

Fakultet elektrotehnike i računarstva
Zavod za elektroniku, mikroelektroniku,
računalne i inteligentne sustave

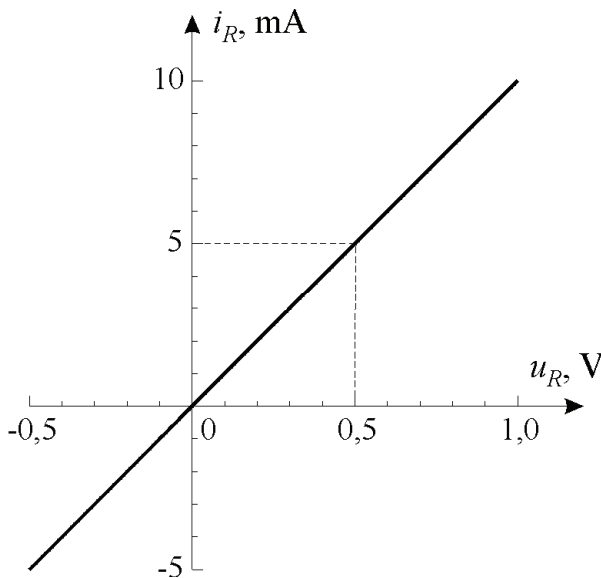
Elektronika 1

Ž. Butković, J. Divković Pukšec, A. Barić

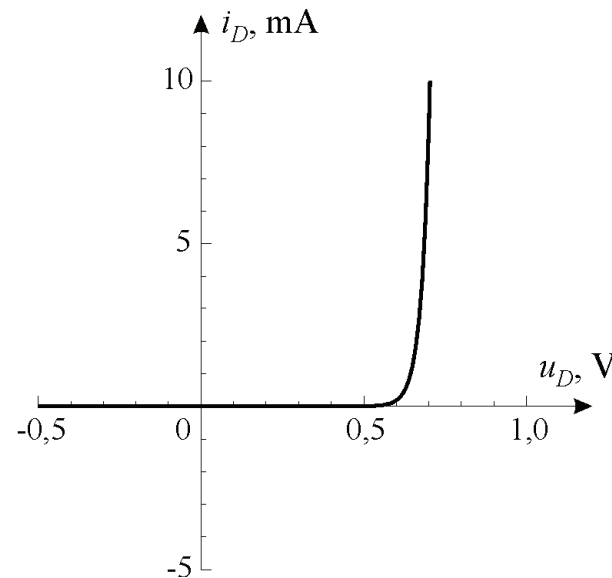
4. Sklopovi s diodama

Usporedba diode i otpornika

otpornik – $100\ \Omega$



silicijska *pn*-dioda

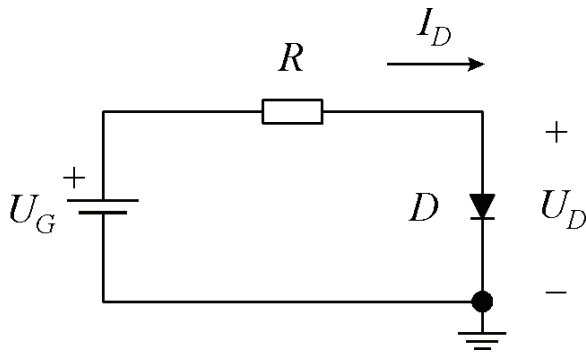


Specifičnost analize elektroničkih sklopova – zbog nelinearnih karakteristika elektroničkih elemenata

Statička analiza

Statičkom analizom proračunavaju se istosmjerne struje i naponi elektroničkih sklopova

Primjer sklopa



Iz strujnog kruga:

$$U_G = R I_D + U_D$$

Druga jednačba:

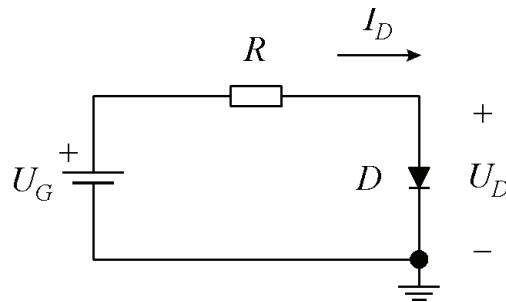
$$I_D = f(U_D)$$

npr. za propusnu polarizaciju

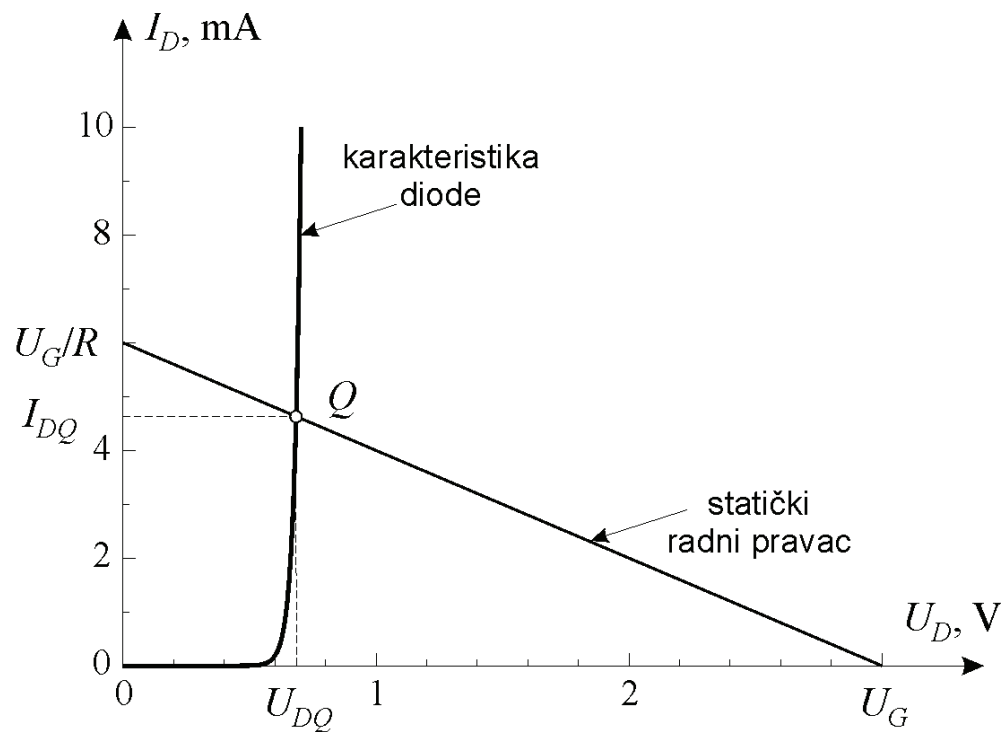
$$I_D = I_S \exp (U_D/U_T)$$

Primjer 4.1

Izračunati struju I_D i napon U_D za sklop prema slici. Napon $U_G = 3\text{ V}$, otpor $R = 500\ \Omega$, struja zasićenja diode $I_S = 10\text{ fA}$ i temperatura je sobna, $U_T = 25\text{ mV}$.



Grafička analiza



Statički radni pravac:

$$U_G = R I_D + U_D$$

nagib - - $1/R$

Statička radna točka Q

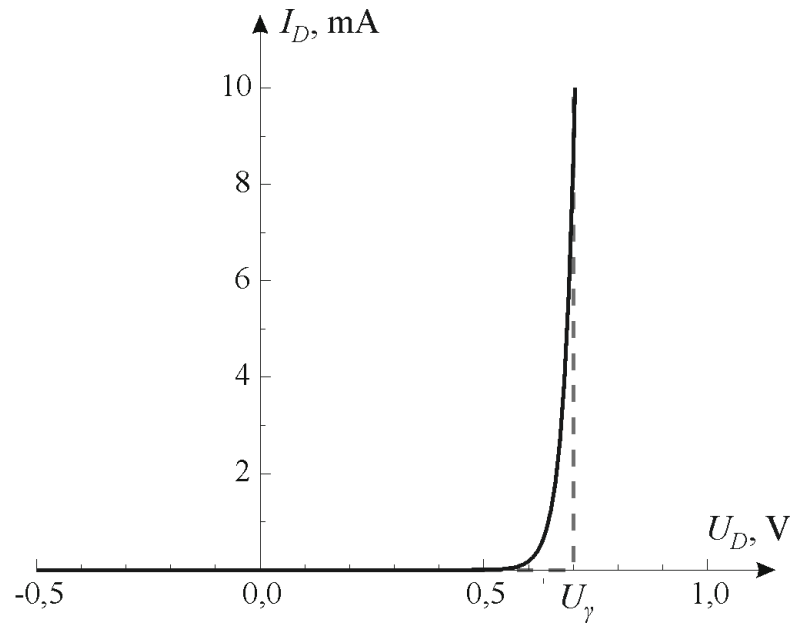
Primjer:

