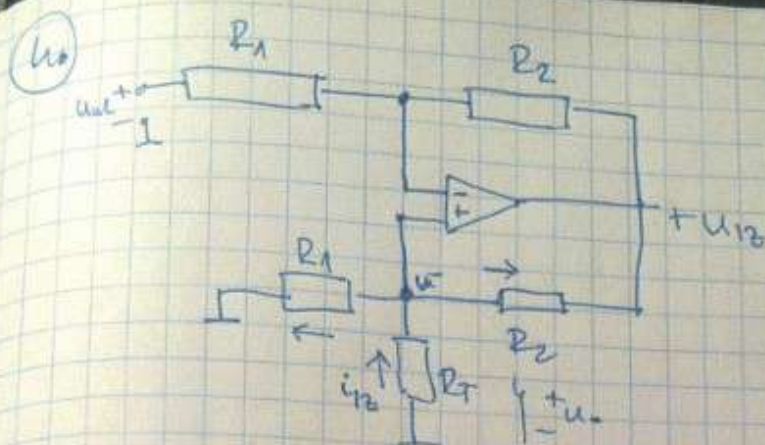
~~$R_{ul} = U_{ul}$~~

$$R_{ul} = \frac{U_{ul}}{i_{ul}} = \frac{i_B r_{BE} + (1+h_{fe}) i_B \cdot R_{E1}}{i_B} = r_{BE} + (1+h_{fe}) R_{E1} = \dots = \boxed{52,8 \text{ k}\Omega}$$

otpor iz (E) u (B) se preslikava $(1+h_{fe})$ x veći

(B) u (E) $(1+h_{fe})$ x manji

$$A_I = \frac{i_{iz}}{i_{ul}} = \frac{\frac{U_{iz}}{R_T}}{\frac{U_{ul}}{R_{ul}}} = \frac{U_{iz}}{U_{ul}} \cdot \frac{R_{ul}}{R_T} = A_V \cdot \frac{R_{ul}}{R_T} = -4,55 \cdot \frac{52,8}{4} = \boxed{-60}$$



$$u_{ucl} = 0.5 \text{ sin } \omega t \text{ V}$$

$$R_1 = 1 \text{ k}\Omega$$

$$R_2 = 2 \text{ k}\Omega$$

$$R_T = 3 \text{ k}\Omega$$

$$i_{12} = ? \quad f(u_{ucl}) =$$

$$(1) \quad \frac{u_{ucl} - u^-}{R_1} = \frac{u^- - u_{12}}{R_2}$$

$$(2) \quad u^- = -i_{12} \cdot R_T$$

$$(3) \quad i_{12} = \frac{u^-}{R_1} + \frac{u^- - u_{12}}{R_2}$$

$$(2) \rightarrow (3) \quad i_{12} = -i_{12} \cdot \frac{R_T}{R_1} - i_{12} \cdot \frac{R_T}{R_2} - \frac{u_{12}}{R_2}$$

$$i_{12} \left(1 + \frac{R_T}{R_2} + \frac{R_T}{R_1} \right) = -\frac{u_{12}}{R_2} \quad (4)$$

$$(2) \rightarrow (1) \quad \frac{u_{ucl}}{R_1} + i_{12} \cdot \frac{R_T}{R_1} = -i_{12} \cdot \frac{R_T}{R_2} - \frac{u_{12}}{R_2} \quad (5)$$

$$(4) \rightarrow (5) = \frac{u_{ucl}}{R_1} + i_{12} \left(\frac{R_T}{R_1} + \frac{R_T}{R_2} \right) = i_{12} \left(1 + \frac{R_T}{R_1} + \frac{R_T}{R_2} \right)$$

$$i_{12} = \frac{u_{ucl}}{R_1} = \frac{0.5}{1\text{k}} = \boxed{0.5 \text{ }\mu\text{A}}$$