



B. Tech, Spring-2021

EPHY108L

Problem Set-1

- ✓ 1. Consider two vectors $\vec{A} = 2\hat{i} - \hat{j} + 3\hat{k}$ and $\vec{B} = \hat{i} + \hat{j} - 2\hat{k}$. Find a third vector \vec{C} (say), which is perpendicular to both \vec{A} and \vec{B} . Further find the angle between \vec{A} and \vec{B} .
- ✓ 2. Find a unit vector, which lies in the $x - y$ plane, and which is perpendicular to \vec{A} of previous problems. Similarly, find a unit vector which is perpendicular to \vec{B} , and lies in the $x - z$ plane.
- ✓ 3. Calculate $\vec{A} \cdot (\vec{B} \times \vec{A})$ for the vectors of the previous problem. Does this result hold only for the above defined vectors only?
- ✓ 4. Consider two distinct general vectors \vec{A} and \vec{B} . Show that $|\vec{A} + \vec{B}| = |\vec{A} - \vec{B}|$ implies that \vec{A} and \vec{B} are perpendicular.
- ✓ 5. If three sides of the rectangular box are $\vec{A}, \vec{B}, \vec{C}$. What is the volume of the box?
- ✓ 6. A particle moves along the space curve $\vec{r} = (t^2 + t)\hat{i} + (3t - 2)\hat{j} + (2t^3 - 4t^2)\hat{k}$. Find the velocity at time $t = 2$.
- ✓ 7. Due to a force field, a particle of mass 5 units moves along a space curve whose position vector is given as a function of time t by $\vec{r} = (2t^3 + t)\hat{i} + (3t^4 - t^2 + 8)\hat{j} - 12t^2\hat{k}$. Find the velocity, momentum, acceleration and force field at any time t .
- ✓ 8. A particle of mass 2 units moves in a force field depending on time t given by $\vec{F} = 24t^2\hat{i} + (36t - 16)\hat{j} - 12t\hat{k}$. Assuming that at $t = 0$ the particle is located at $\vec{r}_0 = 3\hat{i} - \hat{j} + 4\hat{k}$ and has velocity $\vec{v}_0 = 6\hat{i} + 15\hat{j} - 8\hat{k}$. Find the velocity and position at any time t .
- ✓ 9. Position of a particle in xy plane is given by $\vec{r}(t) = A(e^{at}\hat{i} + e^{-at}\hat{j})$, where α and A are constants. Calculate the velocity and acceleration of the particle, as functions of time t .
- ✗ 10. Acceleration of a particle in the xy plane is given by $\vec{a}(t) = -\omega^2\vec{r}(t)$, where $\vec{r}(t)$ denotes its position, and ω is a constant. If $\vec{r}(0) = a\hat{j}$ and $\vec{v}(0) = a\omega\hat{i}$. Then obtain an expression for $\vec{r}(t)$ in cartesian coordinates.
- ✓ 11. The rate of change of acceleration of a particle is called jerk which can be defined as $\vec{j}(t)$. If the jerk of a particle is given by, $\vec{j}(t) = a\hat{i} + bt\hat{j} + ct^2\hat{k}$, where a, b, c are constants. Assuming that at time $t = 0$, the particle was located at the origin, and its velocity and acceleration were zero, obtain its position $\vec{r}(t)$, as a function of time in cartesian coordinates.