$$U_G = 3 \text{ V}, R = 500 \text{ } \Omega$$

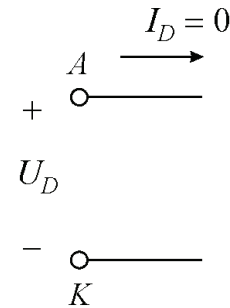
$$U_{DQ} = 0,68 \text{ V}$$

$$I_{DQ} = 4,6 \text{ mA}$$

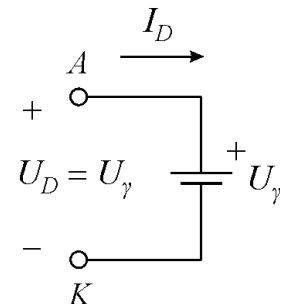
Model diode za statičku analizu



$$U_D < U_\gamma$$

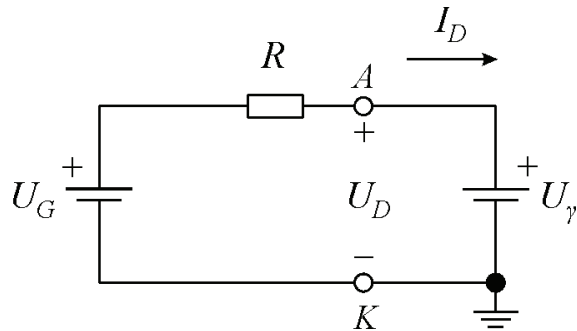


$$U_D > U_\gamma$$



Analitički postupak – Primjer 4.2

Za $U_D > U_\gamma$



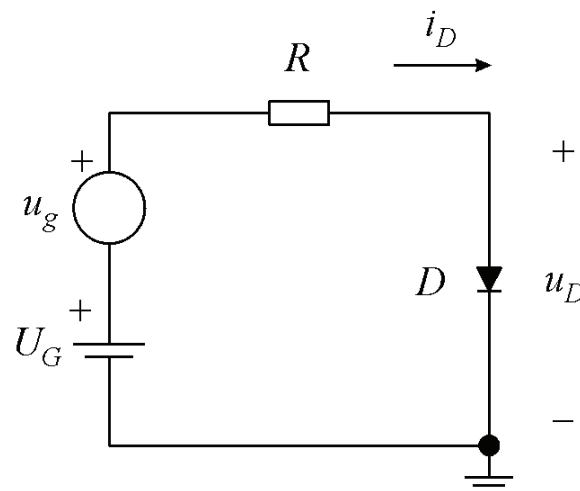
$$U_D = U_\gamma = U_{DQ}$$

$$I_D = \frac{U_G - U_\gamma}{R} = I_{DQ}$$

Primjer 4.2 - Ponoviti proračun struje i napona diode sklopa iz primjera 4.1 korištenjem modela diode za statičku analizu. Napon koljena diode $U_\gamma = 0,7 \text{ V}$.

Analiza uz priključak malog signala

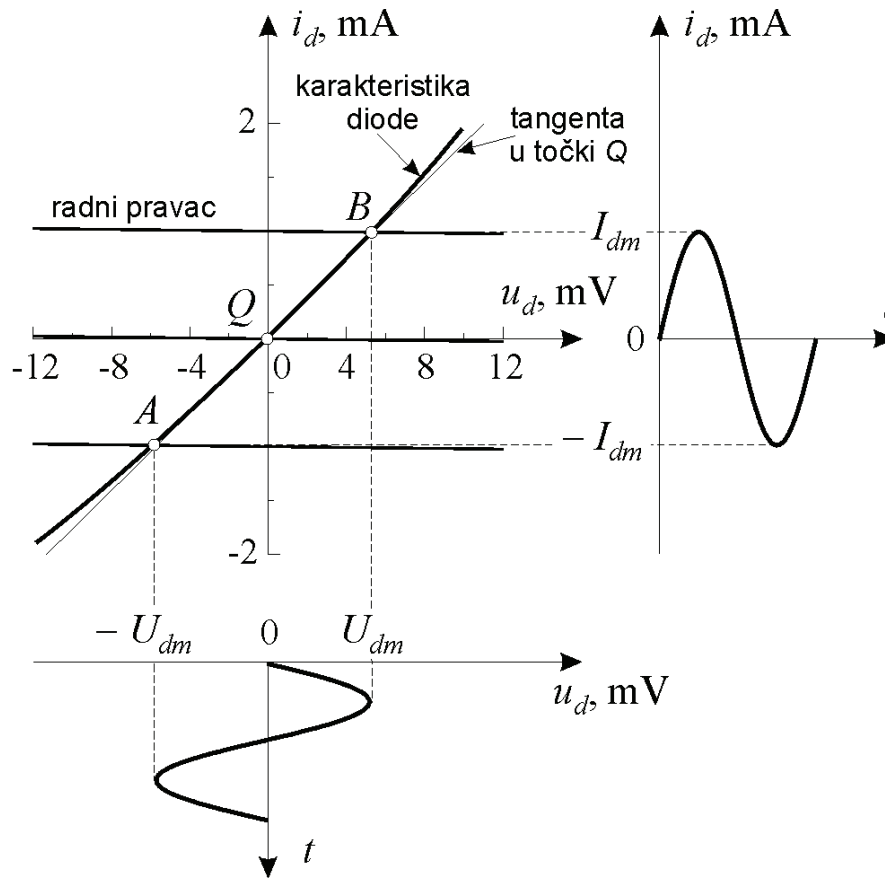
Primjer sklopa



Ulazni napon: $u_G = U_G + u_g = U_G + U_{gm} \sin \omega t$

Iz strujnog kruga: $u_G = R i_D + u_D$

Grafička analiza (2)



Nagib karakteristike:

$$\left. \frac{di_D}{du_D} \right|_Q = \left. \frac{\Delta i_D}{\Delta u_D} \right|_Q = \frac{I_{dm}}{U_{dm}} = \frac{i_d}{u_d} = g_d$$

g_d – dinamička vodljivost

$r_d = 1/g_d$ – dinamički otpor

Primjer:

$$U_{gm} = 0,5 \text{ V}$$

$$I_{dm} = 1 \text{ mA}, U_{dm} = 5,6 \text{ mV}$$

$$g_d = 0,18 \text{ S}, r_d = 5,6 \Omega$$

Uvjeti rada diode u režimu malog signala

Struja diode oko radne točke

$$i_D = i_D|_Q + \left. \frac{di_D}{du_D} \right|_Q (u_D - U_{DQ}) + \left. \frac{d^2 i_D}{du_D^2} \right|_Q \frac{(u_D - U_{DQ})^2}{2!} + \dots$$

Uz $i_D = I_S \exp(u_D/U_T)$

$$\left. \frac{di_D}{du_D} \right|_Q = \frac{I_S}{U_T} \exp\left(\frac{u_D}{U_T}\right) \Big|_Q = \frac{I_{DQ}}{U_T} \quad \left. \frac{d^2 i_D}{du_D^2} \right|_Q = \frac{I_S}{U_T^2} \exp\left(\frac{u_D}{U_T}\right) \Big|_Q = \frac{I_{DQ}}{U_T^2}$$

$$\text{uz } u_D - U_{DQ} = u_d \rightarrow i_D = I_{DQ} \left[1 + \frac{u_d}{U_T} + \frac{1}{2!} \left(\frac{u_d}{U_T} \right)^2 + \dots \right]$$

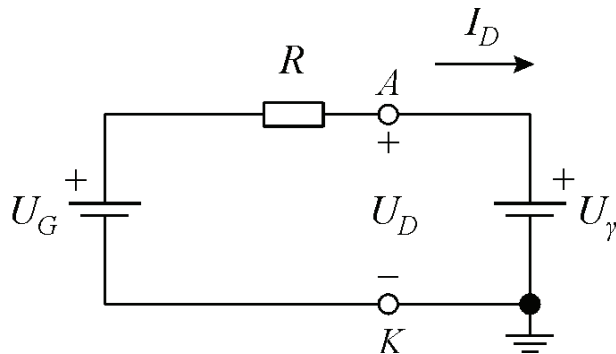
Uvjet za režim malog signala: $u_d \ll U_T$ ($U_{dm} \ll U_T$)

$$\left. \frac{di_D}{du_D} \right|_Q = \frac{I_{DQ}}{U_T} = g_d = \frac{1}{r_d} \quad \text{uz linearni rad} \rightarrow i_D = I_{DQ} + i_d = I_{DQ} + \frac{u_d}{r_d}$$

