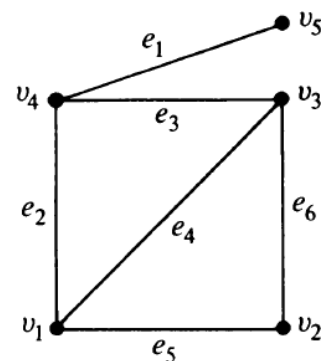
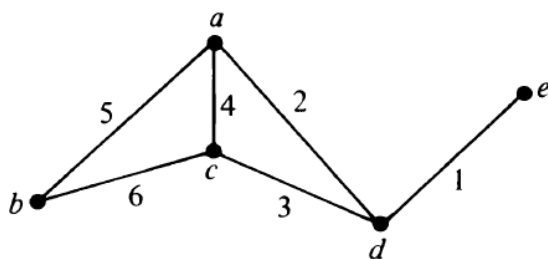


## Tutorial 13

- ✓ 1. Let  $G$  be a simple graph. Show that the relation  $R$  on the set of vertices of  $G$  such that  $uRv$  if and only if there is an edge associated to  $\{u,v\}$  is a symmetric, irreflexive relation on  $G$ .
- ✓ 2. How many edges are there in a graph with 10 vertices each of degree six?
- ✓ 3. Which of the following statements is/are TRUE for an undirected graph?  
 P: Number of odd degree vertices is even  
 Q: Sum of degrees of all vertices is even  
 (A) P Only  
 (B) Q Only  
 (C) Both P and Q  
 (D) Neither P nor Q
- ✓ 4. Prove that the sum of the degrees of the vertices of any finite graph is even.
- ⑤ 5. Show that any graph where the degree of every vertex is even has an Eulerian cycle. Show that if there are exactly two vertices  $a$  and  $b$  of odd degree, there is an Eulerian path from  $a$  to  $b$ . Show that if there are more than two vertices of odd degree, it is impossible to construct an Eulerian path.
6. An  $n$ -cube is a cube in  $n$  dimensions. A cube in one dimension is a line segment; in two dimensions, it's a square, in three, a normal cube, and in general, to go to the next dimension, a copy of the cube is made and all corresponding vertices are connected. If we consider the cube to be composed of the vertices and edges only, show that every  $n$ -cube has a Hamiltonian circuit.
- ✓ 7. Show that following graphs are isomorphic:



- ✓ 8. Draw an undirected graph represented by the given adjacency matrix.

$$\begin{bmatrix} 1 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 0 \end{bmatrix}$$