Assignment 1

Amaan - EP20BTECH11003

Download all python codes from

https://github.com/RaghavJuyal/AI1103/blob/main/ Assignment1/Codes/Assignment1.py

and latex-tikz codes from

https://github.com//AI1103/tree/main/Assignment1/ Assignment1.tex

Question 5.27

Find the probability distribution of number of doublets in three throws of a pair of dice?

Solution

Let $X \in \{0, 1, 2, 3\}$ denote a random variable whose value represents the number of doublets obtained in 3 throws of a pair of dice. We can describe the whole experiment using Binomial probability distribution, given by,

$$Pr(X = r) = {}^{n}C_{r}p^{r}q^{n-r}$$
 (0.0.1)

where, r is the number of successes, n is the total number of trials(throws) and p and q are the probabilities of success(doublet) and failure(no doublet) respectively, such that,

$$p + q = 1 \tag{0.0.2}$$

Given, n=3, and, we can find,

$$p = \frac{1}{6} \tag{0.0.3}$$

$$q = \frac{5}{6} \tag{0.0.4}$$

Putting the above information in the equation

(0.0.1), we get,

$$Pr(X=0) = \frac{125}{216} \tag{0.0.5}$$

$$Pr(X = 0) = \frac{125}{216}$$
 (0.0.5)
 $Pr(X = 1) = \frac{25}{72}$ (0.0.6)

$$Pr(X=2) = \frac{5}{72} \tag{0.0.7}$$

$$Pr(X=3) = \frac{1}{216} \tag{0.0.8}$$

X=r	0	1	2	3
Pr(X=r)	125 216	$\frac{25}{72}$	<u>5</u>	$\frac{1}{216}$