Analitički postupak

Metoda superpozicije

uz: $u_G = U_G + u_g$ - analiza posebno za statiku, a posebno za dinamiku

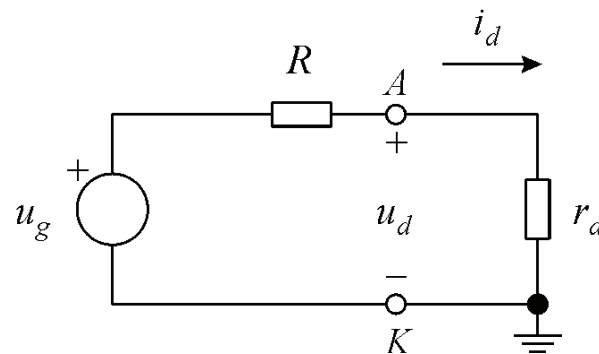


statička analiza

$$U_D = U_\gamma = U_{DQ}$$

$$I_D = \frac{U_G - U_\gamma}{R} = I_{DQ}$$

$$r_d = \frac{U_T}{I_{DQ}}$$



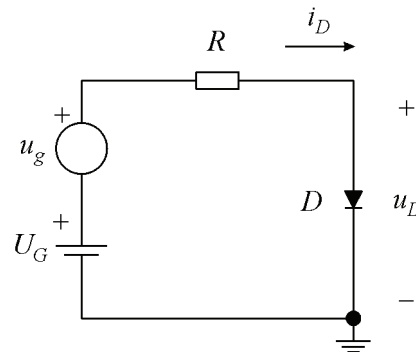
dinamička analiza

$$i_d = \frac{u_g}{R + r_d}$$

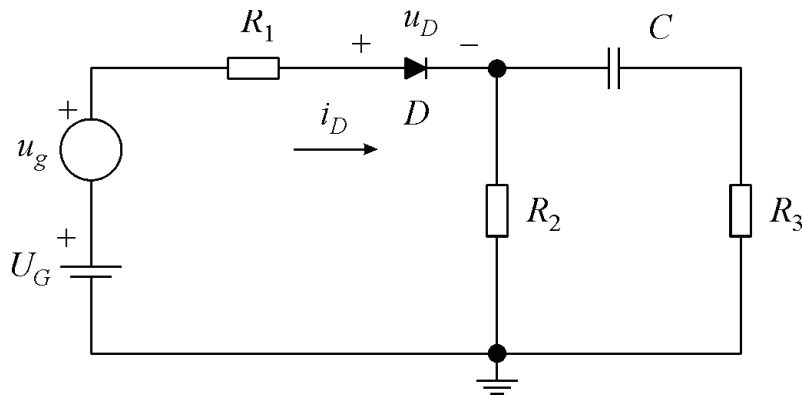
$$u_d = r_d i_d$$

Primjer 4.3

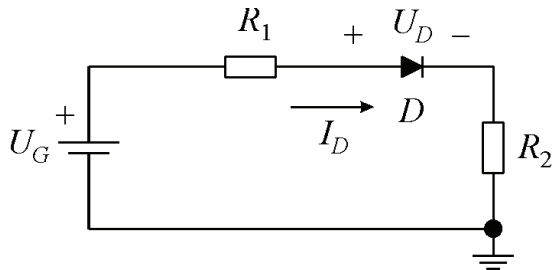
Za sklop sa slike analitički proračunati napon u_D i struju i_D diode. Napon $u_G = 3 + 0,5 \sin \omega t$ V, otpor $R = 500 \, \Omega$, napon koljena diode $U_\gamma = 0,7$ V i temperatura je sobna, $U_T = 25$ mV.



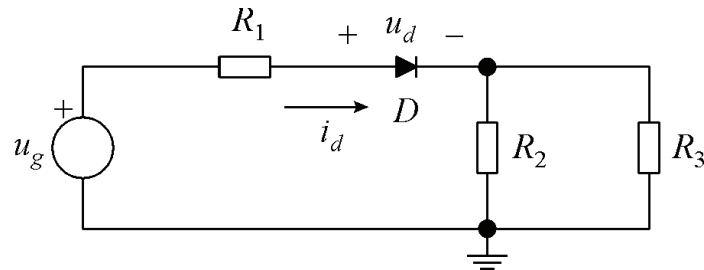
Utjecaj reaktivnih elemenata



Reaktivne komponente se različito ponašaju u statičkim i dinamičkim uvjetima.

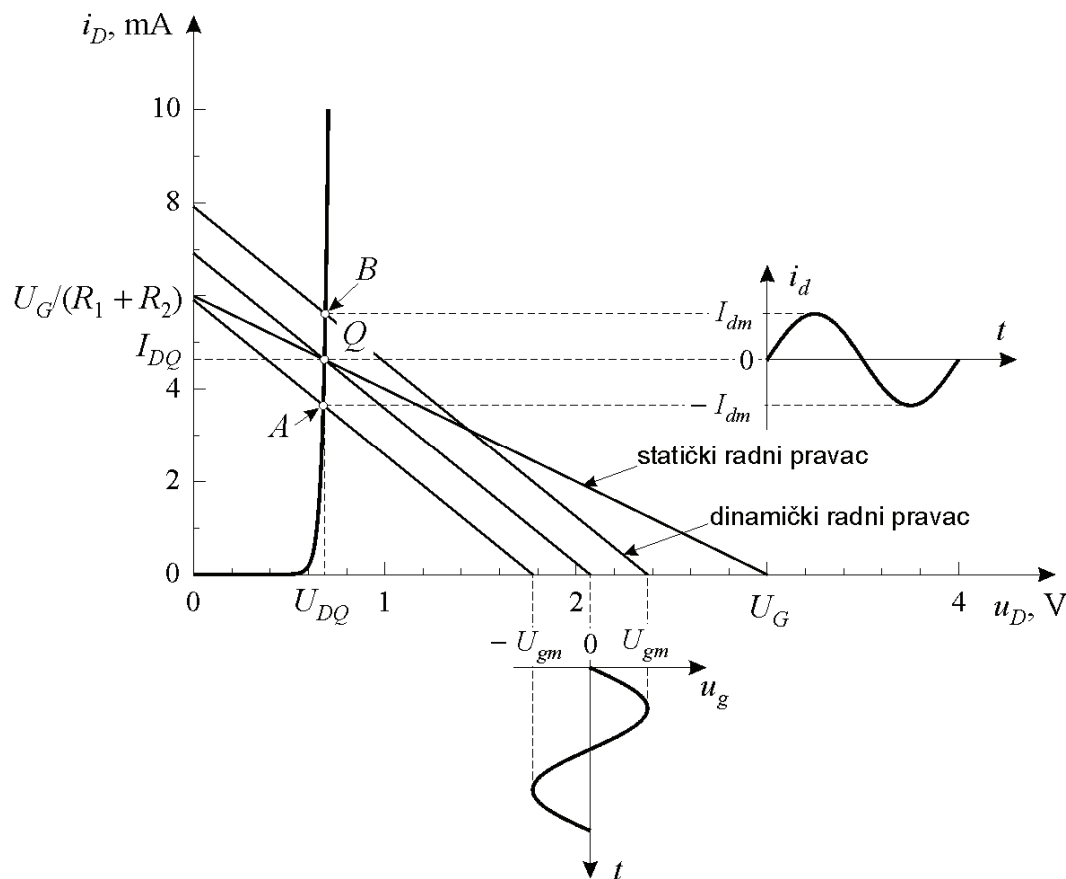


statička analiza



dinamička analiza

Grafička analiza



Statički radni pravac:

$$U_G = (R_1 + R_2) I_D + U_D$$

nagib: $-1/(R_1 + R_2)$

Dinamički radni pravac:

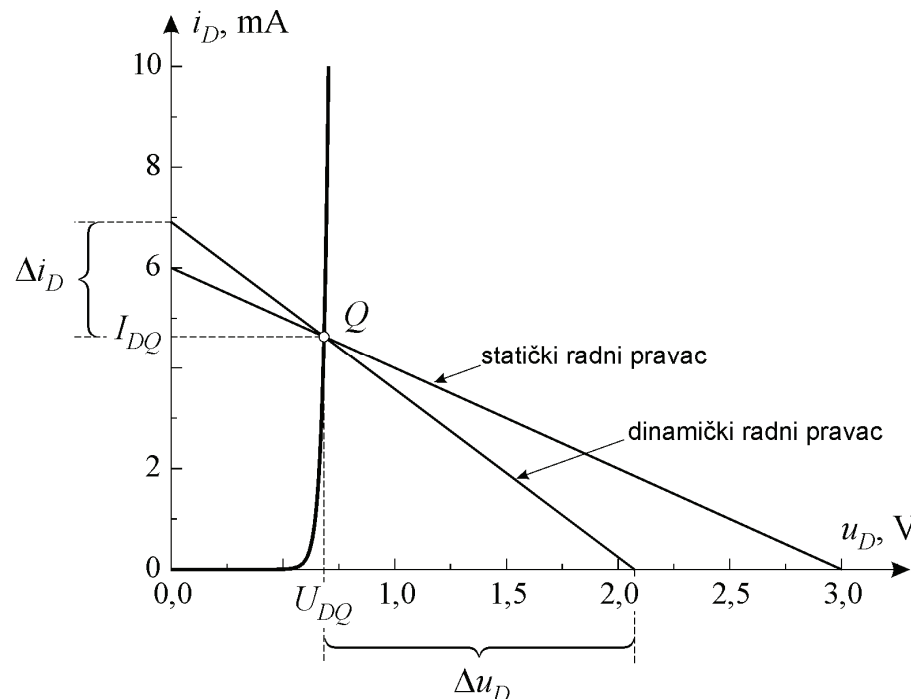
$$u_g = (R_1 + R_2 \parallel R_3) i_d + u_d$$

nagib: $-1/(R_1 + R_2 \parallel R_3)$

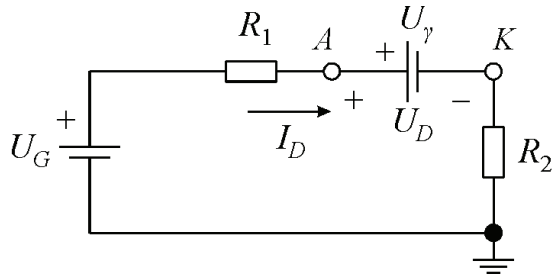
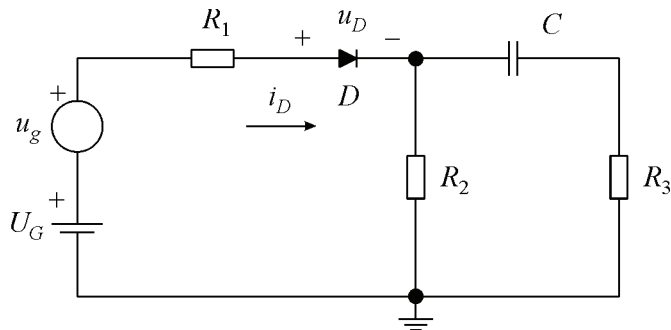
Primjer 4.4

Konstruirati statički radni pravac i dinamički radni pravac za napon $u_g = 0$ za primjer sa zadnjeg grafičkog prikaza. Zadano je: $U_G = 3 \text{ V}$, $R_1 = 100 \Omega$ i $R_2 = R_3 = 400 \Omega$.

Rješenje:



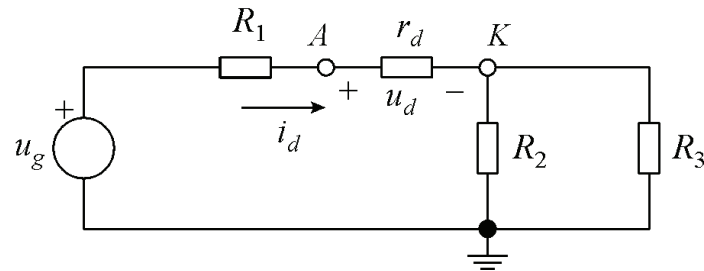
Analitički postupak



statička analiza

$$U_D = U_{DQ} = U_\gamma$$

$$I_D = I_{DQ} = \frac{U_G - U_\gamma}{R_1 + R_2}$$



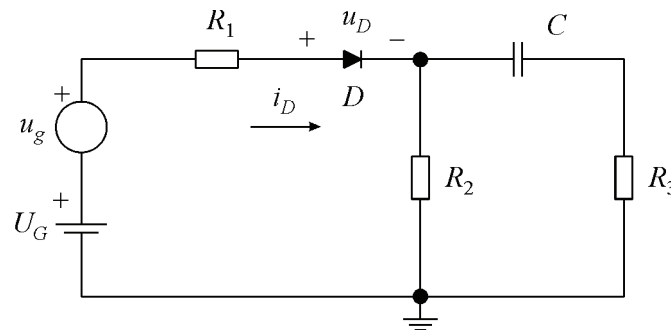
dinamička analiza

$$i_d = \frac{u_g}{R_1 + r_d + R_2 \parallel R_3}$$

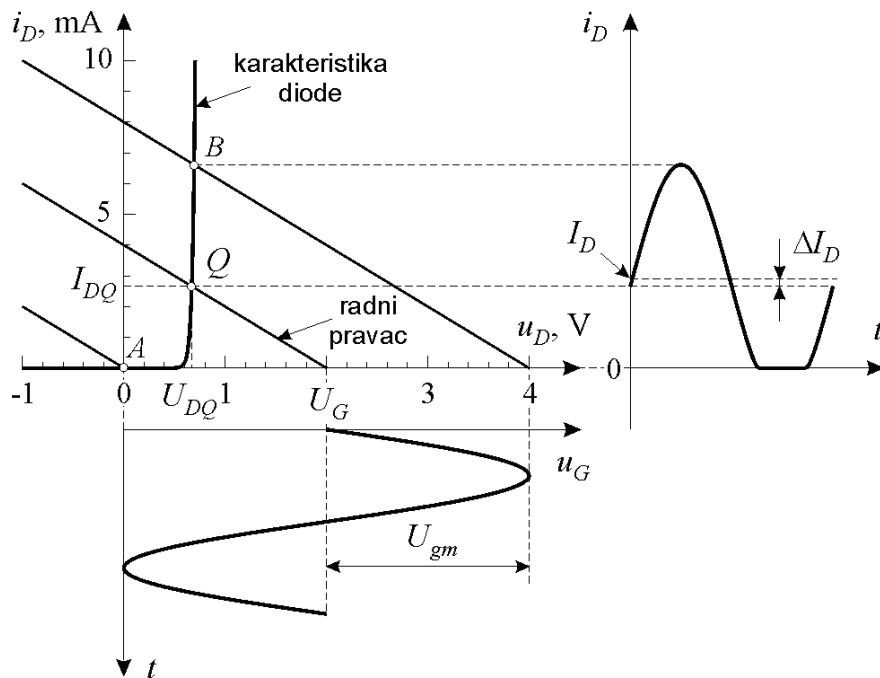
$$u_d = r_d i_d$$

Primjer 4.5

Za sklop sa slike analitički proračunati napon u_D i struju i_D diode. Napon $u_G = 3 + 0,3 \sin \omega t$ V, otpori $R_1 = 100 \, \Omega$, $R_2 = R_3 = 400 \, \Omega$, napon koljena diode $U_\gamma = 0,7$ V i temperatura je sobna, $U_T = 25$ mV.



Priključak velikog signala

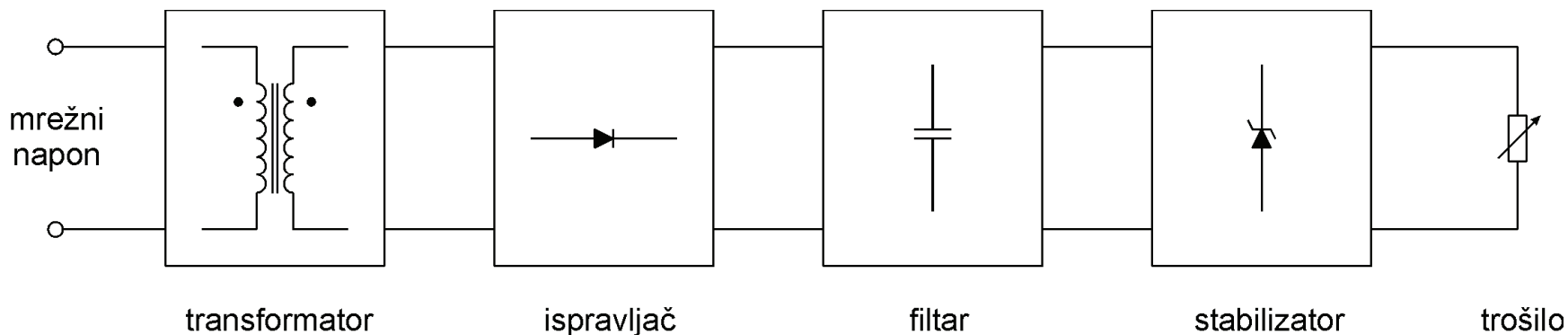


Hod radne točke po nelinearnom dijelu karakteristike

Posljedica nelinearnog rada:

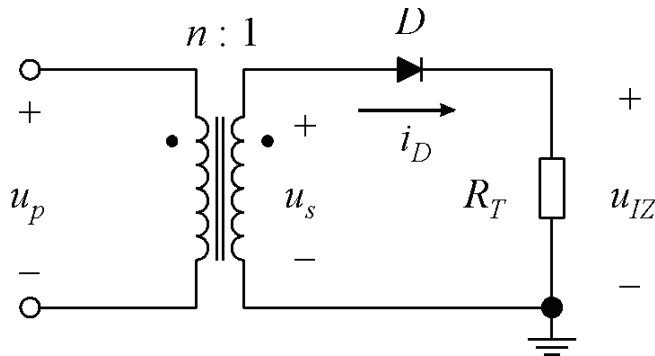
- ❑ izobličenje struje
 - ❑ dodatna istosmjerna struja ΔI_D
- $$I_D = I_{DQ} + \Delta I_D$$

Izvor napajanja



- ❑ Mrežni napon – $f = 50 \text{ Hz}$, $U_{\text{pef}} = 220 \text{ V}$, $U_{\text{pm}} = 310 \text{ V}$
- ❑ Transformator – smanjuje ulazni napon, izolira izvor od napona u primaru
- ❑ Ispravljač – ispravlja izmjenični napon, daje istosmjerni pulsirajući napon
- ❑ Filtar – guši izmjenične komponente
- ❑ Stabilizator – održava stalni istosmjerni napon
- ❑ Trošilo – elektronički sklopovi i uređaji

Poluvalni ispravljač (1)



Mrežni napon – $u_p = U_{pm} \sin \omega t$

Napon sekundara – $u_s = U_{sm} \sin \omega t$

Omjer transformacije: $n = U_{pm}/U_{sm}$

Za $u_D = u_s - u_{IZ} > U_\gamma \rightarrow$ dioda vodi $\rightarrow u_D = U_\gamma, u_{IZ} = u_s - U_\gamma$

Za $u_D < U_\gamma \rightarrow$ dioda ne vodi $\rightarrow i_D = 0, u_D = u_s, u_{IZ} = 0$

Poluvalni ispravljač (2)

Uz idealnu diodu:

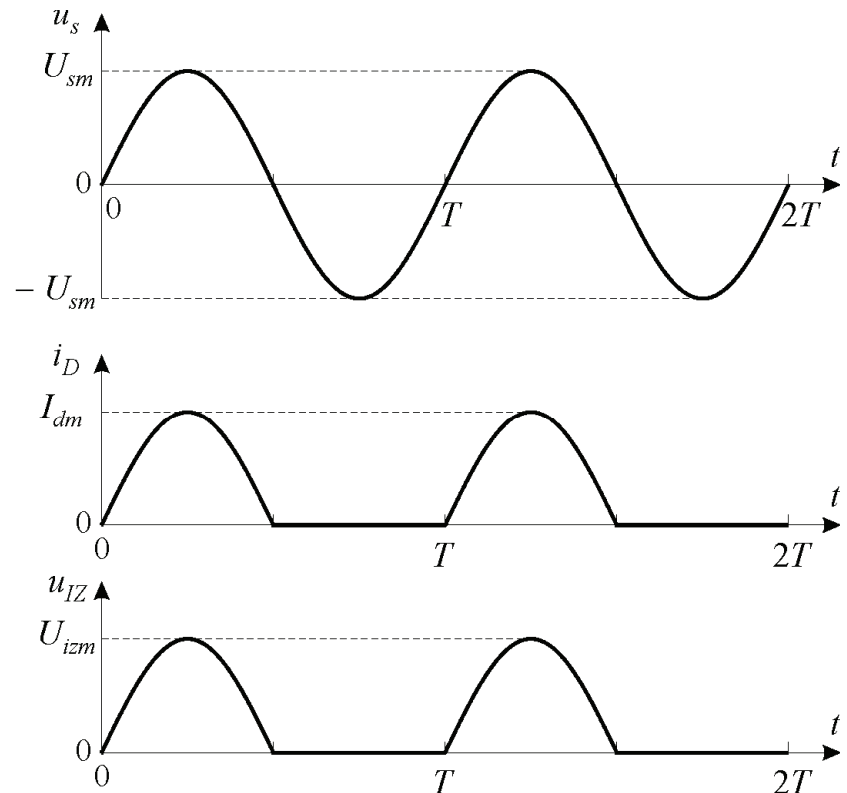
$$\text{za } u_D < 0 \rightarrow i_D = 0$$

$$\text{za } u_D > 0 \rightarrow u_D = 0$$

$$i_D = \begin{cases} u_s / R_T & \text{za } u_s > 0 \\ 0 & \text{za } u_s < 0 \end{cases}$$

$$u_{IZ} = i_D R_T$$

$$u_{IZ} = \begin{cases} u_s & \text{za } u_s > 0 \\ 0 & \text{za } u_s < 0 \end{cases}$$



Poluvalno ispravljeni napon (1)

Srednja vrijednost

$$U_{IZ} = \frac{1}{T} \int_0^T u_{IZ}(t) dt = \frac{1}{2\pi} \left(U_{sm} \int_0^{\pi} \sin \omega t d\omega t + \int_{\pi}^{2\pi} 0 d\omega t \right) = \frac{U_{sm}}{\pi} = 0,318 U_{sm}$$

Efektivna vrijednost

$$U_{izef} = \left[\frac{1}{T} \int_0^T u_{IZ}^2(t) dt \right]^{\frac{1}{2}} = \left[\frac{1}{2\pi} \left(U_{sm}^2 \int_0^{\pi} \sin^2 \omega t d\omega t + \int_{\pi}^{2\pi} 0 d\omega t \right) \right]^{\frac{1}{2}} = \frac{U_{sm}}{2}$$

Razvojem poluvalno ispravljenog napona u Fourierov red

$$u_{IZ} = U_{sm} \left[\frac{1}{\pi} + \frac{\sin \omega t}{2} - \frac{2}{\pi} \left(\frac{\cos 2 \omega t}{1 \cdot 3} + \frac{\cos 4 \omega t}{3 \cdot 5} + \dots \right) \right] = U_{IZ} + u_{izv}$$

Poluvalno ispravljeni napon (2)

$$U_z \quad U_{izef} = \sqrt{U_{IZ}^2 + U_{izvef}^2}$$

Efektivna vrijednost napona valovitosti

$$U_{izvef} = \sqrt{U_{izef}^2 - U_{IZ}^2} = U_{sm} \sqrt{\frac{1}{4} - \frac{1}{\pi^2}} = 0,386 U_{sm}$$

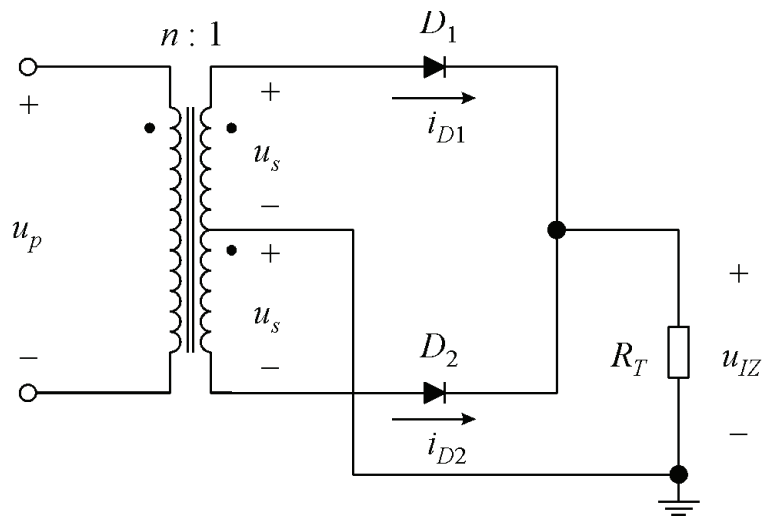
Faktor valovitosti

$$r = \frac{U_{izvef}}{U_{IZ}} = \sqrt{\left(\frac{U_{izef}}{U_{IZ}}\right)^2 - 1} = \sqrt{\frac{\pi^2}{4} - 1} = 1,21$$

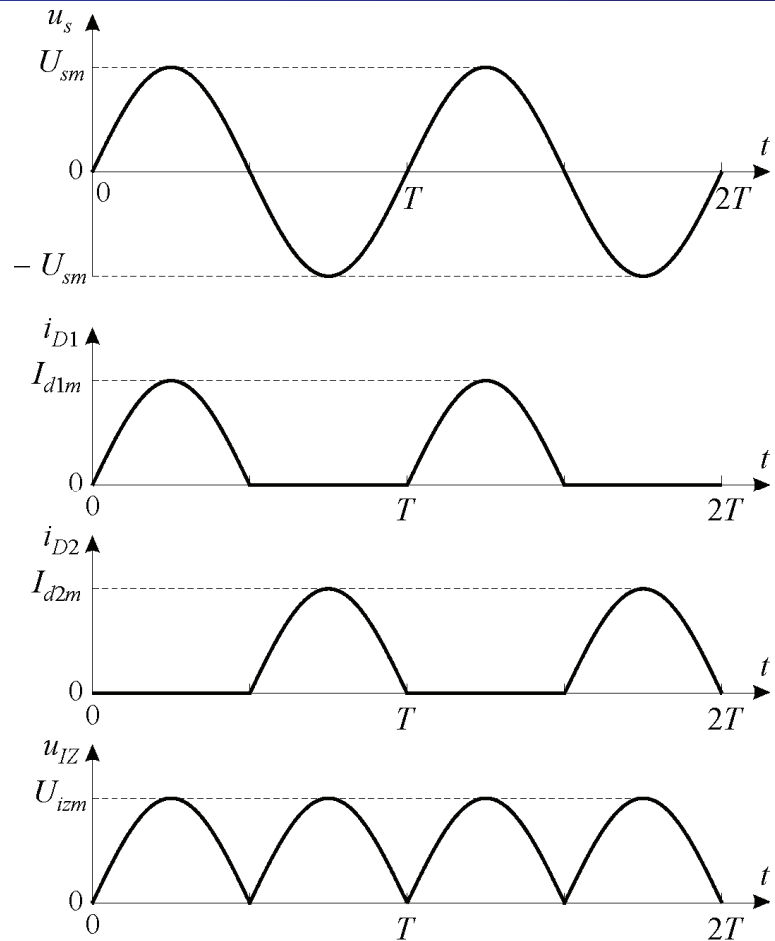
Maksimalna struja diode u vođenju – U_{sm}/R_T

Maksimalni zaporni napon diode – U_{sm}

Punovalni ispravljač



$$u_{IZ} = (i_{D1} + i_{D2}) R_T$$



Punovalno ispravljeni napon (1)

Srednja vrijednost

$$U_{IZ} = \frac{2}{T} \int_0^{T/2} u_{IZ}(t) dt = \frac{U_{sm}}{\pi} \int_0^{\pi} \sin \omega t d\omega t = \frac{2U_{sm}}{\pi} = 0,637U_{sm}$$

Efektivna vrijednost

$$U_{izef} = \left[\frac{2}{T} \int_0^{T/2} u_{IZ}^2(t) dt \right]^{1/2} = \left(\frac{U_{sm}^2}{\pi} \int_0^{\pi} \sin^2 \omega t d\omega t \right)^{1/2} = \frac{U_{sm}}{\sqrt{2}} = 0,707U_{sm}$$

Razvojem punovalno ispravljenog napona u Fourierov red

$$u_{IZ} = U_{sm} \left[\frac{2}{\pi} - \frac{4}{\pi} \left(\frac{\cos 2\omega t}{1 \cdot 3} + \frac{\cos 4\omega t}{3 \cdot 5} + \dots \right) \right] = U_{IZ} + u_{izv}$$

Punovalno ispravljeni napon (2)

Efektivna vrijednost napona valovitosti

$$U_{izvef} = \sqrt{U_{izef}^2 - U_{IZ}^2} = U_{sm} \sqrt{\frac{1}{2} - \frac{4}{\pi^2}} = 0,308 U_{sm}$$

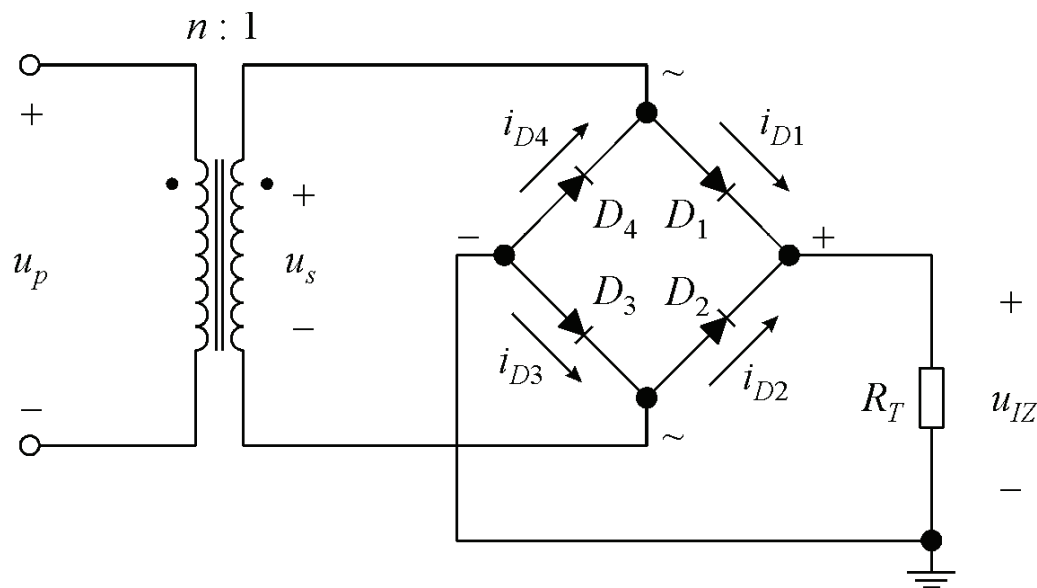
Faktor valovitosti

$$r = \frac{U_{izvef}}{U_{IZ}} = \sqrt{\left(\frac{U_{izef}}{U_{IZ}}\right)^2 - 1} = \sqrt{\frac{\pi^2}{8} - 1} = 0,483$$

Maksimalna struja dioda u vođenju – U_{sm}/R_T

Maksimalni zaporni napon dioda – $2U_{sm}$

Punovalni ispravljač – mosni ili Graetzov spoj



Valni oblici – isti kao i kod
prethodnog punovalnog
ispravljača

Maksimalna struja dioda u
vođenju – U_{sm}/R_T

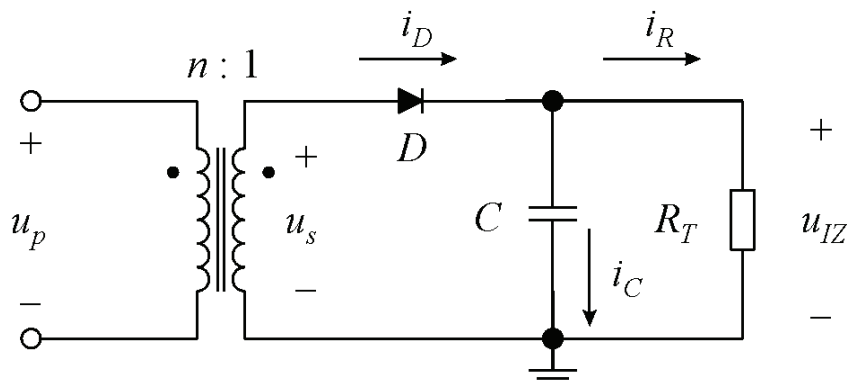
Maksimalni zaporni napon
dioda – U_{sm}

Realizacija – sve 4 diode u
istom kućištu

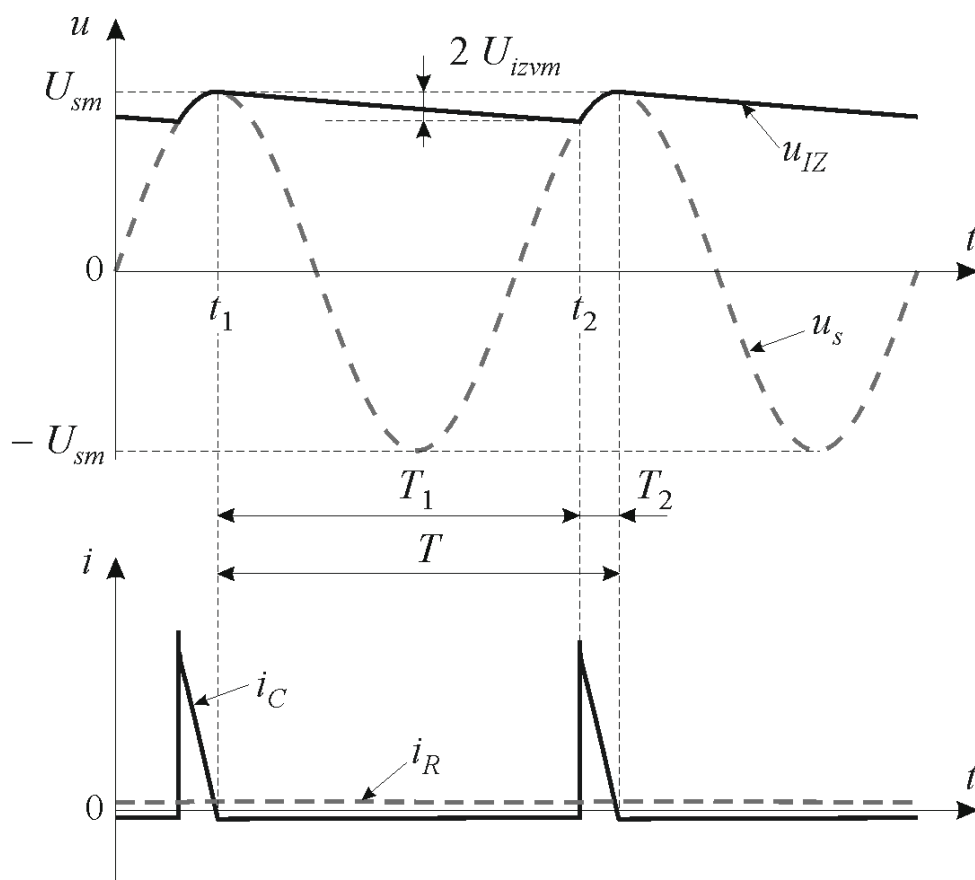
Ispravljač s kapacitivnim opterećenjem (1)

Smanjuje valovitost ispravljenog napona

C i R_T – niskopropusni filter koji guši izmjenične komponente ispravljenog napona



Ispravljač s kapacitivnim opterećenjem (2)



Kroz $T_1 - u_s < u_{IZ}$ dioda ne vodi,
kondenzator se izbija

$$u_{IZ}(t) = U_{sm} \exp\left(-\frac{t - t_1}{\tau}\right) \quad \tau = R_T C$$

Za $t = t_2 - u_s = u_{IZ}$ dioda provede

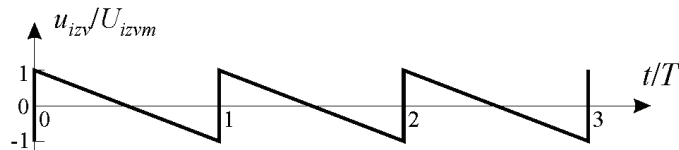
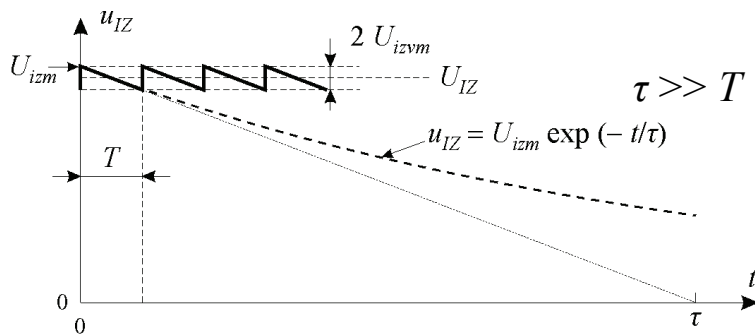
$$U_{sm} \cos \omega(t_2 - t_1) = U_{sm} \exp\left(-\frac{t_2 - t_1}{\tau}\right)$$

Kroz $T_2 - u_s = u_{IZ}$ dioda vodi,
kondenzator se nabija

$$u_{IZ}(t) = u_s(t) = U_{sm} \cos \omega(t - t_1)$$

Maksimalni zaporni napon diode –
 $2U_{sm}$

Pojednostavljeni valni oblik napona trošila



Za $t = 0$ $u_{IZ}(0) = U_{izm} = U_{sm}$

Za $t = T_2 \approx T$

$$u_{IZ}(T) = U_{izm} \exp\left(-\frac{T}{\tau}\right) \approx U_{izm} \left(1 - \frac{T}{\tau}\right)$$

$$u_{IZ}(0) - u_{IZ}(T) = 2U_{izvm}$$

$$U_{izvm} = U_{izm} \frac{T}{2\tau}$$

Srednja vrijednost $U_{IZ} = u_{IZ} - u_{izv} = U_{izm} - U_{izvm} = U_{izm} \left(1 - \frac{T}{2\tau}\right)$

Izmjenični napon valovitosti $u_{izv} = U_{izvm} \left(1 - \frac{2t}{T}\right)$

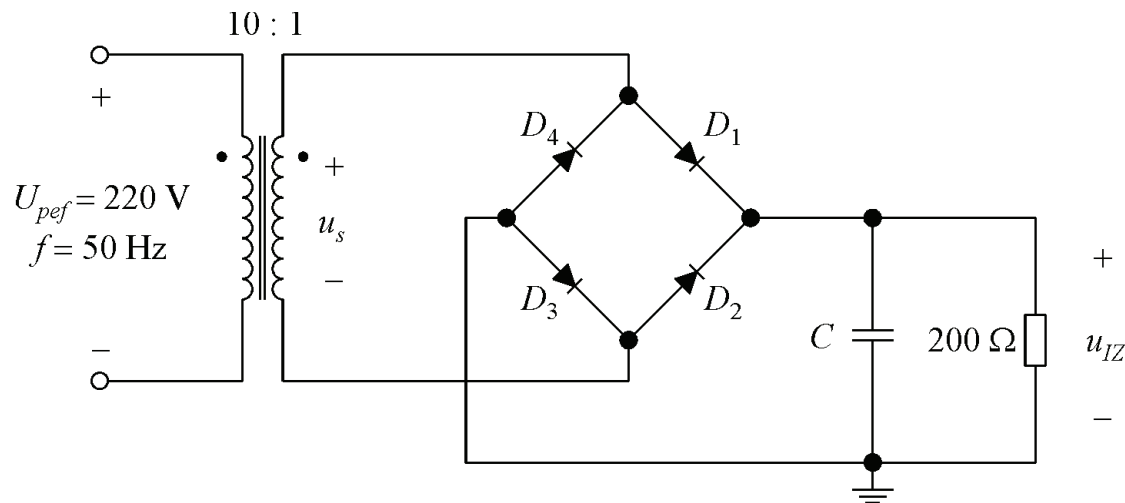
$$U_{izvef} = \left[\frac{1}{T} \int_0^T u_{izv}^2(t) dt \right]^{1/2} = \frac{U_{izvm}}{\sqrt{3}}$$

Faktor valovitosti $r = \frac{U_{izvef}}{U_{IZ}} = \frac{T/(2\tau)}{\sqrt{3}[1 - T/(2\tau)]}$

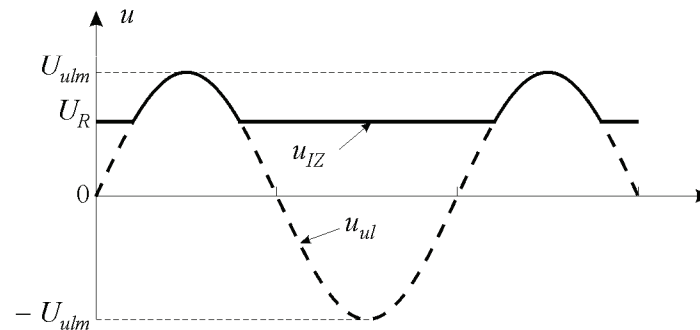
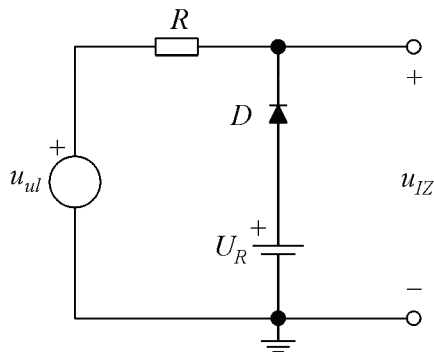
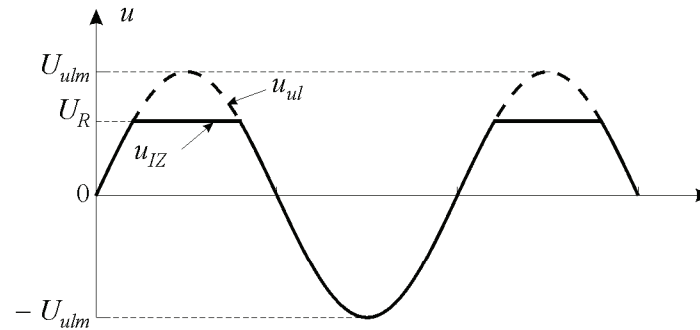
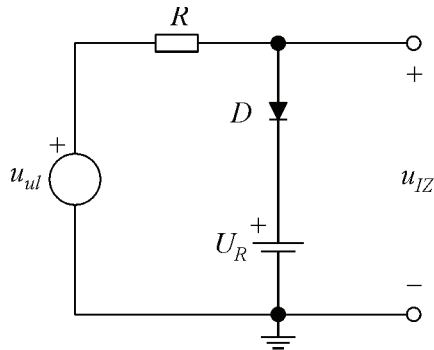
Primjer 4.6 (1)

Za punovalni ispravljač u Graetzovom spoju s kapacitivnim opterećenjem na slici izračunati srednju vrijednost napona trošila i faktor valovitosti uz:

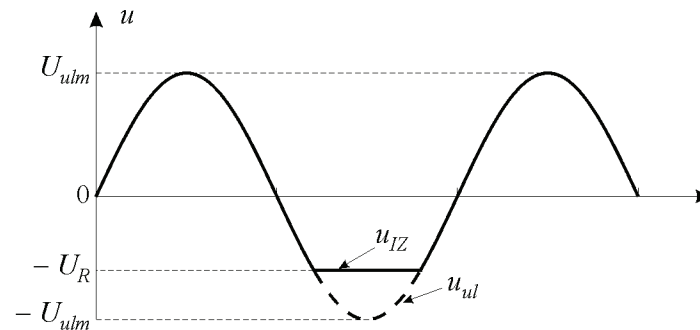
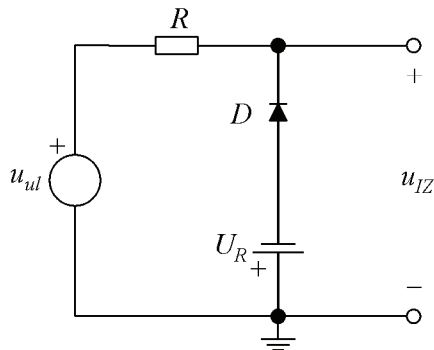
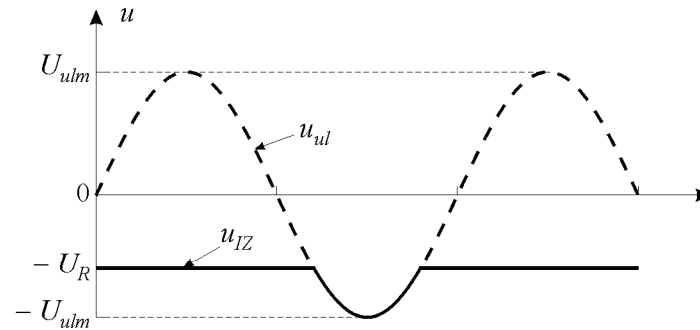
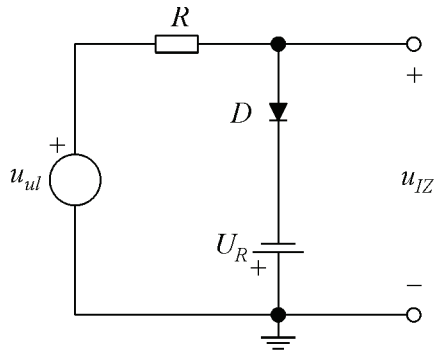
- a) $C = 0$,
- b) $C = 1000 \mu\text{F}$.



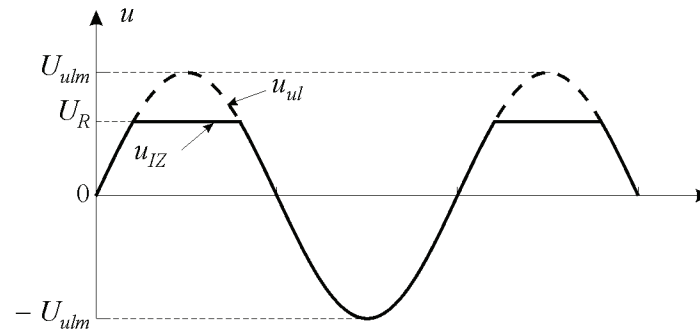
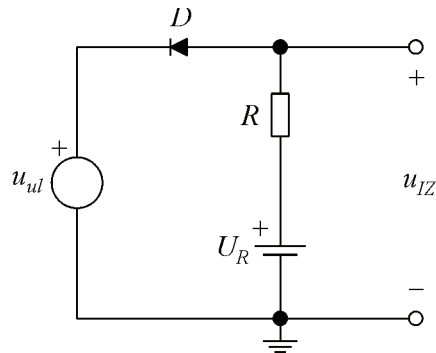
Paralelni diodni ograničavači (1)



Paralelni diodni ograničavači (2)



Serijski diodni ograničavač

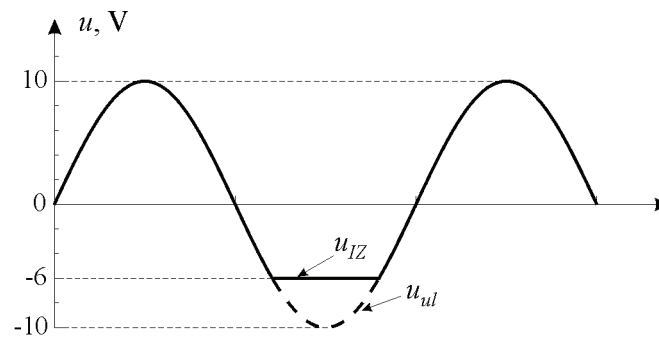
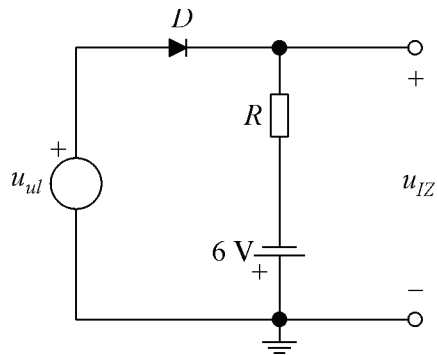


Primjer 4.7

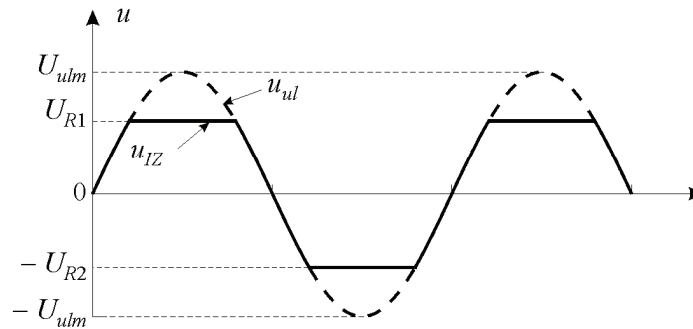
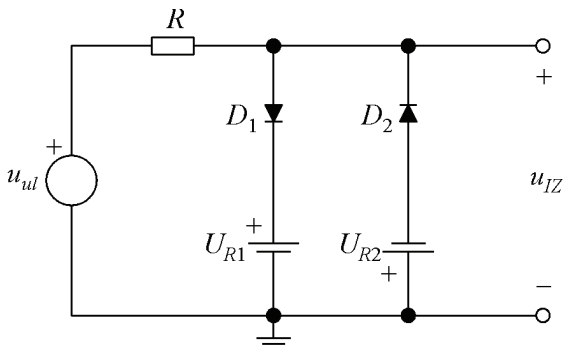
Nacrtati spoj serijskog diodnog ograničavača koji će ulazni napon

$u_{ul} = 10 \sin \omega t$ V ograničiti ispod razine od -6 V.

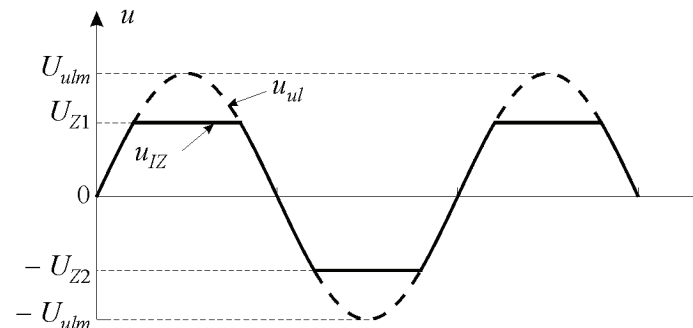
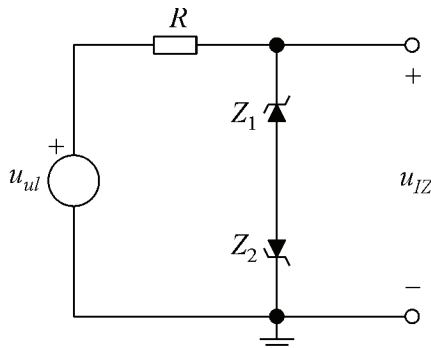
Rješenje:



Dvostrani ograničavači



Dvostrani paralelni diodni ograničavač



Dvostrani ograničavač sa Zenerovim diodama